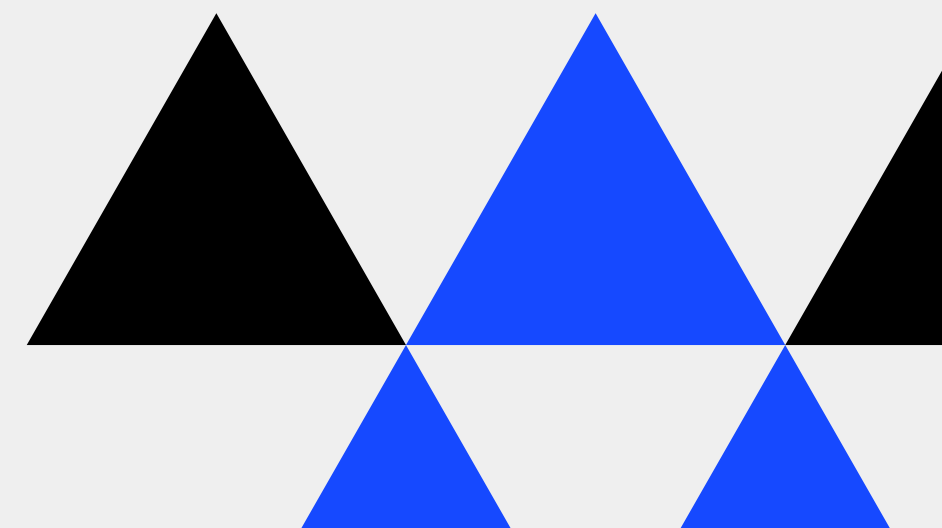


# Lab 8

CS 135

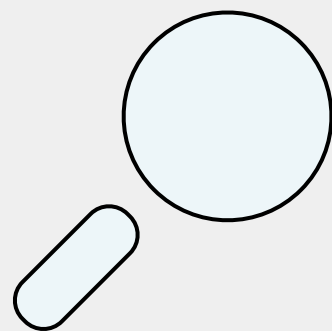


# Problem 1

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Callie wants to send the message  $M = 13$  to Alice.

Using Alice's public and private keys, calculate the ciphertext  $C$ , and the value for  $R$  when Alice recovers the message.



Encryption/Decryption Setup:

Alice's Setup:

- Choose 2 prime numbers (11, 3)
- Calculate the product  $n=pq$
- Calculate  $m=(p-1)(q-1)$
- Choose numbers  $e$  and  $d$  so that  $ed$  has a remainder of 1 when divided by  $m$
- Publish her public key  $(n, e)$

XYZ encrypts a message  $M$  for Alice:

- Finds Alice's public key  $(n, e)$
- Finds the remainder  $C$  when  $M^e$  is divided by  $n$
- Sends ciphertext  $C$  to Alice

Alice receives and decrypts ciphertext  $C$ :

- Uses her private key  $(n, d)$
- finds remainder  $R$  when  $C^d$  is divided by  $n$ .
- $R$  matches the message  $M$  that XYZ wanted to send to Alice.

