

**EECS2040 Data Structure Hw #6 (Chapter 7 Sorting, Chapter 8 Hashing)**  
**due date 6/27/2021,by 108061217 鍾永恒**

**Part 2 Coding**

You should submit:

- (a) All your source codes (C++ file).
- (b) Show the execution trace of your program.

1. (50%) **Sorting:**

Write a C++ program to perform 5 different sorting , **insertion sort**, **median-of-three quick sort**, **iterative merge sort**, **recursive merge sort**, and **heap sort**, on lists of characters, integer, floating point numbers, and C++ strings.

- a. You need to write the 5 sorting **function templates** (refer to example programs in textbook or pptx)
- b. Randomly generate a list of 20 characters as an input unsorted list.
- c. Randomly generate a list of 20 integers as an input unsorted list.
- d. Randomly generate a list of 20 floats as an input unsorted list.
- e. Randomly generate a list of 20 string objects as an input unsorted list.

**Show your results** using the above 3 lists in your program.

ANS:

## List of characters:

```
InsertionSort:
I,X,W,p,l,h,o,s,p,o,P,I,w,P,N,v,H,X,w,B,
I,X,W,p,l,h,o,s,p,o,P,I,w,P,N,v,H,X,w,B,
I,W,X,p,l,h,o,s,p,o,P,I,w,P,N,v,H,X,w,B,
I,W,X,p,l,h,o,s,p,o,P,I,w,P,N,v,H,X,w,B,
I,W,X,l,p,h,o,s,p,o,P,I,w,P,N,v,H,X,w,B,
I,W,X,h,l,p,o,s,p,o,P,I,w,P,N,v,H,X,w,B,
I,O,W,X,h,l,p,s,p,o,P,I,w,P,N,v,H,X,w,B,
I,O,W,X,h,l,p,s,p,o,P,I,w,P,N,v,H,X,w,B,
I,O,W,X,h,l,p,p,s,o,P,I,w,P,N,v,H,X,w,B,
I,O,O,W,X,h,l,p,p,s,P,I,w,P,N,v,H,X,w,B,
I,O,O,P,W,X,h,l,p,p,s,I,w,P,N,v,H,X,w,B,
I,I,O,O,P,W,X,h,l,p,p,s,w,P,N,v,H,X,w,B,
I,I,O,O,P,W,X,h,l,p,p,s,w,P,N,v,H,X,w,B,
I,I,O,O,P,W,X,h,l,p,p,s,w,N,v,H,X,w,B,
I,I,N,O,O,P,P,W,X,h,l,p,p,s,w,v,H,X,w,B,
I,I,N,O,O,P,P,W,X,h,l,p,p,s,v,w,H,X,w,B,
H,I,I,N,O,O,P,P,W,X,h,l,p,p,s,v,w,X,w,B,
H,I,I,N,O,O,P,P,W,X,X,h,l,p,p,s,v,w,w,B,
H,I,I,N,O,O,P,P,W,X,X,h,l,p,p,s,v,w,w,B,
B,H,I,I,N,O,O,P,P,W,X,X,h,l,p,p,s,v,w,w,
final list
B,H,I,I,N,O,O,P,P,W,X,X,h,l,p,p,s,v,w,w,

generate another list
QuickSort:
l,q,X,x,l,y,v,x,i,Y,m,S,Y,k,k,J,R,a,B,i,
l,i,X,x,l,y,v,x,i,Y,m,S,Y,k,k,J,R,a,B,q,
l,i,X,B,l,y,v,x,i,Y,m,S,Y,k,k,J,R,a,x,q,
l,i,X,B,a,y,v,x,i,Y,m,S,Y,k,k,J,R,l,x,q,
l,i,X,B,a,R,v,x,i,Y,m,S,Y,k,k,J,y,l,x,q,
l,i,X,B,a,R,J,X,i,Y,m,S,Y,k,k,v,y,l,x,q,
l,i,X,B,a,R,J,X,i,Y,k,S,Y,k,m,v,y,l,x,q,
k,i,X,B,a,R,J,X,i,Y,k,S,Y,l,m,v,y,l,x,q,
k,i,X,B,a,R,J,X,i,Y,Y,S,k,l,m,v,y,l,x,q,
S,i,X,B,a,R,J,X,i,Y,Y,k,k,l,m,v,y,l,x,q,
S,J,X,B,a,R,i,X,i,Y,Y,k,k,l,m,v,y,l,x,q,
S,J,R,B,a,X,i,X,i,Y,Y,k,k,l,m,v,y,l,x,q,
B,J,R,S,a,X,i,X,i,Y,Y,k,k,l,m,v,y,l,x,q,
B,J,R,S,a,X,i,X,i,Y,Y,k,k,l,m,v,y,l,x,q,
B,J,R,S,a,X,i,X,i,Y,Y,k,k,l,m,v,y,l,x,q,
B,J,R,S,a,X,Y,X,i,Y,i,k,k,l,m,v,y,l,x,q,
B,J,R,S,a,X,Y,X,Y,i,i,k,k,l,m,v,y,l,x,q,
B,J,R,S,Y,X,Y,X,a,i,i,k,k,l,m,v,y,l,x,q,
B,J,R,S,Y,X,X,Y,a,i,i,k,k,l,m,v,y,l,x,q,
B,J,R,S,X,X,Y,Y,a,i,i,k,k,l,m,v,y,l,x,q,
B,J,R,S,X,X,Y,Y,a,i,i,k,k,l,m,v,y,l,x,q,
B,J,R,S,X,X,Y,Y,a,i,i,k,k,l,m,y,v,x,q,
B,J,R,S,X,X,Y,Y,a,i,i,k,k,l,m,q,v,x,y,
B,J,R,S,X,X,Y,Y,a,i,i,k,k,l,m,q,v,x,y,
final list
B,J,R,S,X,X,Y,Y,a,i,i,k,k,l,m,q,v,x,y,
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generate another list
iterative merge sort:
o,s,q,l,k,E,g,T,D,E,U,o,u,r,N,I,S,J,f,A,
o,s,l,q,E,k,T,g,D,E,U,o,r,u,I,N,J,S,A,f,
l,o,q,s,E,T,g,k,D,E,U,o,I,N,r,u,A,J,S,f,
E,T,g,k,l,o,q,s,D,E,I,N,U,o,r,u,A,J,S,f,
D,E,E,I,N,T,U,g,k,l,o,o,q,r,s,u,A,J,S,f,
A,D,E,E,I,J,N,S,T,U,f,g,k,l,o,o,q,r,s,u,
final list
A,D,E,E,I,J,N,S,T,U,f,g,k,l,o,o,q,r,s,u,

generate another list

recursive merge sort:
link:
6,18,3,10,11,15,4,12,16,5,19,20,14,7,0,1,17,9,13,8,
final list
D,F,G,H,R,T,U,U,X,Y,c,d,e,f,h,n,o,q,u,w,

generate another list

HeapSort:
y,y,v,w,r,u,t,o,u,C,g,D,l,W,J,Y,O,b,Y,B,
y,w,v,u,r,u,t,o,b,C,g,D,l,W,J,Y,O,B,Y,y,
w,u,v,o,r,u,t,Y,b,C,g,D,l,W,J,Y,O,B,Y,y,
v,u,u,o,r,l,t,Y,b,C,g,D,B,W,J,Y,O,w,Y,y,
u,r,u,o,g,l,t,Y,b,C,O,D,B,W,J,Y,v,w,Y,y,
u,r,t,o,g,l,Y,Y,b,C,O,D,B,W,J,u,v,w,Y,y,
t,r,l,o,g,J,Y,Y,b,C,O,D,B,W,u,u,v,w,Y,y,
r,o,l,b,g,J,Y,Y,W,C,O,D,B,t,u,u,v,w,Y,y,
o,g,l,b,O,J,Y,Y,W,C,B,D,r,t,u,u,v,w,Y,y,
l,g,Y,b,O,J,D,Y,W,C,B,o,r,t,u,u,v,w,Y,y,
g,b,Y,Y,O,J,D,B,W,C,l,o,r,t,u,u,v,w,Y,y,
b,Y,Y,W,O,J,D,B,C,g,l,o,r,t,u,u,v,w,Y,y,
Y,W,Y,C,O,J,D,B,b,g,l,o,r,t,u,u,v,w,Y,y,
Y,W,J,C,O,B,D,Y,b,g,l,o,r,t,u,u,v,w,Y,y,
W,O,J,C,D,B,Y,Y,b,g,l,o,r,t,u,u,v,w,Y,y,
O,D,J,C,B,W,Y,Y,b,g,l,o,r,t,u,u,v,w,Y,y,
J,D,B,C,O,W,Y,Y,b,g,l,o,r,t,u,u,v,w,Y,y,
D,C,B,J,O,W,Y,Y,b,g,l,o,r,t,u,u,v,w,Y,y,
C,B,D,J,O,W,Y,Y,b,g,l,o,r,t,u,u,v,w,Y,y,
final list
B,C,D,J,O,W,Y,Y,b,g,l,o,r,t,u,u,v,w,Y,y,
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## List of integers:

```
InsertionSort:
374,197,312,267,364,46,132,404,118,487,490,159,181,183,145,261,424,421,2,392,
197,374,312,267,364,46,132,404,118,487,490,159,181,183,145,261,424,421,2,392,
197,312,374,267,364,46,132,404,118,487,490,159,181,183,145,261,424,421,2,392,
197,267,312,374,364,46,132,404,118,487,490,159,181,183,145,261,424,421,2,392,
197,267,312,364,374,46,132,404,118,487,490,159,181,183,145,261,424,421,2,392,
46,197,267,312,364,374,132,404,118,487,490,159,181,183,145,261,424,421,2,392,
46,132,197,267,312,364,374,404,118,487,490,159,181,183,145,261,424,421,2,392,
46,132,197,267,312,364,374,404,118,487,490,159,181,183,145,261,424,421,2,392,
46,118,132,197,267,312,364,374,404,487,490,159,181,183,145,261,424,421,2,392,
46,118,132,197,267,312,364,374,404,487,490,159,181,183,145,261,424,421,2,392,
46,118,132,197,267,312,364,374,404,487,490,159,181,183,145,261,424,421,2,392,
46,118,132,159,197,267,312,364,374,404,487,490,181,183,145,261,424,421,2,392,
46,118,132,159,181,197,267,312,364,374,404,487,490,183,145,261,424,421,2,392,
46,118,132,159,181,183,197,267,312,364,374,404,487,490,145,261,424,421,2,392,
46,118,132,145,159,181,183,197,267,312,364,374,404,487,490,261,424,421,2,392,
46,118,132,145,159,181,183,197,261,267,312,364,374,404,424,487,490,421,2,392,
46,118,132,145,159,181,183,197,261,267,312,364,374,404,421,424,487,490,2,392,
2,46,118,132,145,159,181,183,197,261,267,312,364,374,404,421,424,487,490,392,
2,46,118,132,145,159,181,183,197,261,267,312,364,374,392,404,421,424,487,490,
final list
2,46,118,132,145,159,181,183,197,261,267,312,364,374,392,404,421,424,487,490,

generate another list
QuickSort:
212,490,192,0,205,129,422,93,305,295,296,31,344,108,151,209,154,283,113,124,
212,124,192,0,205,129,422,93,305,295,296,31,344,108,151,209,154,283,113,490,
212,124,192,0,205,129,113,93,305,295,296,31,344,108,151,209,154,283,422,490,
212,124,192,0,205,129,113,93,154,295,296,31,344,108,151,209,305,283,422,490,
212,124,192,0,205,129,113,93,154,209,296,31,344,108,151,295,305,283,422,490,
212,124,192,0,205,129,113,93,154,209,151,31,344,108,296,295,305,283,422,490,
212,124,192,0,205,129,113,93,154,209,151,31,108,344,296,295,305,283,422,490,
108,124,192,0,205,129,113,93,154,209,151,31,212,344,296,295,305,283,422,490,
108,31,192,0,205,129,113,93,154,209,151,124,212,344,296,295,305,283,422,490,
108,31,93,0,205,129,113,192,154,209,151,124,212,344,296,295,305,283,422,490,
0,31,93,108,205,129,113,192,154,209,151,124,212,344,296,295,305,283,422,490,
0,31,93,108,205,129,113,192,154,209,151,124,212,344,296,295,305,283,422,490,
0,31,93,108,205,129,113,192,154,124,151,209,212,344,296,295,305,283,422,490,
0,31,93,108,151,129,113,192,154,124,205,209,212,344,296,295,305,283,422,490,
0,31,93,108,151,129,113,124,154,192,205,209,212,344,296,295,305,283,422,490,
0,31,93,108,124,129,113,151,154,192,205,209,212,344,296,295,305,283,422,490,
0,31,93,108,113,124,129,151,154,192,205,209,212,344,296,295,305,283,422,490,
0,31,93,108,113,124,129,151,154,192,205,209,212,283,296,295,305,344,422,490,
0,31,93,108,113,124,129,151,154,192,205,209,212,283,296,295,305,344,422,490,
0,31,93,108,113,124,129,151,154,192,205,209,212,283,295,296,305,344,422,490,
final list
0,31,93,108,113,124,129,151,154,192,205,209,212,283,295,296,305,344,422,490,

