

Residual Neural Network

Why Deep Residual Learning?

- “Degradation of Accuracy” Problem
 - Accuracy gets saturated then decreases rapidly with the depth increase
 - The problem is not caused by overfitting
 - Adding more layers to a suitably deep model leads to higher training error
- Not all systems are similarly easy to optimize

Deep Residual Learning Network in Short

- Let the stacked layers fit a residual mapping
- Feedforward Neural Networks with “Shortcut connections”
 - Skipping one or more layers
 - These connections perform identity mapping
 - Their outputs are added to the outputs of the stacked layers
- Results from the experiments on the paper:
 - Deep residual nets are easy to optimize, but the counterpart “plain” nets (that simply stack layers) exhibit higher training error when the depth increases
 - Deep residual nets can easily enjoy accuracy gains from greatly increased depth, producing results substantially better than previous networks.

Related Works

- Residual Representations

- VLAD and Fisher Vector are powerful shallow representations for image retrieval and classification.
- Encoding residual vectors is shown to be more effective than encoding original vectors.

- Shortcut Connections

- An early practice of training multi-layer perceptrons (MLPs) is to add a linear layer connected from the network input to the output. Few intermediate layers are directly connected to auxiliary classifiers for addressing vanishing/exploding gradients.
- An “inception” layer is composed of a shortcut branch and a few deeper branches
- “highway networks” present shortcut connections with gating functions [15].
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Residual Learning Reformulation

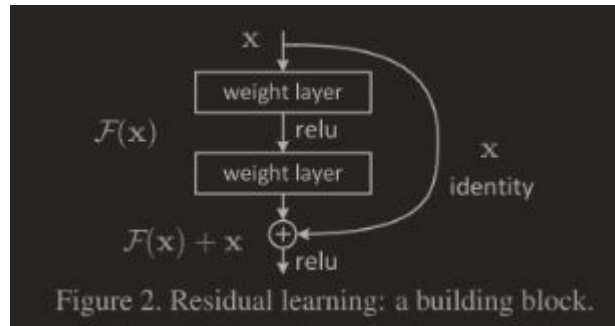
- $\mathbf{H}(\mathbf{x})$ is an underlying mapping to be fit by a few stacked layers.
- The hypothetical residual function $\mathbf{F}(\mathbf{x}) := \mathbf{H}(\mathbf{x}) - \mathbf{x}$
- The original function becomes $\mathbf{F}(\mathbf{x}) + \mathbf{x}$
- This reformulation is motivated by the counterintuitive phenomena about the degradation problem.
- The degradation problem suggests that the solvers might have difficulties in approximating identity mappings by multiple nonlinear layers.
- With the residual learning reformulation, if identity mappings are optimal, the solvers may simply drive the weights of the multiple nonlinear layers toward zero to approach identity mappings.

Residual Learning

- In real cases, it is unlikely that identity mappings are optimal, but reformulation may help to precondition the problem.
- If the optimal function is closer to an identity mapping than to a zero mapping, it should be easier for the solver to find the perturbations with reference to an identity mapping than to learn the function as a new one.
- The learned residual functions in general have small responses, suggesting that identity mappings provide reasonable preconditioning.

Identity Mapping by Shortcuts

- Residual learning to every few stacked layers.
- Building block formula: $\mathbf{y} = \mathbf{F}(\mathbf{x}, \{\mathbf{W}_i\}) + \mathbf{x}$. (1)
 - \mathbf{x} and \mathbf{y} are the input and output vectors of the layers.
 - The function $\mathbf{F}(\mathbf{x}, \{\mathbf{W}_i\})$ represents the residual mapping to be learned.
 - For the example in Fig. 2 that has two layers, $\mathbf{F} = \mathbf{W}_2\sigma(\mathbf{W}_1\mathbf{x})$ in which σ denotes activation function
 - The biases are omitted for simplifying notations.
 - The operation $\mathbf{F} + \mathbf{x}$ is performed by a shortcut connection and element-wise addition.
 - We adopt the second nonlinearity after the addition (i.e., $\sigma(y)$, see Fig. 2).
 - The shortcut connections in Equation (1) introduce neither extra parameter nor computation complexity.



Identity Mapping by Shortcuts (Continued)

- The dimensions of x and F must be equal in Eqn.(1). If this is not the case (e.g., when changing the input/output channels), we can perform a linear projection W_s by the shortcut connections to match the dimensions: **$y = F(x, \{W_i\}) + W_s x$. (2)**
- Square matrix W_s can also be used in Eqn.(1). But the paper argued the identity mapping is sufficient for addressing the degradation problem and is economical, and thus W_s is only used when matching dimensions.
- The form of the residual function F is flexible. The function F which represents more than three layers are possible. If F has only a single layer, Eqn.(1) is similar to a linear layer: $y = W_1 x + x$ with no observed advantages yet.
- Although the above notations are about fully-connected layers for simplicity, they are applicable to convolutional layers. The function $F(x, \{W_i\})$ can represent multiple convolutional layers. The element-wise addition is performed on two feature maps, channel by channel.

Read More

He, K., Zhang, X., Ren, S., & Sun, J. (2016). Deep Residual Learning for Image Recognition. 2016 IEEE Conference on Computer Vision and Pattern Recognition (CVPR). DOI:10.1109/cvpr.2016.90. (Alternate link: <https://arxiv.org/pdf/1512.03385.pdf>.)