

# Modeling Attention in Panoramic Video: A Reinforcement Learning Approach

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**Abstract**—Panoramic video provides an immersive and interactive experience by enabling humans to control the field of view (FoV) through head movement (HM). Thus, HM plays a key role in modeling human attention to panoramic video. This paper establishes a database collecting subjects' HM positions on panoramic video sequences. From this database, we find that the HM data are highly consistent across subjects. Furthermore, we find that deep reinforcement learning (DRL) can be applied to predict HM positions, via maximizing the reward of imitating human HM scanpaths through the agent's actions. Based on our findings, we propose a DRL based HM prediction (DHP) approach with offline and online versions, called offline-DHP and online-DHP, respectively. In offline-DHP, multiple DRL workflows are run to determine some potential HM positions at each panoramic frame. Then, a heat map of the potential HM positions, called the HM map, is generated as the output of offline-DHP. In online-DHP, the next HM position of one subject is estimated given the currently observed HM position. Online-DHP is achieved by developing a DRL algorithm, upon the learned model of offline-DHP. Finally, the experimental results validate that the offline-DHP and online-DHP are effective in offline and online prediction of HM positions for panoramic video, and that the learned offline-DHP model can improve the performance of online-DHP.

**Index Terms**—Panoramic video, head movement, reinforcement learning, deep learning.

## 1 INTRODUCTION

DURING the past years, panoramic video [1] has become increasingly popular due to its immersive and interactive experience. To achieve this immersive and interactive experience, humans can control the field of view (FoV) in the range of  $360^\circ \times 180^\circ$  by wearing head-mounted displays (HMDs), when watching panoramic video. In other words, humans are able to freely move their heads within a sphere to make their FoVs focus on the attractive content (see Figure 1 for an example). The content outside the FoVs cannot be observed by humans, i.e., without any attention. Consequently, head movement (HM) plays a key role in deploying human attention to panoramic video. HM prediction thus emerges as an increasingly important problem in modeling attention to panoramic video. Given the predicted HM, the visual attention within the FoV can be further modeled using the conventional saliency detection methods [2] for 2D video. The same as traditional 2D video, the attention model can be extensively utilized in many areas of panoramic video, such as region-of-interest (ROI) compression [3], visual quality assessment [?], [4], rendering [5], synopsis [6], and automatic cinematography [7].

Unfortunately, few approaches have been proposed in modeling human attention on panoramic video, especially predicting the positions of HM. Benefiting from the most recent success of deep reinforcement learning (DRL) [8], this paper proposes a DRL-based HM prediction (DHP) approach for modeling attention to panoramic video. In the proposed approach, the DRL algorithm is applied to maximize the *reward* of making the *agent's actions*

of HM scan paths simulate the HM behaviors of humans. In fact, HM prediction can be classified into two categories: offline and online prediction. The offline HM prediction refers to modeling attention on panoramic video for multiple subjects, whereas the online prediction aims at predicting the next HM position of one subject based on the ground-truth of his/her HM positions at the current and previous frames. In this paper, our DHP approach includes both online and offline HM prediction, named offline-DHP and online-DHP, respectively. The codes for our offline-DHP and online-DHP approaches are downloadable from <https://github.com/YuhangSong/dhp>.

To our best knowledge, there exists no offline work to predict the HM positions of multiple subjects in viewing panoramic video. The closest work is saliency detection on 2D video [2]. The earliest approach for saliency detection was proposed by Itti *et al.* [9], in which the features of color, intensity and orientation are combined to generate the saliency map of an image. Later, Itti *et al.* [10] proposed adding two features to [9], namely, motion and flicker contrast, for video saliency detection. Recently, several advanced approaches have been proposed for video saliency prediction. These advanced works include the earth mover's distance (EMD) approach [11] and the Boolean map-based saliency model (BMS) [12]. Most recently, deep learning has been successfully applied in saliency detection, such as SALICON [13] and Liu's approach [14]. Saliency detection in 2D video assumes that humans are able to view all the content of each video frame. However, this assumption does not hold for panoramic video, because subjects can only see a limited range of the FoV at a single sight, rather than the full panoramic range of  $360^\circ \times 180^\circ$ . In fact, different regions of panoramic video are accessible to subjects via changing the positions of HM [15]. In this paper, we find that different subjects are highly consistent in terms of HM positions. This finding is based on establishing and analyzing a new database, which consists of the HM data of 58 subjects viewing 76 panoramic video

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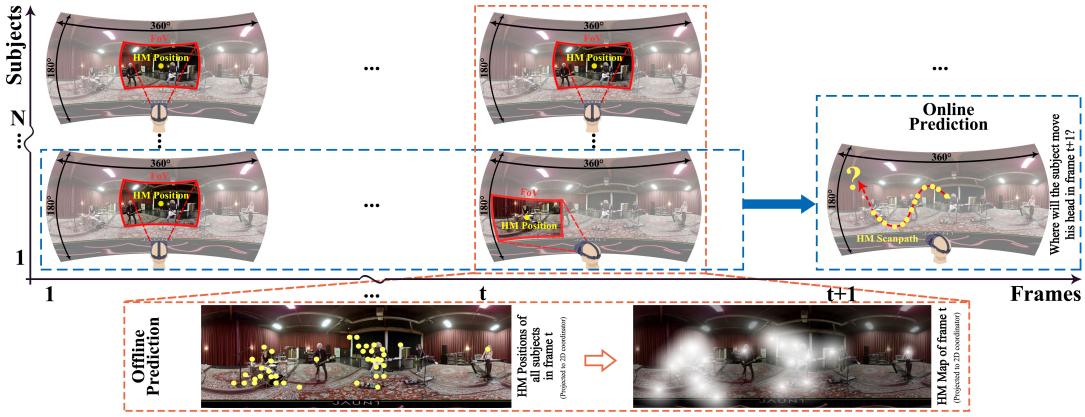


Fig. 1: Illustration for FoVs and HM positions across different subjects. The heat map of HM positions from all subjects is also shown, which is defined as the HM map.

sequences. Then, we propose the offline-DHP approach to predict the consistent HM positions on panoramic video via generating the HM maps for each single frame. The HM maps are in the form of a sphere, and the positions in the HM maps are thus represented by the longitude and latitude in the geographic coordinate system (GDS) [16]. This paper visualizes the spherical HM maps by projecting them onto the 2D plane. Figure 1 demonstrates an example of the ground-truth HM map for a panoramic video frame. Similar to the saliency maps of 2D video, the HM maps of panoramic video are obtained by convoluting the HM positions with a 2D Gaussian filter<sup>1</sup>.

Specifically, our offline-DHP approach yields the HM maps of panoramic video via predicting the HM scanpaths of multiple agents, since subjects interactively control their HM positions along with some scanpaths according to video content. First, we find from our database that the HM scanpaths of different subjects are highly consistent. Meanwhile, subjects are normally initialized to view the center of the front region in the beginning frames of panoramic video. Therefore, the HM positions at the subsequent frames can be yielded on the basis of the predicted scanpaths. Additionally, we find from our database that the magnitudes and directions of HM scanpaths are with similarity across subjects. In light of these findings, our offline-DHP approach models both the magnitudes and directions of HM scanpaths as the *actions* of multiple DRL agents and takes the viewed panoramic content as the *observation* of the *environment*. As such, the DRL model can be learned to predict HM positions. In training the DRL model, a *reward* is designed to measure the difference of *actions* between the DRL agents and subjects, indicating how well the agents imitate humans in terms of HM scanpaths. Then, the *reward* is optimized to learn the parameters in the DRL model. Given the learned model, the HM maps of panoramic video are generated upon the predicted HM positions, obtained from the scanpaths of several agents in multiple DRL workflows.

For online HM prediction, the latest work of [17] proposed a deep 360 pilot, which automatically shifts viewing direction (equivalent to the HM position) when watching panoramic video. Specifically, the salient object is detected and tracked across panoramic video frames, via leveraging a region-based convolutional neural network (RCNN) [18] and recurrent neural network (RNN). Given the detected salient object and previous viewing

directions, the deep 360 pilot predicts to transit HM position by learning a regressor. Since the deep 360 pilot relies heavily on one salient object, it is only suitable for some specific scenes that include one salient object, e.g., the sports scenes in [17]. It is still challenging to predict HM positions online for generic panoramic video, which may include more than one salient object (e.g., the panoramic video in Figure 1). In this paper, we propose an online approach, namely online-DHP, to predict the HM positions on generic panoramic video. In contrast to [17], our online-DHP approach does not need to detect the salient object using the RCNN. Rather, our online-DHP approach is based on attention-related content by leveraging the learned model of our offline-DHP approach. Then, a DRL algorithm is developed in our online-DHP approach to predict the HM positions in an online manner. Specifically, in the DRL algorithm, the *agent* predicts the *action* of the HM scanpath in the next frame, according to the ground-truth of the previous HM scanpath and *observation* of video content. Consequently, the HM positions at the incoming frames can be predicted for our online-DHP approach.

The main contributions of this paper are three-fold:

- We establish a new panoramic video database that consists of HM positions of 58 subjects across 76 panoramic video sequences, with a thorough analysis of their HM data.
- We propose an offline-DHP approach to detect HM maps of panoramic video, and this approach predicts the consistent HM positions of multiple subjects.
- We develop an online-DHP approach to predict the HM position of one subject at the next panoramic frame, based on video content and HM positions until the current frame.

## 2 RELATED WORK

### 2.1 Saliency detection

The only approach for predicting the HM positions of panoramic videos is the most recent work of [7], in which Pano2Vid was proposed to obtain the FoV at each panoramic video frame. However, Pano2Vid primarily focuses on virtually generating a potential HM position at one frame, rather than modeling HM maps of multiple subjects at this frame. The closest work on predicting HM maps is saliency detection for 2D video, which is briefly reviewed in the following.

Saliency detection aims to predict the visual attention of humans on 2D videos, by generating saliency maps of video frames. The studies on visual saliency begin in 1998, when Itti and Koch [9]

1. The two dimensions of the Gaussian filter are longitude and latitude, respectively.

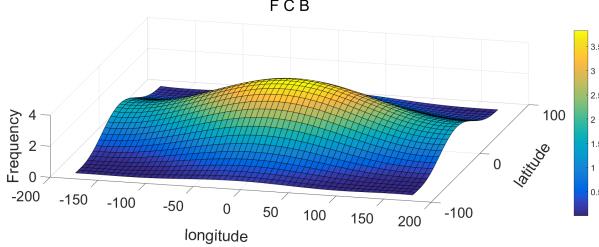


Fig. 2: Distribution of 58 subjects' HM positions at different panoramic regions. It is calculated from all panoramic video frames of the PVS-HM database.

found that the features of intensity, color and orientation in an image can be employed to detect its saliency map. Subsequently, they extended their work to video saliency detection [10], in which two dynamic features of motion and flicker contrast are combined with [9] to detect saliency in 2D videos. Both [9] and [10] can be considered to be heuristic approaches for detecting saliency, since they utilize the understanding of the HVS to develop the computational models. Recently, some advanced heuristic approaches, e.g., [11], [12], [19], [20], [21], [22], [23], [24], [25], have been proposed to detect saliency in 2D videos. Specifically, [19] proposed a novel feature called *surprise*, which measures how the visual change attracts human observers, based on the Kullback-Leibler (KL) divergence between spatio-temporal posterior and prior beliefs. Given the feature of *surprise*, a Bayesian framework was developed in [19] for video saliency detection. Some other Bayesian frameworks [20], [21] were also developed to detect video saliency. Besides, Lin *et al.* [11] quantified the earth mover's distance (EMD) to measure the center-surround difference in spatio-temporal receptive field, generating saliency maps for 2D videos. Zhang *et al.* [12] explored the surround cue for saliency detection, by characterizing a set of binary images with random thresholds on color channels. Recently, [24] and [25] have investigated that some features (e.g., motion vector) in compressed domain are of high correlation with human attention, and these features are thus explored in video saliency detection.