generate another list
iterative merge sort:
122,103,283,155,138,280,416,415,201,418,159,413,409,351,266,466,332,188,411,489
103,122,155,283,138,280,415,416,201,418,159,413,351,409,266,466,188,332,411,489
103,122,155,283,138,280,415,416,159,201,413,418,266,351,409,466,188,332,411,489
103,122,138,155,280,283,415,416,159,201,266,351,409,413,418,466,188,332,411,489
103,122,138,155,159,201,266,280,283,351,409,413,415,416,418,466,188,332,411,489
103,122,138,155,159,188,201,266,280,283,332,351,409,411,413,415,416,418,466,489
final list
103,122,138,155,159,188,201,266,280,283,332,351,409,411,413,415,416,418,466,489

generate another list
483 207 20 328 316 171 389 322 306 354 447 428 309 82 83 448 215 351 215 416
recursive merge sort:
link:
3,0,17,14,18,8,2,20,4,13,7,16,11,5,15,6,1,19,10,9,
final list
20,82,83,171,207,215,215,306,309,316,322,328,351,354,389,416,428,447,448,483,

generate another list
270 374 330 31 77 448 349 409 136 260 398 472 320 418 152 488 442 41 162 248
HeapSort:
488,442,472,409,398,448,418,374,162,260,77,330,320,349,152,270,31,41,136,248,
472,442,448,409,398,330,418,374,162,260,77,248,320,349,152,270,31,41,136,488,
448,442,418,409,398,330,349,374,162,260,77,248,320,136,152,270,31,41,472,488,
442,409,418,374,398,330,349,270,162,260,77,248,320,136,152,41,31,448,472,488,
418,409,349,374,398,330,152,270,162,260,77,248,320,136,31,41,442,448,472,488,
409,398,349,374,260,330,152,270,162,41,77,248,320,136,31,418,442,448,472,488,
398,374,349,270,260,330,152,31,162,41,77,248,320,136,409,418,442,448,472,488,
374,270,349,162,260,330,152,31,136,41,77,248,320,398,409,418,442,448,472,488,
349,270,330,162,260,320,152,31,136,41,77,248,374,398,409,418,442,448,472,488,
330,270,320,162,260,248,152,31,136,41,77,349,374,398,409,418,442,448,472,488,
320,270,248,162,260,77,152,31,136,41,330,349,374,398,409,418,442,448,472,488,
270,260,248,162,41,77,152,31,136,320,330,349,374,398,409,418,442,448,472,488,
260,162,248,136,41,77,152,31,270,320,330,349,374,398,409,418,442,448,472,488,
248,162,152,136,41,77,31,260,270,320,330,349,374,398,409,418,442,448,472,488,
162,136,152,31,41,77,248,260,270,320,330,349,374,398,409,418,442,448,472,488,
152,136,77,31,41,162,248,260,270,320,330,349,374,398,409,418,442,448,472,488,
136,41,77,31,152,162,248,260,270,320,330,349,374,398,409,418,442,448,472,488,
77,41,31,136,152,162,248,260,270,320,330,349,374,398,409,418,442,448,472,488,
41,31,77,136,152,162,248,260,270,320,330,349,374,398,409,418,442,448,472,488,
final list
31,41,77,136,152,162,248,260,270,320,330,349,374,398,409,418,442,448,472,488,
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## List of floating point numbers:

```
InsertionSort:
4.84,4.53,1.96,0.26,3.21,3.21,0.67,4.44,3.46,0.09,3.52,1.23,4.75,2.14,2.26,2.82,0.53,1.39,3.92,0.22,
4.53,4.84,1.96,0.26,3.21,3.21,0.67,4.44,3.46,0.09,3.52,1.23,4.75,2.14,2.26,2.82,0.53,1.39,3.92,0.22,
1.96,4.53,4.84,0.26,3.21,3.21,0.67,4.44,3.46,0.09,3.52,1.23,4.75,2.14,2.26,2.82,0.53,1.39,3.92,0.22,
0.26,1.96,4.53,4.84,3.21,3.21,0.67,4.44,3.46,0.09,3.52,1.23,4.75,2.14,2.26,2.82,0.53,1.39,3.92,0.22,
0.26,1.96,3.21,4.53,4.84,3.21,0.67,4.44,3.46,0.09,3.52,1.23,4.75,2.14,2.26,2.82,0.53,1.39,3.92,0.22,
0.26,1.96,3.21,3.21,4.53,4.84,4.44,3.46,0.09,3.52,1.23,4.75,2.14,2.26,2.82,0.53,1.39,3.92,0.22,
0.26,0.67,1.96,3.21,3.21,4.44,4.53,4.84,3.46,0.09,3.52,1.23,4.75,2.14,2.26,2.82,0.53,1.39,3.92,0.22,
0.26,0.67,1.96,3.21,3.21,3.46,4.44,4.53,4.84,0.09,3.52,1.23,4.75,2.14,2.26,2.82,0.53,1.39,3.92,0.22,
0.09,0.26,0.67,1.96,3.21,3.21,3.46,4.44,4.53,4.84,3.52,1.23,4.75,2.14,2.26,2.82,0.53,1.39,3.92,0.22,
0.09,0.26,0.67,1.96,3.21,3.21,3.46,3.52,4.44,4.53,4.84,1.23,4.75,2.14,2.26,2.82,0.53,1.39,3.92,0.22,
0.09,0.26,0.67,1.23,1.96,3.21,3.21,3.46,3.52,4.44,4.53,4.84,4.75,2.14,2.26,2.82,0.53,1.39,3.92,0.22,