# Problem 1 Answer

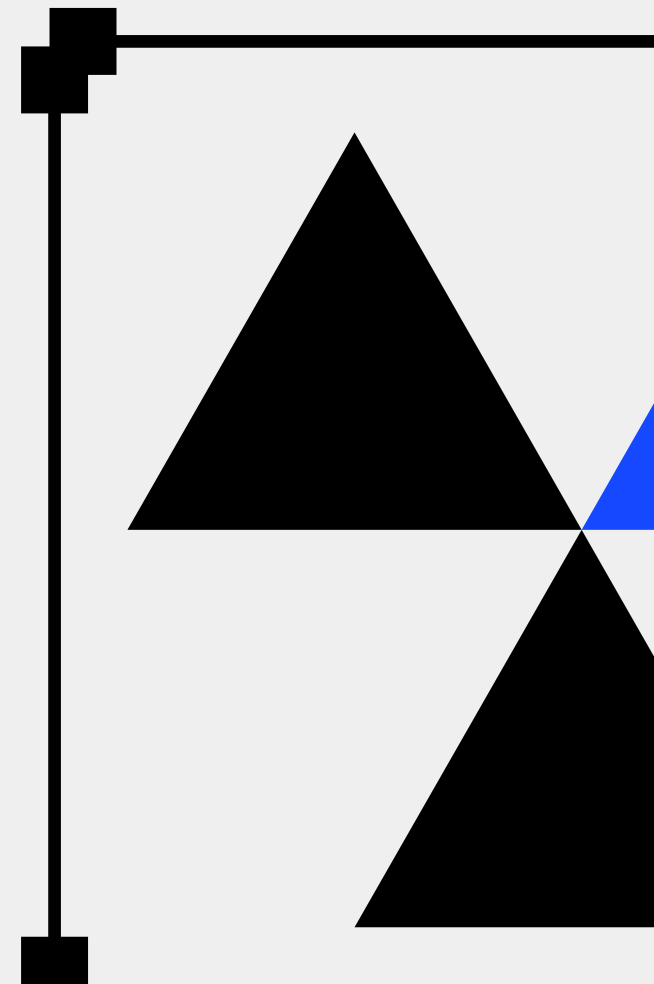
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Callie encrypts message  $M = 13$ :

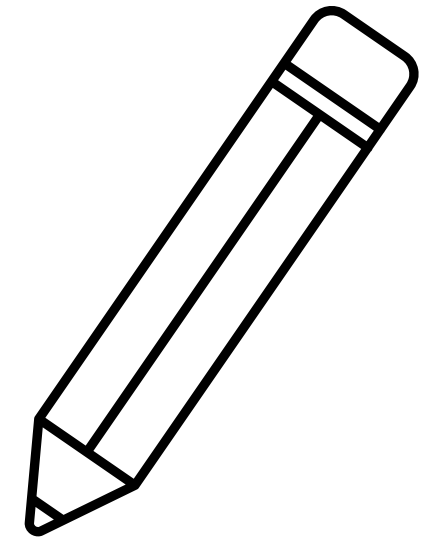
- Alice's public key is  $(n, e) = (33, 3)$  (e is 3, d is 7)
- When  $M^e = 13^3 = 2197$  is divided by 33, the remainder is  $C = 19$
- Callie sends the ciphertext  $C = 19$  to Alice

Alice receives and decrypts ciphertext  **$C = 19$** :

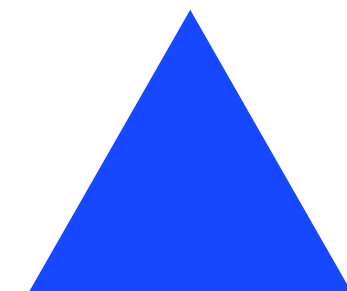
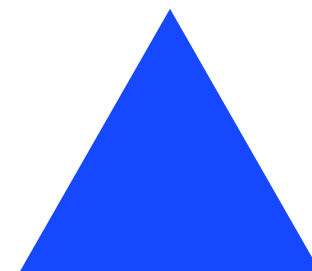
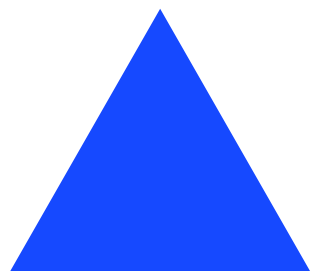
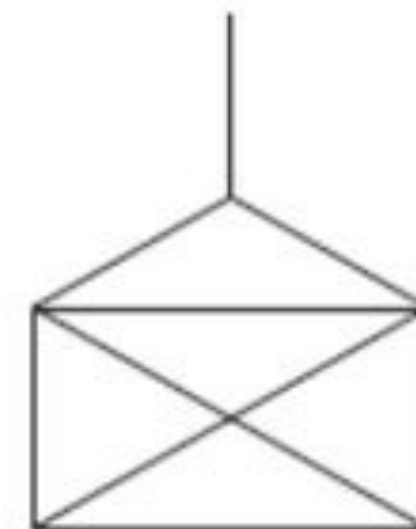
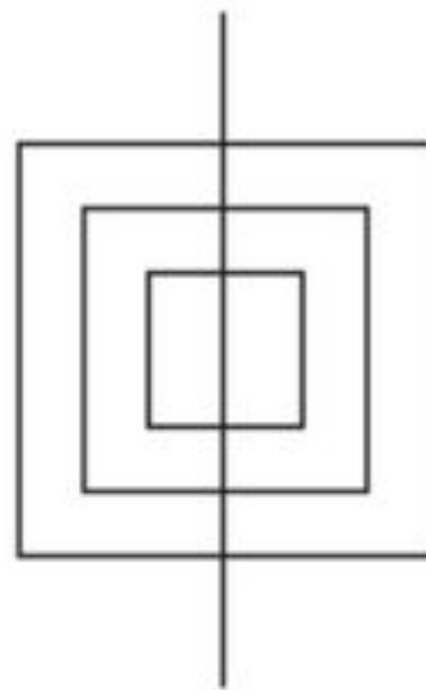
- Alice uses her private key  $(n, d) = (33, 7)$
- When  $19^7 = 893, 871, 739$  is divided by 33, the remainder  $R = 13$
- **$R = 13 = M$** , aka the OG message



