Essentials of CS284 (Spring 2023, Prof. Akcam)

Data Structures in Java!

1/18/23

- Object Oriented Programming
 - A set of entities that collaborate with each other in order to perform some specific task
 - These entities are called objects
- Java is a collection of classes
 - Class a named description for a group of entities that have the same characteristics
 - Entities: objects
 - Characteristics: attributes (DATA FIELDS) for each object and the operations (METHODS) that can be performed on these objects
- UML Diagrams
 - Graphical representation of classes

Class Name
Attributes
Methods

Rectangle
double width double height
Rectangle(double x, double y) double area()

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- \blacksquare Rectangle(double x, double y) \rightarrow Constructor (matches class name!)
- Access modifiers: public and private access
 - Prefer private access majority of the time in industry you do not want all methods to have access
 - o For this class most of the time, methods will be public, attributes will be private
- Constructor
 - Does not have return type
- Java uses curly braces :)

1/20/23

- Java has a variety of primitive data types
 - o byte, short, int, long, float, double, char boolean
 - Class names are also types!
- Special support is provided for Strings through the java.lang.String class
- How many bits from -128 to 127?
 - o 8 bits, 1 byte
- How many bits in a short (-32768 to 32767)
 - o 16 bits, 2 bytes
- Static method references / is used for several objects
 - o Indicates that a method is a class method
 - You can have multiple static methods, but you cannot have two methods with the same name if one is static
 - You can have instance methods of the same name in Java
 - Called using dot notation (Rectangle.getNumberOfRectangles();)
 - Static methods cannot call instance methods
- Constructors initialize data fields
 - You can make multiple constructors
- ++ shortcut is add one (increment), - shortcut is minus one (decrement)
- Instance methods = non-static methods
- Static methods = class methods
- Objects are instantiated using the "new" keyword
 - You can make as many instances as needed
 - If you do not use a new keyword, you make an instance but you do not allocate space for it
- ★ Rectangle Project used on 1/20/23!!

(https://github.com/humnasul/cs284notes/tree/main/class%20code/oop/Rectangle)

1/23/23

- ★ Person Project used on 1/23/22!!
 - (https://github.com/humnasul/cs284notes/tree/main/class%20code/oop/Person)
- If the attribute consists of two words, use camel case
- /** xxx */
- private static final int SENIOR_AGE = 65;
 - o final keyword means value cannot be changed
 - Capitalize final variables for readability
- Constructor initializes variables for use
- You need to initialize an array of a certain size or with values
 - Arrays start at 0
- Arrays are initialized by default in Java
 - o int[] scores = new int[5] initializes [0,0,0,0,0]
- names.length → gives you length of array names
- Enhanced for loop

```
for (int i : scores) {
          System.out.println(i);
}
```

- 2D arrays have rows and columns
 - double matrix[][] = new double[ROWS][COLS]

1/25/23

```
int x = 4
double y = x
- This code works
double x = 8.9
int y = x
```

- This code gives an error

```
String greeting = "Welcome";
String welcome = greeting;
System.out.println(welcome);
greeting = "hello";
System.out.println(welcome);
```

- Both print statements print "Welcome"
 - Value of welcome does not change when variable greeting changes

```
int[] data1 = {1,2,3,4,5};
int[] data2 = data1;
System.out.println(data1[0]);
data2[0] = 8;
System.out.println(data1[0]);
```

- First print statement prints 1, second print statement prints 8
- Strings are immutable, values within them cannot be changed
- You must make an object to call non-static methods from main (because main is static)
 - o Do not make everything static to fix the problem!
- Java math class has math functions for use

1/27/23

- You can have multiple constructors with different parameters
 - o They must have different parameters otherwise error
- If a class extends another class (inheritance), you need to call super() from the constructors to reference the superclass

```
public Rectangle() {
   this(0,0);
}
```

