

Table 1: Test results of the six methods for problems 3.1-3.2

| TP | DIM | ISP | NDKM1 | | | NDKM2 | | | ACGD | | | SCGP | | | TTMDY | | | HCGP | | | | | | | | |
|-----|-------|---------|-------|----|--------|------------|-----|----|--------|------|-----|------|--------|------------|-------|-----|--------|------------|-----|-----|--------|------------|----|----|--------|------------|
| | | | #IT | FV | PT | Norm | #IT | FV | PT | Norm | #IT | FV | PT | Norm | #IT | FV | PT | Norm | #IT | FV | PT | Norm | | | | |
| 3.1 | 5000 | x_1^0 | 3 | 7 | 0.8977 | 0 | 4 | 9 | 0.0387 | 0 | 19 | 48 | 0.0653 | 5.8575E-10 | 2 | 6 | 0.0884 | 0 | 45 | 191 | 0.1434 | 8.8689E-10 | 17 | 38 | 0.0833 | 8.3688E-10 |
| | 5000 | x_2^0 | 3 | 7 | 0.0206 | 0 | 4 | 9 | 0.0175 | 0 | 20 | 59 | 0.0613 | 4.7625E-10 | 3 | 10 | 0.0171 | 0 | 50 | 216 | 0.1623 | 6.0668E-10 | 3 | 10 | 0.0231 | 0 |
| | 5000 | x_3^0 | 3 | 8 | 0.0133 | 0 | 4 | 10 | 0.0158 | 0 | 19 | 56 | 0.0639 | 6.5736E-10 | 2 | 8 | 0.0104 | 0 | 54 | 244 | 0.1748 | 8.8715E-10 | 19 | 42 | 0.0533 | 8.3426E-10 |
| | 5000 | x_4^0 | 5 | 7 | 0.0141 | 0 | 6 | 8 | 0.0146 | 0 | 19 | 41 | 0.0568 | 7.0236E-10 | 32 | 115 | 0.0996 | 1.4486E-10 | 69 | 282 | 0.2044 | 7.7707E-10 | 17 | 35 | 0.0365 | 6.7910E-10 |
| | 5000 | x_5^0 | 5 | 7 | 0.0164 | 0 | 6 | 8 | 0.0177 | 0 | 19 | 41 | 0.0591 | 7.0005E-10 | 24 | 73 | 0.0690 | 0 | 74 | 302 | 0.2214 | 6.6563E-10 | 17 | 35 | 0.0436 | 6.7866E-10 |
| | 5000 | x_6^0 | 5 | 7 | 0.0159 | 0 | 6 | 8 | 0.0157 | 0 | 19 | 41 | 0.0502 | 7.0005E-10 | 24 | 73 | 0.0697 | 0 | 74 | 302 | 0.2151 | 6.6563E-10 | 17 | 35 | 0.0485 | 6.7866E-10 |
| | 5000 | x_7^0 | 5 | 7 | 0.0143 | 0 | 6 | 8 | 0.0157 | 0 | 17 | 40 | 0.0534 | 3.9053E-10 | 14 | 32 | 0.0327 | 8.5720E-10 | 42 | 174 | 0.1479 | 7.4894E-10 | 15 | 31 | 0.0482 | 7.3444E-10 |
| | 25000 | x_1^0 | 3 | 7 | 0.0989 | 0 | 4 | 9 | 0.0448 | 0 | 20 | 50 | 0.1838 | 3.4075E-10 | 2 | 6 | 0.0260 | 0 | 50 | 207 | 0.4440 | 9.7741E-10 | 18 | 38 | 0.1633 | 9.3567E-10 |
| | 25000 | x_2^0 | 3 | 7 | 0.0290 | 0 | 4 | 9 | 0.0406 | 0 | 22 | 61 | 0.1951 | 2.6139E-10 | 3 | 10 | 0.0337 | 0 | 52 | 224 | 0.4742 | 3.4491E-10 | 3 | 10 | 0.0366 | 0 |
| | 25000 | x_3^0 | 3 | 8 | 0.0403 | 0 | 4 | 10 | 0.0514 | 0 | 21 | 58 | 0.2126 | 3.8315E-10 | 2 | 8 | 0.0267 | 0 | 56 | 252 | 0.5234 | 5.0491E-10 | 19 | 44 | 0.1703 | 9.3273E-10 |
| | 25000 | x_4^0 | 5 | 7 | 0.0574 | 0 | 5 | 7 | 0.0524 | 0 | 20 | 43 | 0.1585 | 4.2915E-10 | 24 | 69 | 0.1925 | 0 | 73 | 298 | 0.6002 | 5.0661E-10 | 17 | 37 | 0.1442 | 7.5906E-10 |
| | 25000 | x_5^0 | 5 | 7 | 0.0472 | 0 | 5 | 7 | 0.0475 | 0 | 20 | 43 | 0.1681 | 4.2886E-10 | 32 | 106 | 0.2752 | 4.2207E-10 | 80 | 322 | 0.6624 | 9.0684E-10 | 17 | 37 | 0.1507 | 7.5896E-10 |
