

# SOLUTIONS

## Assignment 4: Frequency Analysis of LTI Systems

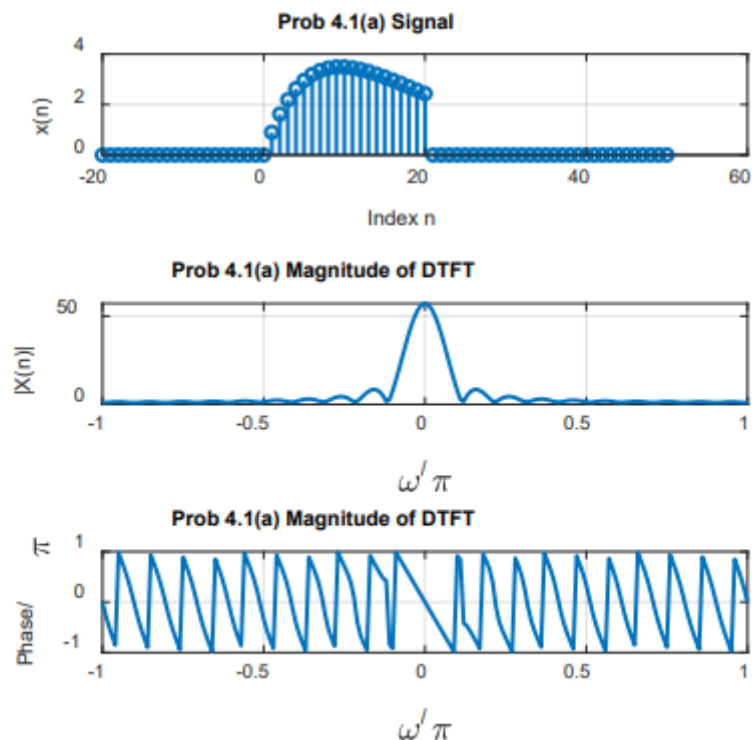
### Digital Signal Processing (EN.525.627.8X)

1. A)

```
n=[-20:50]; %Index n exceeds interval where signal is non-zero
n1=n(1); n2=n(end); %Limits for index n
x=n.*(0.9).^n.*[stepseq(0,n1,n2)-stepseq(21,n1,n2)];
```



```
%Calculate and Display DTFT
w=[-100:100]*pi/100;
X=dtft(x,n,w);
MagX=abs(X);
PhaseX=angle(X)/pi;
subplot(3,1,2), plot(w/pi,MagX,'LineWidth',2);grid on;
set(gca,'FontSize',16);
ylabel('|X(n)|'); xlabel('\omega/\pi');
```

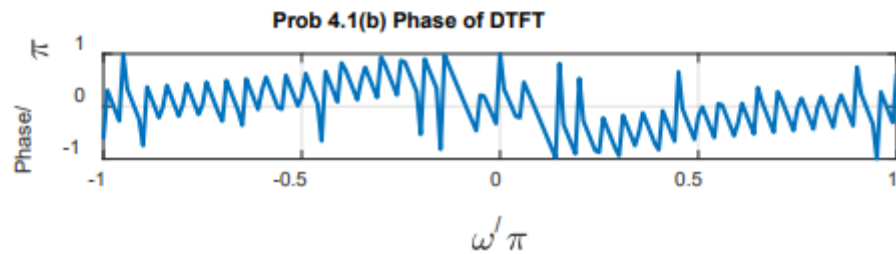
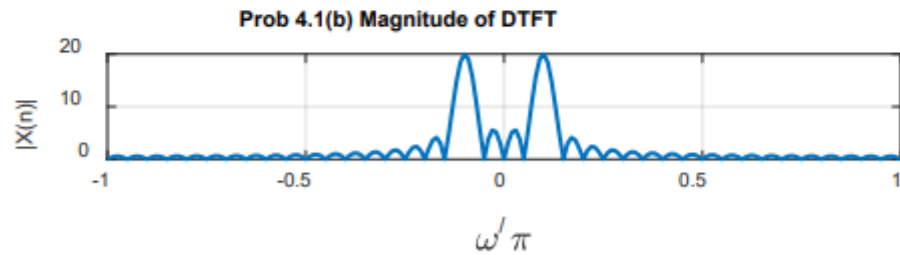
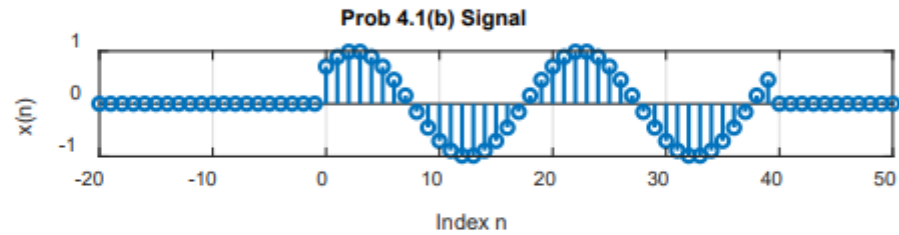