• Even if the two variables referenced by this() are doubles, the 0 and 0 will be automatically converted

	default	private	protected	public
Same Class	Yes	Yes	Yes	Yes
Same package subclass	Yes	No	Yes	Yes
Same package non- subclass	Yes	No	Yes	Yes
Different package subclass	No	No	Yes	Yes
Different package non- subclass	No	No	No	Yes

- https://www.geeksforgeeks.org/access-modifiers-java/
- For this class, use private for data fields and use public / default for methods

1/30/23

- Method overloading
 - Runtime specifies which toString() to utilize
 - You can have multiple methods of the same name, but different parameter lists
 - A different return type does not count as overloading

Overriding	Overloading
- Methods have - Same name - Same parameter list - Same return type - Final methods cannot be overridden - The method will be overridden in subclass (multiple classes involved) - Static methods cannot be overridden - Runtime polymorphism	 Methods have Same name Different parameter list Methods are defined in the same class Compile-time polymorphism Static methods can be overloaded Cannot overload by return type

Interface	Abstract Class
 Only can have abstract methods Only have static & final variables Cannot provide an implementation of abstract class Uses the keyword "implements" Can extend another Java interface only Members must be public 	 Can have abstract & non-abstract (concrete) methods Can have non-final variables, final, static, non-static variables Can provide an implementation of an interface Uses the keyword "extends" Can extend another Java class, implement multiple interfaces Members can be private, protected, default

Abstract classes

- You cannot create an object declaration inside
- Use an abstract class when you need a base class for two or more subclasses that share some attributes
- An abstract class can implement an interface, but an interface cannot extend an abstract class

public abstract void drawHere();

- In an abstract class, the subclasses of the abstract class must have this abstract method
 - Almost like delegating tasks to subclasses
- Can have constructors
 - Abstract classes have variables, you may want to initialize variables

- You cannot make objects that can use the constructors, but subclasses will have super() that can access the abstract class' constructor
- An abstract class can implement an interface but does not have to define all the methods of the interface
 - Implementation of methods is responsibility of subclasses
- You cannot have more than one base class / superclass for a subclass
- Abstract classes and Interfaces both cannot have objects / be instantiated
- ★ Used IntelliJ Rectangle project (https://github.com/humnasul/cs284notes/tree/main/class%20code/oop/Rectangle)

2/1/23

- Methods to call are determined at runtime when you use polymorphism
- Object.equals() method checks if two objects are equivalent
- getClass() returns the runtime class of the object "this".
- Downcasting converting superclass type to subclass type

2/3/23

- "Throwable" class is superclass to all classes
- Checked exceptions
 - Normally not due to programmer error
 - Beyond control of programmer
 - Ex: IOException, FileNotFoundException
- Unchecked exceptions
 - o Programmer error
- Process finished with exit code 0 : successful (System.exit(0);)
- Process finished with exit code 1: interrupts execution of program (System.exit(1);)
 - There is an error in the code and execution stopped
- If trying to add JUnit to a project, do @Test in the file and do alt + enter
 - o JUnit 5.8.1

- Make sure you have multiple test cases: 2 + 2 = 4 AND 2 * 2 = 4
- Testing functions in JUnit: assertEquals, assertNotEquals, assertNull, assertTrue, assertFalse

2/6/23

- Lists
- ArrayList
 - Arrays have a fixed size
 - Constant time access to elements
 - o Removal is linear
 - Insertion is linear
 - o .add() adds elements chronologically
- LinkedList
 - Grow and shrink no fixed size
 - Linear time access
 - Linear time insertion and removal (except if previous element is supplied, then constant)

```
Pair(E fst, F snd) {

//default access modifier, package private

//only accessible within package

first = fst;

second = snd;
}
```

★ Used Lists project

(https://github.com/humnasul/cs284notes/tree/main/class%20code/lists%2C%20sets%2 C%20etc/Lists)

2/8/23 + 2/10/23

★ 2/8/23 - coded in Lists project in IntelliJ

(https://github.com/humnasul/cs284notes/tree/main/class%20code/lists%2C%20sets%2 C%20etc/Lists)