Benefiting from the most recent success of deep learning, deep neural networks (DNNs) [13], [14], [26], [27], [28], [29], [30] have also been developed to detect 2D video saliency, rather than exploring the HVS-related features as in heuristic saliency detection approaches. These DNNs can be viewed as data-driven approaches. For static saliency detection, SALICON [19] fine-tuned the existing convolutional neural networks (CNNs), with a new saliency-related loss function. For dynamic saliency detection, [28] leveraged a deep convolutional 3D (C3D) network to learn the representations of human attention on 16 consecutive frames, and then a long short-term memory (LSTM) network connected with a mixture density network was learned to generate saliency maps using Gaussian mixture distribution. Similarly, Liu *et al.* [14] combined a CNN and multi-stream LSTM to detect saliency in videos with multiple faces. Moreover, other DNN structures have been developed to detect either static saliency [26], [27] or dynamic saliency [28], [29], [30].

Although saliency detection has been thoroughly studied in predicting eye movement on 2D videos, no works have been developed to predict HM positions on panoramic videos. Similar to saliency detection for 2D videos, this paper proposes generating HM maps that represent the HM positions of multiple subjects. Hence, the HM maps model attention to panoramic videos. To obtain the HM maps of panoramic video, a DRL approach is

developed for deciding the *actions* of HM from multiple *agents*. The *actions* are decided based on the *environment* of the panoramic video content, the features of which are automatically learned and then extracted by a DNN. Thus, our approach takes advantage of both deep learning and reinforcement learning, driven by the HM data of our panoramic video database. Note that although few works apply DRL to predict human attention, the attention model is widely used in the opposite direction to improve the performance of reinforcement learning, e.g., [31], [32], [33], [34].

## 2.2 Virtual cinematography

Virtual cinematography of panoramic video, which directs an imaginary camera to virtually capture natural FOV (NFOV), was proposed in [7], [17], [35], [36], [37]. In general, virtual cinematography attempts to agree with the HM positions of humans at each panoramic video frame. The early work of [35] proposed cropping the object-of-interest in panoramic video, such that the NFOV can be generated for virtual cinematography. Later, in [36], the cropped object-of-interest is tracked across frames by a Kalman filter, for automatically controlling the virtual camera in virtual cinematography of panoramic video. The approach of [36] can work on both compressed and uncompressed domains, because two methods were developed to detect the object-of-interest in compressed and uncompressed domains. The works of [35], [36] were both designed for the task of online virtual cinematography. These works can be considered as heuristic approaches, which are not trained or even evaluated on the ground-truth HM data of human subjects.

Most recently, data-driven approaches have boosted the development of virtual cinematography for panoramic videos. Specifically, Pano2Vid [7] learns to generate NFOV at each panoramic frame. However, the learning mechanism of Pano2Vid is offline. In fact, NFOV can be estimated at each frame in an online manner, which uses the observed HM positions of the previous frames to correct the estimation of NFOV at the current frame. To this end, online virtual cinematography [17], [37] has been studied in a data-driven way. Specifically, a state-of-the-art virtual cinematography approach, the deep 360 pilot, was proposed in [17], which is a deep-learning-based *agent* that smoothly tracks the object-of-interest for panoramic video. In other words, the *agent* transits the HM position across video frames to track the key object detected by the RCNN, given the observed HM positions at previous frames. Consequently, NFOV can be generated online for automatically displaying the object-of-interest in virtual cinematography of panoramic videos. In fact, object-of-interest tracking in panoramic video refers to continuously focusing and refocusing the intended targets. Both focusing and refocusing require a subject to catch up the object. Such a task is challenging in extreme-sports videos, as the object-of-interest may be moving fast. Therefore, Lin *et al.* [37] investigated two focus assistance techniques to help the subject track the key object in viewing panoramic video, in which the potential HM position attended to the object-of-interest needs to be determined and provided for the subject.

The above approaches of [7], [17], [35], [36], [37] all depend on the detector of the object-of-interest. Thus, they can only be applied in some specific panoramic videos with salient objects, such as video conferencing or classroom scenes in [35], [36] and the sports videos in [7], [17], [37]. Different from these conventional approaches, our online-DHP approach is based on the learned model of our offline approach, which encodes HM-related

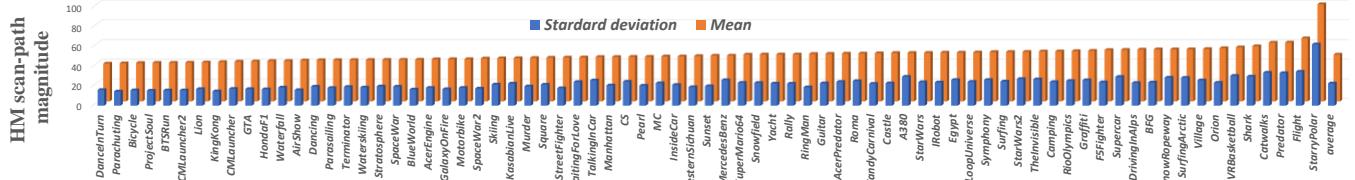


Fig. 3: Mean and standard deviation for the HM scanpath magnitude over different subjects, for the 76 panoramic video sequences in our PVS-HM database. The last column also shows the mean and standard deviation, averaged over all 76 sequences.

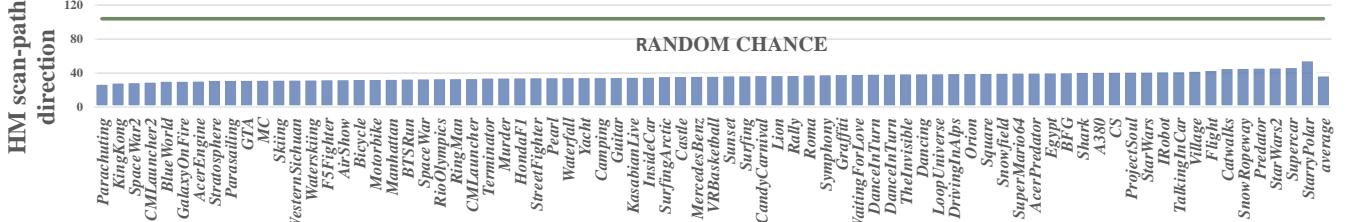


Fig. 4: Circular standard deviation for the HM scanpath directions, over the 76 panoramic video sequences in our PVS-HM database. The average results are also shown in the last column.

content rather than detecting the object-of-interest. Consequently, our approach is object free and thus more suitable for generic panoramic videos.

### 3 DATABASE ESTABLISHMENT AND ANALYSIS

#### 3.1 Database establishment

In this section, we collect a new database that includes 76 panoramic video sequences with the HM data of 58 subjects, called the PVS-HM database. Our PVS-HM database allows quantitative analysis of subjects' HM on panoramic video, and it can also be used for learning to predict where humans look at panoramic video. Our database is available at <https://github.com/YuhangSong/dhp> for facilitating future research. In the following, we present how we conducted the experiment to obtain the PVS-HM database.

First, we selected 76 panoramic video sequences from YouTube and VRCun, with resolutions ranging from 3K to 8K. As shown in Table 1, the content of these sequences is diverse, including computer animation (CA), driving, action sports, movies, video games, scenery, and so forth. Then, the duration of each sequence was cut to be from 10 to 80 seconds (averagely 26.9 seconds), such that fatigue can be reduced when viewing panoramic video. To ensure video quality, all panoramic video sequences were compressed using H.265 [38] without any change in bit-rates. Note that the audio tracks were removed to avoid the impact of acoustic information on visual attention.

In our experiment, 58 subjects (41 males and 17 females, ranging in age from 18 to 36) wore the HMD of an HTC Vive to view all 76 panoramic video sequences at a random display order. When watching panoramic video, the subjects were seated on a swivel chair and were allowed to turn around freely, such that all panoramic regions are accessible. To avoid eye fatigue and motion sickness, the subjects had a 5 minute rest after viewing each session of 19 sequences. With the support of the software development kit (SDK) of HTC Vive, we recorded the posture data of each subject as they viewed the panoramic video sequences. Based on the recorded posture data, the HM data of all 58 subjects at each frame of the panoramic video sequences were obtained and stored for our PVS-HM database, in terms of longitude and latitude in the GDS.

#### 3.2 Database analysis

In this section, we mine our PVS-HM database to analyze HM data of different subjects across panoramic video sequences. Specifically, we have the following six findings.

*Finding 1: The HM positions on panoramic video possess front center bias (FCB).*

*Analysis:* We investigate whether FCB exists when people view panoramic video. This investigation is performed by calculating the numbers of HM positions in different regions of video frames. First, the  $360^\circ \times 180^\circ$  panoramic region of each frame is equally segmented to be  $60^\circ \times 30^\circ$  grids. Then, the numbers of HM positions of 58 subjects are counted for each segmented grid. Consequently, the frequency of HM positions in different panoramic regions is obtained, and it is shown in Figure 2. Note that the frequency results presented in Figure 2 are obtained by averaging over all panoramic video frames of the PVS-HM database. We can see from this figure that the HM positions of 58 subjects are more likely to be attracted by the front center regions. This completes the analysis of Finding 1.

*Finding 2: When watching panoramic video, different subjects are highly consistent in HM positions.*

*Analysis:* In our PVS-HM database, we randomly divide all 58 subjects into two equal-size groups, A and B. For each frame of 76 sequences, the ground-truth HM maps of Groups A and B are generated by convolving with a 2D Gaussian filter over the collected HM data, along with longitude and latitude. They are denoted as  $\mathbf{H}_A$  and  $\mathbf{H}_B$ , respectively. For a panoramic frame, we quantify the correlation between  $\mathbf{H}_A$  and  $\mathbf{H}_B$  using linear correlation coefficient (CC) [39]. Table 1 lists the average CC ( $\pm$  standard deviations) between  $\mathbf{H}_A$  and  $\mathbf{H}_B$  over all frames, for each sequence. We further show in Table 1 the CC values between  $\mathbf{H}_A$  and the maps generated by Gaussian distribution, uniform distribution and FCB. It can be seen from this table that the CC values of Groups A and B are rather high, and that the average CC result of the two groups is significantly higher than those of a Gaussian distribution, uniform distribution and FCB. Thus, it is clear that the HM positions of different subjects are highly consistent. This completes the analysis of Finding 2.

*Finding 3: The magnitude of HM scanpaths is similar across subjects, when viewing the same panoramic video.*

*Analysis:* The HM scanpaths can be decomposed into magnitude

TABLE 1: CC values between the ground-truth HM maps of Groups A and B, for each panoramic video sequence.

