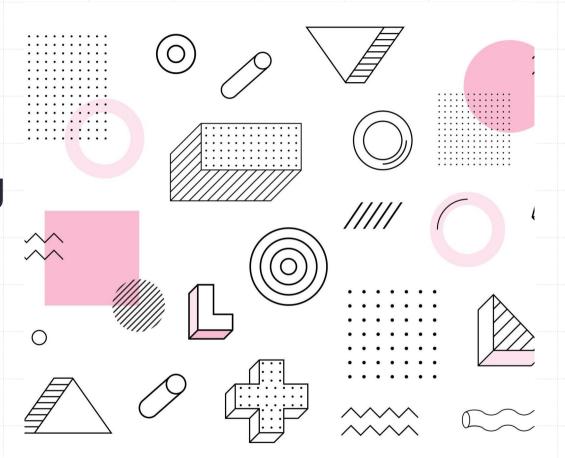
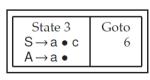
### Chapter 6: Bottom-Up Parsing (Shift-Reduce)

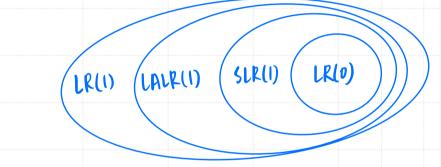
陳奇業 成功大學資訊工程系



1	Star	$t \rightarrow$	S	\$	
2	S	$\rightarrow$	Α	В	
3			a	С	
4			Χ	A	С
5	Α	$\rightarrow$	a		
6	В	$\rightarrow$	b		
7			λ		

	State 0						
Sta	rt → • S \$	4					
S	$\rightarrow$ • A B	2					
S	$\rightarrow$ • a c	3					
S	$\rightarrow$ • x A c	1					
Α	→ • a	3					
-							





shift/reduce conflict

 $Follow(A) = \{c, b, \$\}$ 

State 0
Start  $\rightarrow$  • S \$
S  $\rightarrow$  • A<sub>1</sub> B
S  $\rightarrow$  • a c
S  $\rightarrow$  • x A<sub>2</sub> c

State 2 S $\rightarrow$ a $\bullet$ c A <sub>1</sub> $\rightarrow$ a $\bullet$	Goto 8

C	Case 1:
C	
C	
C	
C	
C	

$$Start \rightarrow S\$ \rightarrow A_1B\$ \rightarrow A_1b\$ \begin{array}{c} Follow(A_1) = \{b,\$\} \\ Start \rightarrow S\$ \rightarrow A_1B\$ \rightarrow A_1\$ \end{array}$$

#### Case 2:

$$Start \rightarrow S\$ \rightarrow xA_2c\$$$
  $Follow(A_2) = \{c\}$ 



- In this section, we consider LALR(k) (Lookahead Ahead LR with k tokens of lookahead)
  parsing, which offers a more specialized computation of the symbols that can follow a
  nonterminal.
- LALR offers superior lookahead analysis for constructing the bottom-up parsing table.
- LALR(1) parsers can be built by first constructing an LR(1) parser and then merging states

- LALR(1) parsers can be built by
- 1. An LR(1) parser and then merging states (may be quite inefficient) 似学之
- 2. An LR(0) parser with LALR propagation graph

```
procedure CompleteTable(Table, grammar)
   call ComputeLookahead()
   foreach state \in Table do
      foreach rule ∈ Productions(grammar) do
          call TryRuleInState(state, rule)
   call AssertEntry(StartState, GoalSymbol, accept)
end
procedure AssertEntry(state, symbol, action)
   if Table[state][symbol] = error
   then Table[state][symbol] \leftarrow action
   else
      call ReportConflict(Table[state][symbol], action)
end
```

```
procedure TryRuleInState(s, r)
   if LHS(r)\rightarrowRHS(r)\bullet \in s
   then
       foreach X \in Follow(LHS(r)) do
           call AssertEntry(s, X, reduce r)
end
```

end

```
procedure TryRuleInState(s, r)
   if LHS(r) \rightarrow RHS(r) \bullet \in s
   then
        foreach X \in \Sigma do
          \bullet if X \in ItemFollow((s, LHS(r) \rightarrow RHS(r) \bullet))
            then call AssertEntry(s, X, reduce r)
```

```
procedure ComputeLookahead()
call BuildItemPropGraph()
call EvalItemPropGraph()
end
```

- We have not formally named each LR(0) item, but an item occurs at most once in any state. Thus, the pair  $(s, A \to \alpha \bullet \beta)$  suffices to identify an item  $A \to \alpha \bullet \beta$  that occurs in state s.
- For each valid state and item pair, we create a vertex v in the LALR propagation graph.

```
procedure BuildItemPropGraph()
    foreach s \in States do
         foreach item \in state do
             v \leftarrow Graph.AddVertex((s, item))
             ItemFollow(v) ← Ø itemfollon phis Ø
    foreach p \in ProductionsFor(Start) do
         ItemFollow((StartState, Start \rightarrow \bullet RHS(p))) \leftarrow \{\$\}
    foreach s \in States do
         foreach A \rightarrow \alpha \bullet B\gamma \in s do
             v \leftarrow Graph \cdot FINDVERTEX((s, A \rightarrow \alpha \bullet By))
             call Graph. AddEdge(v, (Table[s][B], A \rightarrow \alpha B \bullet \gamma))
             foreach (w \leftarrow (s, B \rightarrow \bullet \delta)) \in Graph.Vertices do
                 ItemFollow(w) \leftarrow ItemFollow(w) \cup First(\gamma)
                 if AllDeriveEmpty(\gamma)
                  then call Graph. Add Edge(v, w)
end
```