- Algorithm efficiency
 - Getting a precise measure of the performance of an algorithm
 - Using Big-O notation expresses the performance of an algorithm as a function of the number of times to be processed
 - Processing time increases in proportion to the number of inputs n
 - Target
 - If target is present, for loop will execute (on average) (n+1) / 2 times
 - If target is not present, for loop will execute n times
 - o O(n) is referred to as Big O
 - Linear growth rate
 - n * m occurs when there are nested loops each iteration of of the outer loop, n, causes iterations of the inner loop, denoted as m (inner loop must be constant time, like an if)

- \circ O(n²) \rightarrow quadratic growth rate
 - Ex: for loop inside for loop
 - If there if an if inside both nested for loops, we don't consider the time spent processing the for loop because it is trivial in comparison
- If you have a nested if and you have two conditions compared with &&, replacing the && with || reduces the time because only one of the conditions has to be checked / be true
 - Max number of times is 2
- Logarithmic growth rate (asked on tests)
 - Pay attention to where for loop starts, where for loop ends, and what happens within the loop
 - O(logbase2 n)

Notations: in order from most efficient to least

- 1. O(1) constant
- 2. O(log n) logarithmic
- 3. O(n) linear
- 4. O(n logn) log linear
- 5. Popular for sorting algorithms
- 6. O(n^2) quadratic
- 7. O(n^3) cubic
- 8. O(2ⁿ) exponential
- 9. O(n!) factorial

- $2n = O(n) \rightarrow the constant 2 is irrelevant$
- f(n) = O(g(n))
 - We can say that g(n) is the the max growth rate
- O(g(n)) is a set of functions
- The c-value provides the upper bound
 - Creates a tighter bound
- Comparing growth rates: 100n == 7n + 50
 - Both are dependent on n, BUT the constants (7 and 100) don't make a big difference)
 - Both are linear time, both have a time of Big O(n)

2/13/23

```
    0 <= f(n) <= c g(n)</li>
    τ(n) = n^2 + 5n + 25
    0 <= n^2 + 5n + 25 <= c n^2</li>
    1 + 5/n + 25/n^2 <= c</li>
    no = 5, c = 3; 1 + 5/5 + 25/25
    1 + 1 + 1 <= c</li>
    3 <= c</li>
```

★ Reviewed Big O example 2 in slides

2/15/23

- exponential and factorial algorithms have a much longer runtime
- Single linked list (singly)
 - Link only goes in one direction
- Double linked list
 - o next = node → associates with data
- ★ "Linked" package inside "Lists" project in intelliJ

(https://github.com/humnasul/cs284notes/tree/main/class%20code/lists%2C%20sets%2 C%20etc/Lists/src/Linked)

2/22/23

- Linked lists
 - When head == null, tail also == null
 - You need to assign both
 - Establish links for the new nodes first, then do previous and next of the previously existing nodes
 - How does a compiler know where to place a node?
 - Provide the location or iterate through starting with the head or tail for placement

2/24/23

- Big O Constants get dropped
- Quiz answers
- 1. O(n)
- 2. $n/2 * n = O(n^2)$
- 3. C = 2, n0 = 4
 - a. If you have 2 positive numbers choose the larger value for n0 relating to the solution
 - i. You want to achieve the higher intersection point
- Linked lists
 - o EX: 12 15 20 25
 - If you want to remove head (12) ...
 - head = head.next;
 - o Points to next value
 - head.prev = null;
 - Ensures that the value before the newly assigned head is null
 - If you want to remove tail (25) ...
 - if (tail.data == number)
 - o tail = tail.previous;
 - o tail.next = null;
 - Remove internal node (20)
 - current = head;
 - loop until (current.data = number)
 - current.next.previous = current.previous;
 - current.previous.next = current.next;
 - Make sure head and tail aren't null for you to start at
 - Elements before head should be null and elements after tail should be null
 - Insertion at head or tail is O(n), insertion anywhere else is O(n)
- Intro to stacks
 - Last-in, first-out = LIFO
 - Operations:
 - empty() test for an empty stack
 - peek() inspect the top element
 - pop() retrieve the top element
 - Removes top element and changes the top element (head)
 - Put a new element on the stack (E push (E obj))
 - Adds element to the top (changing top element aka head)
 - o Palindromes reading from bottom or top will be the same word
 - tail != liat

