

# Multi-start PSO with CCD Local Optimizer (MPSO-CCD)

A Global Optimization Technique

User Manual

by

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# Table of Contents

1. Serial Implementation . . . . .	1
1.1 Flowchart . . . . .	1
1.2 Required Files . . . . .	2
1.2.1 Header Files . . . . .	2
1.2.2 C Files . . . . .	2
1.3 Compiling and Executing the Code . . . . .	3
1.3.1 Compiling the Code . . . . .	3
1.3.2 Executing the Code . . . . .	3
1.3.2.1 Using Command Line . . . . .	4
1.3.2.2 Using Job Script . . . . .	4
1.4 Example . . . . .	4
1.4.1 functions.h file . . . . .	5
1.4.2 functions.c file . . . . .	5
1.4.3 main.c file . . . . .	6
1.4.4 Outputs . . . . .	8
1.5 Optimization Algorithms . . . . .	9
1.5.1 PSO Algorithm . . . . .	9
1.5.1.1 Introduction . . . . .	9
1.5.1.2 Implementation of the PSO Algorithm . . . . .	10
1.5.2 CCD Algorithm . . . . .	11
1.5.2.1 Introduction . . . . .	11
1.5.2.2 Implementation of the CCD Algorithm . . . . .	11
1.5.3 Brent Algorithm . . . . .	12
1.5.3.1 Introduction . . . . .	12
1.5.3.2 Implementation of the Brent Algorithm . . . . .	13
1.5.4 MPSO-CCD Algorithm . . . . .	13
1.5.4.1 Introduction . . . . .	13
1.5.4.2 Implementation of the MPSO-CCD Algorithm . . . . .	14

1.6	Supportive Functions . . . . .	16
1.6.1	Supportive Functions for PSO . . . . .	16
1.6.2	Math Related Functions . . . . .	16
1.6.3	Random Number Generators . . . . .	17
2.	Parallel Implementation . . . . .	18
2.1	Required Files . . . . .	18
2.1.1	Header Files . . . . .	18
2.1.2	C Files . . . . .	18
2.2	Compiling and Executing the Parallel Code . . . . .	19
2.2.1	Compiling the Parallel Code . . . . .	19
2.2.2	Executing the Parallel Code . . . . .	20
2.2.2.1	Using Command Line . . . . .	20
2.2.2.2	Using Job Script . . . . .	20
2.3	Parallel PSO Versions . . . . .	20
2.4	Example of Parallel Implementation . . . . .	21
2.4.1	mpimain.c file . . . . .	21
2.5	Source Code . . . . .	24
	Bibliography . . . . .	25

# Introduction

This manual provides the stepwise guidelines for the serial as well as parallel implementation of MPSO-CCD algorithm [1]. It is a global optimization technique which combines the particle swarm optimization (PSO) algorithm with the cyclic coordinate descent(CCD) local optimizer. Therefore it incorporates the global search characteristics of the PSO algorithm with the local search capability of the CCD algorithm. This unique combination provides a better performance by balancing the exploration-exploitation trade-off. We further implement the MPSO-CCD algorithm in a parallel environment to increase the scalability.

# Chapter 1

## Serial Implementation

This chapter presents the compilation and execution of the serial version of the MPSO-CCD algorithm written in C programming language.

### 1.1 Flowchart

The implementation procedures can be demonstrated by the following flowchart.