# Problem 2

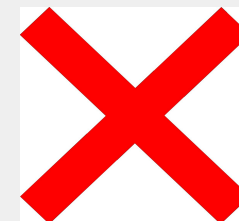
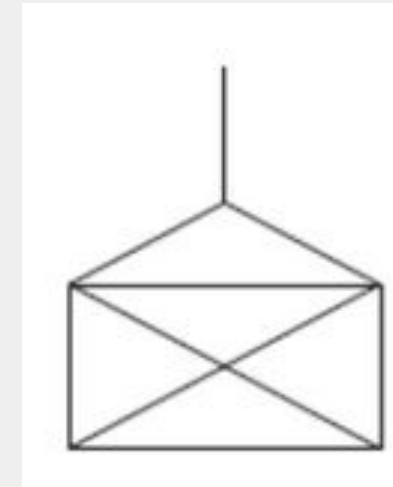
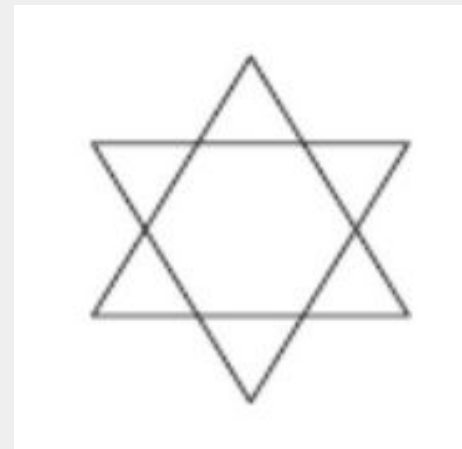
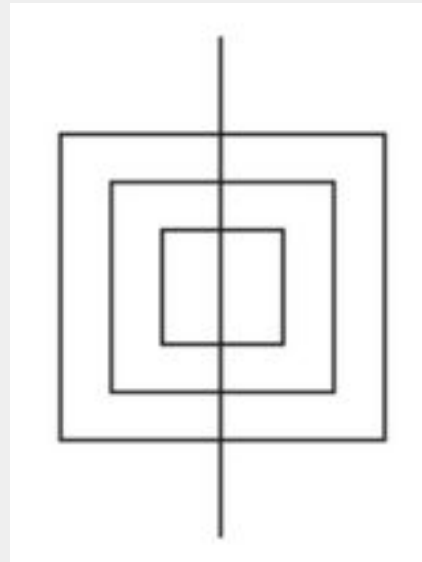


Determine whether each of the following figures can be drawn in one continuous motion without lifting the pencil or retracing any part of the drawing. Explain your reasoning (Hint: think about vertex degrees!)