★ Both pop() and push() alter the head



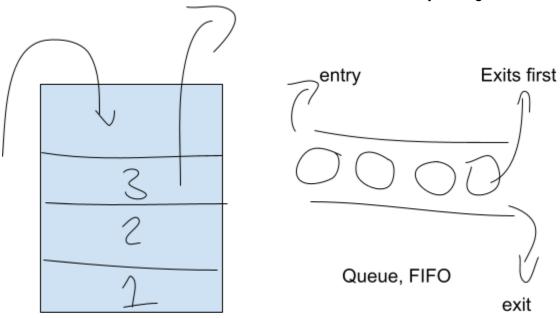
- Last one you put if the first one you take out
- Test questions
 - o For this provided link list, implement an insert method

2/27/23

- StringBuilder adds functions to String to allow you to easy access diff parts and manipulate
- Palindromes
 - o Ignore case
 - buildReverse() → returns reversed String
- Stacks can be used as a solution to counting balanced parenthesis
 - Have a stack with parenthesis and if the size is even then parenthesis are done properly
 - Have two stacks one with open parenthesis and one with closed parentheses;
 make sure the sizes are equal
- Vectors
 - Can grow and shrink in size
 - We use vectors to implement stacks in java
 - Vector applications can be applied to stacks as a result
- Stack program
 - Embed node class into linkedstack file so that the linkedlist and linkedstack can use nodes directly as elements

3/1/23

- Queues
 - Widely used data structure
 - o FIFO list : first-in, first-out
 - Opposite of stack
 - Examples of use
 - Operating systems
 - Tasks and resources
 - Printing queues
 - o Queues ensure that tasks are done in the order they were generated



Stack, LIFO

- Queue functions
 - queue.offer(x)
 - o queue.peek()
- Queue interface

```
public interface Queue<E> extends Collection<E> {

// Returns entry at front of queue without removing it. If the
// queue is empty, throws NoSuchElementException
E element()

// Insert an item at the rear of a queue
boolean offer(E item)

// Return element at front of queue without removing it; returns null
E peek()

// Remove and return entry from front of queue; returns null if queue
E poll()

// Removes entry from front of queue and returns it if queue not empty
E remove()
}
```

https://docs.oracle.com/javase/7/docs/api/java/util/Queue.html#:~:text=Interface%20Queue&text=A%20collection%20designed%20for%20holding.%2C%20extraction%2C%20and%20inspection%20operations.

- Simulations + Queues
 - Simulations are used to study the performance of a physical system by using a physical, mathematical, or computer model of the system
 - Queueing theory
 - EX: used to simulate structure of bridges etc.
- Simulation Example: Blue Sky Airlines
 - Creating 2 waiting lines
 - Strategies:
 - Take turns serving passengers from both lines so that the average time for all is not too long
 - Serve the passenger waiting the longest
 - Serve any frequency flyers before any regular passengers
 - Will annoy regular passengers
 - Consider potential events in time intervals
- ★ IntelliJ Look at StackInt project → Queues package (https://github.com/humnasul/cs284notes/tree/main/class%20code/data%20structures%20in%20java/StackInt/src/Queues)