Category	Name	CC	Category	Name	CC	Category	Name	CC	Category	Name	CC
CA	AcerEngine	0.891 $\pm$ 0.058	Others	A380	0.867 $\pm$ 0.058	Driving	AirShow	0.883 $\pm$ 0.033	Show	BTSRun	0.926 $\pm$ 0.041
	AcerPredator	0.876 $\pm$ 0.063		Camping	0.851 $\pm$ 0.073		Bicycle	0.953 $\pm$ 0.021		Catwalks	0.834 $\pm$ 0.069
	BFG	0.732 $\pm$ 0.101		CandyCarnival	0.830 $\pm$ 0.088		DrivingInAlps	0.858 $\pm$ 0.073		DanceInTurn	0.934 $\pm$ 0.030
	CMLauncher	0.894 $\pm$ 0.041		Lion	0.937 $\pm$ 0.034		F5Fighter	0.572 $\pm$ 0.109		Dancing	0.906 $\pm$ 0.052
	CMLauncher2	0.924 $\pm$ 0.045		MercedesBenz	0.685 $\pm$ 0.137		HondaFI	0.944 $\pm$ 0.020		Graffiti	0.906 $\pm$ 0.037
	LoopUniverse	0.881 $\pm$ 0.044		RingMan	0.923 $\pm$ 0.032		InsideCar	0.903 $\pm$ 0.036		Guitar	0.866 $\pm$ 0.096
	Orion	0.810 $\pm$ 0.082		Shark	0.812 $\pm$ 0.116		Rally	0.925 $\pm$ 0.025		KasabianLive	0.819 $\pm$ 0.087
	Pearl	0.838 $\pm$ 0.120		Square	0.842 $\pm$ 0.076		Stratosphere	0.792 $\pm$ 0.090		NotBeAloneTonight	0.695 $\pm$ 0.104
	Roma	0.896 $\pm$ 0.054		TalkingInCar	0.858 $\pm$ 0.078		VRBasketball	0.739 $\pm$ 0.098		Symphony	0.826 $\pm$ 0.068
	Yacht	0.780 $\pm$ 0.126		IRobot	0.907 $\pm$ 0.029		BlueWorld	0.793 $\pm$ 0.159		Supercar	0.915 $\pm$ 0.041
VideoGame	WaitingForLove	0.867 $\pm$ 0.083	Movie	KingKong	0.740 $\pm$ 0.091	Scenery	Murder	0.921 $\pm$ 0.058	ActionSports	Flight	0.834 $\pm$ 0.072
	CS	0.872 $\pm$ 0.061		Predator	0.743 $\pm$ 0.132		ProjectSoul	0.946 $\pm$ 0.024		Motorbike	0.746 $\pm$ 0.105
	GalaxyOnFire	0.895 $\pm$ 0.062		StarWars	0.910 $\pm$ 0.038		StarWars2	0.912 $\pm$ 0.035		Parachuting	0.777 $\pm$ 0.103
	GTA	0.930 $\pm$ 0.026		StarWars3	0.912 $\pm$ 0.035		Terminator	0.908 $\pm$ 0.054		Parasailing	0.836 $\pm$ 0.058
	MC	0.728 $\pm$ 0.124		TheInvisible	0.871 $\pm$ 0.052		LoopRopeWay	0.842 $\pm$ 0.076		Skiing	0.748 $\pm$ 0.099
	SpaceWar	0.681 $\pm$ 0.116		Orion	0.810 $\pm$ 0.082		Orion	0.810 $\pm$ 0.082		SnowRopeway	0.728 $\pm$ 0.093
	SpaceWar2	0.577 $\pm$ 0.148		RingMan	0.923 $\pm$ 0.032		Stratosphere	0.792 $\pm$ 0.090		Surfing	0.850 $\pm$ 0.080
	StreetFighter	0.930 $\pm$ 0.023		Roma	0.896 $\pm$ 0.054		TheInvisible	0.858 $\pm$ 0.078		SurfingArctic	0.695 $\pm$ 0.119
	Overall	0.830 $\pm$ 0.075		Yacht	0.780 $\pm$ 0.126		Yacht	0.780 $\pm$ 0.126		WesternSiehuan	0.826 $\pm$ 0.068
				IRobot	0.907 $\pm$ 0.029		IRobot	0.907 $\pm$ 0.029		WesternSiehuan	0.826 $\pm$ 0.068

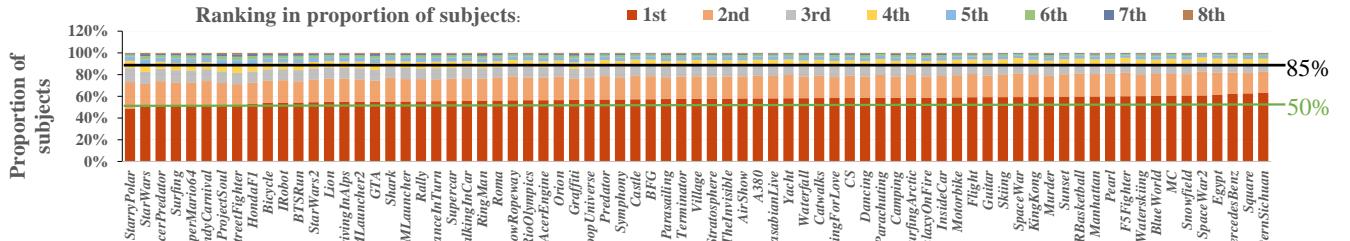
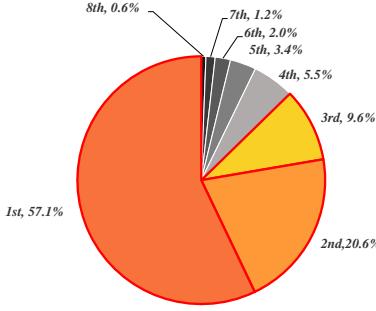


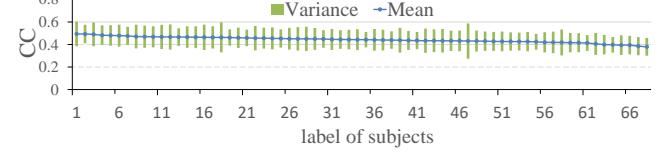
Fig. 5: Distribution of the HM scanpaths over 8 discrete directions, for the 76 sequences from our PVS-HM database. Note that the proportions of subjects, whose HM scanpath directions fall into each discrete direction, are ranked in the descending order and are then shown in this figure.



and direction. Here, we measure the magnitude of HM scanpaths across different subjects. For each individual sequence in our PVS-HM database, Figure 3 plots the mean and standard deviation of HM scanpath magnitude over all 58 subjects. The last column of Figure 3 also shows the mean and standard deviation of HM scanpath magnitudes, averaged over all 76 sequences. As shown in this figure, the standard deviation is considerably less than the mean value, for all 76 sequences and for the overall results. Thus, we can conclude that similarity exists for the magnitude of HM scanpaths across subjects, when the subjects watch the same panoramic sequence. This completes the analysis of *Finding 3*.

*Finding 4: The direction of HM scanpaths on panoramic video is highly consistent across subjects.*

*Analysis:* In our PVS-HM database, we evaluate the consistency of the HM scanpath direction among all 58 subjects. Specifically, we evaluate the direction of the scanpath starting from the consistent HM regions, since *Finding 2* has shown that the HM positions of different subjects are highly consistent. In our PVS-HM database, the consistent regions are extracted from 76 panoramic video sequences, which have the HM positions of at least 12 subjects within a small *great-circle distance* range of  $3^\circ$  [40]. For each panoramic video sequence, Figure 4 shows the circular standard deviation [41] of HM scanpath directions, starting from the



consistent HM regions within one-second time slot<sup>2</sup>. The last column of Figure 4 also reports the circular standard deviation averaged over all 76 sequences. We can see from this figure that the circular standard deviation of the HM scanpath direction is  $38.1^\circ$  on average, and it is significantly less than the value of  $103.9^\circ$  of randomly generated HM scanpath directions. Moreover, the HM scanpath directions of all 76 sequences have considerably smaller circular standard deviations, compared to the random scanpaths. This implies that high consistency exists on directions of HM scanpaths across subjects. Consequently, *Finding 4* is validated.

*Finding 5: Almost 50% subjects are consistent in one HM scanpath direction (among 8 uniformly quantized directions), and over 85% of subjects are consistent in three directions for HM scanpaths.*

*Analysis:* The distribution of HM scanpath directions in the PVS-HM database is analyzed as follows. Only HM scanpaths falling into consistent HM regions (mentioned in *Finding 4*) are selected for the analysis. Specifically, we discretize continuous  $0 - 360^\circ$  directions of HM scanpaths through 8-level uniform quantization:  $\{0^\circ, 45^\circ, 90^\circ \dots, 315^\circ\}$ . Then, we count the proportions of subjects whose HM scanpaths belong to the same discretized direction. Next, these proportions are ranked by their values in each extracted HM region, i.e., ranking from the 1-st to the 8-th. For each ranking, the proportions of subjects are averaged over all HM regions for each panoramic sequence, which are shown in Figure 5. As shown in this figure, for all 76 sequences, the HM scanpaths of 50% subjects or more are consistent in the first ranked direction,

2. We conducted our experiments with time slot being 0.1, 1 and 2 seconds, and the results are similar.

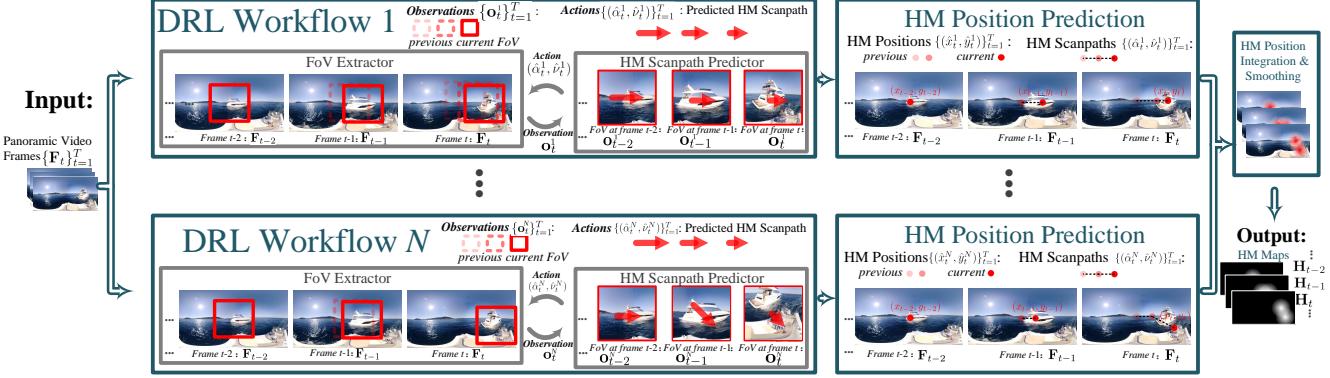


Fig. 8: Overall framework of the offline-DHP approach.

TABLE 2: Definitions of notations in the offline-DHP approach.