The ItemFollow sets are initially empty, except for the augmenting item Start →
 S\$ in the LR(0) start-state.

```
procedure BuildItemPropGraph()
    foreach s \in States do
         foreach item \in state do
              v \leftarrow Graph.AddVertex((s, item))
              ItemFollow(v) \leftarrow \emptyset
    foreach p \in ProductionsFor(Start) do
         ItemFollow((StartState, Start \rightarrow \bullet RHS(p))) \leftarrow \{\$\}
    foreach s \in States do
         foreach A \rightarrow \alpha \bullet B\gamma \in s do
              v \leftarrow Graph \cdot FINDVERTEX((s, A \rightarrow \alpha \bullet B\gamma))
              call Graph . AddEdge(v, (Table[s][B], A \rightarrow \alpha B \bullet \gamma))
              foreach (w \leftarrow (s, \mathsf{B} \rightarrow \bullet \delta)) \in Graph.Vertices do
                  ItemFollow(w) \leftarrow ItemFollow(w) \cup First(\gamma)
                  if AllDeriveEmpty(\gamma)
                   then call Graph.AddEdge(v, w)
end
```

Edges are placed in the graph between items i and j when the symbols that follow the reducible form of item i should be included in the corresponding set of symbols for item j.

```
foreach s \in States do

foreach item \in state do

v \leftarrow Graph \cdot Addded{DDVertex}((s, item))

ItemFollow(v) \leftarrow \emptyset

foreach p \in ProductionsFor(Start) do

ItemFollow((StartState, Start \rightarrow \bullet RHS(p))) \leftarrow \{\$\}

foreach s \in States do

foreach A \rightarrow \alpha \bullet B\gamma \in s do

v \leftarrow Graph \cdot FindVertex((s, A \rightarrow \alpha \bullet B\gamma))

call Graph \cdot Addded Edge(v, (Table[s][B], A \rightarrow \alpha B \bullet \gamma))

foreach (w \leftarrow (s, B \rightarrow \bullet \delta)) \in Graph \cdot Vertices do

ItemFollow(w) \leftarrow ItemFollow(w) \cup First(\gamma)

if AllDeriveEmpty(\gamma)

then call Graph \cdot Addded Edge(v, w)

end
```

procedure BuildItemPropGraph()

• For the item  $A \to \alpha \bullet B\gamma$ , any symbol in First( $\gamma$ ) can follow each closure item  $B \to \bullet \delta$ .

```
foreach item \in state do

v \leftarrow Graph \cdot Add \text{NodVertex}((s, item))

ItemFollow(v) \leftarrow \emptyset

foreach p \in ProductionsFor(Start) do

ItemFollow((StartState, Start \rightarrow \bullet RHS(p))) \leftarrow \{\$\}

foreach s \in States do

foreach A \rightarrow \alpha \bullet B\gamma \in s do

v \leftarrow Graph \cdot FindVertex((s, A \rightarrow \alpha \bullet B\gamma))

call Graph \cdot Add Edge(v, (Table[s][B], A \rightarrow \alpha B \bullet \gamma))

foreach (w \leftarrow (s, B \rightarrow \bullet \delta)) \in Graph \cdot Vertices do

ItemFollow(w) \leftarrow ItemFollow(w) \cup First(\gamma)

if All DeriveEmpty(\gamma)

then call Graph \cdot Add Edge(v, w)

end
```

procedure BuildItemPropGraph()

foreach  $s \in States$  do

• Consider again the item  $A \to \alpha \bullet B \gamma$  and the closure items introduced when B is a nonterminal. When  $\gamma \Longrightarrow^* \lambda$ , either because  $\gamma$  is absent or because the string of symbols in  $\gamma$  can derive  $\lambda$ , then any symbol that can follow A can also