3/3/23

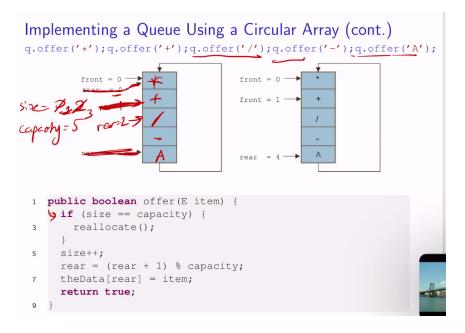
- Peek returns data from the front
- Using a single-linked list to implement a queue
 - public class ListQueue<E> implements Queue<E> { }
- Implementing a queue using a circular array
 - The time efficiency of using a single or double linked list to implement a queue is acceptable
 - Storage space is increased when using a linked list due to references stored in the nodes
 - TIME EFFICIENCIES AND STORAGE ISSUES CAN BE PREVENTED USING... circular arrays!!
- Circular arrays
 - Rear is connected to the front of the array
 - If the first element is empty but the rest are filled (5 spots total), the rear is 4+1 %
 which is 0, going back to the front!
- Reallocate:

```
private void reallocate() {
   int newCapacity = 2 * capacity;
   E[] newData = (E[])new Object[newCapacity];
   int j = front;
   for (int i = 0; i < size; i++) {
      newData[i] = theData[j];
      j = (j + 1) % capacity;
   }
   front = 0;
   rear = size - 1;
   capacity = newCapacity;
   theData = newData;
}</pre>
```

Links:

0

- https://www.baeldung.com/java-generic-array
- https://docs.oracle.com/javase/8/docs/api/java/util/Iterator.html



- ► All three implementations (double-linked list, single-linked list, circular array) are comparable in terms of computation time
- \blacktriangleright All operations are $\mathcal{O}(1)$ regardless of implementation
- Although reallocating an array is $\mathcal{O}(n)$, it is amortized over n items, so the cost per item is $\mathcal{O}(1)$
- ► Linked-list implementations require more storage due to the extra space required for the links
 - ► Each node for a single-linked list stores two references (one for the data, one for the link)
 - ► Each node for a double-linked list stores three references (one for the data, two for the links)
- ► A double-linked list requires 1.5 times the storage of a single-linked list
- ► A circular array that is filled to capacity requires half the storage of a single-linked list to store the same number of elements, but a recently reallocated circular array is half empty, and requires the same storage as a single-linked list
- All three implementations (double-linked list, single-linked list

★ Look at queues iterator implementation on Canvas

Stacks do not implement iterators because it is implied that
 (https://github.com/humnasul/cs284notes/blob/main/class%20code/data%20structures%20in%20java/ListQueue-Iterator.java)

> TEST TOPICS

- One question runtime analysis
- One question lists
- One question java basics
- One questions stacks or queues
- UML diagram
- Visibilities for methods etc.
- 6 questions total one is bonus (5 required)
- TOPICS: All topics on canvas + queues
 - To review: abstract classes, interfaces, etc.

> NOTES FROM TEST REVIEW

- Abstract classes can have constructors
 - You can call super();
- Interfaces can only have static and final attributes
- o Know difference between overloading / overriding
 - Overloading is within same class
 - Overriding is subclass overriding a superclass
- Animal bird (inheritance relationship)
 - Animal toString(), getName()
 - Bird toString(), getSeeds()
 - Animal aBird = new Animal();
 - aBird.toString();
 - Will call animal's toString()
 - Animal aBird = new Bird();
 - aBird.toString();
 - Will call bird's toString()
 - toString method is overridden, so the bird class's' method will be called
 - At runtime, it binds to include the overridden bird methods
 - aBird.getSeeds();
 - Not a valid call!! syntax error
 - ((Bird) aBird).getSeeds();
 - This will cast aBird as a bird so you can access the method
 - Bird.getName();
 - Will call getName from Bird class (overridden)

ADDITIONAL NOTES

- Public can be accessed by any class, private can only be accessed by the class it is defined in
- Polymorphism allows for several implementations of the same interfaces
- You can only extend one class
- Arraylists removal and insertion is linear time; not fixed size
 - You need to use the non-primitive type when making an array list

- EX: ArrayList<Integer>, ArrayList<Boolean>
- SLL's do not have a previous field