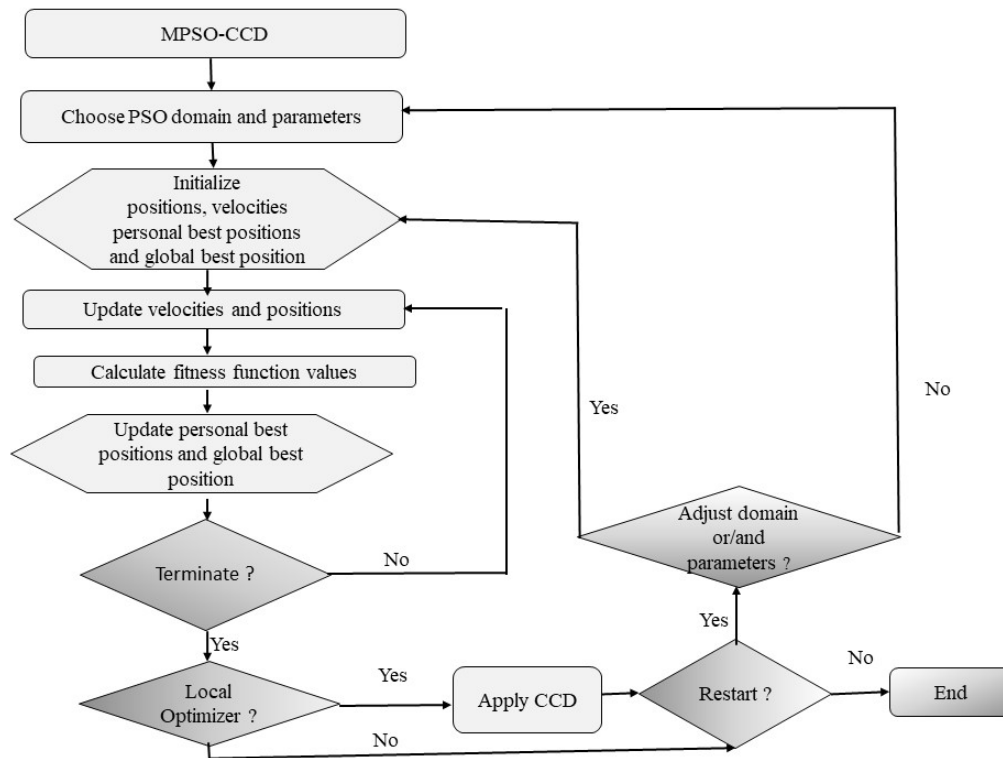


Figure 1.1. Flowchart of the MPSO-CCD algorithm.

## 1.2 Required Files

The following are the files required to implement the serial version of the PSO algorithm. All files must be in the same directory, say “mpso\_ccd\_serial”.

### 1.2.1 Header Files

1. Basic C Libraries.

`stdio.h`, `stdlib.h`, `string.h`, `math.h`, `time.h`, `assert.h`

2. Program Related Header files.

`pso.h`   `functions.h`   `randomlib.h`   `matmul2.h`

### 1.2.2 C Files

1. `pso.c`: PSO related functions file.

This file contains the function headers of optimization algorithms such as PSO algorithm, CCD algorithm, Brent algorithm, MPSO-CCD, and some other supportive functions. The corresponding function headers are included in `pso.h` file.

2. `functions.c`: Objective functions file.

This file contains the objective functions. In the current form, it has some of the common benchmark functions such as Sphere, Rastrigin, Rosenbrock, Griewank, Ackley, etc. If required, users can define their own functions and put in this file. The function, called `functionLookup()`, is then used to select a particular objective function to be minimized.

3. `matmul2.c`: Math related functions file.

This file consists some math related functions which are not included in the basic math library, called `math.h`, but they are essential to facilitate the PSO algorithm implementation such as matrix multiplications, transposing matrix, etc. The corresponding function headers are included in the file `matmul2.h`.

4. `randomlib.c`: Random numbers generators.

This file contains the functions related to random number generators. These random number generators are based on the algorithm in a FORTRAN version [3]. Since the PSO algorithm is stochastic algorithm, these functions are essential to initialize and re-initialize the PSO particle positions, velocities, etc.

#### 5. `main.c`: Main file (Driver file)

This file is a driver of the entire program and contains the `main()` function. It performs the following tasks:

- Creates necessary local and global variables.
- Setups random seeds.
- Initializes random number generators.
- Receives PSO parameters from command line.
- Initializes PSO domain.
- Executes optimization functions.
- Writes outputs.

#### 6. `job.sh`: Optional file

## 1.3 Compiling and Executing the Code

Assuming all above mentioned files are in the same directory, the following commands are used to compile and run the program.

### 1.3.1 Compiling the Code

The following command can be used for compiling the code.

```
$g++ main.c pso.c functions.c matmul2.c randomlib.c -o pso
```

It produces `pso` as a binary object.

### 1.3.2 Executing the Code

The following command can be used for executing the code.