1B)

```
%Create and Display DT Signal x(n)
n=[-20:50]; %Index n exceeds interval where signal is non-zero
n1=n(1); n2=n(end); %Limits for index n
x=cos(pi*n/10-pi/4).*[stepseq(0,n1,n2)-stepseq(40,n1,n2)];
```



```
PhaseX=angle(X)/pi;
subplot(3,1,2), plot(w/pi,MagX,'LineWidth',2);grid on;
set(gca,'FontSize',16)
ylabel('|X(n)|'); xlabel('\omega/\pi');
```



2.

a. & b.) Key lines of MATLAB code

```
n=[-10:110]; %Index n exceeds interval where signal is non-zero
n1=n(1); n2=n(end); %Limits for index n
MM=[10 25 50 101];
for m=[1:4]
```

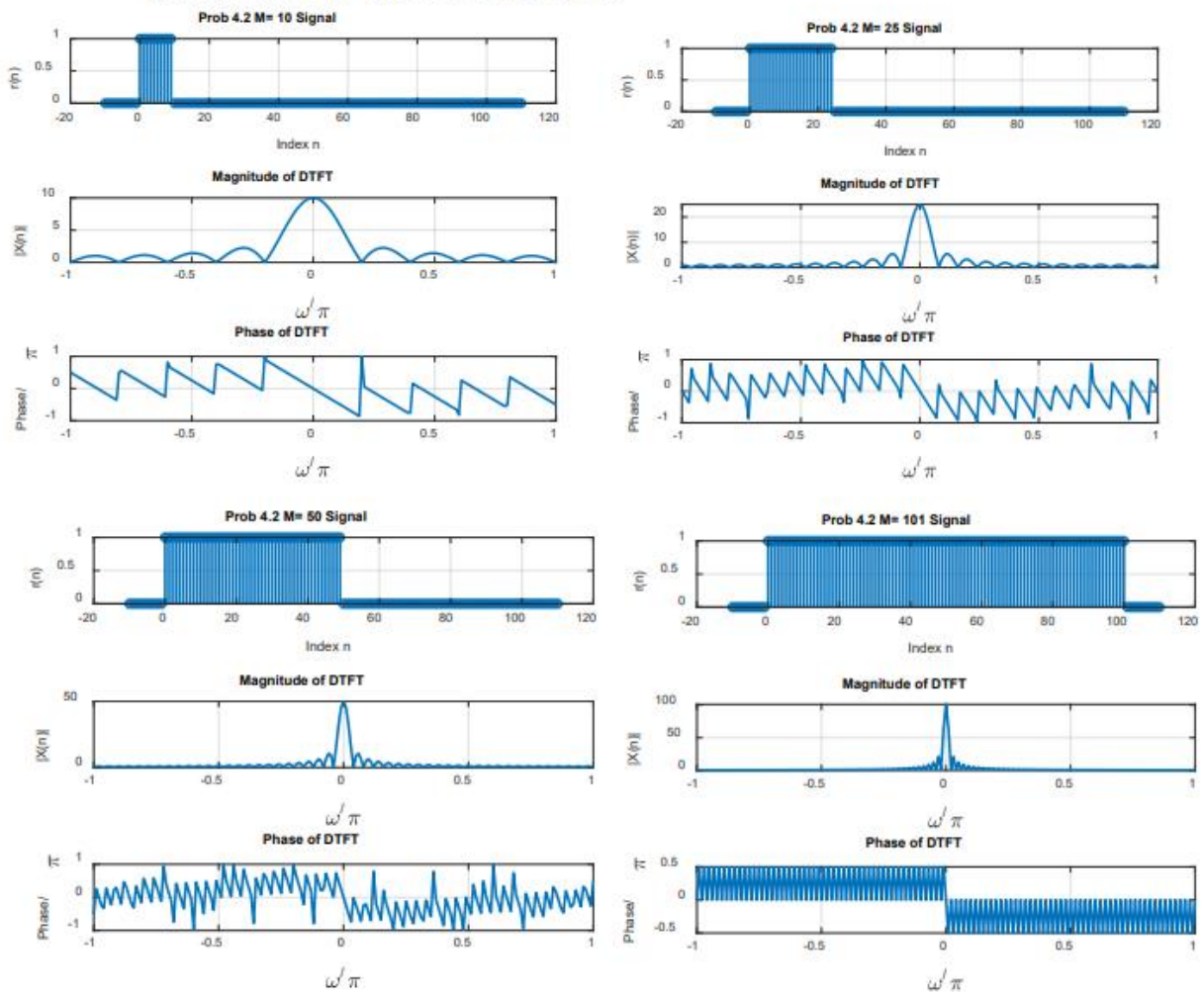
```
M=MM(m);
r=[stepseq(0,n1,n2)-stepseq(M,n1,n2)];
```



```
%Calculate and Display DTFT
```

```
w=[-100:100]*pi/100;
R=dtft(r,n,w);
MagR=abs(R);
PhaseR=angle(R)/pi;
subplot(3,1,2), plot(w/pi,MagR,'LineWidth',2);grid on;
set(gca,'FontSize',16)
ylabel('|X(n)|'); xlabel('\omega/\pi');
```