follow B.

```
procedure BuildItemPropGraph()
    foreach s \in States do
         foreach item \in state do
              v \leftarrow Graph.AddVertex((s, item))
              ItemFollow(v) \leftarrow \emptyset
    foreach p \in ProductionsFor(Start) do
         ItemFollow((StartState, Start \rightarrow \bullet RHS(p))) \leftarrow \{\$\}
    foreach s \in States do
         foreach A \rightarrow \alpha \bullet B\gamma \in s do
             v \leftarrow Graph \cdot FINDVERTEX((s, A \rightarrow \alpha \bullet B\gamma))
              call Graph. AddEdge(v, (Table[s][B], A \rightarrow \alpha B \bullet \gamma))
              foreach (w \leftarrow (s, B \rightarrow \bullet \delta)) \in Graph.Vertices do
                  ItemFollow(w) \leftarrow ItemFollow(w) \cup First(\gamma)
                  if AllDeriveEmpty(γ)
                   then call Graph. Add Edge(v, w)
end
```

```
Prop Edges
                                                                                                            LR(0) Item
                                                                                                                                                          Initialize
                                                                                                 State
                                                                                                                             Goto
procedure BuildItemPropGraph()
                                                                                                                                    Placed by Step
                                                                                                                                                          ItemFollow
                                                                                                                             State
                                                                                                                              210
    foreach s \in States do
                                                                                                                                                       First(\gamma)
         foreach item \in state do
                                                                                                                                                                  2,3,4
                                                                                                             Start → • S $
             v \leftarrow Graph.AddVertex((s, item))
             ItemFollow(v) \leftarrow \emptyset
    foreach p \in ProductionsFor(Start) do
        ItemFollow((StartState, Start \rightarrow \bullet RHS(p))) \leftarrow \{\$\}
                                                                                                                                9
                                                                                                                                                          C
                                                                                                                               10
                                                                                                                                     19
    foreach s \in States do
                                                                                                                                8
                                                                                                                                     17
                                                                                                                                             9,10
         foreach A \rightarrow \alpha \bullet B\gamma \in s do
                                                                                                                                     16
             v \leftarrow Graph \cdot FINDVERTEX((s, A \rightarrow \alpha \bullet B_{\gamma}))
             call Graph . AddEdge(v, (Table[s][B], A \rightarrow \alpha B \bullet \gamma))
                                                                                                         11 S → a • c
             foreach (w \leftarrow (s, B \rightarrow \bullet \delta)) \in Graph.Vertices do
                                                                                                          12 A→a•
                  ItemFollow(w) \leftarrow ItemFollow(w) \cup First(\gamma)
                                                                                                         13 Start \rightarrow S • $
                  if AllDeriveEmpty(\gamma)
                                                                                                         14 Start→S $ •
                  then call Graph.AddEdge(v, w)
                                                                                                         15 S→a c•
end
                                                                                                         16 B→b•
                                                                                                         17 S→A B•
                                                                                                         18 S→x A • c
                                                                                                                              11
```

procedure BuildItemPropGraph( )	State	LR(0) Item	State		p Edges d by Step	Initial ItemFo	
foreach $s \in States$ do				27)		$First(\gamma)$	28)
<b>foreach</b> <i>item</i> ∈ <i>state</i> <b>do</b>	0	1 Start → • S \$	4	13		\$	2,3,4
$v \leftarrow Graph.AddVertex((s, item))$		2 S→ • A B	2	8	5	b	5
$ItemFollow(v) \leftarrow \emptyset$		$\begin{array}{cccccccccccccccccccccccccccccccccccc$	3 1	6			
foreach $p \in ProductionsFor(Start)$ do		5 A→ • a	3	12			
$ItemFollow((StartState, Start \rightarrow \bullet RHS(p))) \leftarrow \{\$\}$	1	6 S→x • A c	9	18		С	7
foreach $s \in States$ do		7 A→ • a	10	19			
foreach $A \rightarrow \alpha \bullet B\gamma \in s$ do	2	8 S→A•B	8	17	9,10		
$v \leftarrow Graph \cdot FINDVERTEX((s, A \rightarrow \alpha \bullet B\gamma))$		9 B→ • b 10 B→ •	7	16			
call Graph. AddEdge(v, (Table[s][B], $A \rightarrow \alpha B \bullet \gamma$ ))		10 B→ • 11 S→a•c	6	15			
<b>foreach</b> $(w \leftarrow (s, B \rightarrow \bullet \delta)) \in Graph.Vertices do$	3	11 3→a•c 12 A→a•	0	15			
$ItemFollow(w) \leftarrow ItemFollow(w) \cup First(\gamma)$	4	13 Start→S•\$	5	14			
if AllDeriveEmpty(γ)	5	14 Start→S \$ •					
then call $Graph.AddEdge(v, w)$	6	15 S→a c•					
end	7	16 B→b•					
	8	17 S→A B•					
	9	18 S→x A • c	11	20			
	10	19 A→a•	11	20			
	11	20 S→x A c •					
	11	1 20 3 → X A C •				l ,	

LR(0) Item

Prop Edges

Initialize

```
procedure BuildItemPropGraph()
    foreach s \in States do
         foreach item \in state do
             v \leftarrow Graph.AddVertex((s, item))
             ItemFollow(v) \leftarrow \emptyset
    foreach p \in PRODUCTIONSFOR(Start) do
        ItemFollow((StartState, Start \rightarrow \bullet RHS(p))) \leftarrow \{\$\}
    foreach s \in States do
         foreach A \rightarrow \alpha \bullet B\gamma \in s do
             v \leftarrow Graph \cdot FINDVERTEX((s, A \rightarrow \alpha \bullet B_{\gamma}))
             call Graph . AddEdge(v, (Table[s][B], A \rightarrow \alpha B \bullet \gamma))
             foreach (w \leftarrow (s, B \rightarrow \bullet \delta)) \in Graph.Vertices do
                  ItemFollow(w) \leftarrow ItemFollow(w) \cup First(\gamma)
                 if AllDeriveEmpty(γ)
                  then call Graph.AddEdge(v, w)
end
                                                    公 B可推到入乡加建
```