$\{\mathbf{F}_t\}_{t=1}^T$	The panoramic frames with frame number $t$ ranging from 1 to $T$ , as the input to offline-DHP.
$\{\mathbf{H}_t\}_{t=1}^T$	The HM maps for frames from 1 to $T$ , as the output of offline-DHP.
$\{m\}_{m=1}^M$	The subjects from 1 to $M$ , with $m$ being the $m$ -th subject.
$\{n\}_{n=1}^N$	The DRL workflows from 1 to $N$ , with $n$ being the $n$ -th workflow.
$\{\mathbf{o}_t^n\}_{t=1}^T$	The FoVs for frames from 1 to $T$ , as the <i>observation</i> of the $n$ -th DRL workflow.
$(x_t^m, y_t^m)$	The ground-truth HM position of the $m$ -th subject at frame $t$ .
$(\hat{x}_t^n, \hat{y}_t^n)$	The HM position predicted by the $n$ -th DRL workflow at frame $t$ .
$\pi_t$	The predicted probability distribution of the HM direction at frame $t$ , as the <i>policy</i> of DRL.
$\hat{\alpha}_t^n$	The predicted HM scanpath direction at frame $t$ from the $n$ -th DRL workflow, as the <i>action</i> of DRL.
$\alpha_t^m$	The ground-truth HM scanpath direction of the $m$ -th subject at frame $t$ .
$\hat{\nu}_t^n$	The predicted HM scanpath magnitude at frame $t$ from the $n$ -th DRL workflow, also as the <i>action</i> of DRL.
$\nu_t^m$	The ground-truth HM scanpath magnitude of the $m$ -th subject at frame $t$ .
$r_{n,t}^\alpha$	The <i>reward</i> for deciding $\hat{\alpha}_t^n$ in the $n$ -th DRL workflow.
$r_{n,t}^\nu$	The <i>reward</i> for deciding $\hat{\nu}_t^n$ in the $n$ -th DRL workflow.
$\mathbf{f}_t^n$	The extracted LSTM feature at frame $t$ , as part of the <i>observed state</i> in the $n$ -th DRL workflow.

and the HM scanpaths of over 85% of subjects are consistent in top 3 directions. Figure 6 also shows the proportions of subjects with HM scanpath directions ranking from the 1-st to the 8-th, which are averaged over all 76 sequences in the PVS-HM database. As seen in this figure, the directions of the HM scanpaths from 57.1%, 20.6% and 9.6% subjects belong to the top 3 ranked directions. In contrast, the HM scanpath directions of 12.7% of subjects fall into the other 5 directions. Therefore, *Finding 5* is validated.

*Finding 6:* For one subject, the HM scanpath at the current time interval relies on that at the previous time interval and observed video content.

*Analysis:* For each individual subject, the vectors of HM scanpaths across the time interval of 0.3 second are extracted from all 76 sequences in our PVS-HM database. Here, we calculate the CC values of HM scanpath vectors between two successive time periods, and then we average the CC values over all 76 sequences for each subject. Figure 7 shows the average CC values for each of the 58 subjects, which range from 0.39 - 0.51. This figure implies that the HM scanpath at the current time interval is somewhat correlated with that at the previous time interval. However, the CC value in Figure 7 is not sufficiently large, indicating that there exist other factors influencing the HM scanpath. Actually, [17] shows that the current HM scanpath of one subject is also related to the observed video content. The above completes the validation of *Finding 6*.

## 4 OFFLINE-DHP APPROACH

### 4.1 Framework of offline-DHP

In this section, we present our offline-DHP approach, in light of our findings in Section 3.2. Figure 8 shows the overall framework of

our approach, in which the multiple DRL workflows are embedded to generate the HM maps of input panoramic video frames. The notations used in this figure and in our approach are listed in Table 2.

As shown in Figure 8, the input to our offline-DHP approach is the panoramic video frames  $\{\mathbf{F}_t\}_{t=1}^T$ . Since *Finding 2* has shown that the HM positions are highly consistent across different subjects, we propose to generate the HM maps for modeling human attention to panoramic video, viewed as the output of our offline-DHP approach. The HM map  $\mathbf{H}_t$  of frame  $t$  represents the probability of each pixel being the HM position. Similar to the saliency maps of 2D videos,  $\mathbf{H}_t$  is obtained by convoluting the predicted HM positions  $\{(\hat{x}_t^n, \hat{y}_t^n)\}_{n=1}^N$  with a 2D Gaussian filter. Because *Finding 5* has indicated that the HM scanpaths of different subjects are consistent in more than one direction, the HM positions  $\{(x_t^m, y_t^m)\}_{m=1}^M$  of  $M$  subjects may be different from each other. Accordingly, this paper assumes that the number of predicted HM positions  $N$  is equivalent to  $M$  at each frame, for predicting the HM positions of all subjects. In other words, to obtain  $(\hat{x}_t^n, \hat{y}_t^n)$ , our offline-DHP approach applies one DRL workflow to estimate the HM positions of one subject. Then,  $N$  DRL workflows are run to obtain  $N$  HM positions  $\{(\hat{x}_t^n, \hat{y}_t^n)\}_{n=1}^N$  at frame  $t$ , simulating the ground-truth HM positions of  $M$  ( $= N$ ) subjects at this frame. At a panoramic frame, each of the DRL workflows works independently to generate an HM position by randomly sampling actions based on a learned policy  $\pi_t$ . Note that all DRL workflows share the same policy  $\pi_t$  in our approach.

In a single DRL workflow,  $\{(\hat{x}_t^n, \hat{y}_t^n)\}_{t=1}^T$  can be modeled by determining a series of *actions*:  $\{\hat{\alpha}_t^n\}_{t=1}^T$  and  $\{\hat{\nu}_t^n\}_{t=1}^T$ . It is worth pointing out that  $\{\hat{\alpha}_t^n\}_{t=1}^T$  and  $\{\hat{\nu}_t^n\}_{t=1}^T$  are predictable as the

*actions* of the DRL workflow, since *Findings 3* and *4* have indicated that subjects are consistent in the magnitudes and directions of HM scanpaths. As can be seen in Figure 8, in each workflow, one HM scanpath is generated through the interaction between the FoV extractor<sup>3</sup> and HM scanpath predictor. Specifically, Figure 8 shows that FoV  $\mathbf{o}_t^n$  is extracted via making its center locate at the HM position  $(\hat{x}_t^n, \hat{y}_t^n)$ , in which  $(\hat{x}_t^n, \hat{y}_t^n)$  is generated by the predicted *action* of HM scanpaths  $(\hat{\alpha}_{t-1}^n, \hat{\nu}_{t-1}^n)$  at the previous video frame. Then, the content of the extracted FoV works as the *observation* of DRL, for predicting the next *action* of HM scanpath  $(\hat{\alpha}_t^n, \hat{\nu}_t^n)$ . The HM scanpath generated by each DRL workflow is forwarded to obtain HM positions at incoming frames. Subsequently, the HM positions from multiple DRL workflows are integrated, and then smoothed by a 2D Gaussian filter. Finally, the HM maps  $\{\mathbf{H}_t\}_1^T$  of the panoramic video are obtained, which model the heat maps for the HM positions at each frame.

## 4.2 DRL model of the offline-DHP approach

As described in Section 4.1, the DRL workflow is a key component in our offline-DHP framework, which targets at predicting the HM scanpaths. This section presents how to train the DRL model of each workflow for predicting the HM maps. In this section, we take the  $n$ -th workflow as an example. Figure 9 shows the framework of training the DRL model. As shown in this figure, the FoV of the input video frame is extracted based on the *action* of the HM scanpath predicted at the previous frame. The extracted FoV, as the *observation*, is then fed into the DRL network. In addition, the *reward*, which measures the similarity between the predicted and ground-truth HM scanpaths, is estimated to evaluate the *action* made by the DRL model. Then, the *reward* is used to make decision on the *action* through the DRL model, i.e., the HM scanpath at the current frame. Finally, the *environment* of our DRL model is comprised by the *observation* of the extracted FoV and the *reward* of HM scanpath prediction.

In training the DRL model, the *environment* interacts with the HM scanpath predictor. The interaction is achieved in our DRL model through the following procedure.

- (1) At frame  $t$ , the FoV extractor obtains the current *observation*  $\mathbf{o}_t^n$  ( $103^\circ \times 60^\circ$ ) from the input video frame  $\mathbf{F}_t$ , according to the predicted HM position  $(\hat{x}_t^n, \hat{y}_t^n)$ . In our work,  $\mathbf{o}_t^n$  is projected onto the 2D region and is then down-sampled to  $42 \times 42$ .
- (2) The current  $\mathbf{o}_t^n$  and the LSTM feature  $\mathbf{f}_{t-1}^n$  from the last frame are delivered to the DRL network in the HM scanpath predictor. In our work, the DRL network contains four convolutional layers and one LSTM layer [42], which are used to extract the spatial and temporal features, respectively. The details about the architecture of the DRL network can be found in Figure 9.
- (3) At frame  $t$ , the DRL network produces the LSTM feature  $\mathbf{f}_t^n$ , HM scanpath magnitude  $\hat{\nu}_t^n$  and policy  $\pi_t$ . Here,  $\pi_t$  is modeled by the probability distribution over the *actions* of HM scanpath directions.
- (4) Given  $\pi_t$ , the HM scanpath predictor randomly samples an *action*  $\hat{\alpha}_t^n$  with standard deviation  $\varepsilon$ , such that the exploration is ensured in decision making. Here,  $\hat{\alpha}_t^n$  includes 8 discrete directions in GDS:  $\{0^\circ, 45^\circ, \dots, 315^\circ\}$ .
- (5) *Environment* is updated using  $\hat{\nu}_t^n$  and  $\hat{\alpha}_t^n$ , leading to  $(\hat{x}_t^n, \hat{y}_t^n) \rightarrow (\hat{x}_{t+1}^n, \hat{y}_{t+1}^n)$ . The FoV extractor returns a new *observation*  $\mathbf{o}_{t+1}^n$  according to the HM position  $(\hat{x}_{t+1}^n, \hat{y}_{t+1}^n)$ . The

3. Note that the extracted FoV is  $103^\circ \times 60^\circ$ , which is the same as the setting of the HMD.

*reward* estimator returns the *rewards*  $r_{n,t}^\nu$  and  $r_{n,t}^\alpha$  in predicting  $\hat{\nu}_t^n$  and  $\hat{\alpha}_t^n$ , based on the ground-truth HM scanpaths of  $\{\nu_t^m\}_{m=1}^M$  and  $\{\alpha_t^m\}_{m=1}^M$ .

(6) A set of experiences  $\{\mathbf{o}_t^n, \mathbf{f}_{t-1}^n, \hat{\nu}_t^n, \hat{\alpha}_t^n, r_{n,t}^\nu, r_{n,t}^\alpha\}$  are stored in an experience buffer for frame  $t$ . In addition,  $\mathbf{o}_{t+1}^n$  and  $\mathbf{f}_t^n$  are preserved for processing frame  $t+1$ .

(7) Once  $t$  meets the termination condition of exceeding the maximum frame number  $T$ , all experiences in the buffer are delivered to the optimizer for updating the DRL network.

**Reward Estimation.** Next, we focus on modeling the *rewards*  $r_{n,t}^\alpha$  and  $r_{n,t}^\nu$  in determining the *actions* of HM scanpaths. When training the DRL model, our goal is to make the prediction of  $\hat{\alpha}_t^n$  and  $\hat{\nu}_t^n$  approach the ground-truth HM scanpaths. Thus, the *rewards*  $r_{n,t}^\alpha$  and  $r_{n,t}^\nu$  can be represented by the differences from  $\hat{\alpha}_t^n$  to  $\{\alpha_t^m\}_{m=1}^M$  and from  $\hat{\nu}_t^n$  to  $\{\nu_t^m\}_{m=1}^M$ , respectively. In our approach, these differences are measured by Gaussian distributions. We further consider the distances from predicted HM position  $(\hat{x}_t^n, \hat{y}_t^n)$  to  $\{(x_t^m, y_t^m)\}_{m=1}^M$  in calculating the *rewards* of  $r_{n,t}^\alpha$  and  $r_{n,t}^\nu$ , which are also modeled by the 2D Gaussian distribution. This consideration is because only the consistent HM regions have similar HM scanpaths, according to the analysis of *Finding 4*. Then,  $r_{n,t}^\alpha$  can be written as

$$r_{n,t}^\alpha = \frac{1}{N} \sum_{m=1}^M e^{-\frac{1}{2} \left( \frac{D_d(\hat{\alpha}_t^n, \alpha_t^m)}{\rho} \right)^2} e^{-\frac{1}{2} \left( \frac{D_s((\hat{x}_t^n, \hat{y}_t^n), (x_t^m, y_t^m))}{\varrho} \right)^2}, \quad (1)$$

In (1),  $D_d$  defines the phase difference, and  $D_s$  denotes the great-circle distance [43]. Moreover,  $\rho$  and  $\varrho$  are the standard deviations of Gaussian distributions, as the hyper-parameters. Similarly, we have

$$r_{n,t}^\nu = \frac{1}{N} \sum_{m=1}^M e^{-\frac{1}{2} \left( \frac{\hat{\nu}_t^n - \nu_t^m}{\varsigma} \right)^2} e^{-\frac{1}{2} \left( \frac{D_d(\hat{\alpha}_t^n, \alpha_t^m)}{\rho} \right)^2} e^{-\frac{1}{2} \left( \frac{D_s((\hat{x}_t^n, \hat{y}_t^n), (x_t^m, y_t^m))}{\varrho} \right)^2}. \quad (2)$$

where  $\varsigma$  is the hyper-parameter for the standard deviation of the HM scanpath magnitude.

