

**1. What are the inputs and outputs for this neuron (physical meaning)?**

- The inputs for this neuron are the hourly energy consumption data from 5:00 AM to 8:00 PM, in 1-hour intervals, for 3 days.
- The outputs for this neuron are the predicted rates of energy consumption for a 4th day, in 1-hour intervals from 5:00 AM to 8:00 PM.

**2. Which activation function is used in the three architectures above? Why?**

- A linear activation function is used for three architectures.
- Because we can reduce a polynomial regression equation into a set of inputs for a neuron that utilizes a linear activation function, in order to achieve the same result as a polynomial equation would.

**3. Compare the training and testing total error obtained using the architectures on Figure 1:**

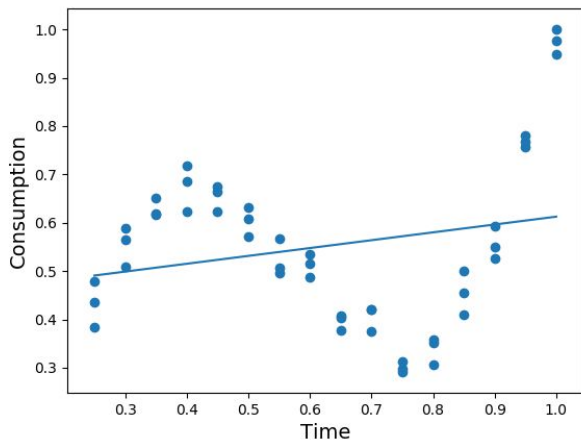
- For each architecture used, training error was consistently higher than testing error, this is because there are more points in the training data.