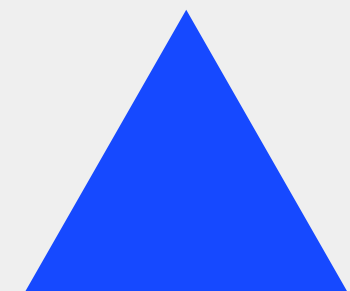
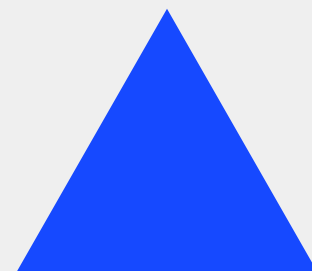


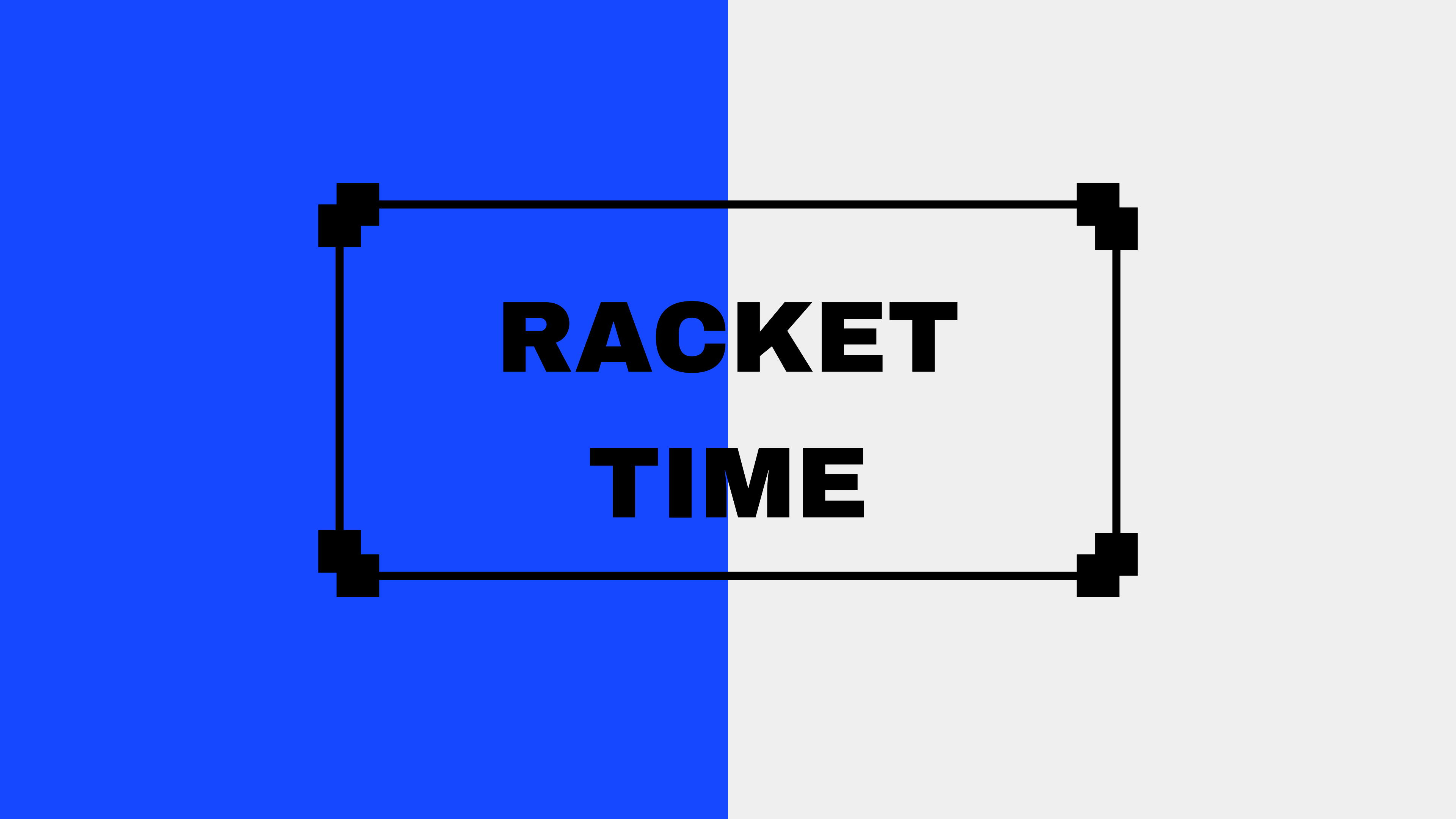
# Problem 2 Answer

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Condition: The drawing must have 0 or 2 vertices with odd degree.





**RACKET**  
**TIME**