| | 25000 | x_6^0 | 5 | 7 | 0.0463 | 0 | 5 | 7 | 0.0542 | 0 | 20 | 43 | 0.1562 | 4.2886E-10 | 24 | 70 | 0.2011 | 0 | 80 | 322 | 0.6574 | 9.0683E-10 | 17 | 37 | 0.1448 | 7.5896E-10 |
| | 25000 | x_7^0 | 5 | 7 | 0.0471 | 0 | 6 | 8 | 0.0509 | 0 | 17 | 40 | 0.1370 | 3.9047E-10 | 3 | 12 | 0.0397 | 0 | 46 | 190 | 0.4004 | 3.8120E-10 | 15 | 31 | 0.1272 | 7.3492E-10 |
| | 50000 | x_1^0 | 3 | 7 | 0.1374 | 0 | 4 | 9 | 0.0877 | 0 | 20 | 50 | 0.2994 | 4.8193E-10 | 2 | 6 | 0.0481 | 0 | 50 | 211 | 0.8949 | 2.5272E-10 | 18 | 40 | 0.2409 | 6.6160E-10 |
| | 50000 | x_2^0 | 3 | 7 | 0.0689 | 0 | 4 | 9 | 0.0739 | 0 | 21 | 61 | 0.3729 | 3.6439E-10 | 3 | 10 | 0.0644 | 0 | 52 | 224 | 0.9613 | 4.8782E-10 | 3 | 10 | 0.0674 | 0 |
| | 50000 | x_3^0 | 3 | 8 | 0.0638 | 0 | 4 | 10 | 0.0848 | 0 | 20 | 58 | 0.3270 | 5.4214E-10 | 2 | 8 | 0.0477 | 0 | 56 | 252 | 1.0177 | 7.1408E-10 | 20 | 44 | 0.2594 | 6.5953E-10 |
| | 50000 | x_4^0 | 5 | 7 | 0.0888 | 0 | 5 | 7 | 0.0900 | 0 | 20 | 43 | 0.2975 | 6.1619E-10 | 24 | 69 | 0.3403 | 0 | 77 | 310 | 1.2967 | 8.1239E-10 | 18 | 37 | 0.2440 | 5.3672E-10 |
| | 50000 | x_5^0 | 5 | 7 | 0.0771 | 0 | 5 | 7 | 0.0855 | 0 | 20 | 43 | 0.2840 | 6.1598E-10 | 32 | 85 | 0.4244 | 6.6612E-10 | 81 | 326 | 1.3223 | 9.6291E-10 | 18 | 37 | 0.2475 | 5.3669E-10 |
| | 50000 | x_6^0 | 5 | 7 | 0.0842 | 0 | 5 | 7 | 0.0799 | 0 | 20 | 43 | 0.2850 | 6.1598E-10 | 31 | 85 | 0.4277 | 5.2162E-10 | 81 | 326 | 1.3314 | 9.6291E-10 | 18 | 37 | 0.2484 | 5.3669E-10 |
| | 50000 | x_7^0 | 5 | 7 | 0.0818 | 0 | 6 | 8 | 0.1044 | 0 | 17 | 40 | 0.2587 | 3.9046E-10 | 3 | 13 | 0.0734 | 0 | 42 | 174 | 0.7525 | 9.8343E-10 | 15 | 31 | 0.2046 | 7.3498E-10 |
| 3.2 | 5000 | x_1^0 | 9 | 19 | 0.0620 | 1.0041E-10 | 7 | 18 | 0.0263 | 0 | 17 | 73 | 0.0754 | 2.8178E-10 | 20 | 72 | 0.0701 | 3.4695E-11 | 97 | 588 | 0.3749 | 9.5036E-10 | 23 | 66 | 0.0698 | 5.1459E-10 |
| | 5000 | x_2^0 | 6 | 14 | 0.0280 | 1.4200E-11 | 6 | 14 | 0.0209 | 0 | 16 | 74 | 0.0682 | 2.4515E-10 | 2 | 8 | 0.0108 | 0 | 96 | 590 | 0.3670 | 9.8843E-10 | 15 | 48 | 0.0446 | 4.7412E-10 |
| | 5000 | x_3^0 | 6 | 15 | 0.0229 | 7.7028E-11 | 6 | 15 | 0.0268 | 0 | 18 | 82 | 0.0758 | 2.3270E-10 | 2 | 9 | 0.0118 | 0 | 87 | 547 | 0.3353 | 4.7132E-10 | 19 | 59 | 0.0766 | 3.8532E-10 |
| | 5000 | x_4^0 | 1 | 3 | 0.0395 | 0 | 1 | 3 | 0.0072 | 0 | 16 | 66 | 0.0767 | 3.7411E-10 | 32 | 184 | 0.1397 | 0 | 97 | 589 | 0.3687 | 5.2488E-10 | 16 | 51 | 0.0659 | 4.8215E-11 |
| | 5000 | x_5^0 | 1 | 3 | 0.0069 | 0 | 1 | 3 | 0.0067 | 0 | 16 | 66 | 0.0632 | 3.7453E-10 | 35 | 210 | 0.1710 | 0 | 102 | 613 | 0.4024 | 8.4380E-10 | 21 | 59 | 0.0665 | 6.7163E-10 |
| | 5000 | x_6^0 | 1 | 3 | 0.0071 | 0 | 1 | 3 | 0.0054 | 0 | 16 | 66 | 0.0738 | 3.7453E-10 | 35 | 210 | 0.1493 | 0 | 102 | 613 | 0.4087 | 8.4380E-10 | 21 | 59 | 0.0807 | 6.7163E-10 |