Goto

State

LR(0) Item

 $6 S \rightarrow x \bullet A C$ 

8 S→A • B

11 S → a • c

13 **Start**→**S**•\$

14 Start→S \$ •

15 S→a c•

17  $S \rightarrow A B \bullet$ 18  $S \rightarrow x A \bullet c$ 

16 B→b•

19 A→a•

11 | 20 S→x A c •

10

12 A → a •

12	
12	
18 19	
17 16	
10	

15

14

20

Prop Edges

Placed by Step

1 Start  $\rightarrow$  S \$

→ A B
| a c
| x A c

 $\rightarrow$  a

λ

Initialize

*ItemFollow* 

 $First(\gamma)$ 



procedure BuildItemPropGraph()

foreach  $item \in state do$ 

 $ItemFollow(v) \leftarrow \emptyset$ 

foreach  $A \rightarrow \alpha \bullet B\gamma \in s$  do

 $v \leftarrow Graph.AddVertex((s, item))$ 

 $ItemFollow((StartState, Start \rightarrow \bullet RHS(p))) \leftarrow \{\$\}$ 

 $v \leftarrow Graph \cdot FINDVERTEX((s, A \rightarrow \alpha \bullet B_{\gamma}))$ 

then call Graph.AddEdge(v, w)

call Graph. Add Edge  $(v, (Table[s][B], A \rightarrow \alpha B \bullet \gamma))$ 

**foreach**  $(w \leftarrow (s, B \rightarrow \bullet \delta)) \in Graph.Vertices$ **do** 

 $ItemFollow(w) \leftarrow ItemFollow(w) \cup First(\gamma)$ 

foreach  $p \in PRODUCTIONSFOR(Start)$  do

**if** AllDeriveEmpty(γ)

foreach  $s \in States$  do

foreach  $s \in States$  do

end

```
LR(0) Item
                                              Prop Edges
State
                                  Goto
                                  State
                                           Placed by Step
                                                        (29)
                                                                   First(\gamma)
          1 Start \rightarrow • S $
                                             13
           2 S \rightarrow \bullet AB
                                                         5
                                             11
               S \rightarrow \bullet x A c
                                             12
           6 S \rightarrow x \bullet A C
                                             18
                                             19
           7 A→ • a
                                     10
                                             17
                                                       9,10
           8 S \rightarrow A \bullet B
                                      8
           9 B \rightarrow \bullet b
                                             16
          10 B→ •
         11 S → a • c
                                             15
          12 A → a •
         13 Start \rightarrow S • $
                                             14
```

20

14 Start→S \$ •

15 S→a c•

16 B→b• 17 S→A B• 18  $S \rightarrow x A \bullet c$ 

19 A→a•

11 | 20 S→x A c •

10

1 Start  $\rightarrow$  S \$

 $\rightarrow$  A B a c x A c

 $\rightarrow$  a

Initialize

ItemFollow

2,3,4

```
procedure EvalItemPropGraph( )
   repeat
       changed \leftarrow false
       foreach (v, w) \in Graph.Edges do
           old \leftarrow ItemFollow(w)
           ItemFollow(w) \leftarrow ItemFollow(w) \cup ItemFollow(v)
          if ItemFollow(w) \neq old
          then changed ← true 有以类设备true
   until not changed
end
```

			3		. •		. 9.10				
State	LR(0) Item	Goto State	Placed by		Initialize ItemFollo First(γ)		Step 1	Item 1 2	Prop To 13 5,8	Initial \$ \$	
0	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	4 2 3	13 8 11	5	\$ 2 b	2,3,4		3 4	11 6	\$ \$	
	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	1 3	6 12					5×	12   /18 546	り推列ル	\$
	6 S→x•A c 7 A→•a	9 10	18 19		С	7		7 8	/ 19 <i>9</i> ,10,17	C	\$
2	$ \begin{array}{ccc} 8 & S \rightarrow A \bullet B \\ 9 & B \rightarrow \bullet b \\ 10 & B \rightarrow \bullet \end{array} $	8 7	16	9,10				9 10	16		\$ \$
3	11 S→a•c 12 A→a•	6	15					11 12	15		\$ b \$ \$
4 5	,	5	14					13 14	14		\$ \$
6	15 S→a c•							15 16			\$
7 8								17			\$ \$
9	18 S→x A•c	11	20					18	20		\$

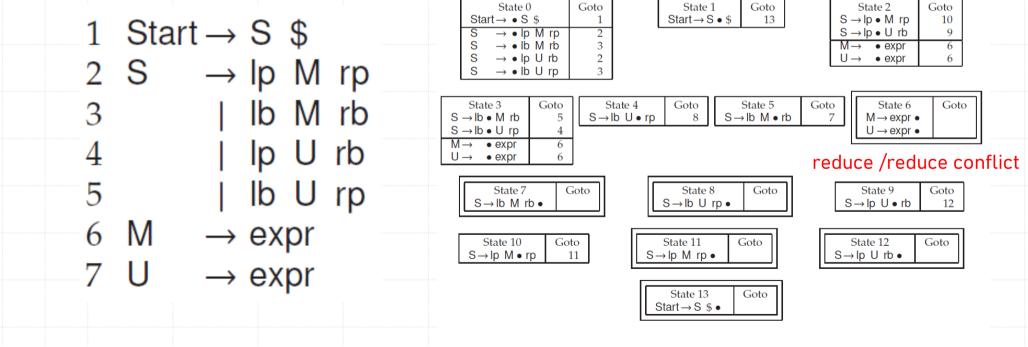


Figure 6.36: LR(0) construction.