### 1.3.2.1 Using Command Line

1. Linux/Mac Machines

```
$ ./pso
```

2. Windows Machines

```
$pso
```

### 1.3.2.2 Using Job Script

If the user chooses to run the program using job script submission, the following commands should be included in the `job.sh` file.

```
#!/bin/bash
#$ -V
#$ -cwd
#$ -j y
#$ -S /bin/bash
#$ -N pso
#$ -q serial
#$ -P hostname
$ ./pso
OR
$pso
```

The job should be submitted using the following command.

```
qsub job.sh
```

## 1.4 Example

We provide an example `main.c` file which is used to minimize the Rosenbrock function. The Rosenbrock function can be defined as follows.

$$f(\mathbf{x}) = \sum_{j=1}^{n-1} [100(x_{j+1} - x_j^2) + (x_j - 1)^2]$$

It has a global minimum value  $f(\mathbf{x}^*) = 0$  at  $\mathbf{x}^* = (1, 1, 1, \dots, 1)$ .



#### 1.4.1 **functions.h** file

```
double Rosenbrock(double * x, int nd);
```

#### 1.4.2 **functions.c** file

```
double Rosenbrock(double * x, int nd) {  
    double sum = 0;  
    int i;  
    for (i=0; i<(nd-1); i++){  
        sum += 100*pow(x[i+1]- pow(x[i],2),2)+pow(x[i]-1,2);  
    }  
    return (sum);  
}
```

### 1.4.3 main.c file

```
#include <stdio.h>
#include <stdlib.h>
#include <string.h>
#include <math.h>
#include <time.h>
#include "randomlib.h"
#include "matmul2.h"
#include "pso.h"
#include "assert.h"
#include "functions.h"

int main(int argc, char*argv[]){
    /*=== Initializing random numbers ===*/
    int i,j,k, seed1,seed2;
    srand((unsigned)time(NULL));
    seed1= rand()%30000; seed2= rand()%30000;
    RandomInitialise(seed1,seed2);

    char funName[80];
    strcpy(funName, "Rosenbrock");
    fptr f = functionLookup(funName);

    /* Rosenbrock function is an objective function
    which is inside "functions.c" file */

    /*=== Setting up PSO parameters ===*/
    int np = 50, nd = 5, ni = 500, maxRun = 10;
    double l = -10, u = 10;
    /*
    np: number of PSO particles
    nd: dimension of the problem to be optimized
    ni: maximum iterations allowed per run
    maxRun: maximum runs (re-starts) allowed
```

```

l: lower bound of each component of the domain
u: upper bound of each component of the domain
*/
/*=== Initializing PSO domain ===*/
double*lb = (double*)malloc(sizeof(double)*nd);
double*ub = (double*)malloc(sizeof(double)*nd);
double *gbest = (double*)malloc(sizeof(double)*nd);
for(i = 0; i < nd; i++){
lb[i] = l; ub[i] = u;
gbest[i] = (ub[i]-lb[i])/3;
}

double start,finish, ellapse_time;
double value = 9999999;

/*=== Start optimization ===*/
start = time(NULL);
mpso_ccd(f, nd, np, ni, maxRun, lb, ub, &value, gbest);
finish= time(NULL);
ellapse_time = difftime(finish, start);

/* === Writing outputs ===*/
printf("\n === PSO Parameters Used ===\n");
printf("Best value obtained: %lf\n",value);
printf("Random seeds: %d, %d\n",seed1,seed2);
printf("Dimension of problem: %d\n",nd);
printf("Number of PSO particles used: %d\n",np);
printf("Maximum iterations per run allowed: %d\n",ni);
printf("Maximum runs allowed : %d\n", maxRun);
printf("Wall-clock time: %lf\n",ellapse_time);
printf("\n === Optimal Solution ===\n");
for(j=0;j<nd;j++){printf("%lf\n", gbest[j]);}
free(lb);free(ub);free(gbest);

```

```
        return 0;
    }
```

#### 1.4.4 Outputs

**\*\*===== PSO Parameters Used =====\*\***

Best value obtained: 0.000000

Random seeds: 18186, 29619

Dimension of problem: 5

Number of PSO particles used: 50

Maximum iterations per run allowed: 500

Maximum runs allowed : 10

Wall-clock time: 0.000000

**\*\*===== Optimal Solution =====\*\***

1.000000

1.000000

1.000000

1.000000

1.000000

## 1.5 Optimization Algorithms

This section provides a brief overview of the optimization algorithms that are used in this program.