0.09,0.26,0.67,1.23,1.96,3.21,3.21,3.46,3.52,4.44,4.53,4.75,4.84,2.14,2.26,2.82,0.53,1.39,3.92,0.22,
0.09,0.26,0.67,1.23,1.96,2.14,2.26,3.21,3.21,3.46,3.52,4.44,4.53,4.75,4.84,2.82,0.53,1.39,3.92,0.22,
0.09,0.26,0.67,1.23,1.96,2.14,2.26,2.82,3.21,3.21,3.46,3.52,4.44,4.53,4.75,4.84,0.53,1.39,3.92,0.22,
0.09,0.26,0.53,0.67,1.23,1.39,1.96,2.14,2.26,2.82,3.21,3.21,3.46,3.52,4.44,4.53,4.75,4.84,3.92,0.22,
0.09,0.26,0.53,0.67,1.23,1.39,1.96,2.14,2.26,2.82,3.21,3.21,3.46,3.52,3.92,4.44,4.53,4.75,4.84,0.22,
0.09,0.22,0.26,0.53,0.67,1.23,1.39,1.96,2.14,2.26,2.82,3.21,3.21,3.46,3.52,3.92,4.44,4.53,4.75,4.84,
final list
0.09,0.22,0.26,0.53,0.67,1.23,1.39,1.96,2.14,2.26,2.82,3.21,3.21,3.46,3.52,3.92,4.44,4.53,4.75,4.84,
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```
generate another list
QuickSort:
0.19,2.71,2.4,4.46,1.97,2.77,1.61,0.47,1.87,2.74,2.66,0.23,2.27,4.62,0.49,4.01,1.35,1.17,1.97,4.82,
0.19,2.71,2.4,4.46,1.97,2.77,1.61,0.47,1.87,2.74,2.66,0.23,2.27,4.62,0.49,4.01,1.35,1.17,1.97,4.82,
0.19,2.71,2.1,1.97,1.97,2.77,1.61,0.47,1.87,2.74,2.66,0.23,2.27,4.62,0.49,4.01,1.35,1.17,4.46,4.82,
0.19,2.71,2.1,1.97,1.97,1.17,1.61,0.47,1.87,2.74,2.66,0.23,2.27,4.62,0.49,4.01,1.35,2.77,4.46,4.82,
0.19,2.71,2.1,1.97,1.97,1.17,1.61,0.47,1.87,1.35,2.66,0.23,2.27,4.62,0.49,4.01,2.74,2.77,4.46,4.82,
0.19,2.71,2.1,1.97,1.97,1.17,1.61,0.47,1.87,1.35,2.66,0.23,2.27,4.62,0.49,4.01,2.74,2.77,4.46,4.82,
0.19,0.49,2.1,1.97,1.97,1.17,1.61,0.47,1.87,1.35,2.66,0.23,2.27,2.71,4.62,4.01,2.74,2.77,4.46,4.82,
0.19,0.49,0.23,1.97,1.97,1.17,1.61,0.47,1.87,1.35,2.66,2.2,2.27,2.71,4.62,4.01,2.74,2.77,4.46,4.82,
0.19,0.49,0.23,0.47,1.97,1.17,1.61,1.97,1.87,1.35,2.66,2.2,2.27,2.71,4.62,4.01,2.74,2.77,4.46,4.82,
0.19,0.47,0.23,0.49,1.97,1.17,1.61,1.97,1.87,1.35,2.66,2.2,2.27,2.71,4.62,4.01,2.74,2.77,4.46,4.82,
0.19,0.23,0.47,0.49,1.97,1.17,1.61,1.97,1.87,1.35,2.66,2.2,2.27,2.71,4.62,4.01,2.74,2.77,4.46,4.82,
0.19,0.23,0.47,0.49,1.97,1.17,1.61,1.35,1.87,1.97,2.66,2.2,2.27,2.71,4.62,4.01,2.74,2.77,4.46,4.82,
0.19,0.23,0.47,0.49,1.87,1.17,1.61,1.35,1.97,1.97,2.66,2.2,2.27,2.71,4.62,4.01,2.74,2.77,4.46,4.82,
0.19,0.23,0.47,0.49,1.35,1.17,1.61,1.87,1.97,1.97,2.66,2.2,2.27,2.71,4.62,4.01,2.74,2.77,4.46,4.82,
0.19,0.23,0.47,0.49,1.17,1.35,1.61,1.87,1.97,1.97,2.66,2.2,2.27,2.71,4.62,4.01,2.74,2.77,4.46,4.82,
0.19,0.23,0.47,0.49,1.17,1.35,1.61,1.87,1.97,1.97,2.66,2.2,2.27,2.71,4.62,4.01,2.74,2.77,4.46,4.82,
0.19,0.23,0.47,0.49,1.17,1.35,1.61,1.87,1.97,1.97,2.66,2.2,2.27,2.71,4.62,4.01,2.74,2.77,4.46,4.82,
0.19,0.23,0.47,0.49,1.17,1.35,1.61,1.87,1.97,1.97,2.66,2.2,2.27,2.71,4.62,4.01,2.74,2.77,4.46,4.82,
0.19,0.23,0.47,0.49,1.17,1.35,1.61,1.87,1.97,1.97,2.66,2.2,2.27,2.71,4.62,4.01,2.74,2.77,4.46,4.82,
0.19,0.23,0.47,0.49,1.17,1.35,1.61,1.87,1.97,1.97,2.66,2.2,2.27,2.71,4.62,4.01,2.74,2.77,4.46,4.82,
final list
0.19,0.23,0.47,0.49,1.17,1.35,1.61,1.87,1.97,1.97,2.2,2.27,2.66,2.71,2.74,2.77,4.01,4.46,4.62,4.82,
```

```
generate another list
iterative merge sort:
4.78,0.49,1.05,4.53,1.15,1.84,2.35,1.69,3.23,1.27,1.91,1.94,2.5,2.43,1.4,4.47,0.21,1.53,3.46,0.6,
0.49,4.78,1.05,4.53,1.15,1.84,1.69,2.35,1.27,3.23,1.91,1.94,2.43,2.5,1.4,4.47,0.21,1.53,0.6,3.46,
0.49,1.05,4.53,4.78,1.15,1.69,1.84,2.35,1.27,1.91,1.94,3.23,1.4,2.43,2.5,4.47,0.21,0.6,1.53,3.46,
0.49,1.05,1.15,1.69,1.84,2.35,4.53,4.78,1.27,1.4,1.91,1.94,2.43,2.5,3.23,4.47,0.21,0.6,1.53,3.46,
0.49,1.05,1.15,1.27,1.4,1.69,1.84,1.91,1.94,2.35,2.43,2.5,3.23,4.47,4.53,4.78,0.21,0.6,1.53,3.46,
0.21,0.49,0.6,1.05,1.15,1.27,1.4,1.53,1.69,1.84,1.91,1.94,2.35,2.43,2.5,3.23,3.46,4.47,4.53,4.78,
final list
0.21,0.49,0.6,1.05,1.15,1.27,1.4,1.53,1.69,1.84,1.91,1.94,2.35,2.43,2.5,3.23,3.46,4.47,4.53,4.78,
```

generate another list

recursive merge sort:

link:

13,12,16,10,15,1,0,5,3,18,2,7,9,17,20,19,4,8,6,14,

final list

0.07,0.37,0.62,0.84,1.05,1.12,1.22,1.55,2.37,2.91,3.53,3.61,3.96,4.08,4.26,4.27,4.32,4.54,4.72,4.85,

generate another list

HeapSort:

```
4.51,4.51,4.07,3.34,4.3,3.1,2.99,2.85,2.99,2.39,3.63,1.29,0.48,0.1,3.6,2.37,0.53,0.44,2.01,1.98,
4.51,4.3,4.07,3.34,3.63,3.1,2.99,2.85,2.99,2.39,1.98,1.29,0.48,0.1,3.6,2.37,0.53,0.44,2.01,4.51,
4.3,3.63,4.07,3.34,2.39,3.1,2.99,2.85,2.99,2.01,1.98,1.29,0.48,0.1,3.6,2.37,0.53,0.44,4.51,4.51,
4.07,3.63,3.1,3.34,2.39,1.29,2.99,2.85,2.99,2.01,1.98,0.44,0.48,0.1,3.6,2.37,0.53,4.3,4.51,4.51,
3.63,3.34,3.1,2.99,2.39,1.29,2.99,2.85,0.53,2.01,1.98,0.44,0.48,0.1,3.6,2.37,4.07,4.3,4.51,4.51,
3.34,2.99,3.1,2.85,2.39,1.29,2.99,2.37,0.53,2.01,1.98,0.44,0.48,0.1,3.6,3.63,4.07,4.3,4.51,4.51,
3.1,2.99,2.99,2.85,2.39,1.29,1.36,2.37,0.53,2.01,1.98,0.44,0.48,0.1,3.34,3.63,4.07,4.3,4.51,4.51,
2.99,2.85,2.99,2.37,2.39,1.29,1.36,0.53,2.01,1.98,0.44,0.48,3.1,3.34,3.63,4.07,4.3,4.51,4.51,
2.99,2.85,1.36,2.37,2.39,1.29,0.48,0.53,2.01,1.98,0.44,2.99,3.1,3.34,3.63,4.07,4.3,4.51,4.51,
2.85,2.39,1.36,2.37,2.01,1.29,0.48,0.53,0.44,1.98,2.99,2.99,3.1,3.34,3.63,4.07,4.3,4.51,4.51,
2.39,2.37,1.36,1.98,2.01,1.29,0.48,0.53,0.44,2.85,2.99,2.99,3.1,3.34,3.63,4.07,4.3,4.51,4.51,
2.37,2.01,1.36,1.98,0.44,1.29,0.48,0.53,2.39,2.85,2.99,2.99,3.1,3.34,3.63,4.07,4.3,4.51,4.51,
2.01,1.98,1.36,0.53,0.44,1.29,0.48,0.2,37,2.39,2.85,2.99,2.99,3.1,3.34,3.63,4.07,4.3,4.51,4.51,
1.98,0.53,1.36,0.44,1.29,0.48,2.01,2.37,2.39,2.85,2.99,2.99,3.1,3.34,3.63,4.07,4.3,4.51,4.51,
1.36,0.53,1.29,0.44,0.48,1.98,2.01,2.37,2.39,2.85,2.99,2.99,3.1,3.34,3.63,4.07,4.3,4.51,4.51,
1.29,0.53,0.48,0.44,1.36,1.98,2.01,2.37,2.39,2.85,2.99,2.99,3.1,3.34,3.63,4.07,4.3,4.51,4.51,
0.53,0.44,0.48,0.1,2.9,1.36,1.98,2.01,2.37,2.39,2.85,2.99,2.99,3.1,3.34,3.63,4.07,4.3,4.51,4.51,
0.48,0.44,0.53,1.29,1.36,1.98,2.01,2.37,2.39,2.85,2.99,2.99,3.1,3.34,3.63,4.07,4.3,4.51,4.51,
0.44,0.48,0.53,1.29,1.36,1.98,2.01,2.37,2.39,2.85,2.99,2.99,3.1,3.34,3.63,4.07,4.3,4.51,4.51,
final list
0.0,4.4,0.48,0.53,1.29,1.36,1.98,2.01,2.37,2.39,2.85,2.99,2.99,3.1,3.34,3.63,4.07,4.3,4.51,4.51,
```