State	LR(0) Item	Goto State	Prop Placed	Edges by Step	Initia ItemFore First( $\gamma$ )	
0	1 Start $\rightarrow$ • S \$ 2 S $\rightarrow$ • lp M rp 3 S $\rightarrow$ • lb M rb 4 S $\rightarrow$ • lp U rb 5 S $\rightarrow$ • lb U rp	1 2 3 2 3	?? 6 10 7 11		\$	2,3,4,5
2	6 S $\rightarrow$ Ip $\bullet$ M rp 7 S $\rightarrow$ Ip $\bullet$ U rb 8 M $\rightarrow$ $\bullet$ expr 9 U $\rightarrow$ $\bullet$ expr	10 9 6 6	?? ?? 14 15		rp rb	8 9
3	10 S $\rightarrow$ lb $\bullet$ M rb 11 S $\rightarrow$ lb $\bullet$ U rp 12 M $\rightarrow$ $\bullet$ expr 13 U $\rightarrow$ $\bullet$ expr	5 4 6 6	?? ?? 14 15		rb rp	12 13
6	$14  M \rightarrow expr \bullet \\ 15  U \rightarrow expr \bullet$					

ItemFollow(14) = ItemFollow(15) $= \{rb, rp\}$ 

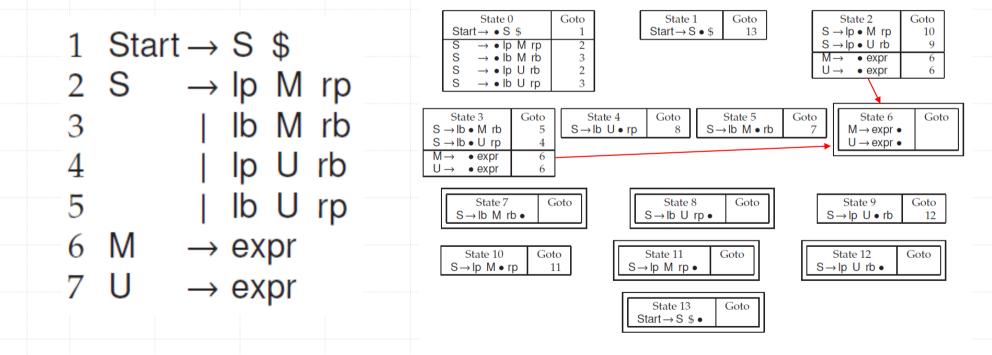


Figure 6.36: LR(0) construction.

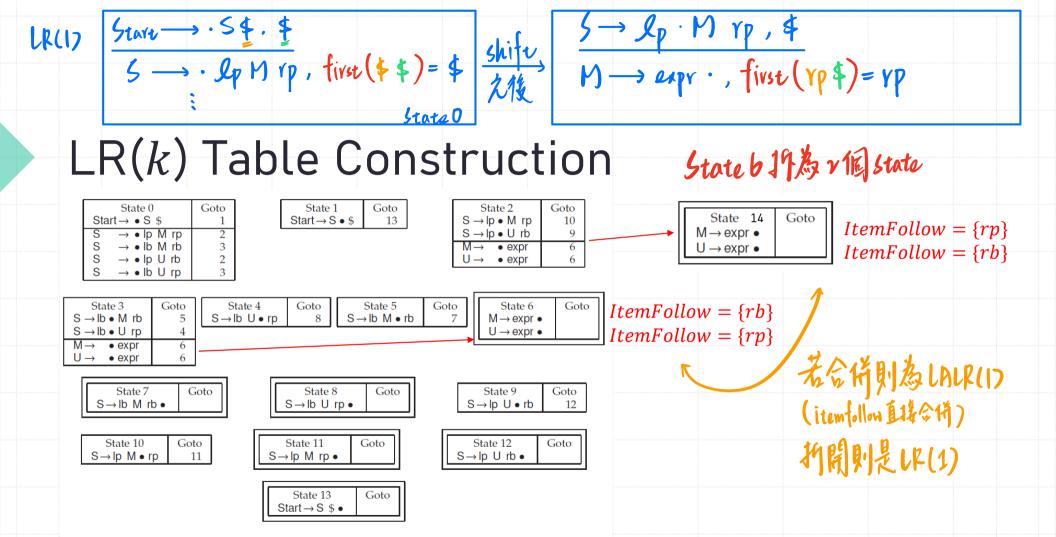
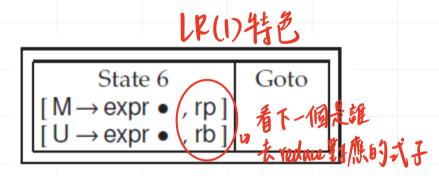


Figure 6.36: LR(0) construction.

- For LR(k), we extend an item's notation from  $A \to \alpha \bullet \beta$  to  $[A \to \alpha \bullet \beta, w]$ .
- For LR(1), w is a (terminal) symbol that can follow A when this item becomes reducible.
- For LR(k),  $k \ge 0$ , w is a k-length string that can follow A after reduction.
- If symbols x and y can both follow A when  $A \to \alpha \bullet \beta$  becomes reducible, then the corresponding LR(1) state contains both  $[A \to \alpha \bullet \beta, x]$  and  $[A \to \alpha \bullet \beta, y]$ .
- Notice how nicely the notation for LR(k) generalizes LR(0). For LR(0), w must be a 0-length string. The only such string is  $\lambda$ , which provides no information at a possible point of reduction, since  $\lambda$  does not occur as input.