### 1.5.1 PSO Algorithm

#### 1.5.1.1 Introduction

The particle swarm optimization algorithm (PSO) is a bio-inspired stochastic optimization technique developed by [2]. It is a population-based search algorithm which mimics the behavior of bird flocking, fish schooling, etc. In the algorithm, the total population is called swarm, and individuals are called particles. Particles are points in the search space of the underlying optimization problem. Consider the PSO system with  $N_p$  particles and  $n$  dimensions. Then the  $i^{th}$  particle maintains a triple of vectors  $(\mathbf{X}_i^{(k)}, \mathbf{V}_i^{(k)}, \mathbf{Y}_i^{(k)}) \in \mathbb{R}^n \times \mathbb{R}^n \times \mathbb{R}^n$  for  $1 \leq i \leq N_p$ , where  $\mathbf{X}_i^{(k)} \in \mathbb{R}^n$  is the current position,  $\mathbf{V}_i^{(k)} \in \mathbb{R}^n$  is the current velocity, and  $\mathbf{Y}_i^{(k)} \in \mathbb{R}^n$  is the personal best position. For simplicity, the dimension of vectors is not written explicitly, which is the same as the dimension of the underlying optimization problem. The velocity and the position of each particle  $i$  are updated by using the following equations[8].

$$\mathbf{V}_i^{(k+1)} = w\mathbf{V}_i^{(k)} + c_1r_1(\mathbf{Y}_i^{(k)} - \mathbf{X}_i^{(k)}) + c_2r_2(\hat{\mathbf{Y}}^{(k)} - \mathbf{X}_i^{(k)}) \quad (1.1)$$

$$\mathbf{X}_i^{(k+1)} = \mathbf{X}_i^{(k)} + \mathbf{V}_i^{(k+1)} \quad (1.2)$$

where  $\hat{\mathbf{Y}}^{(k)}$  represents the global best position and  $r_1, r_2 \in U[0, 1]$  are random numbers chosen from a random uniform distribution  $U[0, 1]$ . There are three components in the velocity equation with corresponding learning parameters  $w, c_1, c_2 \in \mathbb{R}_0^+$  where  $\mathbb{R}_0^+$  is the set of positive real numbers including zero. Here  $w$  is a weight parameter for the inertia component  $w\mathbf{V}_i^{(k)}$ ,  $c_1$  is a parameter for the cognitive component  $c_1r_1(\mathbf{Y}_i^{(k)} - \mathbf{X}_i^{(k)})$ , and  $c_2$  is a parameter for the social component  $c_2r_2(\hat{\mathbf{Y}}^{(k)} - \mathbf{X}_i^{(k)})$ . Parameters  $c_1$  and  $c_2$  are also called acceleration coefficients.

Furthermore, the personal best and the global best positions are updated as follows:

$$\mathbf{Y}_i^{(k+1)} = \begin{cases} \mathbf{X}_i^{(k+1)} & \text{if } f(\mathbf{X}_i^{(k+1)}) < f(\mathbf{Y}_i^{(k)}) \\ \mathbf{Y}_i^{(k)} & \text{otherwise} \end{cases} \quad (1.3)$$

$$\hat{\mathbf{Y}}^{(k+1)} = \arg \min \{f(\mathbf{Y}_1^{(k+1)}), f(\mathbf{Y}_2^{(k+1)}), \dots, f(\mathbf{Y}_{N_p}^{(k+1)})\} \quad (1.4)$$

The PSO algorithm has been successfully applied to many optimization problems such as pattern recognition, clustering, classification, neural network training, sensor networks, scheduling, robotics, signal processing, and power systems [4]. Because of the easy implementation and fast convergence to acceptable solutions, the PSO algorithm has received popularity in recent years [4].