For part b divide by  $\max(\text{abs}(R))$  to normalize peak to 1



c.) Width of DTFT peak approaches zero as M increases, signal approaching DC which has zero frequency

**3A:**

Definition of DTFT:

$$X(\omega) = \sum_{n=-\infty}^{\infty} x(n)e^{-j\omega n}$$

$$\text{Euler's Identity: } \cos \omega = \frac{1}{2}(e^{j\omega} + e^{-j\omega})$$

$$X(\omega) = 3 + e^{j\omega} + e^{-j\omega} + 2e^{j2\omega} + 2e^{-j2\omega}$$

From definition above:

$$x(n) = 2\delta(n+2) + \delta(n+1) + 3\delta(n) + \delta(n-1) + 2\delta(n-2)$$

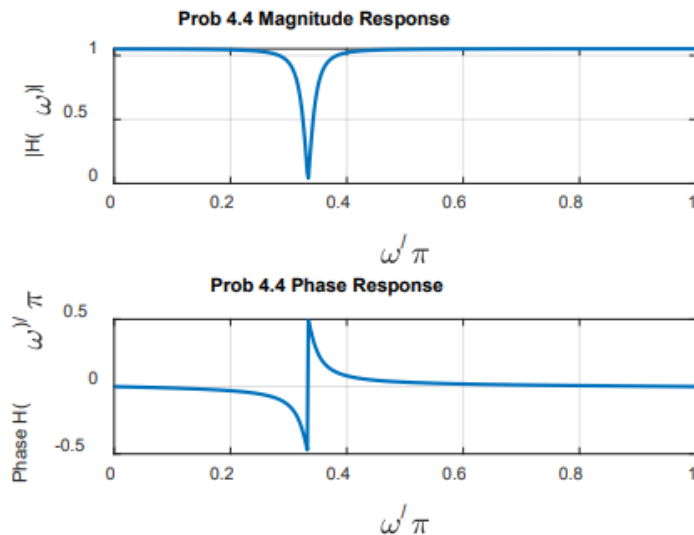
**3B:**

b.) Follow same approach using Euler's Identity to convert sinusoidal signals into exponential signals. Then multiply by the exponential which will change exponents and finally determine  $x(n)$  from definition