3/10/23

- Recursion method calls itself in order to make problem smaller until it reaches a base case
- Stacks are utilized for recursion!!
- When a method goes recursively infinitely, there is a StackOverflowError
- Tail recursion: calculation is embedded, better for performance
 - Second / new parameter used in tail recursion = accommodator
- In general, loops have a smaller runtime than recursion
 - o Recursive solutions are used for readability 100 lines can become 3 lines

3/20/23

- Trees are non-linear and hierarchical
- Tree nodes can have multiple successors BUT one predecessor
 - More than one predecessor = graph
- Trees are recursive data structures because they can be defined recursively
- Binary trees
 - 1 predecessor, at most 2 successors
- Binary tree level calculations vary depending on the textbook used include what you are counting in quizzes and tests
 - Declarations and definitions are needed
- Levels = 1 + the level of its parent
- Height = number of nodes in the longest path the root to a leaf
 - You can also count the branches just make sure you say what you are counting on a quiz / test
- Tree expressions: Node(i,l,r)

3/22/23 + 3/24/23

- Huffman can be used for file compression
- BST runtimes:
 - https://www.geeksforgeeks.org/complexity-different-operations-binary-tree-binary-search -tree-avl-tree/
- Reviewed Tree Walks: preorder, inorder, postorder
 - https://www.geeksforgeeks.org/tree-traversals-inorder-preorder-and-postorder/
- Search operation:
 - Compare values (greater than = go right, less than go left)

3/27/23 + 3/29/23

- Coding BinaryTree.java
 - Size = number of nodes
- Added insert code into BSTree.java 3/29/23

https://github.com/humnasul/cs284notes/tree/main/class%20code/data%20structures%20in%20java/BinaryTrees

4/3/23

- Full, perfect, complete binary trees
 - Different qualities of trees
- Heap and priority queues
 - Heap
 - Complete binary tree
 - The value of the root is the smallest item in the tree
 - Every subtree is a heap
 - Relationship between parent and children
 - Larger number is lower
 - Insert into heap: most runtime is O(log n) when n is the number of nodes (height)
 - Because a heap is a complete binary tree, it can be implemented efficiently using an array rather than a linked data structure

4/5/23

- Merging heaps
 - O (n log n)
- Priority queues
 - Similar to heap implementation, takes advantage of how heaps work
- Do not use arrays.sort() and other algorithms when coding on assignments!!

4/10/23

- Min-heap: upperlevel nodes are smaller than lowerlevel nodes
 - Complete binary tree
 - Levels start from the left
- Selection sort: after first iteration of outer loop, you are on the minimum element
 - Once you find the minimum, you swap with the first element
 - You repeatedly find minimums and swap
 - Number of iterations = n 1
 - Comparisons happen big O n^2 happens several times per run
 - o Swapping is linear O n happen for each provided value, so it is linear
 - General runtime for sort: On^2
- Bubble sort:
 - o Smaller values bubble up, larger values go down
 - Compares adjacent pairs and keeps moving max values to the end (can also move min values to the end in reverse)
 - o After first iteration of outer loop, max value has been bubbled to the bottom
 - The next iteration does not count the last element the last element has been sorted :
 - o Continues the process of iteration and sorting last elements until top is reached
 - General runtime: On^2
 - Number of comparisons runtime: On^2
 - Swaps: On^2
 - Every comparison does swap if needed, swap is n^2
- Bubble sort will do better if there are performance tests done and the list is almost sorted, otherwise it is selection sort

4/12/23 + 4/14/23

- Insertion sort
 - Does not find max and min, but compares adjacent elements
 - Runtime complexity: On^2
 - In best case, number of comparisons is On
- Merge sort
 - Iterating through and comparing elements
 - Steps
 - Split the array into two halves
 - Sort the left half
 - Sort the right half
 - Merge the split array
 - Runtime: O(n logn)
- Tests will not have examples with duplicate elements

 Merge sort quiz will ask for order of operations - splitting FULLY and then merging