### 1.5.1.2 Implementation of the PSO Algorithm

**Name:** `pso()`

**Purpose:** to minimize a multi-dimensional optimization problem using the standard PSO algorithm.

**Usage:** `void pso(double (*fn)(double* x, int nd), int nd, int np, int ni, double* lb, double* ub, double* value, double* gbest)`

**Arguments:**

- `fn` - function to be minimized with the following arguments:
- `nd` - dimension of the problem (Input).
- `np` - number of particles (Input).
- `ni` - maximum number of iterations allowed (Input).
- `lb` - vector of length `nd` which consists lower bounds domain (Input).
- `ub` - vector of length `nd` which consists upper bounds of domain (Input).
- `value` - function value at the `gbest` (Input/Output).
- `gbest` - vector of length `nd` containing the best estimate of the minimum found (Input/Output).

## 1.5.2 CCD Algorithm

### 1.5.2.1 Introduction

The CCD algorithm uses the coordinates of  $\mathbb{R}^n$  as the search directions and searches along one coordinate at a time while fixing the other coordinates. Starting with an initial guess  $\mathbf{x}^{(1)} = (\mathbf{x}_1^{(1)}, \mathbf{x}_2^{(1)}, \mathbf{x}_3^{(1)} \dots, \mathbf{x}_n^{(1)})$ , the next estimate  $\mathbf{x}^{(k+1)}$  is obtained from  $\mathbf{x}^{(k)}$  by iteratively solving the following one dimensional optimization problems:

$$\mathbf{x}_j^{k+1} = \arg \min_{t \in \mathbb{R}} f(\mathbf{x}_1^{k+1}, \dots, \mathbf{x}_{j-1}^{k+1}, t, \mathbf{x}_{j+1}^k, \dots, \mathbf{x}_n^k)$$

for  $j = 1, 2, \dots, n$ . Therefore, a sequence of points  $\mathbf{x}^{(1)}, \mathbf{x}^{(2)}, \mathbf{x}^{(3)}, \dots$  are generated iteratively so that

$$f(\mathbf{x}^{(1)}) \geq f(\mathbf{x}^{(2)}) \geq f(\mathbf{x}^{(3)}) \geq \dots$$

The CCD algorithm like steepest descent converges to a stationary point if the objective function  $f$  is differentiable. However, for non-differentiable functions, the algorithm can stall at a point which may not be a stationary point, leading to premature termination [5]. One of the reasons for such behavior might be because of the presence of a valley caused by non-differentiability. This issue can be resolved by using a strategy, called *acceleration step* [5].

### 1.5.2.2 Implementation of the CCD Algorithm

This is a local search algorithm, which is used to refine the solution obtained from the PSO algorithm.

**Name:** `ccd_local_optimizer()`

**Purpose:** to minimize multi-dimensional function using cyclic coordinate descent (CCD) algorithm.

Usage: **void** ccd\_local\_optimizer(**double** (\*fun) (**double\*** y, **int** nd),  
**int** nd, **double\*** lb, **double\*** ub,  
**double\*** value, **double\*** x

Arguments:

- fun - function to be minimized (Input).
- nd - dimension of the problem (Input).
- lb - vector of length nd which consists lower bounds of domain (Input).
- ub - vector of length nd which consists upper bounds of domain (Input).
- value - function value (Input/Output).
- x - initial guess (Input/Output).

### 1.5.3 Brent Algorithm

#### 1.5.3.1 Introduction

The Brent algorithm [6] combines the bisection method, secant method, and inverse quadratic interpolation and searches for a function minimum over the given range. It was derived from an earlier algorithm by Theodorus Dekker [7]. In our implementation, the original Brent algorithm has been slightly modified, where the golden section method is used instead of the secant method. Therefore, the modified Brent algorithm combines golden section, bisection, and quadratic interpolation methods. It has the ability to switch between gold section and quadratic interpolation during the execution. It converges super-linearly at a rate of about 1.324 to the solution as long as a solution exists within the specified interval. The following are the inputs and outputs of Brent algorithm.

**Inputs:** The Brent algorithm works in the interval domain  $[l, u]$  with lower bound  $l$  and upper bound  $u$ ,  $l < u$ , so that the minimum will be searched over a range  $[l, u]$ . The objective function for the algorithm is a univariate function  $g(x)$ ,  $x \in [l, u]$ . An acceptable tolerance  $tol > 0$  is provided as a termination criterion.