**Optimization.** Next, we need to optimize the *rewards*  $r_{n,t}^\alpha$  and  $r_{n,t}^\nu$ , when learning the network parameters of our DRL model in Figure 9. Our offline-DHP approach utilizes the asynchronous DRL method [8] to learn the DRL parameters with optimized *rewards*. Hence, multiple workflows are run to interact with multiple *environments* with workflow-specific parameter vectors  $\{\theta_\nu^n, \theta_\pi^n, \theta_V^n\}$ , producing  $\hat{\nu}_t^n$ ,  $\hat{\alpha}_t^n$  and  $V$ . Here,  $V$  denotes *state value* output by the DRL network, which is obtained using the same way as [8]. Meanwhile, global-shared parameter vectors  $\{\theta_\nu, \theta_\pi, \theta_V\}$ <sup>4</sup> are updated via accumulating gradient. For more details about the workflow-specific and global-shared parameter vectors, refer to [8]. In our approach, *reward*  $r_{n,t}^\nu$  is optimized to train  $\theta_\nu$  as follows,

$$d\theta_\nu \leftarrow d\theta_\nu + \nabla_{\theta_\nu} \sum_{t=1}^T r_{n,t}^\nu. \quad (3)$$

Besides, we can optimize *reward*  $r_{n,t}^\alpha$  by

$$d\theta_V \leftarrow d\theta_V + \nabla_{\theta_V} \sum_{t=1}^T \left( \sum_{i=t}^T \gamma^{i-t} r_{n,i}^\alpha - V(\mathbf{o}_t^n, \mathbf{f}_{t-1}^n; \theta_V^n) \right)^2, \quad (4)$$

4. As can be seen in Figure 9,  $\{\theta_\nu, \theta_\pi, \theta_V\}$  share all CNN and LSTM layers in our offline-DHP approach, but they are separated at the output layer.

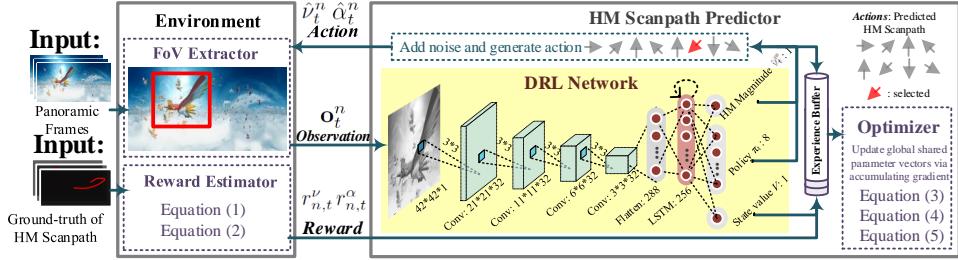


Fig. 9: Framework of training the DRL model to obtain each DRL workflow of the offline-DHP approach (Figure 8).

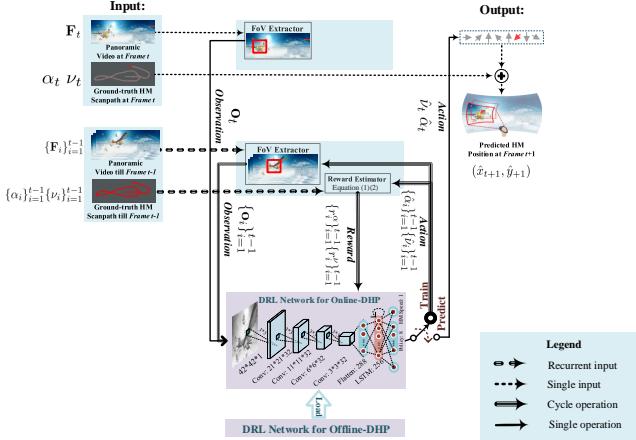


Fig. 10: Framework of the online-DHP approach.

$$\begin{aligned} d\theta_\pi &\leftarrow d\theta_\pi + \nabla_{\theta_\pi} \sum_{t=1}^T \log \pi(\hat{\alpha}_t^n | \mathbf{o}_t^n, \mathbf{f}_{t-1}^n; \theta_\pi^n) \cdot \\ &\quad \left( \sum_{i=t}^T \gamma^{i-t} r_{n,i}^\alpha - V(\mathbf{o}_t^n, \mathbf{f}_{t-1}^n; \theta_V^n) \right), \end{aligned} \quad (5)$$

where  $\gamma$  is the discount factor of *Q-learning* [44]. In addition,  $V(\mathbf{o}_t^n, \mathbf{f}_{t-1}^n; \theta_V^n)$  denotes state value  $V$  yielded by  $\mathbf{o}_t^n, \mathbf{f}_{t-1}^n$  and  $\theta_V^n$ ;  $\pi(\hat{\alpha}_t^n | \mathbf{o}_t^n, \mathbf{f}_{t-1}^n; \theta_\pi^n)$  stands for the probability of *action*  $\hat{\alpha}_t^n$  that is made by policy  $\pi_t$  from  $\mathbf{o}_t^n, \mathbf{f}_{t-1}^n$  and  $\theta_\pi^n$ . Finally, upon the above equations, RMSProp [45] is applied to optimize *rewards* in the training data. As a result, the workflow-specific and global-shared parameter vectors can be learned to predict HM scanpaths. Finally, these learned parameter vectors can be used to determine the scanpaths and positions of HM through each DRL workflow in our offline-DHP approach.

## 5 ONLINE-DHP APPROACH

In this section, we present our online-DHP approach. The online-DHP approach refers to predicting the specific subject's HM position  $(\hat{x}_{t+1}, \hat{y}_{t+1})$  at frame  $t+1$ , given his/her HM positions  $\{(x_1, y_1), \dots, (x_t, y_t)\}$  till frame  $t$ . Note that the definition of notations in this section is similar to those of Section 4, and the only difference is that  $n$  and  $m$  are removed in all notations as there is only one subject/workflow in online-DHP. Additionally, we define the subject as the *viewer*, whose HM positions need to be predicted online. Figure 10 shows the framework of our online-DHP approach. According to *Finding 6*, the current HM

scanpath is correlated with the previous HM scanpaths and the video content. Therefore, the input to our online-DHP framework is the *viewer's* HM scanpath  $\{(\alpha_1, \nu_1), \dots, (\alpha_{t-1}, \nu_{t-1})\}$  and frame content  $\{\mathbf{F}_1, \dots, \mathbf{F}_t\}$ , and the output is the predicted HM position  $(\hat{x}_{t+1}, \hat{y}_{t+1})$  at the next frame for the *viewer*. This can be seen as online prediction of HM positions  $\{(\hat{x}_t, \hat{y}_t)\}_{t=1}^T$ . To this end, our online-DHP consists of two stages: the training and prediction stages. At the first stage, the parameters of the DRL network are trained. At the second stage, the *action* of HM scanpath is generated upon the trained DRL network, to predict the HM position online. In the following, we discuss these two stages with more details.

### 5.1 Stage I: Training

At the beginning frame, the HM position  $(\hat{x}_1, \hat{y}_1)$  of the *viewer* is initialized to be the center of front region, which is the general setting of the panoramic video player. Then, the trained DRL network of offline-DHP is loaded as the initial DRL network for online prediction, both sharing the same structure. The reason for loading the offline-DHP network is that it encodes the knowledge of HM related features. Later, this initial DRL network is fine-tuned by the *viewer's* HM scanpath at incoming frames.

Next, we focus on the algorithm of training the DRL network in our online-DHP approach. As aforementioned, the initial parameters of the DRL network at the first frame are directly from those of offline-DHP. At each of the incoming frames, several episodes are run to update the DRL network for online-DHP. The following summarizes the procedure of one episode at frame  $t+1$ .

- 1) Iterate the following steps from  $i = 1$  to  $t$ . At each iteration,  $(\hat{\alpha}_i, \hat{\nu}_i)$  and  $(\alpha_i, \nu_i)$  are the predicted and ground-truth *actions* of the HM scanpath for the *viewer*, and  $\mathbf{o}_i$  is the *observation* of the FoV content.
- 2) Take *action* of  $(\hat{\alpha}_i, \hat{\nu}_i)$  using the DRL network, given the current *observation*  $\{\mathbf{o}_1, \dots, \mathbf{o}_i\}$  till frame  $i$ . The *action* of  $\hat{\alpha}_i$  selects one among 8 discrete HM scanpath directions, i.e.,  $\{0^\circ, 45^\circ, \dots, 315^\circ\}$ . The *action* of  $\hat{\nu}_i$  is a scalar of HM scanpath magnitude.
- 3) Calculate *rewards*  $(r_i^\alpha, r_i^\nu)$  from the *reward estimator* with (1) and (2), which measures how close the *action*  $(\hat{\alpha}_i, \hat{\nu}_i)$  to the ground-truth HM scanpath  $(\alpha_i, \nu_i)$ . Here, the sums in (1) and (2) are not required for the *reward* calculation, since the ground-truth HM scanpath of online prediction is from a single *viewer*, rather than from all subjects.

- 4) Generate new *observation*  $\mathbf{o}_{i+1}$  from the FoV extractor with the above *action*  $(\hat{\alpha}_i, \hat{\nu}_i)$ , and then it is input to the DRL network.
- 5) Update the DRL network using (3), (4) and (5) and stop iterations, if the iteration number  $i$  is equivalent to  $t$ . Otherwise, go to step 2) for the next iteration.

Here, the definitions of *action*, *reward* and *observation* are the same as those in Section 4.2. The above iterations share the same implementation of training the DRL model in offline-DHP, which is already presented in Section 4.2.

Once the above iterations are terminated, our algorithm moves to the next episode. After a number of episodes, the training stage ends for frame  $t + 1$ , when meeting the termination conditions. In our approach, there are two termination conditions. The first condition is the maximum number  $E$  of episodes. The second one is based on the metric of mean overlap (MO), which measures how close the predicted HM position to the ground-truth HM position. MO ranges from 0 to 1, and larger MO indicates more precise prediction. Specifically, MO is defined as,

$$\text{MO} = \frac{A(\text{FoV}_p \cap \text{FoV}_g)}{A(\text{FoV}_p \cup \text{FoV}_g)}, \quad (6)$$

where  $\text{FoV}_p$  and  $\text{FoV}_g$  represent the FoVs at predicted and ground-truth HM positions, respectively. In (6),  $A$  represents the area of a panoramic region, which counts for number of pixels.