**$y = ax + b$  (x neuron)**

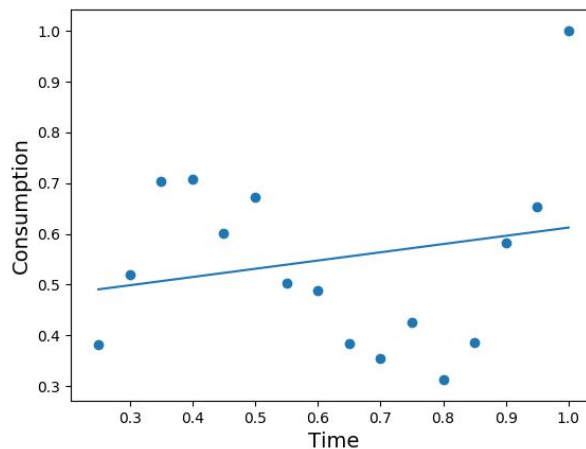
Training Total Error: 1.336

Testing Total Error: .478

Training:  $y = ax + b$  Training Error: 1.336



Testing:  $y = ax + b$  Testing Error: 0.478

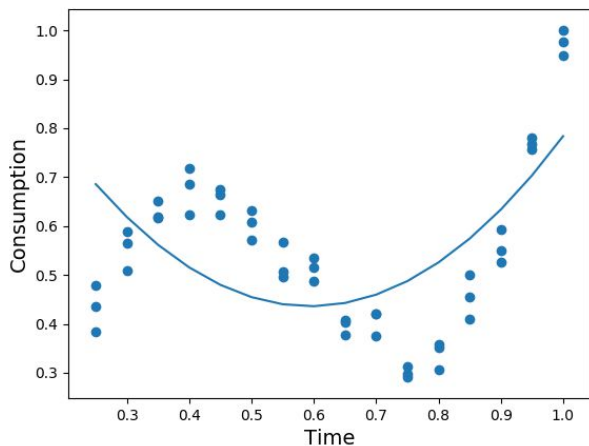


**$y = ax^2 + bx + c$  ( $x^2$  neuron)**

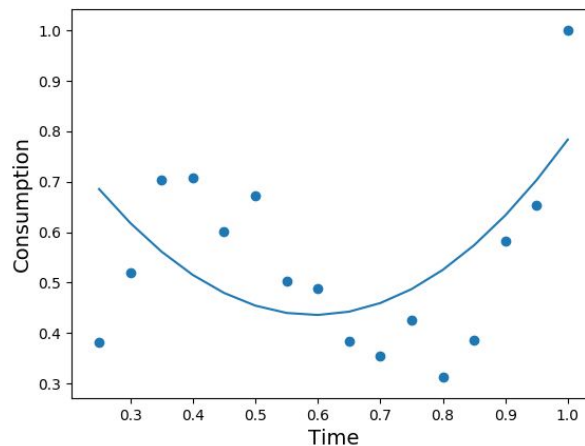
Training Total Error: .941

Testing Total Error: .379

Training:  $y = ax^2 + bx + c$  Training Error: 0.941



Testing:  $y = ax^2 + bx + c$  Testing Error: 0.379

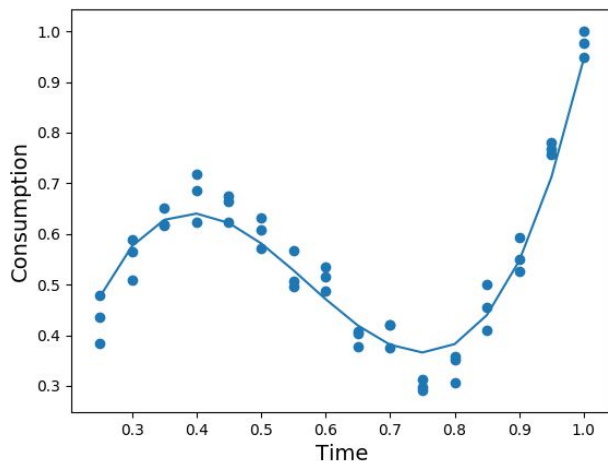


$$y = ax^3 + bx^2 + cx + d \text{ (x}^3 \text{ neuron)}$$

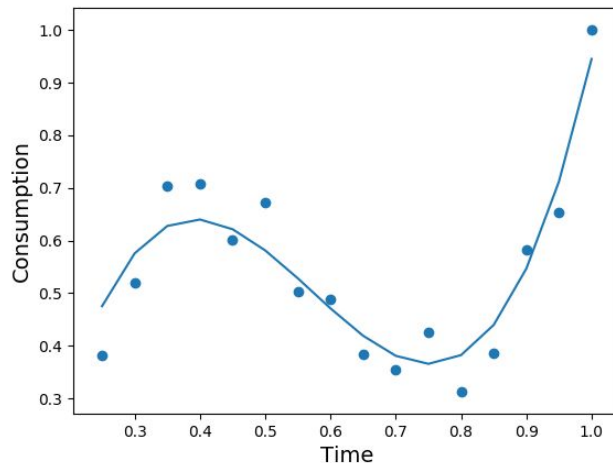
Training Total Error: .087

Testing Total Error: .053

Training:  $y = ax^3 + bx^2 + cx + d$  Training Error: 0.087



Testing:  $y = ax^3 + bx^2 + cx + d$  Testing Error: 0.053



4. Report the number of iterations, the learning rate, and data pre-processing steps you may have chosen (such as normalization of input data). Clearly explain why you selected these values and steps

Iterations = 25000

Learning rate for linear and quadratic = .01

Learning rate for cubic = .3

#### Preprocessing steps.

1. Load data from file
2. Add preceding column of ones for bias input
3. Combine data for days 1, 2 and 3
4. Sort the data by hour of occurrence (x) in ascending order
5. Save linear instance
6. Add column of  $x^2$
7. Reorder columns
8. Save quadratic instance
9. Add column of  $x^3$
10. Reorder columns
11. Save cubic instance
12. Normalization of input and testing data

#### Reasoning

Having a higher alpha for linear and quadratic anchored our regression lines to unfavorable positions due to being over influenced, meanwhile our 3rd degree improved with a higher alpha.

We utilized these preprocessing steps for our input in order to simplify the use of the linear activation function as a representation of polynomial regression. We represent each added degree as a new input column for our training data.