| | 5000 | x_7^0 | 1 | 3 | 0.0053 | 0 | 1 | 3 | 0.0068 | 0 | 15 | 61 | 0.0727 | 3.3464E-10 | 78 | 526 | 0.3255 | 6.3464E-10 | 68 | 407 | 0.2638 | 7.1894E-10 | 22 | 58 | 0.0820 | 2.1895E-10 |
| | 25000 | x_1^0 | 9 | 19 | 0.1315 | 4.8700E-10 | 7 | 18 | 0.0987 | 0 | 17 | 73 | 0.2127 | 6.3019E-10 | 21 | 73 | 0.2374 | 9.8647E-10 | 101 | 612 | 1.3133 | 9.2314E-10 | 24 | 69 | 0.2407 | 4.0531E-10 |
| | 25000 | x_2^0 | 6 | 14 | 0.0759 | 3.1690E-12 | 6 | 14 | 0.0653 | 0 | 17 | 74 | 0.2347 | 5.6009E-10 | 2 | 8 | 0.0374 | 0 | 102 | 627 | 1.3451 | 7.7535E-10 | 16 | 51 | 0.1721 | 2.0744E-10 |
| | 25000 | x_3^0 | 6 | 15 | 0.0798 | 1.7505E-11 | 6 | 15 | 0.0768 | 0 | 17 | 82 | 0.2341 | 5.2295E-10 | 2 | 9 | 0.0332 | 0 | 105 | 649 | 1.4014 | 7.9802E-10 | 20 | 62 | 0.2155 | 1.6763E-10 |
| | 25000 | x_4^0 | 1 | 3 | 0.0263 | 0 | 1 | 3 | 0.0170 | 0 | 16 | 66 | 0.2079 | 8.5745E-10 | 23 | 114 | 0.2855 | 0 | 106 | 637 | 1.3429 | 7.3824E-10 | 18 | 55 | 0.2017 | 9.0689E-10 |
| | 25000 | x_5^0 | 1 | 3 | 0.0134 | 0 | 1 | 3 | 0.0162 | 0 | 16 | 66 | 0.2123 | 8.5764E-10 | 23 | 120 | 0.3139 | 0 | 101 | 613 | 1.3312 | 3.9582E-10 | 23 | 65 | 0.2064 | 9.1829E-11 |
| | 25000 | x_6^0 | 1 | 3 | 0.0128 | 0 | 1 | 3 | 0.0152 | 0 | 16 | 66 | 0.2093 | 8.5764E-10 | 23 | 120 | 0.3061 | 0 | 101 | 613 | 1.3005 | 3.9582E-10 | 23 | 65 | 0.2104 | 9.1827E-11 |
| | 25000 | x_7^0 | 1 | 3 | 0.0134 | 0 | 1 | 3 | 0.0151 | 0 | 15 | 61 | 0.1973 | 3.3485E-10 | 106 | 708 | 1.5470 | 0 | 63 | 383 | 0.8369 | 6.1257E-10 | 22 | 58 | 0.2092 | 2.1896E-10 |
| | 50000 | x_1^0 | 9 | 19 | 0.2043 | 4.2318E-10 | 7 | 16 | 0.1759 | 0 | 16 | 73 | 0.3892 | 8.9117E-10 | 21 | 76 | 0.4386 | 6.9513E-10 | 102 | 618 | 2.6118 | 8.6051E-10 | 24 | 69 | 0.4949 | 5.8327E-10 |
| | 50000 | x_2^0 | 6 | 14 | 0.1428 | 1.8121E-12 | 6 | 14 | 0.1427 | 0 | 17 | 74 | 0.3916 | 7.9420E-10 | 2 | 8 | 0.0652 | 0 | 100 | 621 | 2.6332 | 5.3533E-10 | 17 | 54 | 0.3496 | 9.0964E-11 |
| | 50000 | x_3^0 | 6 | 15 | 0.1388 | 9.0148E-12 | 6 | 15 | 0.1434 | 0 | 18 | 82 | 0.4419 | 7.4042E-10 | 2 | 9 | 0.0804 | 0 | 107 | 661 | 2.8087 | 7.9156E-10 | 21 | 65 | 0.4448 | 7.2625E-11 |
| | 50000 | x_4^0 | 1 | 3 | 0.0269 | 0 | 1 | 3 | 0.0264 | 0 | 17 | 70 | 0.3640 | 2.3149E-10 | 23 | 114 | 0.5154 | 0 | 107 | 643 | 2.7611 | 9.5604E-10 | 18 | 58 | 0.3423 | 6.4125E-10 |
| | 50000 | x_5^0 | 1 | 3 | 0.0274 | 0 | 1 | 3 | 0.0297 | 0 | 17 | 70 | 0.3760 | 2.3152E-10 | 20 | 95 | 0.4669 | 0 | 101 | 613 | 2.7271 | 5.6353E-10 | 23 | 65 | 0.4160 | 1.1385E-10 |
| | 50000 | x_6^0 | 1 | 3 | 0.0274 | 0 | 1 | 3 | 0.0260 | 0 | 17 | 70 | 0.3877 | 2.3152E-10 | 20 | 95 | 0.4789 | 0 | 101 | 613 | 2.6345 | 5.6353E-10 | 23 | 65 | 0.4074 | 1.1385E-10 |