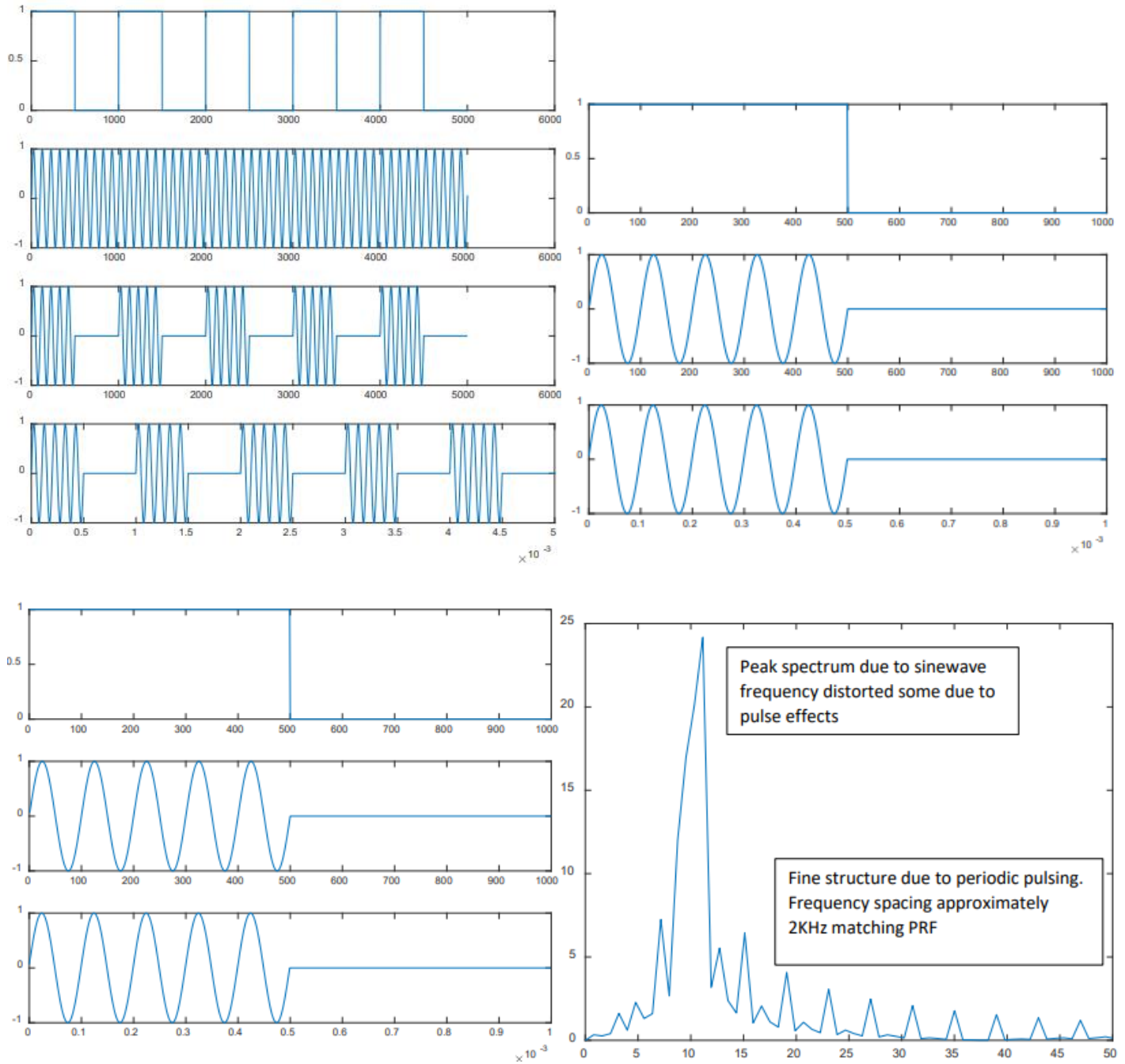
**4:**

```
%Determine Frequency response magnitude and phase
%y(n)=x(n)-x(n-1)+x(n-2)+0.95y(n-1)-0.9025y(n-2)
%Group y terms on left and x terms on right
%y(n)-0.95y(n-1)+0.9025y(n-2)=x(n)-x(n-1)+x(n-2)
%A and B Coefficients
A=[1 -0.95 0.9025]; B=[1 -1 1];
[H,w]=freqz(B,A);
subplot(2,1,1)
    plot(w/pi,abs(H),'Linewidth',2),grid on
    set(gca,'FontSize',16)
    xlabel('\omega/\pi'), ylabel('|H(\omega)|')
    title('Prob 4.4 Magnitude Response')

subplot(2,1,2)
    plot(w/pi,angle(H)/pi,'Linewidth',2),grid on
    set(gca,'FontSize',16)
    xlabel('\omega/\pi'), ylabel('Phase H(\omega)/\pi')
    title('Prob 4.4 Phase Response')
```