State 3	Goto
$[S \rightarrow lb \bullet M rb, $]$	5
$[S \rightarrow lb \bullet U rp, $]$	4
[ M → • expr , rb ]	14
$[U \rightarrow \bullet expr, rp]$	14

 $[S \rightarrow lb \bullet M \ rb, \$]$  is not ready for reduction, but indicates that \$ will follow the reduction to S when the item eventually becomes reducible

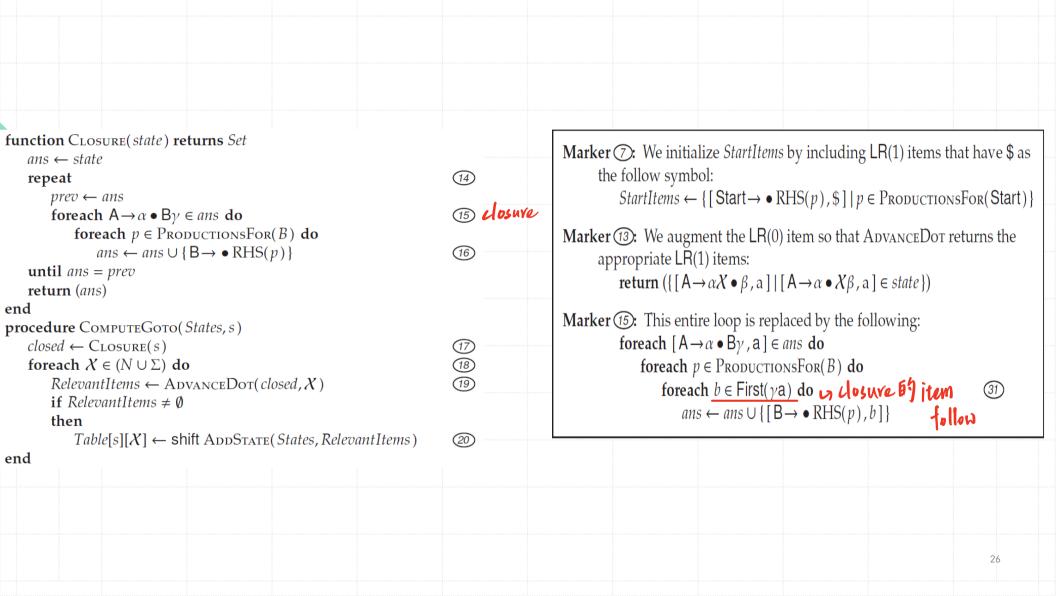


The item calls for a reduction by rule  $M \rightarrow expr$  when rp is the next input token.

#### **function** ComputeLR0(*Grammar*) **returns** (*Set*, *State*) $States \leftarrow \emptyset$ $StartItems \leftarrow \{Start \rightarrow \bullet RHS(p) \mid p \in ProductionsFor(Start)\}$ StartState ← AddState(States, StartItems) while $(s \leftarrow WorkList.ExtractElement()) \neq \bot do$ 8 **call** ComputeGoto(States, s) return ((States, StartState)) end function AddState(States, items) returns State **if** *items* ∉ *States* 9 then $s \leftarrow newState(items)$ 10 $States \leftarrow States \cup \{s\}$ $WorkList \leftarrow WorkList \cup \{s\}$ 11 $Table[s][\star] \leftarrow error$ (12) **else** $s \leftarrow FindState(items)$ return (s) end **function** AdvanceDot(state, X) **returns** Set **return** ({ $A \rightarrow \alpha X \bullet \beta \mid A \rightarrow \alpha \bullet X\beta \in state })$ (13)end

the follow symbol:  $StartItems \leftarrow \{ [Start \rightarrow \bullet RHS(p), \$] | p \in ProductionsFor(Start) \}$ **Marker** (13): We augment the LR(0) item so that AdvanceDot returns the appropriate LR(1) items: return ({ [ $A \rightarrow \alpha X \bullet \beta$ , a] | [ $A \rightarrow \alpha \bullet X \beta$ , a]  $\in state$ }) **Marker** 15: This entire loop is replaced by the following: foreach  $[A \rightarrow \alpha \bullet B\gamma, a] \in ans do$ **foreach**  $p \in ProductionsFor(B)$  **do** foreach  $b \in First(\gamma a)$  do  $ans \leftarrow ans \cup \{[B \rightarrow \bullet RHS(p), b]\}\$ 

**Marker** (7): We initialize *StartItems* by including LR(1) items that have \$ as



```
procedure CompleteTable(Table, grammar)
   call ComputeLookahead()
   foreach state ∈ Table do
      foreach rule ∈ Productions(grammar) do
          call TryRuleInState(state, rule)
   call AssertEntry(StartState, GoalSymbol, accept)
end
procedure AssertEntry(state, symbol, action)
   if Table[state][symbol] = error
   then Table[state][symbol] \leftarrow action
   else
      call ReportConflict(Table[state][symbol], action)
end
```

procedure TryRuleInState(s, r)

if LHS(r)  $\rightarrow$  RHS(r)  $\bullet$   $\in$  sthen

foreach  $X \in \text{Follow}(\text{LHS}(r))$  do

call AssertEntry(s, X, reduce r)

end



procedure TryRuleInState(s, r)

if [LHS(r) $\rightarrow$ RHS(r) $\bullet$ , w]  $\in$  sthen call AssertEntry(s, w, reduce r)
end