| | 50000 | x_7^0 | 1 | 3 | 0.0292 | 0 | 1 | 3 | 0.0270 | 0 | 15 | 61 | 0.3278 | 3.3487E-10 | 58 | 382 | 1.5689 | 6.6334E-11 | 63 | 383 | 1.6137 | 6.1012E-10 | 22 | 58 | 0.3696 | 2.1897E-10 |

Table 2: Test results of the six methods for problems 3.3-3.4

| TP | DIM | ISP | NDKM1 | | | NDKM2 | | | ACGD | | | SCGP | | | TTMDY | | | HCGP | | | | | | | | |
|-----|-------|---------|-------|----|--------|-------|-----|----|--------|------|-----|------|--------|------------|-------|-----|--------|------------|-----|-----|--------|------------|----|----|--------|------------|
| | | | #IT | FV | PT | Norm | #IT | FV | PT | Norm | #IT | FV | PT | Norm | #IT | FV | PT | Norm | #IT | FV | PT | Norm | | | | |
| 3.3 | 5000 | x_0^1 | 3 | 4 | 0.0710 | 0 | 3 | 4 | 0.0119 | 0 | 19 | 46 | 0.0739 | 1.3132E-11 | 2 | 3 | 0.0075 | 0 | 47 | 189 | 0.1864 | 3.6649E-10 | 2 | 3 | 0.0091 | 0 |
| | 5000 | x_0^2 | 3 | 4 | 0.0123 | 0 | 3 | 4 | 0.0111 | 0 | 12 | 21 | 0.0448 | 2.1586E-10 | 2 | 3 | 0.0088 | 0 | 52 | 206 | 0.2064 | 7.8074E-10 | 2 | 3 | 0.0081 | 0 |
| | 5000 | x_0^3 | 4 | 5 | 0.0159 | 0 | 3 | 4 | 0.0111 | 0 | 13 | 22 | 0.0417 | 6.4222E-10 | 16 | 31 | 0.0540 | 7.3942E-11 | 52 | 204 | 0.1993 | 4.4483E-10 | 7 | 11 | 0.0188 | 0 |
| | 5000 | x_0^4 | 2 | 3 | 0.0102 | 0 | 2 | 3 | 0.0090 | 0 | 15 | 27 | 0.0468 | 2.3164E-11 | 27 | 68 | 0.0892 | 6.0928E-10 | 79 | 314 | 0.2879 | 5.8703E-10 | 8 | 14 | 0.0212 | 0 |
| | 5000 | x_0^5 | 2 | 3 | 0.0096 | 0 | 2 | 3 | 0.0082 | 0 | 13 | 25 | 0.0484 | 8.8107E-12 | 26 | 67 | 0.0778 | 2.5174E-10 | 79 | 314 | 0.2710 | 5.8079E-10 | 8 | 14 | 0.0303 | 0 |
| | 5000 | x_0^6 | 2 | 3 | 0.0092 | 0 | 2 | 3 | 0.0093 | 0 | 13 | 25 | 0.0438 | 8.8108E-12 | 27 | 68 | 0.0904 | 6.1786E-10 | 79 | 314 | 0.2704 | 5.8079E-10 | 8 | 14 | 0.0227 | 0 |
| | 5000 | x_0^7 | 4 | 5 | 0.0156 | 0 | 13 | 28 | 0.0482 | 0 | 9 | 35 | 0.0456 | 0 | 26 | 111 | 0.1064 | 3.8626E-11 | 61 | 246 | 0.2422 | 5.9076E-10 | 9 | 16 | 0.0260 | 0 |
| | 25000 | x_0^1 | 3 | 4 | 0.0445 | 0 | 3 | 4 | 0.0425 | 0 | 19 | 37 | 0.2058 | 3.7560E-10 | 2 | 3 | 0.0269 | 0 | 47 | 189 | 0.6016 | 8.1497E-10 | 2 | 3 | 0.0228 | 0 |
| | 25000 | x_0^2 | 3 | 4 | 0.0367 | 0 | 3 | 4 | 0.0475 | 0 | 17 | 32 | 0.1872 | 6.9262E-10 | 2 | 3 | 0.0252 | 0 | 54 | 214 | 0.6954 | 9.4518E-10 | 2 | 3 | 0.0207 | 0 |
| | 25000 | x_0^3 | 4 | 5 | 0.0530 | 0 | 4 | 5 | 0.0534 | 0 | 19 | 75 | 0.2826 | 0 | 22 | 81 | 0.2728 | 0 | 52 | 204 | 0.6794 | 9.9202E-10 | 17 | 34 | 0.1972 | 6.3731E-10 |
| | 25000 | x_0^4 | 2 | 3 | 0.0244 | 0 | 2 | 3 | 0.0252 | 0 | 23 | 70 | 0.2885 | 2.9180E-10 | 28 | 50 | 0.2724 | 6.3402E-10 | 81 | 322 | 1.0554 | 7.2141E-10 | 17 | 35 | 0.1915 | 8.4511E-10 |