Finally, the training DRL network can be obtained at frame  $t + 1$ , once satisfying one of the above termination conditions. Algorithm 1 presents the summary of the training stage in online-DHP.

**Algorithm 1:** Algorithm for the training stage of online-DHP to predict the HM position at frame  $t + 1$ .

- 1: **Input:** Panoramic video frames  $\{\mathbf{F}_1, \dots, \mathbf{F}_t\}$ , and the ground-truth HM positions of the viewer  $\{(x_1, y_1), \dots, (x_t, y_t)\}$ .
- 2: Initialize the DRL network of online-DHP with parameter vectors  $\{\theta_\nu, \theta_\pi, \theta_V\}$ , by loading the network of offline-DHP.
- 3: **for**  $e = 1$  **to**  $E$  **do**
- 4:   Initialize the HM position to be center of front region:  $\hat{x}_1 = 0, \hat{y}_1 = 0$ .
- 5:   Initialize the LSTM feature to be the zero vector:  $\mathbf{f}_0 = \mathbf{0}$ .
- 6:   **for**  $i = 1$  **to**  $t - 1$  **do**
- 7:     Extract *observation*  $\mathbf{o}_i$  (i.e., FoV) from  $\mathbf{F}_i$  according to  $(\hat{x}_i, \hat{y}_i)$ .
- 8:     Obtain *policy*  $\pi_i$  and LSTM feature  $\mathbf{f}_i$  using the DRL network with  $\{\mathbf{o}_i, \mathbf{f}_{i-1}, \theta_\pi\}$ .
- 9:     Select *action*  $\hat{\alpha}_i$  according to the  $\epsilon$ -greedy policy of  $\pi_i$ .
- 10:    Generate *action*  $\hat{\nu}_i$  using the DRL network given  $\mathbf{o}_i, \mathbf{f}_{i-1}$  and  $\theta_\nu$ .
- 11:    Calculate  $(\hat{x}_{i+1}, \hat{y}_{i+1})$  with regard to  $\hat{\alpha}_i, \hat{\nu}_i$ , and  $(\hat{x}_i, \hat{y}_i)$ .
- 12:    Estimate *rewards*  $r_i^\nu$  and  $r_i^\alpha$  through (1) and (2) for  $(\hat{\alpha}_i, \hat{\nu}_i)$ .
- 13:    Calculate MO between  $(\hat{x}_i, \hat{y}_i)$  and  $(x_i, y_i)$ , denoted as  $\text{MO}_i$ .
- 14:    Store a set of experience:  $\{\mathbf{o}_i, \mathbf{f}_{i-1}, \hat{\nu}_i, \hat{\alpha}_i, r_i^\nu, r_i^\alpha\}$ .
- 15:    *i*  $\leftarrow i + 1$ .
- 16:   **end for**
- 17:   Update  $\{\theta_\nu, \theta_\pi, \theta_V\}$  according to (3), (4), (5), in which  $\{\theta_\nu^n, \theta_\pi^n, \theta_V^n\}$  are replaced by  $\{\theta_\nu, \theta_\pi, \theta_V\}$ .
- 18:   *e*  $\leftarrow e + 1$ .
- 19:   Calculate the average MO through  $\text{MO} = \frac{\sum_{i=1}^{t-1} \text{MO}_i}{t-1}$ .
- 20:   **if**  $\text{MO} > th_{\text{MO}}$  **then**
- 21:     **break**
- 22:   **end if**
- 23: **end for**
- 24: **Return:** The trained parameter vectors:  $\{\theta_\nu, \theta_\pi, \theta_V\}$ .

## 5.2 Stage II: Prediction

When the average MO is larger than a threshold  $th_{\text{mo}}$ , the switch of Figure 10 is turned to “predict”, and the DRL network makes an action of HM scanpath at frame  $t + 1$ . Note that if the number

of training episodes exceeds  $E$ , the “predict” is also switched on, such that the training episodes end in a limited time. When entering the prediction stage, the DRL model trained at the first stage is used to produce the HM position as follows.

First, the LSTM features  $\{\mathbf{f}_i\}_{i=1}^{t-1}$  are sequentially updated from frame 1 to  $t - 1$ , upon the observed FoVs  $\{\mathbf{o}_i\}_{i=1}^{t-1}$  and the DRL parameters  $\theta_\pi$  of the training stage. Note that the LSTM feature is initialized with the zero vector  $\mathbf{0}$  at frame 1. Then,  $\{\mathbf{o}_t, \mathbf{f}_{t-1}, \theta_\pi\}$  produce action  $\hat{\alpha}_t$  of the HM scanpath direction. In addition, the HM scanpath magnitude  $\hat{\nu}_t$  is generated using  $\{\mathbf{o}_t, \mathbf{f}_{t-1}, \theta_\nu\}$ , in which the parameters of  $\theta_\nu$  are obtained at the training stage. Afterwards, the HM position  $(\hat{x}_{t+1}, \hat{y}_{t+1})$  at frame  $t + 1$  can be predicted, given the ground-truth HM position  $(x_t, y_t)$  and the estimated HM scanpath  $(\hat{\alpha}_t, \hat{\nu}_t)$  at frame  $t$ . Algorithm 2 presents the summary of the prediction stage in online-DHP. Finally, online-DHP is achieved by alternating between the stages of training and prediction till the currently proposed frame.

**Algorithm 2:** Algorithm for the prediction stage of online-DHP at frame  $t + 1$ .

- 1: **Input:** The trained parameter vectors:  $\{\theta_\nu, \theta_\pi, \theta_V\}$  from the training stage, panoramic video frames  $\{\mathbf{F}_1, \dots, \mathbf{F}_t\}$ , and the ground-truth HM positions of the viewer  $\{(x_1, y_1), \dots, (x_t, y_t)\}$ .
- 2: Initialize the LSTM feature with the zero vector:  $\mathbf{f}_0 = \mathbf{0}$ .
- 3: **for**  $i = 1$  **to**  $t - 1$  **do**
- 4:   Extract *observation*  $\mathbf{o}_i$  (i.e., FoV) from  $\mathbf{F}_i$  according to  $(x_i, y_i)$ .
- 5:   Obtain LSTM feature  $\mathbf{f}_i$  using the DRL network with  $\{\mathbf{o}_i, \mathbf{f}_{i-1}, \theta_\pi\}$ .
- 6:   *i*  $\leftarrow i + 1$ .
- 7: **end for**
- 8: Extract *observation*  $\mathbf{o}_t$  (i.e., FoV) from  $\mathbf{F}_t$  according to  $(x_t, y_t)$ .
- 9: Obtain *policy*  $\pi_t$  using the DRL network with  $\{\mathbf{o}_t, \mathbf{f}_{t-1}, \theta_\pi\}$ .
- 10: Choose *action*  $\hat{\alpha}_t$  using the greedy policy based on  $\pi_t$ .
- 11: Generate HM magnitude  $\hat{\nu}_t$  using the DRL network with  $\{\mathbf{o}_t, \mathbf{f}_{t-1}, \theta_\nu\}$ .
- 12: Estimate HM position  $(\hat{x}_{t+1}, \hat{y}_{t+1})$  at frame  $t + 1$ , upon  $\hat{\alpha}_t, \hat{\nu}_t$  and  $(x_t, y_t)$ .
- 13: **Return:** The HM position at frame  $t + 1$ :  $(\hat{x}_{t+1}, \hat{y}_{t+1})$ .

## 6 EXPERIMENTAL RESULTS

This section presents the experimental results to validate the effectiveness of our offline-DHP and online-DHP approaches. In Section 6.1, we discuss the settings of both offline-DHP and online-DHP in our experiments. Sections 6.2 and 6.3 compare the performance of our offline-DHP and online-DHP approaches with other approaches in predicting HM positions, in the offline and online scenarios, respectively.

### 6.1 Settings

For evaluating the performance of offline-DHP, we randomly divided all 76 panoramic sequences of our PVS-HM database into a training set (61 sequences) and a test set (15 sequences). In training the DRL model, the hyperparameters  $\rho$ ,  $\varrho$  and  $\varsigma$  of (1) and (2) were tuned over the training set, when estimating the *reward* of HM scanpath prediction. As a result,  $\rho$ ,  $\varrho$  and  $\varsigma$  were set to be 42, 0.7 and 1.0. In addition, we followed [8] to set other hyperparameters of DRL. For example, we chose the discount factor  $\gamma$  of (4) and (5) to be 0.99 for *reward* optimization. In our experiments, all 61 training sequences, each of which corresponds to a local DRL network, were used to update the global network as the trained DRL model. The number of DRL workflows  $N$  in the offline-DHP framework was set to be 58, the same as the number of subjects in our PVS-HM database. Similar to [40], the HM positions predicted by 58 DRL workflows were convoluted with a 2D Gaussian filter at each panoramic frame, in order to generate

TABLE 3: CC results of offline HM map prediction by our and other approaches over 15 test sequences.

CC	Method	StarryPolar	Symphony	SpaceWar	RioOlympics	InsideCar	SpaceWar2	Sunset	BlueWorld	Waterfall	Dancing	CMLauncher2	Guitar	KingKong	BTSRun	WaitingForLove	Average
Non-FCB	Our	0.185	<b>0.710</b>	<b>0.573</b>	<b>0.717</b>	<b>0.783</b>	<b>0.673</b>	<b>0.673</b>	<b>0.678</b>	<b>0.763</b>	<b>0.837</b>	<b>0.585</b>	<b>0.645</b>	<b>0.751</b>	<b>0.764</b>	<b>0.471</b>	<b>0.654</b>
	BMS	<b>0.450</b>	0.167	0.274	0.228	0.331	0.067	0.463	0.169	0.393	0.121	0.203	0.328	0.105	0.223	0.242	0.242
	OBDL	0.107	0.184	0.028	0.190	0.260	0.100	0.308	0.027	0.025	0.176	0.117	0.066	0.125	0.047	0.222	0.132
	SALICON	0.293	0.129	0.126	0.153	0.364	0.034	0.186	0.265	0.103	0.120	0.166	0.216	0.150	0.063	0.256	0.175
FCB	Our	0.497	<b>0.816</b>	<b>0.574</b>	<b>0.768</b>	<b>0.712</b>	<b>0.655</b>	<b>0.810</b>	<b>0.748</b>	<b>0.797</b>	<b>0.764</b>	<b>0.747</b>	<b>0.652</b>	<b>0.673</b>	<b>0.679</b>	<b>0.677</b>	<b>0.704</b>
	BMS	<b>0.692</b>	0.567	0.520	0.494	0.495	0.368	0.711	0.500	0.655	0.414	0.546	0.494	0.311	0.322	0.503	0.506
	OBDL	0.510	0.540	0.321	0.441	0.496	0.455	0.638	0.464	0.434	0.408	0.468	0.461	0.410	0.288	0.598	0.462
	SALICON	0.664	0.563	0.456	0.539	0.528	0.452	0.658	0.596	0.525	0.355	0.667	0.461	0.362	0.346	0.628	0.520
FCB Only		0.557	0.747	0.317	0.403	0.292	0.239	0.585	0.477	0.583	0.387	0.735	0.356	0.271	0.201	0.497	0.443

TABLE 4: NSS results of offline HM map prediction by our and other approaches over 15 test sequences.