**Outputs:** The algorithm returns an estimate  $x$  for the local minimum of  $g$  with accuracy:  $3\sqrt{\epsilon}|x| + tol$  where  $\sqrt{\epsilon} = 10^{-6}$ . It obtains an estimate of a local minimum



of the objective function which coincides with the global minimum only if the function is unimodal. If the function does not have local minimum within the given range, it returns  $l$  if  $g(l) < g(u)$ , otherwise it returns  $u$ .

### 1.5.3.2 Implementation of the Brent Algorithm

This function is supplied into `ccd_local_optimizer()` to perform one dimensional line search using the Brent algorithm.

**Name:** `brent_algorithm()`

**Purpose:** to minimize one dimensional function using a Brent algorithm.

**Usage:** `double brent_algorithm(double l, double u, double (*g)(double t), double tol)`

**Arguments:**

- $l$  - lower bound of the interval  $[l, u]$  (Input).
- $u$  - upper bound of the interval  $[l, u]$  (Input).
- $g$  - one dimensional function to be minimized.
- $tol$  - Acceptable tolerance for the minimum location.

## 1.5.4 MPSO-CCD Algorithm

### 1.5.4.1 Introduction

To improve the performance of the PSO algorithm, a multi-start approach can be used where the standard PSO (i.e `ps()`) is repeated multiple times by re-initializing the particles. After each run, the global best position is recorded and re-used as an initial guess for the next run. The particles are re-initialized in the entire search space and the standard PSO is executed again for the next run. This process is repeated multiple times and has the ability to generate points in each part of the search space, increasing the exploration. This strategy significantly improves the global search capability of the standard PSO algorithm. However, it still lacks the ability to exploit the local domain as compared with some existing local search algorithms. To increase the

local search ability, we combine the PSO algorithm with the CCD algorithm to make a new hybrid algorithm, called MPSO-CCD. It increases both exploration as well as exploitation abilities.

#### 1.5.4.2 Implementation of the MPSO-CCD Algorithm

This algorithm calls the `pso()` and `ccd_local_optimizer()` repeatedly. First, the best estimate `gbest` is obtained by using the `pso()` algorithm. Then the `gbest` vector is provided to the `ccd_local_optimizer()` as an initial guess. It further improves the estimate using the `brent_algorithm()`. This process is repeated `maxRun` times and can be summarized as follows.

Step 1: Apply `pso()`

Step 2: Apply `ccd_local_optimizer()`

Step 3: Repeat Step 1 and Step 2 `maxRun` times or until early criterion criterion is reached.

**Name:** `mpso_ccd()`

**Purpose:** to minimize a multi-dimensional optimization problem.

**Usage:** `void mpso_ccd(double (*fn)(double* x, int nd),  
int nd, int np, int ni, int maxRun,  
double* lb, double* ub, double* value, double* gbest)`

**Arguments:**

- `fn` - function to be minimized (Input).
- `nd` - dimension of the problem (Input).
- `np` - number of particles (Input).
- `ni` - maximum number of iterations per run is allowed (Input).
- `maxRun` - maximum number of runs is allowed (Input).
- `lb` - vector of length `nd` which consists lower bounds domain (Input).

- `ub` - vector of length `nd` which consists upper bounds of domain (Input).
- `value` - function value at the `gbest` (Input/Output).
- `gbest` - vector of length `nd` containing the best estimate of the minimum found (Input/Output).

## 1.6 Supportive Functions

### 1.6.1 Supportive Functions for PSO

Some additional supportive functions are necessary to implement MPSO-CCD algorithm. These functions are supplied to perform some specific tasks such as initializing domain, checking boundary of domain, adjusting domain, etc.

1. **void** update\_best(**double** \* g, **double** \* x, **int** nd)  
    **double\*** ub, **int** nd)
2. **int** lower\_bound\_check(**double** g, **double** l,  
    **double** u, **double** epsilon)
3. **int** upper\_bound\_check(**double** g, **double** l,  
    **double** u, **double** epsilon)

### 1.6.2 Math Related Functions

Some math related functions are also necessary to facilitate the PSO algorithm implementation such as matrix multiplications, transposing matrix, etc. The c code of these functions are included in the file matmul2.c and corresponding function headers are included in the file matmul2.h.