| | 25000 | x_0^5 | 2 | 3 | 0.0270 | 0 | 2 | 3 | 0.0287 | 0 | 14 | 49 | 0.2105 | 0 | 31 | 93 | 0.3532 | 0 | 81 | 322 | 1.0571 | 7.2043E-10 | 17 | 35 | 0.1904 | 8.4507E-10 |
| | 25000 | x_0^6 | 2 | 3 | 0.0271 | 0 | 2 | 3 | 0.0265 | 0 | 14 | 49 | 0.2029 | 0 | 37 | 107 | 0.4015 | 1.6215E-10 | 81 | 322 | 0.9967 | 7.2043E-10 | 17 | 35 | 0.1921 | 8.4507E-10 |
| | 25000 | x_0^7 | 4 | 5 | 0.0474 | 0 | 13 | 28 | 0.1635 | 0 | 10 | 42 | 0.1541 | 0 | 41 | 209 | 0.6300 | 4.9957E-10 | 61 | 246 | 0.7728 | 5.9807E-10 | 15 | 31 | 0.1621 | 7.3051E-10 |
| | 50000 | x_0^1 | 3 | 4 | 0.0691 | 0 | 3 | 4 | 0.0736 | 0 | 19 | 37 | 0.3884 | 4.7924E-10 | 2 | 3 | 0.0463 | 0 | 49 | 197 | 1.2607 | 2.9282E-10 | 2 | 3 | 0.0434 | 0 |
| | 50000 | x_0^2 | 3 | 4 | 0.0776 | 0 | 3 | 4 | 0.0839 | 0 | 17 | 32 | 0.3537 | 9.9633E-10 | 2 | 3 | 0.0438 | 0 | 57 | 226 | 1.4326 | 2.4722E-10 | 2 | 3 | 0.0500 | 0 |
| | 50000 | x_0^3 | 4 | 5 | 0.1027 | 0 | 4 | 5 | 0.0906 | 0 | 20 | 38 | 0.3893 | 7.4072E-10 | 18 | 34 | 0.3396 | 8.4595E-10 | 54 | 212 | 1.3186 | 3.5655E-10 | 17 | 34 | 0.9900 | 9.0866E-10 |
| | 50000 | x_0^4 | 2 | 3 | 0.0458 | 0 | 2 | 3 | 0.0501 | 0 | 29 | 116 | 0.7820 | 5.1298E-10 | 37 | 107 | 0.7803 | 9.9607E-11 | 83 | 330 | 2.1031 | 5.6836E-10 | 18 | 35 | 0.5716 | 6.0442E-10 |
| | 50000 | x_0^5 | 2 | 3 | 0.0450 | 0 | 2 | 3 | 0.0468 | 0 | 21 | 105 | 0.6746 | 0 | 37 | 108 | 0.7884 | 1.7198E-10 | 86 | 338 | 2.1001 | 8.0686E-10 | 18 | 35 | 0.5168 | 6.0440E-10 |
| | 50000 | x_0^6 | 2 | 3 | 0.0549 | 0 | 2 | 3 | 0.0462 | 0 | 26 | 100 | 0.7400 | 8.7113E-10 | 30 | 82 | 0.6612 | 0 | 83 | 330 | 2.0682 | 5.6799E-10 | 18 | 35 | 0.5074 | 6.0440E-10 |
| | 50000 | x_0^7 | 4 | 5 | 0.0895 | 0 | 13 | 28 | 0.2900 | 0 | 18 | 50 | 0.3933 | 6.1519E-10 | 29 | 158 | 0.8732 | 3.9361E-11 | 61 | 246 | 1.4678 | 5.9787E-10 | 15 | 31 | 0.4763 | 7.6284E-10 |
| 3.4 | 5000 | x_0^1 | 4 | 6 | 0.0546 | 0 | 4 | 6 | 0.0144 | 0 | 18 | 40 | 0.0707 | 8.0222E-10 | 18 | 48 | 0.0653 | 8.5046E-11 | 57 | 233 | 0.2066 | 6.0879E-10 | 18 | 37 | 0.0749 | 8.3352E-10 |
| | 5000 | x_0^2 | 3 | 5 | 0.0153 | 0 | 3 | 5 | 0.0117 | 0 | 19 | 43 | 0.0687 | 3.5287E-10 | 18 | 37 | 0.0512 | 9.2930E-10 | 56 | 237 | 0.1948 | 5.3432E-10 | 18 | 39 | 0.1218 | 6.5455E-10 |
| | 5000 | x_0^3 | 3 | 5 | 0.0111 | 0 | 3 | 5 | 0.0122 | 0 | 19 | 43 | 0.0638 | 4.2325E-10 | 2 | 5 | 0.0093 | 0 | 42 | 183 | 0.1752 | 9.5386E-10 | 19 | 42 | 0.1116 | 7.7614E-10 |
| | 5000 | x_0^4 | 1 | 2 | 0.0069 | 0 | 2 | 4 | 0.0095 | 0 | 18 | 39 | 0.0639 | 2.8540E-10 | 16 | 34 | 0.0565 | 1.2384E-10 | 45 | 186 | 0.1640 | 4.8273E-10 | 17 | 37 | 0.0751 | 8.4765E-10 |
| | 5000 | x_0^5 | 1 | 2 | 0.0065 | 0 | 2 | 4 | 0.0082 | 0 | 18 | 39 | 0.0579 | 2.8529E-10 | 18 | 48 | 0.0573 | 3.0011E-11 | 50 | 205 | 0.1810 | 7.2745E-10 | 17 | 37 | 0.1073 | 8.4752E-10 |