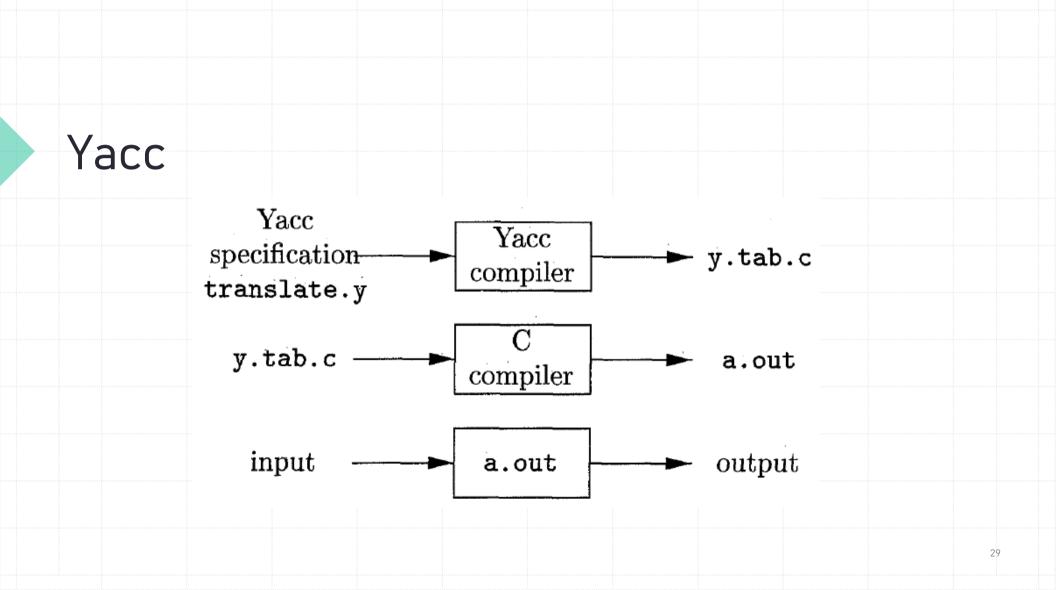
• Exercises 27, 40, 41, 45



# Crafting a Compiler

Charles N. Fischer Ron K. Cytron Richard J. LeBlanc, Jr.





# Disambiguating Rules for Yacc (\*required only when there exists a conflict)

- 1. In a shift/reduce conflict the default is to shift.
- 2. In a reduce/reduce conflict the default is to reduce by the earlier grammar rule in the input sequence.
- 3. Precedence and associativity (left, right, nonassoc) are recorded for each token that have them.

4. Precedence and associativity of a production rule is that (if any) of its final (rightmost) token unless a	
"%prec " overrides. Then it is the token given following %prec.	
5. In a shift/reduce conflict where both the grammar rule and the input (lookahead) have precedence, resolve in favor of the rule of higher precedence. In a tie, use associativity. That is, left assoc. => reduce; right assoc. => shift; nonassoc => error.	

6. Otherwise use 1 and 2.

(Please See Page 238 of the Textbook)

```
}%
                                                            #include <ctype.h>
                                                            %}
                                                                                  declared in "y.tab.h"
                                                            %token DIGIT
                                                            %%
                                                                                         { printf("%d\n", $1); }
                                                                    : expr '\n'
                                                            line
 Yacc
                                                                    : expr '+' term { $$ = $1 + $3; }
                                                            expr
                                                                    term
 declarations
 %%
                                                                    : term '*' factor { $$ = $1 * $3; }
                                                            term
                                                                      factor
 translation rules
                                                            factor : '(' expr ')'
                                                                                         \{ \$\$ = \$2; \}
 %%
                                                                      DIGIT
 supporting C routines
                                                            %%
                                                            yylex() {
                                                                int c;
(head)
               \langle body \rangle_1
                           { \langle semantic action \rangle_1 }
                                                                 c = getchar();
                                                                 if (isdigit(c)) {
                           { \langle semantic action \rangle_2 }
               \langle body \rangle_2
                                                                     yylval = c-'0';
                                                                     return DIGIT;
                           \{ \langle \text{semantic action} \rangle_n \}
              \langle \text{body} \rangle_n
                                                                return c;
```

- The lexical analyzer yylex() produces tokens consisting of a token name and its associated attribute value. If a token name such as DIGIT is returned, the token name must be declared in the first section of the Yacc specification. The attribute value associated with a token is communicated to the parser through a Yacc-defined variable yylval.
- Whenever the lexer returns a token to the parser, if the token has an associated value, the lexer must store the value in yylval before returning. In this first example, we explicitly declare yylval. In more complex parsers, yacc defines yylval as a union and puts the definition in y.tab.h.

return yytext[0];

%}

%%

\n

%%

[\t];

declared in "y.tab.h" #include "y.tab.h♥ extern int yylval; declared by yacc

The Lexer

[0-9]+ { yylval = atoi(yytext); return NUMBER; } /\* ignore whitespace \*/ return 0; /\* logical EOF \*/

statement: NAME '=' expression

%%

%token NAME NUMBER expression

→ NUMBER

A Yacc Parser

{ printf("= %d\n", \$1); }

{ \$\$ = \$1; }

expression: expression '+' NUMBER { \$\$ = \$1 + \$3; } expression '-' NUMBER  $\{ \$\$ = \$1 - \$3; \}$ 

