Things to work on:

Add solutions to all worksheet days

Update problems to better ones as needed

Change all headers to be
```
\section{\centering stuff}
```
instead of
```
\begin{center}
    {\large \textbf{stuff}}
\end{center}
```

Add Learning Outcome information to the top of each worksheet as appropriate (starting w/ 12.5). The Learning Outcomes are listed below the end document here. Each worksheet should get at the top "The Learning Outcomes associated with this worksheet are:" followed by a list of all of the appropriate ones (usually just one or two).

Use new
```
\question{question goes here}
    {final answer goes here}
    {solution goes here}
```
format instead of the large blocks

Chapter 14.1: Multivariate Functions

G4: Surfaces. I can identify standard quadric surfaces including: spheres, ellipsoids, elliptic paraboloids, hyperboloids, cones, and hyperbolic paraboloids. I can match graphs of functions of two variables to their equations and contour plots and determine their domains and ranges.

Mechanics

1. Algebraically describe the domains of each of the following functions. Then sketch them on (separate) xy-planes.

   (a) $f(x,y) = \sqrt{x-y-1}$.

   (b) $f(x,y) = \sqrt{(x-4)(y^2-1)}$.

   (c) $f(x,y) = \cos^{-1}(y-4x^2)$.

   (d) $f(x,y) = \dfrac{1}{4-x^2-y^2}$.

   (e) $f(x,y) = \dfrac{1}{\ln(4-x^2-y^2)}$

2. For each of the surfaces (a)-(g), determine if the proposed descriptions of the level curves are correct. If not, give a correct descriptor. *[Note: consider a point as a circle/ellipse of radius 0]*

   (a) $z = 2x^2 - 3y^2$; Level curves are concentric ellipses.

   (b) $z = x^2 + y^2$; Level curves are concentric circles

   (c) $z = \dfrac{1}{x+y}$; Level curves are lines, whenever $x \neq -y$.

   (d) $z = 2x + 3y$; Level curves are parallel planes.

   (e) $z = \sqrt{25 - x^2 - y^2}$; Level curves are concentric circles, but only if $z > 5$ or $z < -5$

   (f) $z = \sqrt{x^2 + y^2}$; Level curves are concentric circles, but only if $z \geq 0$.

   (g) $z = xy$; Level curves are hyperbolas.

Applications

3. Multivariable functions are often used in economic models to describe how one should price an asset, or how to determine the utility of a product. For example, consider a *utility function* $u(x,y,z)$, where x, y, z represent three independent properties of an object (eg., price, quantity, quality), and u tells you how much you value that item. In this context, what economic significance do the level surfaces $u(x,y,z) = C$ have (assume C is a constant). Give a example of how this phenomenon might manifest in your day-to-day life.

Extensions

4. Find an equation for the level surface of the function $f(x, y, z) = \sqrt{x^2 + y^2 + z^2}$ passing through $(1, 1, 1)$. Sketch a plot of this level surface in $\mathbb{R}^3$.

5. Let $f(x, y) = (x - y)^2$. Determine the equations and shapes of the cross-sections when $x = 0$, $y = 0$, and $x = y$, and describe the level curves. Use this information to produce a sketch of the graph of the surface. Confirm your sketch using a 3d graphing utility.