| | 5000 | x_0^6 | 1 | 2 | 0.0057 | 0 | 2 | 4 | 0.0081 | 0 | 18 | 39 | 0.0541 | 2.8529E-10 | 16 | 34 | 0.0490 | 1.1755E-10 | 50 | 205 | 0.1775 | 7.2745E-10 | 17 | 37 | 0.0820 | 8.4752E-10 |
| | 5000 | x_0^7 | 1 | 2 | 0.0061 | 0 | 2 | 4 | 0.0077 | 0 | 22 | 77 | 0.0873 | 6.0670E-10 | 28 | 100 | 0.0915 | 9.2527E-10 | 37 | 154 | 0.1428 | 4.7713E-10 | 15 | 31 | 0.0724 | 8.4505E-10 |
| | 25000 | x_0^1 | 4 | 6 | 0.0460 | 0 | 4 | 6 | 0.0419 | 0 | 19 | 42 | 0.1939 | 4.6698E-10 | 17 | 36 | 0.1564 | 2.5527E-10 | 59 | 241 | 0.6255 | 6.3276E-10 | 18 | 39 | 0.2367 | 9.3190E-10 |
| | 25000 | x_0^2 | 3 | 5 | 0.0361 | 0 | 3 | 5 | 0.0327 | 0 | 19 | 43 | 0.1848 | 7.8971E-10 | 29 | 101 | 0.3086 | 7.1171E-10 | 58 | 247 | 0.6228 | 5.0626E-10 | 19 | 39 | 0.2334 | 7.3181E-10 |
| | 25000 | x_0^3 | 3 | 5 | 0.0317 | 0 | 3 | 5 | 0.0383 | 0 | 19 | 43 | 0.2013 | 9.4749E-10 | 2 | 5 | 0.0299 | 0 | 44 | 192 | 0.5290 | 8.7485E-10 | 20 | 42 | 0.2724 | 8.6775E-10 |
| | 25000 | x_0^4 | 1 | 2 | 0.0102 | 0 | 2 | 4 | 0.0277 | 0 | 18 | 39 | 0.1788 | 6.3961E-10 | 27 | 87 | 0.2785 | 7.4313E-10 | 50 | 204 | 0.5224 | 9.9113E-10 | 18 | 37 | 0.2724 | 9.4764E-10 |
| | 25000 | x_0^5 | 1 | 2 | 0.0141 | 0 | 2 | 4 | 0.0272 | 0 | 18 | 39 | 0.1795 | 6.3956E-10 | 26 | 75 | 0.2625 | 9.1380E-10 | 55 | 224 | 0.5611 | 4.8352E-10 | 18 | 37 | 0.3007 | 9.4761E-10 |
| | 25000 | x_0^6 | 1 | 2 | 0.0105 | 0 | 2 | 4 | 0.0212 | 0 | 18 | 39 | 0.1773 | 6.3956E-10 | 21 | 72 | 0.2363 | 0 | 55 | 224 | 0.5646 | 4.8352E-10 | 18 | 37 | 0.2499 | 9.4761E-10 |
| | 25000 | x_0^7 | 1 | 2 | 0.0139 | 0 | 2 | 4 | 0.0272 | 0 | 15 | 87 | 0.2214 | 0 | 23 | 60 | 0.2248 | 8.0118E-10 | 44 | 180 | 0.4619 | 7.7250E-10 | 15 | 31 | 0.2057 | 8.4513E-10 |
| | 50000 | x_0^1 | 4 | 6 | 0.0837 | 0 | 4 | 6 | 0.1063 | 0 | 19 | 42 | 0.3577 | 6.6061E-10 | 29 | 99 | 0.5816 | 6.1198E-10 | 59 | 241 | 1.2432 | 8.9377E-10 | 19 | 39 | 0.4351 | 6.5895E-10 |
| | 50000 | x_0^2 | 3 | 5 | 0.0699 | 0 | 3 | 5 | 0.0638 | 0 | 20 | 45 | 0.3739 | 2.9052E-10 | 31 | 92 | 0.5312 | 6.8610E-10 | 60 | 254 | 1.2898 | 3.8481E-10 | 19 | 41 | 0.5044 | 5.1747E-10 |
| | 50000 | x_0^3 | 3 | 5 | 0.0705 | 0 | 3 | 5 | 0.0693 | 0 | 20 | 45 | 0.3540 | 3.4848E-10 | 2 | 5 | 0.0496 | 0 | 43 | 187 | 1.0866 | 5.4214E-10 | 20 | 44 | 0.4648 | 6.1359E-10 |
| | 50000 | x_0^4 | 1 | 2 | 0.0234 | 0 | 2 | 4 | 0.0454 | 0 | 18 | 39 | 0.3124 | 9.0506E-10 | 20 | 60 | 0.3705 | 0 | 45 | 185 | 0.9938 | 8.2498E-10 | 18 | 39 | 0.4638 | 6.7008E-10 |
| | 50000 | x_0^5 | 1 | 2 | 0.0241 | 0 | 2 | 4 | 0.0464 | 0 | 18 | 39 | 0.3254 | 9.0503E-10 | 30 | 82 | 0.5331 | 5.8087E-10 | 50 | 204 | 1.0641 | 8.9909E-10 | 18 | 39 | 0.4534 | 6.7007E-10 |
