

CS 135

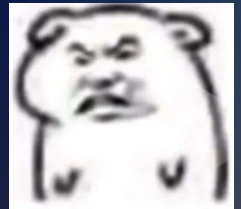
# Lab

# 7

# Problem 1

Find the remainder when  
 $7^{2001}$  is divided by 5.

My calculator tryna solve this:



# Problem 1

Given the lemma and use of Fermat's Little Theorem

$$a \equiv b \pmod{n} \text{ and } c \equiv d \pmod{n} \rightarrow ac \equiv bd \pmod{n}$$

$$7^4 \equiv 1 \pmod{5} \text{ and } 7^4 \equiv 1 \pmod{5} \rightarrow 7^8 \equiv 1 \pmod{5}$$

$$7^8 \equiv 1 \pmod{5} \text{ and } 7^4 \equiv 1 \pmod{5} \rightarrow 7^{12} \equiv 1 \pmod{5} \text{ and so on...}$$

$$\text{Until } 7^{2000} \equiv 1 \pmod{5}$$

$$\text{And since } 7 \equiv 2 \pmod{5} \text{ our final answer is } \mathbf{7^{2001} \equiv 2 \pmod{5}}$$

## Problem 2

What is  $4^{100,000} \pmod{19}$  equal to?



# Problem 2

$$100,000 = 5555 \cdot 18 + 10$$

$$4^{100,000} \equiv (4^{18})^{5555} * 4^{10} \pmod{19}$$

$$\equiv 1^{5555} * 4^{10} \pmod{19}$$

$$\equiv 4^8 * 4^2 \pmod{19}$$

$$\equiv 5 * -3 \pmod{19}$$

$$\equiv 4 \pmod{19}$$

\*want 18 to have FLT work

\*use successive squaring to find these numbers mod 19

# Problem 3

$$x \equiv 3 \pmod{5}$$

$$x \equiv 1 \pmod{7}$$

$$x \equiv 6 \pmod{8}$$

Find  $x$ .



# Problem 3

Step 1: Calculate  $m = 5 \cdot 7 \cdot 8 = 280$

Step 2: Calculate  $M_1 = 56$ ,  $M_2 = 40$ ,  $M_3 = 35$

Step 3: Calculate  $y_1 = M_1^{-1} \equiv 1 \pmod{5}$

$$y_2 = M_2^{-1} \equiv 3 \pmod{7}$$

$$y_3 = M_3^{-1} \equiv 3 \pmod{8}$$

Step 4: Calculate  $X = 3 \cdot 1 \cdot 56 + 1 \cdot 3 \cdot 40 + 6 \cdot 3 \cdot 35$   
 $= 918 \equiv \mathbf{78} \pmod{280}$



**Racket Time!**