4/17/23

- Final exam
 - Part 1 exam on May 4 on paper
 - o Part 2 May 11 / whatever it says online, a lot less points than part 1
 - Online, will be on canvas, can be taken anywhere
 - true/false, fill in the blank, NO CODING, etc.
 - Will not have shell sort on final
 - Merge sort is her favorite so prepare for that
- Shell sort
 - Based on gap sizes
 - https://www.w3resource.com/ODSA/AV/Sorting/shellsortAV.html
 - Runtime: O(n^3/2)
- Heapsort
 - Same time complexity as mergesort (Onlogn)
 - Difference between them is that heapsort does not make separate arrays
 saves memory space
 - Bigger data sets are better with heapsort because less memory is used
 - Once you finish the first iteration of the while loop, the biggest element is found and confirmed
 - Once you get the second iteration, you have found the largest 2 elements in the array
 - Once you get the third iteration, you have found the largest 3 elements in the array

4/19/23

- Set interface under collection umbrella
 - Set objects...
 - Not indexed
 - Do not reveal the order of insertion of items
 - Enable efficient search and retrieval of information
 - Allow for removal of elements without moving other elements around
 - o Includes different methods in interface
 - addAll adding a collection of items, allows for union of sets
 - Iterator iterates through all elements in set
 - removeAll removes values at intersection between sets
 - retainAll keeps only values in the intersection
 - Does NOT have a get method because elements cannot be accessed by index you can use an iterator or for to get the element you're looking for
- Maps and map interface
 - Set of ordered pairs whose elements are known as they key and the value
 - o Includes methods in interface
 - Basics: get, put, isEmpty, remove, size
 - Others:
 - Clear
 - containsKey
 - containsValue
 - Set<Map.Entry<K,V> entrySet ()
 - Set <K> keySet()

4/24/23

- Hash table open addressing
 - Calculate index if index has an element already, increment the index calculated and keep moving upwards
 - If you do not have the condition that if the index is null, the item does not exist, then you need to search the whole table for the item

```
if (table[index] == null) {
  item is not in the table
```

- Much less efficient without that condition → having that condition makes the program more efficient and is the purpose of using a hash table
- When deleting an item
 - You need to ensure that the deleted item is not in the table before you're inserting a new item into the deleted item's spot
- EX of hash table: insert "John", "Jill", "Ken", "Jane" into hash table in notebook
 - Probing happens when there is a collision

4/26/23 + 4/28/23

- Quadratic probing issue: not all table elements may be examined when looking for an insertion index an element may not be able to be placed, even if the table is not full 🙁
- Chaining references a linked list within a hash linked list is called bucket and this
 process is known as bucket hashing
 - Removing an item you can use linked list strategies and move elements together
- Performance of hash tables
 - Load factor has the greatest impact on performance and runtime
 - Lower load factor = better performance
 - If there are no collisions, performance for search and retrieval is O(1)
 REGARDLESS of table size
- Number of comparisons: $c = \frac{1}{2} (1 + \frac{1}{1 L})$
 - L is load factor (how full tree currently is)
- If an item is in the table, on average we must examine the table element corresponding to the item's hash code and then half the items in each list
 - Comparisons calculation: c = 1 + L/2
- Include these formulas on the exam formula sheet
 - She will ask you to calculate

Performance of Hash Tables versus Sorted Array and Binary Search Tree

- ▶ The number of comparisons required for a binary search of a sorted array is $\mathcal{O}(\log n)$
 - ► A sorted array of size 128 requires up to 7 probes (2⁷ is 128) which is more than for a hash table of any size that is 90% full
 - ► A binary search tree performs similarly
- ► Insertion or removal

hash table	$\mathcal{O}(1)$ expected; $\mathcal{O}(n)$ worst case
sorted array	$\mathcal{O}(n)$
BST	$\mathcal{O}(\log n)$; worst case $\mathcal{O}(n)$

•

- AVL Tree: the balance of every node is in the interval [-1, +1]
 - o Balance = right left
 - o If you add something that changes the height of the tree, the balance can change