| | 50000 | x_0^6 | 1 | 2 | 0.0229 | 0 | 2 | 4 | 0.0495 | 0 | 18 | 39 | 0.3269 | 9.0503E-10 | 16 | 34 | 0.2644 | 8.9985E-10 | 50 | 204 | 1.0614 | 8.9908E-10 | 18 | 39 | 0.4518 | 6.7007E-10 |
| | 50000 | x_0^7 | 1 | 2 | 0.0242 | 0 | 2 | 4 | 0.0443 | 0 | 21 | 73 | 0.4241 | 4.0276E-10 | 17 | 39 | 0.3048 | 8.6157E-10 | 47 | 192 | 0.9496 | 9.0225E-10 | 15 | 31 | 0.3367 | 8.4514E-10 |

Table 4: Test results of the six methods for problem 3.7

| TP | DIM | ISP | NDKMI | | | NDKM2 | | | ACGD | | | SCGP | | | TTMDY | | | HCGP | | | | | | | | |
|-----|-------|---------|-------|----|--------|------------|-----|----|--------|------------|-----|------|--------|------------|-------|-----|--------|------------|-----|-----|--------|------------|----|----|--------|------------|
| | | | #IT | FV | PT | Norm | #IT | FV | PT | Norm | #IT | FV | PT | Norm | #IT | FV | PT | Norm | #IT | FV | PT | Norm | | | | |
| 3.7 | 5000 | x_0^1 | 12 | 23 | 0.0515 | 4.5147E-10 | 12 | 24 | 0.0364 | 5.2238E-10 | 20 | 80 | 0.0798 | 3.1109E-10 | 78 | 418 | 0.3002 | 2.3254E-10 | 40 | 240 | 0.1902 | 3.1828E-10 | 23 | 53 | 0.0973 | 4.8906E-12 |
| | 5000 | x_0^2 | 10 | 22 | 0.0428 | 5.0848E-10 | 10 | 22 | 0.0419 | 5.0848E-10 | 21 | 79 | 0.0880 | 9.2029E-10 | 37 | 117 | 0.1478 | 7.8214E-10 | 35 | 208 | 0.1606 | 9.4582E-10 | 22 | 53 | 0.1091 | 2.2027E-10 |
| | 5000 | x_0^3 | 11 | 22 | 0.0488 | 2.1320E-10 | 11 | 22 | 0.0375 | 2.1320E-10 | 18 | 73 | 0.0956 | 4.4267E-10 | 40 | 103 | 0.1383 | 7.8951E-10 | 45 | 271 | 0.2370 | 6.1649E-10 | 22 | 55 | 0.1407 | 9.9265E-10 |
| | 5000 | x_0^4 | 9 | 21 | 0.0372 | 8.1722E-10 | 9 | 21 | 0.0433 | 8.1722E-10 | 17 | 73 | 0.0879 | 3.2815E-10 | 58 | 344 | 0.2427 | 1.1578E-10 | 37 | 227 | 0.1875 | 8.2939E-10 | 15 | 39 | 0.0748 | 1.1250E-10 |
| | 5000 | x_0^5 | 9 | 21 | 0.0314 | 8.1660E-10 | 9 | 21 | 0.0377 | 8.1660E-10 | 17 | 73 | 0.0827 | 3.2823E-10 | 53 | 277 | 0.2137 | 1.7557E-10 | 40 | 245 | 0.1789 | 3.2568E-10 | 15 | 39 | 0.0971 | 1.1421E-10 |
| | 5000 | x_0^6 | 9 | 21 | 0.0482 | 8.1660E-10 | 9 | 21 | 0.0405 | 8.1660E-10 | 17 | 73 | 0.0826 | 3.2823E-10 | 55 | 273 | 0.2188 | 8.1089E-10 | 40 | 245 | 0.2000 | 3.2568E-10 | 15 | 39 | 0.0993 | 1.1421E-10 |
| | 5000 | x_0^7 | 9 | 19 | 0.0274 | 4.9734E-10 | 9 | 19 | 0.0297 | 4.9734E-10 | 18 | 74 | 0.0847 | 7.4873E-10 | 39 | 130 | 0.1510 | 9.7080E-10 | 41 | 249 | 0.1914 | 7.9042E-10 | 19 | 47 | 0.0814 | 2.9294E-10 |
| | 25000 | x_0^1 | 12 | 23 | 0.1299 | 8.8782E-10 | 12 | 26 | 0.1440 | 4.9660E-10 | 20 | 80 | 0.2367 | 6.9939E-10 | 61 | 344 | 0.7938 | 6.6882E-10 | 40 | 240 | 0.5296 | 7.1151E-10 | 23 | 53 | 0.3320 | 1.0653E-11 |
