Seminar 2 - Expenditure function

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1 Jehle & Reny 1.38 - Properties of the Expenditure Function

Verify that the expenditure function obtained from the CES direct utility function in Example 1.3 (JR. pp.39) satisfies all the properties given in Theorem 1.7 (JR. pp.37).

Expenditure Function (JR. pp.35)

We define the expenditure function as theminimum-value function:

$$e(p,u)\equiv \min_{x\in\mathbb{R}^n_+}p\cdot x$$

THEOREM 1.7 Properties of the Expenditure Function (JR. pp.37)

If u(.) is continuous and strictly increasing, then e(p, u) defined in (1.14) is

- 1. Zero when u takes on the lowest level of utility in \mathcal{U} ,
- 2. Continuous on its domain $\mathbb{R}_{++}^n \times \mathcal{U}$,
- 3. For all $p \gg 0$, strictly increasing and unbounded above in u,
- 4. Increasing in p,
- 5. Homogeneous of degree 1 in p,
- 6. Concave in p.

If, in addition, u(.) is strictly quasiconcave, we have

7. Shephard's lemma: e(p,u) is differentiable in p at (p^0,u^0) with $p^0\gg 0$, and

$$\frac{\partial e(p^0, u^0)}{\partial p_i} = x_i^h(p^0, u^0), \quad i = 1, ..., n.$$

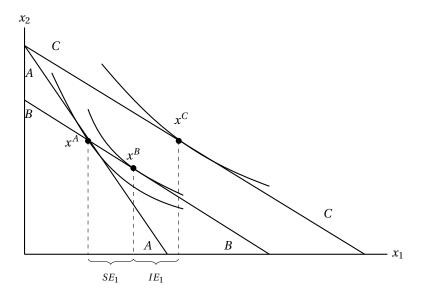


Figure 1: Slutsky decomposition

2 Jehle & Reny 1.44 - Inferior and Normal goods

In a two-good case, show that if one good is inferior, the other good must be normal.

3 Jehle & Reny 1.51 - Substitues and Complements

Consider the utility function, $u(x_1, x_2) = (x_1)^{1/2} + (x_2)^{1/2}$.

- a. Compute the demand functions, $x_i(p_1, p_2, y)$, i = 1, 2.
- b. Compute the substitution term in the Slutsky equation for the effects on x_1 of changes in p_2 .
- c. Classify x_1 and x_2 as (gross) complements or substitutes.