List of C++ strings:

```
InsertionSort:
yLA,Ey, rPE, VCi, LLX, kVL, KytnI, qDEM, RHv, gnbb, qMZ, ISSZ, kNBM, ogx, RL, eaP, QEc, FV, lJR, LczE,
Ey, yLA, rPE, VCi, LLX, kVL, KytnI, qDEM, RHv, gnbb, qMZ, ISSZ, kNBM, ogx, RL, eaP, QEc, FV, lJR, LczE,
Ey, rPE, yLA, VCi, LLX, kVL, KytnI, qDEM, RHv, gnbb, qMZ, ISSZ, kNBM, ogx, RL, eaP, QEc, FV, lJR, LczE,
Ey, VCi, rPE, yLA, LLX, kVL, KytnI, qDEM, RHv, gnbb, qMZ, ISSZ, kNBM, ogx, RL, eaP, QEc, FV, lJR, LczE,
Ey, LLX, VCi, rPE, yLA, kVL, KytnI, qDEM, RHv, gnbb, qMZ, ISSZ, kNBM, ogx, RL, eaP, QEc, FV, lJR, LczE,
Ey, LLX, VCi, kVL, rPE, yLA, KytnI, qDEM, RHv, gnbb, qMZ, ISSZ, kNBM, ogx, RL, eaP, QEc, FV, lJR, LczE,
Ey, KytnI, LLX, VCi, kVL, qDEM, rPE, yLA, RHv, gnbb, qMZ, ISSZ, kNBM, ogx, RL, eaP, QEc, FV, lJR, LczE,
Ey, KytnI, LLX, VCi, kVL, qDEM, rPE, yLA, RHv, gnbb, qMZ, ISSZ, kNBM, ogx, RL, eaP, QEc, FV, lJR, LczE,
Ey, KytnI, LLX, RHv, VCi, kVL, qDEM, rPE, yLA, gnbb, qMZ, ISSZ, kNBM, ogx, RL, eaP, QEc, FV, lJR, LczE,
Ey, KytnI, LLX, RHv, VCi, gnbb, kVL, qDEM, rPE, yLA, qMZ, ISSZ, kNBM, ogx, RL, eaP, QEc, FV, lJR, LczE,
Ey, KytnI, LLX, RHv, VCi, gnbb, kVL, qDEM, qMZ, rPE, yLA, ISSZ, kNBM, ogx, RL, eaP, QEc, FV, lJR, LczE,
Ey, ISSZ, KytnI, LLX, RHv, VCi, gnbb, kVL, qDEM, qMZ, rPE, yLA, kNBM, ogx, RL, eaP, QEc, FV, lJR, LczE,
Ey, ISSZ, KytnI, LLX, RHv, VCi, gnbb, kNBM, kVL, qDEM, qMZ, rPE, yLA, ogx, RL, eaP, QEc, FV, lJR, LczE,
Ey, ISSZ, KytnI, LLX, RHv, VCi, gnbb, kNBM, kVL, ogx, qDEM, qMZ, rPE, yLA, RL, eaP, QEc, FV, lJR, LczE,
Ey, ISSZ, KytnI, LLX, RHv, RL, VCi, gnbb, kNBM, kVL, ogx, qDEM, qMZ, rPE, yLA, eaP, QEc, FV, lJR, LczE,
Ey, ISSZ, KytnI, LLX, RHv, RL, VCi, eaP, gnbb, kNBM, kVL, ogx, qDEM, qMZ, rPE, yLA, QEc, FV, lJR, LczE,
Ey, ISSZ, KytnI, LLX, QEc, RHv, RL, VCi, eaP, gnbb, kNBM, kVL, ogx, qDEM, qMZ, rPE, yLA, FV, lJR, LczE,
Ey, FV, ISSZ, KytnI, LLX, QEc, RHv, RL, VCi, eaP, gnbb, kNBM, kVL, ogx, qDEM, qMZ, rPE, yLA, lJR, LczE,
Ey, FV, ISSZ, KytnI, LLX, QEc, RHv, RL, VCi, eaP, gnbb, kNBM, kVL, lJR, ogx, qDEM, qMZ, rPE, yLA, LczE,
Ey, FV, ISSZ, KytnI, LLX, LczE, QEc, RHv, RL, VCi, eaP, gnbb, kNBM, kVL, lJR, ogx, qDEM, qMZ, rPE, yLA,
final list
Ey, FV, ISSZ, KytnI, LLX, LczE, QEc, RHv, RL, VCi, eaP, gnbb, kNBM, kVL, lJR, ogx, qDEM, qMZ, rPE, yLA,

generate another list

QuickSort:
wJD, HyW, zFONjF, nDp, CSLS, NVRk, NxOK, dC, HVA, yIXBU, VR, DwRQK, EBUj, NiQ, mm, GKhRwX, yJ, KV, lhX, ZLamLY,
wJD, HyW, ZLamLY, nDp, CSLS, NVRk, NxOK, dC, HVA, yIXBU, VR, DwRQK, EBUj, NiQ, mm, GKhRwX, yJ, KV, lhX, zFONjF,
wJD, HyW, ZLamLY, nDp, CSLS, NVRk, NxOK, dC, HVA, lhX, VR, DwRQK, EBUj, NiQ, mm, GKhRwX, yJ, KV, yIXBU, zFONjF,
wJD, HyW, ZLamLY, nDp, CSLS, NVRk, NxOK, dC, HVA, lhX, VR, DwRQK, EBUj, NiQ, mm, GKhRwX, KV, yJ, yIXBU, zFONjF,
KV, HyW, ZLamLY, nDp, CSLS, NVRk, NxOK, dC, HVA, lhX, VR, DwRQK, EBUj, NiQ, mm, GKhRwX, wJD, yJ, yIXBU, zFONjF,
KV, HyW, GKhRwX, nDp, CSLS, NVRk, NxOK, dC, HVA, lhX, VR, DwRQK, EBUj, NiQ, mm, ZLamLY, wJD, yJ, yIXBU, zFONjF,
KV, HyW, GKhRwX, EBUj, CSLS, DwRQK, NxOK, dC, HVA, lhX, VR, NVRk, nDp, NiQ, mm, ZLamLY, wJD, yJ, yIXBU, zFONjF,
KV, HyW, GKhRwX, EBUj, CSLS, DwRQK, NxOK, dC, HVA, lhX, VR, NVRk, nDp, NiQ, mm, ZLamLY, wJD, yJ, yIXBU, zFONjF,
HVA, HyW, GKhRwX, EBUj, CSLS, DwRQK, HVA, dC, NxOK, lhX, VR, NVRk, nDp, NiQ, mm, ZLamLY, wJD, yJ, yIXBU, zFONjF,
HVA, HyW, GKhRwX, EBUj, CSLS, DwRQK, KV, dC, NxOK, lhX, VR, NVRk, nDp, NiQ, mm, ZLamLY, wJD, yJ, yIXBU, zFONjF,
HVA, DwRQK, GKhRwX, EBUj, HVA, HyW, KV, dC, NxOK, lhX, VR, NVRk, nDp, NiQ, mm, ZLamLY, wJD, yJ, yIXBU, zFONjF,
CSLS, DwRQK, GKhRwX, EBUj, HVA, HyW, KV, dC, NxOK, lhX, VR, NVRk, nDp, NiQ, mm, ZLamLY, wJD, yJ, yIXBU, zFONjF,
CSLS, DwRQK, GKhRwX, EBUj, HVA, HyW, KV, dC, NxOK, lhX, VR, NVRk, nDp, NiQ, mm, ZLamLY, wJD, yJ, yIXBU, zFONjF,
CSLS, DwRQK, GKhRwX, EBUj, HVA, HyW, KV, dC, NxOK, lhX, VR, NVRk, nDp, NiQ, mm, ZLamLY, wJD, yJ, yIXBU, zFONjF,
CSLS, DwRQK, GKhRwX, EBUj, CSLS, DwRQK, HVA, HyW, KV, dC, NxOK, lhX, VR, NVRk, nDp, NiQ, mm, ZLamLY, wJD, yJ, yIXBU, zFONjF,
CSLS, DwRQK, EBUj, GKhRwX, HVA, HyW, KV, dC, NxOK, ZLamLY, VR, NVRk, nDp, NiQ, mm, lhX, wJD, yJ, yIXBU, zFONjF,
CSLS, DwRQK, EBUj, GKhRwX, HVA, HyW, KV, NiQ, NxOK, ZLamLY, VR, NVRk, NiQ, nDp, mm, lhX, wJD, yJ, yIXBU, zFONjF,
CSLS, DwRQK, EBUj, GKhRwX, HVA, HyW, KV, NiQ, NVRk, ZLamLY, VR, NxOK, dC, nDp, mm, lhX, wJD, yJ, yIXBU, zFONjF,
CSLS, DwRQK, EBUj, GKhRwX, HVA, HyW, KV, NVRk, NiQ, ZLamLY, VR, NxOK, dC, nDp, mm, lhX, wJD, yJ, yIXBU, zFONjF,
CSLS, DwRQK, EBUj, GKhRwX, HVA, HyW, KV, NVRk, NiQ, NxOK, VR, ZLamLY, dC, nDp, mm, lhX, wJD, yJ, yIXBU, zFONjF,
CSLS, DwRQK, EBUj, GKhRwX, HVA, HyW, KV, NVRk, NiQ, NxOK, VR, ZLamLY, dC, nDp, mm, lhX, wJD, yJ, yIXBU, zFONjF,
CSLS, DwRQK, EBUj, GKhRwX, HVA, HyW, KV, NVRk, NiQ, NxOK, VR, ZLamLY, dC, lhX, mm, nDp, wJD, yJ, yIXBU, zFONjF,
CSLS, DwRQK, EBUj, GKhRwX, HVA, HyW, KV, NVRk, NiQ, NxOK, VR, ZLamLY, dC, lhX, mm, nDp, wJD, yJ, yIXBU, zFONjF,
final list
CSLS, DwRQK, EBUj, GKhRwX, HVA, HyW, KV, NVRk, NiQ, NxOK, VR, ZLamLY, dC, lhX, mm, nDp, wJD, yJ, yIXBU, zFONjF,
```