On a UNIX system, yacc takes your grammar and creates y.tab.c, the C language parser, and y.tab.h, the include file with the token number definitions. Lex creates lex.yy.c, the C language lexer. You need only compile them together with the yacc and lex libraries. The libraries contain usable default versions of all of the supporting routines, including a main() that calls the parser yyparse() and exits.

```
% yacc -d ch3-01.y # makes y.tab.c and "y.tab.h
% lex ch3-01.l # makes lex.yy.c
% cc -o ch3-01 y.tab.c lex.yy.c -ly -ll # compile and link C files
```



```
'(' expression ')' { $$ = $2: }
double vbltable[26]:
                                                                     NUMBER
                                                                     NAME
                                                                                      %union {
     double dval:
                                                        %%
     int vblno:
                                                        Example 3-3. Lexer for calculator with variables and real values ch3-03.1
%token <vblno> NAME
%token <dval> NUMBER
%left '-' '+'
                                                        %{
%left '*' '/'
                                                        #include "v.tab.h"
%nonassoc UMINUS
                                                        #include <math.h>
                                                        extern double vbltable[26]:
%type <dval> expression
                                                        %}
statement list: statement '\n'
         statement_list statement '\n'
                                                        %%
                                                        ([0-9]+|([0-9]*\.[0-9]+)([eE][-+]?[0-9]+)?) {
statement: NAME '=' expression { vbltable[$1] = $3; }
                                                              yylval.dval = atof(yytext); return NUMBER;
                    { printf("= %a\n", $1); }
         expression
                                                        [\t];
                                                                            /* ignore whitespace */
expression: expression '+' expression \{ \$\$ = \$1 + \$3; \}
          expression '-' expression \{ \$\$ = \$1 - \$3; \}
          expression '*' expression { $$ = $1 * $3; }
                                                        [a-z] { yylval.vblno = yytext[0] - 'a'; return NAME; }
          expression '/' expression
                         if($3 == 0.0)
                                                            { return 0; /* end of input */ }
                                yyerror("divide by zero")
                          else
                                $$ = $1 / $3:
                                                        \n
                                                              return yytext[0];
          '-' expression %prec UMINUS { $$ = -$2; }
```

 The generated header file y tab.h includes a copy of the definition so that you can use it in the lexer. Here is the y.tab.h generated from this grammar:

```
#define NAME 257
#define NUMBER 258
#define UMINUS 259
```

typedef union { double dval;

int vblno; } YYSTYPE; extern YYSTYPE yylval;

## Symbol table

```
Example 3-4. Header for parser with symbol table ch3hdr.h
#define NSYMS 20 /* maximum number of symbols */
struct symtab {
```

struct symtab \*symlook();

```
struct symtab {
    char *name;
    double value;
} symtab[NSYMS];
```

/\* look up a symbol table entry, add if not present \*/

for(sp = symtab; sp < &symtab[NSYMS]; sp++) {</pre>

if(sp->name && !strcmp(sp->name, s))

sp->name = strdup(s);

/\* otherwise continue to next \*/

/\* cannot continue \*/

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/\* is it already here? \*/

return sp;

return sp;

/\* is it free \*/
if(!sp->name) {

yyerror("Too many symbols");

struct symtab \*

char \*p:

exit(1):

} /\* symlook \*/

struct symtab \*sp;

symlook(s)
char \*s;

```
%{
#include "ch3hdr.h"
                                            statement: NAME '=' expression { $1->value = $3; }
#include <string.h>
                                                       expression { printf("= %g\n", $1); }
%}
%union {
                                            expression: expression '+' expression \{ \$\$ = \$1 + \$3; \}
      double dval;
                                                        expression '-' expression \{ \$\$ = \$1 - \$3; \}
      struct symtab *symp;
                                                        expression '*' expression \{ \$\$ = \$1 * \$3; \}
                                                        expression '/' expression
%token <symp> NAME
                                                                    \{ if(\$3 == 0.0) \}
%token <dval> NUMBER
                                                                               yyerror("divide by zero"
%left '-' '+'
                                                                         else
%left '*' '/'
                                                                               $$ = $1 / $3;
%nonassoc UMINUS
                                                        '-' expression %prec UMINUS { $$ = -$2; }
                                                        '(' expression ')' { $$ = $2; }
%type <dval> expression
                                                        NUMBER
%%
                                                        NAME
                                                                          { $$ = $1->value; }
statement_list: statement '\n'
           statement list statement '\n'
                                                                                                  40
```

%{ #include "y.tab.h" #include "ch3hdr.h" #include <math.h> %} %%  $([0-9]+|([0-9]*\.[0-9]+)([eE][-+]?[0-9]+)?)$  { yylval.dval = atof(yytext); return NUMBER; Symbol table (Lex) [\t]; /\* ignore whitespace \*/ [A-Za-z][A-Za-z0-9]\* { /\* return symbol pointer \*/ yylval.symp = symlook(yytext); return NAME; "\$" { return 0; } \n return yytext[0]; 41