NSS	Method	StarryPolar	RioOlympics	SpaceWar2	Symphony	SpaceWar	Waterfall	Sunset	BlueWorld	Guitar	Dancing	InsideCar	CMLauncher2	WaitingForLove	BTSRun	KingKong	Average
Non-FCB	Our	0.899	<b>2.806</b>	<b>2.237</b>	<b>3.346</b>	<b>2.180</b>	<b>3.765</b>	<b>2.529</b>	<b>3.196</b>	<b>3.461</b>	<b>5.297</b>	<b>4.402</b>	<b>3.529</b>	<b>2.278</b>	<b>4.572</b>	<b>3.334</b>	<b>3.189</b>
	BMS	<b>1.313</b>	0.772	0.137	0.710	0.807	1.673	1.613	0.841	1.497	0.670	1.657	1.034	0.997	0.546	0.119	0.959
	OBDL	0.126	0.637	0.301	0.260	0.064	0.073	1.015	0.035	0.393	0.980	1.375	0.660	0.964	0.215	0.107	0.480
	SALICON	0.730	0.600	0.251	0.456	0.344	0.410	0.669	1.138	0.965	0.230	1.823	0.921	1.298	0.337	0.203	0.692
FCB	Our	1.825	<b>2.911</b>	<b>2.064</b>	<b>3.756</b>	<b>2.031</b>	<b>3.755</b>	<b>2.943</b>	<b>3.393</b>	<b>3.395</b>	<b>4.608</b>	<b>3.816</b>	<b>4.463</b>	<b>3.351</b>	<b>3.931</b>	<b>2.883</b>	<b>3.275</b>
	BMS	<b>2.206</b>	1.779	1.063	2.537	1.667	2.891	2.507	2.280	2.386	2.366	2.508	3.136	2.434	1.771	1.288	2.188
	OBDL	1.712	1.572	1.371	2.368	1.055	1.920	2.225	2.007	2.377	2.319	2.556	2.777	2.912	1.580	1.693	2.030
	SALICON	2.083	2.024	1.332	2.477	1.493	2.353	2.352	2.619	2.264	1.957	2.672	3.932	3.143	1.915	1.496	2.274
FCB Only		2.388	1.613	0.699	4.123	1.190	3.191	2.406	2.286	1.828	2.151	1.387	5.764	2.600	1.095	1.020	2.249

the HM map. In our experiments, the HM maps in a panorama were projected to the 2D coordination for facilitating visualization.

For evaluating the performance of online-DHP, we compared our approach with [17] and two baseline approaches. Since the DRL network of offline-DHP was learned over 61 training sequences and used as the initial model of online-DHP, our comparison was conducted on all 15 test sequences of our PVS-HM database. In our experiments, the comparison was further carried out over all test sequences of the database presented in [17], in order to test the generalization ability of our online-DHP approach. In our online-DHP approach, the hyperparameters of  $\rho$ ,  $\varrho$ ,  $\varsigma$  and  $\gamma$  were set to be the same as those of the DRL workflows of offline-DHP. Other hyperparameters were identical to those in the latest DRL work of [8]. In addition, the maximum number of episodes and the MO threshold are set to be 500 and XXX, respectively, as the termination conditions in the training stage of online-DHP. The settings of these two values are to be analyzed in Section 6.3.

## 6.2 Performance evaluation on offline-DHP

Now, we evaluate the performance of our offline-DHP approach in predicting the HM maps of all 15 test sequences from the PVS-HM database. To the best of our knowledge, there is no work on predicting the HM maps of panoramic video, and saliency prediction is the closest field. Therefore, we compare our offline-DHP approach to three state-of-the-art saliency detection approaches, OBDL [24], BMS [12] and SALICON [13]. In particular, OBDL [24] and BMS [12] are the latest saliency detection approaches for video and image, respectively. SALICON [13] is a state-of-the-art DNN approach for saliency detection. In addition to the above three approaches, we also compare our approach to the FCB baseline, since *Finding 1* argues that human attention normally biases towards the front-center regions of panoramic video. Here, we model FCB by 2D Gaussian distribution, similar to the center bias of saliency detection. Appendix A presents the details of the FCB modeling. In the field of saliency detection, the center bias [2] is normally combined with saliency maps to improve saliency detection accuracy. Hence, we further report results of HM maps combined with the FCB feature, for our and other approaches. See Appendix A for more details about the combination of FCB. In evaluation, we measure the prediction accuracy of HM maps in terms of CC and normalized scanpath saliency (NSS), which are

two effective evaluation metrics [?] in saliency detection. Note that the larger values of CC and NSS mean more accurate prediction of HM maps.

Table 5 tabulates the results of CC and NSS in predicting the HM maps of 15 test sequences, for our and other approaches. In this table, the results of CC and NSS are averaged over all frames for each test sequence. As shown in this table, when FCB is not integrated, our offline-DHP approach performs best among all four approaches and the FCB baseline, in terms of CC and NSS. More importantly, once integrated with FCB, all four approaches have performance improvement, and our approach still performs considerably better than other approaches. Specifically, our offline-DHP approach increases the average CC value by 0.198, 0.242 and 0.184, compared with OBDL, BMS and SALICON, respectively. Additionally, the increase of average NSS value is 1.087, 1.245 and 1.001 in our approach, in comparison with OBDL, BMS and SALICON. In a word, our offline-DHP approach is effective in predicting the HM maps of panoramic video, much better than other approaches and the FCB baseline.

Next, we move to the comparison of subjective results. Figure 11 shows several frames from two selected sequences and their ground-truth HM maps. In Figure 11, we further visualize the HM maps generated by our and three other approaches. Here, the predicted HM maps are integrated with FCB, since the FCB feature can improve the performance of all four approaches (as presented in Table 5). From this figure, one can observe that the HM maps of our approach are considerably more close to the ground-truth HM maps, compared with other approaches. This indicates that our offline-DHP approach is capable of better locating the HM positions of different subjects on panoramic video. Moreover, Figure 12 plots the HM scanpaths by several subjects and by multiple DRL workflows of offline-DHP, to investigate the agreement between the subjects and DRL workflows. We can see from this figure that the DRL workflows are able to yield similar scanpaths as humans. We further show in Figure 12 the HM positions obtained from the ground-truth and predicted HM scanpaths. As seen in this figure, the HM positions can be well predicted by our offline-DHP approach. In conclusion, our offline-DHP approach is effective in modeling HM maps by predicting both scanpaths and positions of HM for panoramic video.

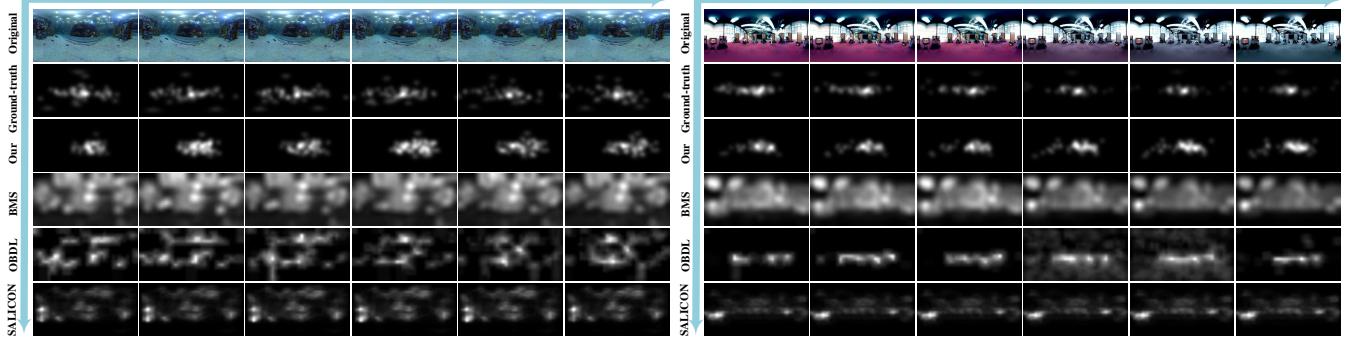


Fig. 11: HM maps of several frames selected from two test sequences in our PVS-HM database. They are all visualized in the 2D coordination. The second row shows the ground-truth HM maps, which are generated upon the HM positions of all 58 subjects. The third to sixth rows show the HM maps of our, BMS [12], OBDL [24], and SALICON [13] approaches.

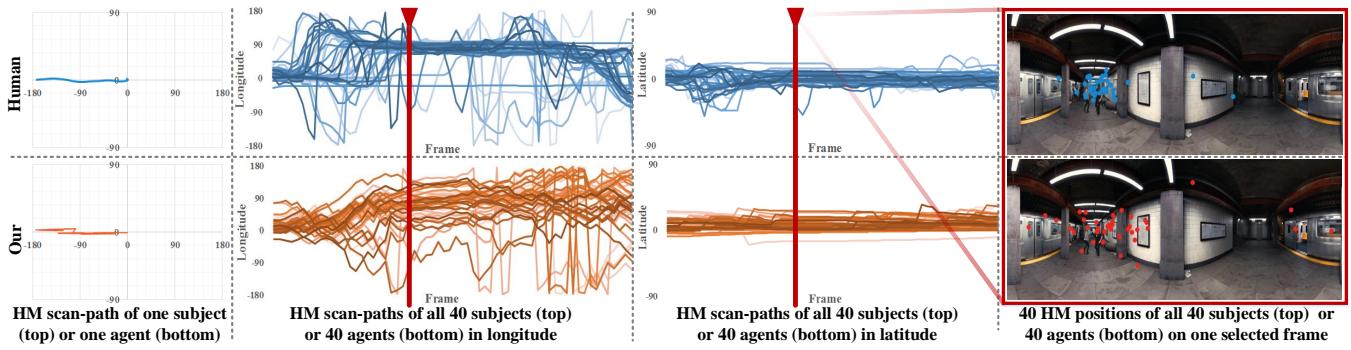


Fig. 12: Visualization in scanpaths and positions of HM generated by ground-truth and our offline-DHP approach, for sequence *Help*. The first column shows scanpath of one subject and one DRL workflow. The second and third columns show scanpaths of all 40 subjects and 40 DRL workflows, in longitude and latitude directions. The last column visualizes HM positions of ground-truth and our approach.

### 6.3 Performance evaluation on online-DHP

This section evaluates the performance of our online-DHP approach for predicting HM positions in the online scenario. The online scenario refers to predicting the HM position of one subject at each panoramic frame upon the observed HM positions of this subject at the previous frames. In our experiments, we compare the performance of online-DHP with the state-of-the-art deep 360 pilot [17], which is the only existing approach for online prediction of HM positions in panoramic video. We also compare our online-DHP approach with two baselines. According to *Finding 6*, the first baseline (called baseline 1) keeps the HM scanpath of the current frame the same as that at the previous frame, such that the online HM position at each frame can be generated. The second baseline (called baseline 2) produces the HM positions, using the randomly generated HM scanpaths. The same as [17], MO of (6) is measured as the metric to evaluate the accuracy of online prediction in HM positions. Note that the larger value of MO means the more accurate online prediction in HM positions.

Table 5 compares the MO results of our and other approaches for the 15 test sequences of our PVS-HM database. Note that the MO results of each sequence are averaged over the predicted HM positions of all 58 subjects in our database. As observed in this table, our online-DHP approach is significantly superior to two baselines, indicating the effectiveness in applying DRL to predict HM positions online. We can further see from Table 5 that our online-DHP approach performs considerably better than the deep 360 pilot [17], with an increase of 0.354 in average MO. In addition, as shown in Table 5, our approach outperforms [17] over almost all sequences. The performance improvement of our approach is probably because (1) the online DRL model of our approach is

capable of generating the accurate *actions* of HM scanpaths; (2) the DRL network of offline-DHP is incorporated in our online prediction as the prior knowledge. Besides, our approach is also effective for the generic panoramic sequences, while [17] fails in scenery panoramic video. For example, the MO result of [17] for the sequence Waterfall is 0.082, far less than 0.667 MO of online-DHP. It is mainly due to the fact that the deep 360 pilot [17] relies heavily on the object detection of RCNN.