1. **struct** matrix { **double** \*\* mat; **int** row; **int** col };
2. **struct** matrix \* get\_matrix( **int** row , **int** col)
3. **struct** matrix \* matrix\_mult( **struct** matrix\* m1,  
    **struct** matrix\* m2)
4. **struct** matrix \* transpose( **struct** matrix \* m )
5. **double** \*\* get\_mat( **int** row , **int** col)
6. **void** free\_matrix( **struct** matrix \* m)
7. **struct** matrix \* readmatrix( **char\*** filename,  
    **int** nrow, **int** ncol)

8. **void** write\_matrix( **char\*** filename, **struct matrix \*** m)

### 1.6.3 Random Number Generators

The files randomlib.c and randomlib.h contain some functions related to random number generators.

1. **void** RandomInitialise(**int** seed1, **int** seed2)
2. **double** RandomUniform(**void**)
3. **double** RandomGaussian(**double** a, **double** b)
4. **int** RandomInt(**int** n1, **int** n2)
5. **double** RandomDouble(**double** a, **double** b)

## Chapter 2

# Parallel Implementation

### 2.1 Required Files

The following are the files required to implement the parallel version of the MPSO-CCD algorithm. We call this parallel algorithm as PMPSO-CCD. All files must be in the same directory, say “mpso\_ccd\_parallel”.

#### 2.1.1 Header Files

1. Basic C Libraries.

`stdio.h`, `stdlib.h`, `string.h`, `math.h`, `time.h`, `assert.h`

2. MPI Library.

`mpi.h`

3. Program Related Header files.

`mpipso.h`   `functions.h`   `randomlib.h`   `matmul2.h`

#### 2.1.2 C Files

1. `mpipso.c`: PSO related functions file.

This file contains the function headers of optimization algorithms such as parallel PSO, CCD, Brent algorithm, parallel MPSO-CCD algorithm, and some other supportive functions. The corresponding function headers are included in `mpipso.h` file.

2. `functions.c`: Objective functions file.

This file is the same as that was in the serial case.

3. `matmul2.c`: Math related functions file.

This file is the same as that was in the serial case.

4. `randomlib.c`: Random numbers generators.

This file is the same as that was in the serial case.

5. `mpimain.c`: Main file (Driver file)

This file is a driver of the entire program and contains the `main()` function. It performs the following tasks:

- Creates necessary local and global variables.
- Setups random seeds.
- Initializes random number generators.
- Receives PSO parameters from command line.
- Setups MPI environment.
- Initializes PSO domain.
- Executes optimization functions.
- Writes outputs.

6. `mpijob.sh`: Optional file

## 2.2 Compiling and Executing the Parallel Code

Assuming all above mentioned files are in the same directory, the following commands are used to compile and run the program.

### 2.2.1 Compiling the Parallel Code

The following command can be used for compiling the parallel code.

Step 1: `$module load intel`

Step 2: `$load impi`

Step 3:

```
$mpicc -o mpipso mpimain.c matmul2.c, randomlib.c mpipso.c
functions.c -lm
```

It produces mpipso as a binary object.

## 2.2.2 Executing the Parallel Code

The following command can be used for executing the code.

### 2.2.2.1 Using Command Line

```
$mpirun -np Ncores ./mpipso
```

### 2.2.2.2 Using Job Script

If the user chooses to run the program using job script submission, the following commands should be included in the mpijob.sh file.

```
#!/bin/bash
#$ -V
#$ -cwd
#$ -j y
#$ -S /bin/bash
#$ -N mpipso
#$ -o $JOB_NAME.o$JOB_ID
#$ -e $JOB_NAME.e$JOB_ID
#$ -q queue type
#$ -pe fill num_processors
#$ -P hostname
module load intel impi
mpirun--machinefile machinefile.$JOB_ID -np $NSLOTS
./mpipso
```

The job should be submitted using the following command.

```
qsub mpijob.sh
```

## 2.3 Parallel PSO Versions

The PSO algorithm can be executed in parallel by using some additional MPI commands in the existing serial code. The parallel versions of the PSO are very similar to



their corresponding serial versions except one additional argument, called myrank. This additional argument is used to keep track of processor rank.