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generate another list

iterative merge sort:
GqtC, WC, BAS, EpY, ZFX, tdgH, npu, rW, XI, OaFB, hoKfS, kZd, rFb, lQcYOb, CywMW, puiE, wb, sbD, nI, xRHx,
GqtC, WC, BAS, EpY, ZFX, tdgH, npu, rW, OaFB, XI, hoKfS, kZd, lQcYOb, rFb, CywMW, puiE, sbD, wb, nI, xRHx,
BAS, EpY, GqtC, WC, ZFX, npu, rW, tdgH, OaFB, XI, hoKfS, kZd, CywMW, lQcYOb, puiE, rFb, nI, sbD, wb, xRHx,
BAS, EpY, GqtC, WC, ZFX, npu, rW, tdgH, CywMW, OaFB, XI, hoKfS, kZd, lQcYOb, puiE, rFb, nI, sbD, wb, xRHx,
BAS, CywMW, EpY, GqtC, OaFB, WC, XI, ZFX, hoKfS, kZd, lQcYOb, npu, puiE, rFb, rW, tdgH, nI, sbD, wb, xRHx,
BAS, CywMW, EpY, GqtC, OaFB, WC, XI, ZFX, hoKfS, kZd, lQcYOb, nI, npu, puiE, rFb, rW, sbD, tdgH, wb, xRHx,
final list
BAS, CywMW, EpY, GqtC, OaFB, WC, XI, ZFX, hoKfS, kZd, lQcYOb, nI, npu, puiE, rFb, rW, sbD, tdgH, wb, xRHx,

generate another list

recursive merge sort:
link:
3,17,12,20,7,1,15,9,10,6,5,14,8,18,13,0,2,11,4,16,
final list
Gd, LpCTaG, MSB, Nw, THC, XsOsEL, aUQY, ew, fNrR, gu, jhrG, oXu, qo, rFmK, tSWM, tcCY, uV, wNON, xQ, yZXd,