| | 25000 | x_0^2 | 11 | 22 | 0.1179 | 1.8015E-10 | 11 | 22 | 0.1512 | 1.8015E-10 | 22 | 83 | 0.2675 | 4.9872E-10 | 56 | 269 | 0.6708 | 7.1871E-11 | 36 | 214 | 0.4929 | 2.5093E-10 | 22 | 53 | 0.3343 | 4.9254E-10 |
| | 25000 | x_0^3 | 11 | 22 | 0.1248 | 4.2982E-10 | 11 | 22 | 0.1553 | 4.2982E-10 | 18 | 73 | 0.2424 | 9.9088E-10 | 38 | 107 | 0.3418 | 6.1155E-10 | 46 | 277 | 0.6759 | 4.2178E-10 | 25 | 62 | 0.3678 | 6.4223E-11 |
| | 25000 | x_0^4 | 10 | 21 | 0.1053 | 2.7654E-10 | 10 | 21 | 0.1120 | 2.7654E-10 | 17 | 73 | 0.2233 | 7.3683E-10 | 37 | 131 | 0.3831 | 2.9247E-10 | 41 | 251 | 0.5373 | 7.7236E-10 | 15 | 39 | 0.2193 | 2.5334E-10 |
| | 25000 | x_0^5 | 10 | 21 | 0.1198 | 2.7650E-10 | 10 | 21 | 0.1136 | 2.7650E-10 | 17 | 73 | 0.2292 | 7.3686E-10 | 55 | 253 | 0.6433 | 5.8680E-10 | 46 | 281 | 0.6149 | 5.7053E-10 | 15 | 39 | 0.2284 | 2.5410E-10 |
| | 25000 | x_0^6 | 10 | 21 | 0.1334 | 2.7650E-10 | 10 | 21 | 0.1109 | 2.7650E-10 | 17 | 73 | 0.2393 | 7.3686E-10 | 42 | 171 | 0.4573 | 9.1138E-10 | 46 | 281 | 0.6437 | 5.7054E-10 | 15 | 39 | 0.2525 | 2.5410E-10 |
| | 25000 | x_0^7 | 9 | 21 | 0.1077 | 4.9460E-10 | 9 | 21 | 0.1140 | 4.9460E-10 | 17 | 72 | 0.2219 | 3.9729E-10 | 41 | 104 | 0.4028 | 3.1409E-10 | 36 | 220 | 0.5160 | 6.4593E-10 | 16 | 37 | 0.2736 | 4.1984E-10 |
| | 50000 | x_0^1 | 12 | 25 | 0.2387 | 5.2034E-10 | 12 | 26 | 0.2524 | 6.9040E-10 | 20 | 80 | 0.4457 | 9.9035E-10 | 77 | 395 | 1.8086 | 2.0487E-10 | 41 | 246 | 1.1335 | 4.9668E-10 | 23 | 53 | 0.6073 | 1.5588E-11 |
| | 50000 | x_0^2 | 11 | 22 | 0.2190 | 2.5811E-10 | 11 | 22 | 0.2210 | 2.5811E-10 | 22 | 83 | 0.5074 | 7.0603E-10 | 41 | 142 | 0.8101 | 2.5606E-11 | 36 | 214 | 1.0093 | 5.8921E-10 | 22 | 53 | 0.5975 | 6.9655E-10 |
| | 50000 | x_0^3 | 11 | 22 | 0.2242 | 5.8204E-10 | 11 | 22 | 0.2124 | 5.8204E-10 | 19 | 77 | 0.4471 | 3.3823E-10 | 46 | 119 | 0.7620 | 4.1111E-10 | 46 | 277 | 1.2469 | 5.9178E-10 | 25 | 62 | 0.6447 | 9.0825E-11 |
| | 50000 | x_0^4 | 10 | 21 | 0.2051 | 3.8893E-10 | 10 | 21 | 0.2029 | 3.8893E-10 | 18 | 77 | 0.4528 | 2.5171E-10 | 45 | 198 | 1.0008 | 7.4229E-10 | 42 | 257 | 1.1770 | 3.0532E-10 | 15 | 39 | 0.3966 | 3.5855E-10 |
| | 50000 | x_0^5 | 10 | 21 | 0.1989 | 3.8890E-10 | 10 | 21 | 0.2026 | 3.8890E-10 | 18 | 77 | 0.4447 | 2.5172E-10 | 59 | 266 | 1.3281 | 3.1759E-10 | 43 | 263 | 1.1866 | 5.6109E-10 | 15 | 39 | 0.4430 | 3.5909E-10 |
| | 50000 | x_0^6 | 10 | 21 | 0.1973 | 3.8890E-10 | 10 | 21 | 0.2037 | 3.8890E-10 | 18 | 77 | 0.4293 | 2.5172E-10 | 92 | 518 | 2.3223 | 5.8842E-10 | 43 | 263 | 1.2210 | 5.6108E-10 | 15 | 39 | 0.4386 | 3.5910E-10 |
| | 50000 | x_0^7 | 9 | 21 | 0.1925 | 7.0096E-10 | 9 | 21 | 0.2105 | 7.0096E-10 | 17 | 72 | 0.3849 | 4.9460E-10 | 39 | 124 | 0.7371 | 9.9933E-10 | 38 | 232 | 1.0835 | 4.1033E-10 | 21 | 52 | 0.5375 | 1.1229E-10 |