## 5: Expected plots



## 5: Example Code

```
% HW4_5_627_SU2020_Script.m
close all
clear
clc

ms=1e-3;
KHz=1e3;
PRT=1*ms;
PRF=1*KHz;
F=10*KHz;
Ta=.001*ms; % Time increment for representing analog signals
Ts=.01*ms; % A2D sampling period

% Set up Index(n) and time(t)
%-----
% Index (n)          Time (ms)
% 1                  0
% 500                 500*Ta
% 501                 501*Ta
% 1000                1000*Ta
% 1001
% 1500
% 1501
% 2000
% 2001
%
%
% 4001
% 4500                4500*Ta
% 5001                5001*Ta
%-----
n=[1:5001];
t=(n-1)*Ta;

figure(1) % 5 replica periodic pulsed sinewave
set(gcf,'Position',[280 358 560 520])
subplot(4,1,1)
p1=stepseq(1,1,5001)-stepseq(500,1,5001);
p2=stepseq(1001,1,5001)-stepseq(1500,1,5001);
p3=stepseq(2001,1,5001)-stepseq(2500,1,5001);
p4=stepseq(3001,1,5001)-stepseq(3500,1,5001);
p5=stepseq(4001,1,5001)-stepseq(4500,1,5001);
p=p1+p2+p3+p4+p5;
plot(n,p)

subplot(4,1,2)
s=sin(2*pi*F*Ta*n);
plot(n,s)

subplot(4,1,3)
out=p.*s;
plot(n,out)
```

```
subplot(4,1,4) %Pulsed sinewave as a function of time
plot(t,out)
```

```
figure(2) % One pulse repetition period sinewave
set(gcf,'position',[700 310 560 420])
n1=1:1000;
subplot(3,1,1)
    p_onecycle=p(n1);
    plot(n1,p_onecycle)

subplot(3,1,2)
    out_onecycle=out(n1);
    plot(n1,out_onecycle)

subplot(3,1,3)
    t1=(n1-1)*Ta;
    plot(t1,out_onecycle)
```

```
figure(3) % sampled pulsed sinewave signal
```

```
ns=[1:10:5001];
ts=(ns-1)*Ts;

out_sampled=p(ns).*s(ns);
subplot(2,1,1)
plot(n,out); hold on
plot(ns,out_sampled,'ro','markersize',2')
grid on
set(gca,'Ylim',1.5*[-1 1])
```

```
subplot(2,1,2)
nls=1:10:1000;
tls=(nls-1)*Ts;
plot(n1,out(n1)); hold on
plot(nls,out(nls),'ro','markersize',2')
grid on
set(gca,'Ylim',1.5*[-1 1])
```

```
figure(4) % Determine DTFT
w=[0:200*pi]/200;
X=dtft(out_sampled,ns,w);
magX=abs(X);
plot(1e3*w/(2*pi),magX)
set(gca,'Xlim',[0 50])
```