To test the generalizability of our approach, we further evaluate the performance of our, the deep 360 pilot [17] and two baseline approaches on the sports-360 dataset of [17]. For such evaluation, our online-DHP is still based on our offline DRL network that is learned from the training sequences of our PVS-HM database. The MO results are shown in Table 6. From this table, one may observe that our online-DHP approach again outperforms [17] and two baselines, despite testing on the test set of [17]. In particular, the MO result of our approach is 0.90 for the panoramic sequences of dance, with 0.11 MO increase over [17]. Additionally, our approach improves the MO results of [17] by 0.07, 0.01, 0.01, and 0.10, for the sequences of skateboarding, parkour, BMX and basketball, respectively. In a word, the online-DHP approach is superior to the state-of-the-art approach [17] in online prediction of HM positions, over almost all classes of panoramic video sequences. Therefore, the generalization capability of our online-DHP approach can be confirmed.

It is interesting to analyze the gain of incorporating the DRL network of offline-DHP in our online-DHP approach, since the online-DHP approach is based on the offline DRL network. Figure 13 shows the MO results of our online-DHP approach with and without the offline DRL network. As observed in this figure, the

TABLE 5: MO results of online HM position prediction by our and other approaches.

Method	KingKing	SpaceWar2	StarryPolar	Dancing	Guitar	BTSRun	InsideCar	RioOlympics	SpaceWar	CMLauncher2	Waterfall	Sunset	BlueWorld	Symphony	WaitingForLove	Average
Online	<b>0.809</b>	<b>0.763</b>	<b>0.549</b>	<b>0.859</b>	<b>0.785</b>	<b>0.878</b>	<b>0.847</b>	<b>0.820</b>	<b>0.626</b>	<b>0.763</b>	<b>0.667</b>	<b>0.659</b>	<b>0.693</b>	0.747	<b>0.836</b>	<b>0.753</b>
Deep 360 Polit	0.340	0.208	0.322	0.537	0.541	0.615	0.206	0.270	0.391	0.205	0.082	0.464	0.352	0.518	0.399	
Baseline 1	0.201	0.206	0.161	0.216	0.203	0.206	0.216	0.203	0.209	0.205	0.203	0.204	0.206	0.202	0.211	0.204
Baseline 2	0.224	0.231	0.197	0.217	0.227	0.237	0.234	0.225	0.216	0.251	0.251	0.209	0.229	0.216	0.225	0.226

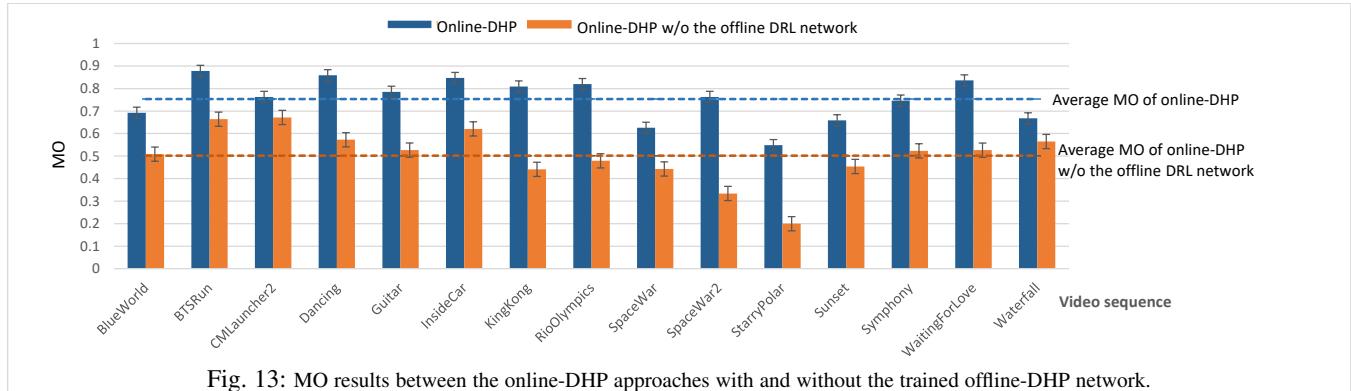


Fig. 13: MO results between the online-DHP approaches with and without the trained offline-DRL network.

TABLE 6: MO results for online prediction of HM positions over the sports-360 dataset.

Method	Skateboarding	Parkour	BMX	Dance	Basketball
DHP	<b>0.78</b>	<b>0.75</b>	<b>0.72</b>	<b>0.90</b>	<b>0.77</b>
Deep 360 Polit	0.71	0.74	0.71	0.79	0.67
Baseline 1	0.20	0.21	0.16	0.22	0.20
Baseline 2	0.22	0.23	0.20	0.22	0.23

offline DRL network is able to increase the MO results of our online-DHP approach, for all 15 sequences. In addition, the MO value can be increased from 0.502 to 0.753 on average, when the offline DRL network is incorporated in online-DHP. Therefore, the learned DRL network of offline-DHL also benefits the online prediction of HM positions in online-DHL.

## 7 CONCLUSION

In this paper, we have proposed the DHP approach to predict HM positions on panoramic video. First, we established a new database named PVS-HM, which includes HM data of 58 subjects viewing 76 panoramic sequences. We found from our database that the HM positions are highly consistent across humans. Thus, the consistent HM positions on each panoramic frame can be represented in the form of the HM map, which encodes possibility of each pixel being the HM position. Second, we proposed the offline-DHP approach to estimate HM maps in an offline manner. To be more specific, our offline-DHP approach leverages DRL to make decision on *actions* of HM scanpaths, via optimizing the *reward* of imitating the way of humans in viewing panoramic video. Afterwards, the HM scanpaths of several *agents* from multiple DRL workflows are integrated to yield the final HM maps. Third, we proposed the online-DHP approach, which online predicts the HM positions of one subject. In online-DHP, the DRL algorithm was developed in determining the HM positions of one *agent* at the incoming frames, given the *observation* of previous HM scanpaths and the current video content. The DRL algorithm is based on the learned model of offline-DHP in extracting spatio-temporal features of attention-related content. Finally, the experimental results showed that both offline-DHP and online-DHP are superior to other conventional approaches, in the offline and online tasks of HM prediction for panoramic video.

Humans always perceive the world around them in a panorama, rather than the 2D plane. Therefore, modeling attention on panoramic video is an important component in establishing human-like computer vision systems. Our work at the current stage mainly focuses on predicting HM positions, as the first step towards attention modeling of panoramic video. The future work should further predict eye fixations within FoV regions of panoramic video. The potential applications of our approach are another promising work in future. For example, the online-DHP approach may be embedded in robotics, to mimic human's way in perceiving the real world. Besides, panoramic video has large perceptual redundancy, since most of panoramic regions cannot be seen by humans. It is thus possible to use the offline-DHP approach to remove such perceptual redundancy, such that the bit-rates of panoramic video coding can be dramatically saved.

## APPENDIX A ANALYSIS OF FCB COMBINED IN HM MAPS

The literature of saliency detection [46] has argued that human attention has strong center bias in images or videos, and that the incorporation of center bias can improve the performance of saliency detection. Similarly, there exists FCB when viewing panoramic videos, as discussed in *Finding 1*. Hence, this appendix presents the combination of the FCB feature and the offline-DHP approach. Here, we apply the FCB feature as an additional channel in generating the HM maps of panoramic videos. Specifically, assume that  $\mathbf{H}^f$  is the HM map generated by the channel of the FCB feature. Similar to the center bias feature of image saliency detection [46], we apply the following 2D Gaussian distribution to model  $\mathbf{H}^f$  at each frame,

$$\mathbf{H}^f(u, v) = \exp \left( -\frac{(u - u_f)^2 + (v - v_f)^2}{\sigma_f^2} \right), \quad (7)$$

where  $(u, v)$  is the longitude and latitude of the GDS location in the map, and  $(u_f, v_f)$  is the longitude and latitude of the front center position in GDS. In addition,  $\sigma_f$  is the standard deviation of the 2D Gaussian distribution.

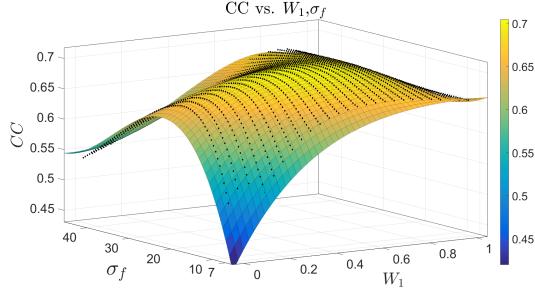


Fig. 14: The fitting surface of CC results between the predicted and ground-truth HM maps at various  $\sigma_f$  and  $w_1$ . The dark dots in this figure represent the CC results at each specific value of  $\sigma_f$  and  $w_1$ , which are used to fit the surface. Note that the CC results are obtained over all training data of the PVS-HM database.

Next, we need to combine  $\mathbf{H}^f$  with the predicted HM map  $\mathbf{H}_t$  by

$$\mathbf{H}_t^c = w_1 \cdot \mathbf{H}^f + w_2 \cdot \mathbf{H}_t, \quad (8)$$

for each panoramic frame. In the above equation,  $\mathbf{H}_t^c$  is the HM map integrated with the FCB feature for frame  $t$ ;  $w_1$  and  $w_2$  are the weights corresponding to the channels of  $\mathbf{H}_c$  and  $\mathbf{H}_t$ , respectively. Given (7) and (8), the following optimization formulation is applied to obtain the values of  $\sigma_f$ ,  $w_1$  and  $w_2$ :

$$\max_{\sigma_f, w_1, w_2} \sum_{t=1}^T \text{CC}(\mathbf{H}_t^c, \mathbf{H}_t^g), \quad \text{s.t. } w_1 + w_2 = 1. \quad (9)$$

In (8),  $\mathbf{H}_t^g$  is the ground-truth HM map of each frame;  $\text{CC}(\cdot, \cdot)$  indicates the CC value of two maps. Then, we solve the above optimization formulation by the least square fitting of CC over all training data of our PVS-HM database. Consequently, the optimal values of  $\sigma_f$ ,  $w_1$  and  $w_2$  are  $21.1^\circ$ ,  $0.52$  and  $0.48$ , respectively. These values are used to integrate the FCB feature in our offline-FCB approach. Note that the same way is applied to obtain the weights of  $w_1$  and  $w_2$ , when combining the FCB feature with other approaches.

Figure 14 shows the results of CC between the predicted and ground-truth HM maps at various values of  $\sigma_f$  and  $w_1$ . From this figure, we can see that CC varies from  $0.44$  to  $0.70$  alongside the increase of  $w_1$  from  $0$  to  $1$ , reaching the maximum value at  $w_1 = 0.52$  given  $\sigma_f = 21.1^\circ$ . This indicates that both the FCB feature and our offline-DHP approach are effective in predicting the HM maps of panoramic video, and that the effectiveness of the FCB feature is different at varying combination weights. In addition, as shown in Figure 14, at  $w_1 = 0.52$ , the CC value increases from  $0.66$  to  $0.70$ , when  $\sigma_f$  grows from  $7^\circ$  to  $21.1^\circ$ , and then it decreases to  $0.63$  till  $\sigma_f = 43.6^\circ$ . Thus, the standard deviation of the 2D Gaussian distribution in (7) is set to be  $21.1^\circ$  for the FCB feature in our experiments.

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