generate another list

HeapSort:
uHH, rzz, j0, pheJ, lpJy, aNYaD, gGJu, iex, fMKD, jmwds, Sns, II, AHy, MV, RE, Hu, PAB, bA, WkobGW, gGDh,
rzz, pheJ, j0, iex, lpJy, aNYaD, gGJu, gGDh, fMKD, jmwds, Sns, II, AHy, MV, RE, Hu, PAB, bA, WkobGW, uHH,
pheJ, lpJy, j0, iex, jmwds, aNYaD, gGJu, gGDh, fMKD, WkobGW, Sns, II, AHy, MV, RE, Hu, PAB, bA, rzz, uHH,
lpJy, jmwds, j0, iex, bA, aNYaD, gGJu, gGDh, fMKD, WkobGW, Sns, II, AHy, MV, RE, Hu, PAB, pheJ, rzz, uHH,
jmwds, iex, j0, gGDh, bA, aNYaD, gGJu, PAB, fMKD, WkobGW, Sns, II, AHy, MV, RE, Hu, lpJy, pheJ, rzz, uHH,
j0, iex, gGJu, gGDh, bA, aNYaD, RE, PAB, fMKD, WkobGW, Sns, II, AHy, MV, Hu, jmwds, lpJy, pheJ, rzz, uHH,
iex, gGDh, gGJu, fMKD, bA, aNYaD, RE, PAB, Hu, WkobGW, Sns, II, AHy, MV, j0, jmwds, lpJy, pheJ, rzz, uHH,
gGJu, gGDh, aNYaD, fMKD, bA, MV, RE, PAB, Hu, WkobGW, Sns, II, AHy, iex, j0, jmwds, lpJy, pheJ, rzz, uHH,
gGDh, fMKD, aNYaD, PAB, bA, MV, RE, AHy, Hu, WkobGW, Sns, II, gGJu, iex, j0, jmwds, lpJy, pheJ, rzz, uHH,
fMKD, bA, aNYaD, PAB, WkobGW, MV, RE, AHy, Hu, II, Sns, gGDh, gGJu, iex, j0, jmwds, lpJy, pheJ, rzz, uHH,
bA, WkobGW, aNYaD, PAB, Sns, MV, RE, AHy, Hu, II, fMKD, gGDh, gGJu, iex, j0, jmwds, lpJy, pheJ, rzz, uHH,
aNYaD, WkobGW, RE, PAB, Sns, MV, II, AHy, Hu, bA, fMKD, gGDh, gGJu, iex, j0, jmwds, lpJy, pheJ, rzz, uHH,
WkobGW, Sns, RE, PAB, Hu, MV, II, AHy, aNYaD, bA, fMKD, gGDh, gGJu, iex, j0, jmwds, lpJy, pheJ, rzz, uHH,
Sns, PAB, RE, AHy, Hu, MV, II, WkobGW, aNYaD, bA, fMKD, gGDh, gGJu, iex, j0, jmwds, lpJy, pheJ, rzz, uHH,
RE, PAB, MV, AHy, Hu, II, Sns, WkobGW, aNYaD, bA, fMKD, gGDh, gGJu, iex, j0, jmwds, lpJy, pheJ, rzz, uHH,
PAB, II, MV, AHy, Hu, Sns, WkobGW, aNYaD, bA, fMKD, gGDh, gGJu, iex, j0, jmwds, lpJy, pheJ, rzz, uHH,
MV, II, Hu, AHy, PAB, RE, Sns, WkobGW, aNYaD, bA, fMKD, gGDh, gGJu, iex, j0, jmwds, lpJy, pheJ, rzz, uHH,
II, AHy, Hu, MV, PAB, RE, Sns, WkobGW, aNYaD, bA, fMKD, gGDh, gGJu, iex, j0, jmwds, lpJy, pheJ, rzz, uHH,
Hu, AHy, II, MV, PAB, RE, Sns, WkobGW, aNYaD, bA, fMKD, gGDh, gGJu, iex, j0, jmwds, lpJy, pheJ, rzz, uHH,
final list
AHy, Hu, II, MV, PAB, RE, Sns, WkobGW, aNYaD, bA, fMKD, gGDh, gGJu, iex, j0, jmwds, lpJy, pheJ, rzz, uHH,
```

I have used four kinds of lists(int , float , char , string). First, I randomly generate a list and then use one of the below sorting function. Then I generate another list and use another sorting function. I keep doing so in my demo until I use every kinds of lists to run every function below. These functions are used to sort list in different ways.

```
void InsertionSort(T*a,const int n)
void QuickSort(T *a, const int left, const int right)
void MergeSort(T *a, const int n)
int rMergeSort(T* a, int* link, const int left, const int right)
void HeapSort(T *a,const int n)
```

## 2. (50%) **Hashing:**

Write a C++ program to implement two simple symbol tables (dictionaries) using hash table with linear probing for collision and hash table with chaining. For simplicity,

- Consider storing only the key (need not consider the (key, value) pair) in the symbol tables.
- Furthermore, the key is a variable-length character array with the first character of the key is an alphabet, e.g., abc, abcde, b, bye, cool,...
- Consider a simple hash function using only the first character of key to hash, so  $h(abcde) = h(abc)$ ,  $h(b) = h(bye)$ ,..., etc. Therefore, collision can happen frequently.
- The initial hash table size can be set to 26 since we have 26 alphabets which are the hashed keys.

Create 2 symbol table classes for linear probing and chaining, respectively. Both must implement at least the following functions:

Constructor,  
Insert(key)  
Search(key)

You may add other functions needed in your program.

Your main function may contains code like:

```
SymbolTable1 d1;
Setup at least 10 key objects
Insert those 10 keys into d1.
```

**Display d1**

**Demo the search function** of d1 (try at least 5 keys)

SymbolTable2 d2;

Setup at least 10 key objects

Insert those 10 keys into d1.

Display d2

Demo the search function of d2(try at least 5 keys)

ANS:

linear probing:

```
Setup and Insert 12 keys objects:GA,D,A,G,L,A2,A1,A3,A4,Z,ZA,E
Display:
ht[0]: A
ht[1]: A2
ht[2]: A1
ht[3]: D
ht[4]: A3
ht[5]: A4
ht[6]: GA
ht[7]: G
ht[8]: ZA
ht[9]: E
ht[10]:
ht[11]: L
ht[12]:
ht[13]:
ht[14]:
ht[15]:
ht[16]:
ht[17]:
ht[18]:
ht[19]:
ht[20]:
ht[21]:
ht[22]:
ht[23]:
ht[24]:
ht[25]: Z
Search("GA"): address:0x555a0a5a5360, key: GA
Search("A"): address:0x555a0a5a53c0, key: A
Search("A2"): address:0x555a0a5a5450, key: A2
Search("ZA"): address:0x555a0a5a5540, key: ZA
Search("E"): address:0x555a0a5a5570, key: E
```

hash table with chaining:

```
Setup and Insert 12 keys objects:A4,D,E,G,L,ZA,A3,GA,Z,A1,A2,A
Display:
0->A4->A3->A1->A2->A
1
2
3->D
4->E
5
6->G->GA
7
8
9
10
11->L
12
13
14
15
16
17
18
19
20
21
22
23
24
25->ZA->Z
Search("A4"): address:0x555a0a5a5b60, key: A4
Search("G"): address:0x555a0a5a5bf0, key: G
Search("ZA"): address:0x555a0a5a5c50, key: ZA
Search("GA"): address:0x555a0a5a5cb0, key: GA
Search("A"): address:0x555a0a5a5d70, key: A
```

According to b. of the problem, the key is a variable-length character array with the first character of the key is an alphabet, so I use the key with type of string. And according to a. , I storing only the key. In both linearprobing and chaining, the function `Insert(const& k)` can insert the key to the tables and the function `Search(const string&k)` can get the address of the searched key.(k is the key that we want to search or insert). The function `Dispaly()` can show the table.