#### 1. Parallel PSO: **mpipso()**

Usage: **void mpipso(double (\*fn)(double\* x, int nd), int nd, int np, int ni, double\* lb, double\* ub, double\* value, double\* gbest, int myrank)**

#### 2. Parallel MPSO-CCD: **pmpso\_ccd()**

Usage: **void pmpso\_ccd(double (\*fn)(double\* x, int nd), int nd, int np, int ni, int maxRun, double\* lb, double\* ub, double\* value, double\* gbest, int myrank )**

## 2.4 Example of Parallel Implementation

We provide an example `mpimain.c` file which is used to minimize the Rosenbrock function. The `functions.h` file and `functions.c` file are the same as that were in the serial case.

### 2.4.1 **mpimain.c** file

```
#include <stdio.h>
#include <stdlib.h>
#include <string.h>
#include "mpi.h"
#include <math.h>
#include <time.h>
#include "randomlib.h"
#include "matmul2.h"
#include "pso.h"
#include "assert.h"
```

```
#include "functions.h"

int main(int argc, char*argv[]){
    /*=== Initializing random numbers ===*/
    int i,j,k, seed1, seed2;
    srand((unsigned)time(NULL));
    seed1= rand()%30000; seed2= rand()%30000;

    char funName[80];
    strcpy(funName, "Rosenbrock");
    fptr f = functionLookup(funName);
    /* Rosenbrock function is an objective function
    which is inside "functions.c" file */

    /*=== Setting up PSO parameters ===*/
    int np = 50, nd = 5, ni = 500, maxRun = 10;
    double l = -10, u = 10;
    /*
    np: number of PSO particles
    nd: dimension of the problem to be optimized
    ni: maximum iterations allowed per run
    maxRun: maximum runs (re-starts) allowed
    l: lower bound of each component of the domain
    u: upper bound of each component of the domain
    */
    /*=== Initializing PSO domain ===*/
    double*lb = (double*)malloc(sizeof(double)*nd);
    double*ub = (double*)malloc(sizeof(double)*nd);
    double *gbest = (double*)malloc(sizeof(double)*nd);
    for(i = 0; i < nd; i++){
        lb[i] = l; ub[i] = u;
        gbest[i] = (ub[i]-lb[i])/3;
    }
    /*==== Setting up MPI environment =====*/
```

```

int myrank, comsize;
MPI_Init(&argc, &argv);
MPI_Comm_size(MPLCOMM_WORLD, &comsize);
MPI_Comm_rank(MPLCOMM_WORLD, &myrank);
MPI_Barrier(MPLCOMM_WORLD);

RandomInitialise(myrank + seed1, seed2);

double start, finish, ellapse_time;
double value = 9999999;

/*=== Start optimization ===*/
start = MPI_Wtime(NULL);
pmpso_ccd(f, nd, np, ni, maxRun, lb, ub, &value, gbest, myrank);
finish = MPI_Wtime(NULL);
ellapse_time = difftime(finish, start);

/* == Writing outputs == */
if(myrank == 0){
printf("\n == PSO Parameters Used ==\n");
printf("Best value obtained: %lf\n", value);
printf("Random seeds: %d, %d\n", seed1, seed2);
printf("Number of processors used: %d\n", comsize);
printf("Dimension of problem: %d\n", nd);
printf("Number of PSO particles used: %d\n", np);
printf("Maximum iterations per run allowed: %d\n", ni);
printf("Maximum runs allowed : %d\n", maxRun);
printf("Wall-clock time: %lf\n", ellapse_time);

printf("\n*===== Optimal Solution =====*\n");
for(j=0;j<nd;j++){printf("%lf\n", gbest[j]);}
}
MPI_Finalize();
free(lb); free(ub); free(gbest);

```

```
        return 0;  
    }
```

## 2.5 Source Code

The complete source code of both serial and parallel implementation can be found on GitHub: [https://github.com/humnath5/MPSO-CCD\\_Package](https://github.com/humnath5/MPSO-CCD_Package).

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