

# Seminar 10. Incomplete Information in Dynamic Games

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## 1 Problem 1 - Screening and signaling

Consider again the strategic situation described in Problem 1 of the set for the ninth seminar, where only player 1 knows which game is being played, while player 2 thinks that the two games are equally likely.

### 1.1 (a) Screening

Assume now that player 2 acts before player 1, and that 2's choice can be observed by 1 before he makes his choice. Show that there is a unique subgame perfect Nash equilibrium.

### 1.2 (b) Signaling

Assume now that player 1 acts before player 2, and that 1's choice can be observed by 2 before she makes her choice. Show that there is a unique separating perfect Bayesian equilibrium.

## 2 Problem 2 - Sequential moves and incomplete information; Perfect Bayesian equilibrium

Consider the situation of Problem 1 of the eighth seminar, but assume now in addition that the pizza comes in 5 different sizes, each with  $x$  slices, where  $x \in \{4, 6, 8, 10, 12\}$ . Player 1 observes  $x$  before making her demand, while player 2 only observes player 1's demand, but not  $x$ , before having to make his own demand. Before observing player 1's demand, player 2 thinks that the 5 different pizza sizes are equally likely, but he may infer something from her demand.

**2.1 (a) Explain what a strategy is for player 1 in this game of incomplete information.**

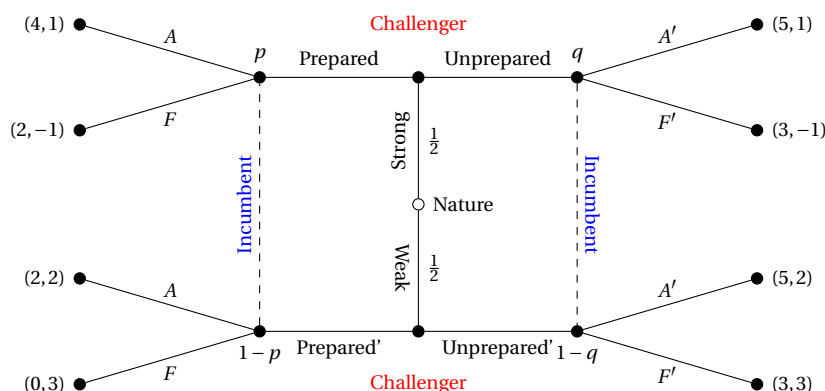
**2.2 (b) perfect Bayesian equilibrium**

Show that the following strategy for player 1 can be part of a perfect Bayesian equilibrium:  $s_1(4) = 2$ ,  $s_1(6) = 3$ ,  $s_1(8) = 4$ ,  $s_1(10) = 5$ ,  $s_1(12) = 11$ . Specify both player 2's strategy and player 2's beliefs.

**2.3 (c) Are there other perfect Bayesian equilibria in this game?**

### 3 Problem 3 - Challenging an incumbent

Consider a market where there is an incumbent firm and a challenger. The challenger is *strong* with probability  $\frac{1}{2}$  and *weak* with probability  $\frac{1}{2}$ ; it knows its type, but the incumbent does not. The challenger may either *prepare* itself for battle or remain *unprepared*. The incumbent observes the challenger's preparedness, but not its type, and chooses whether to *fight* ( $F$ ) or *acquiesce* ( $A$ ). The extensive form and the payoffs are given by the following figure. The challenger's payoff is listed first, the incumbent's second.



**3.1 (a) What are the (pure) strategies for the challenger?**

**3.2 (b) Why is there no perfect Bayesian equilibrium where the weak challenger chooses *Prepared'* ?**

**3.3 (c) Separating**

Show that there is a perfect Bayesian equilibrium where the strong challenger chooses *Prepared* and the weak challenger chooses *Unprepared'*.

### 3.4 (d) Pooling

Show that there is a perfect Bayesian equilibrium where the strong challenger chooses *Unprepared* and the weak challenger chooses *Unprepared'*. What do we call such an equilibrium?