ACM TEMPLATE

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1 To Do List

所有带*的内容。。。

可以从原来的模板里面继承一些好东西过来。

set,map,multiset等的搞基用法,以及注意事项。

生成树计数

2 注意事项

106数量级慎用后缀数组

TLE的时候要冷静哟。。

思考的时候结合具体步骤来的话 会体会到一些不同的东西

C++与G++是很不一样的。。。

map套字符串是很慢的。。。

栈会被记录内存。。。

浮点数最短路要注意取<来判断更新。。。

注意 long long

不要相信.size()

重复利用数组时 小心数组范围

先构思代码框架 每当实际拍马框架变化时 停手 重新思考

有时候四边形不等式也是帮得上忙的 dp 优化是可以水的

结构体里面带数组会非常慢,有时候 BFS 把数组压成数字会快很多。

```
1 void fun(int a[])
2 {
3 printf("%d\n", sizeof(a));
4 }
```

结果是 sizeof(a[0]),如果传数组指针然后要清空的话不要用 sizeof。

sqrt 某些时候会出现 sqrt(-0.00)的问题。

将code::blocks的默认终端改成gnome-terminal

```
1 | gnome-terminal -t $TITLE -x
```

最小割割集找法在残量网络中从源点出发能到的点集记为S原图中S到S'的边即是最小割集 double全局变量初始值可能不是0

3 字符串处理

3.1 *AC自动机

3.1.1 指针

```
const int CHAR=26;
   const int TOTLEN=500000;
 3
   const int MAXLEN=1000000;
 4
   struct Vertex
 5
   {
6
       Vertex *fail,*next[CHAR];
7
       Vertex(){}
8
       Vertex(bool flag)//为什么要这样写?
9
        {
10
            fail=0;
            memset(next,0,sizeof(next));
11
12
       }
13
   };
14 | int size;
15 | Vertex vertex [TOTLEN+1];
16 void init()
17
   {
       vertex[0] = Vertex(0);
18
19
        size=1;
20
21
   void add(Vertex *pos,int cha)
22
23
        vertex[size] = Vertex(0);
24
       pos -> next [cha] = & vertex [size++];
25
   }
26
   void add(vector<int> s)
27
   {
28
        int l=s.size();
29
        Vertex *pos=&vertex[0];
        for (int i=0; i<1; i++)
30
31
        {
32
            if (pos->next[s[i]] == NULL)
33
                 add(pos,s[i]);
34
            pos=pos->next[s[i]];
       }
35
36
   }
   void bfs()
37
38
   {
39
       queue < Vertex *> que;
40
       Vertex *u=&vertex[0];
        for (int i=0; i<CHAR; i++)</pre>
41
42
            if (u->next[i]!=NULL)
43
            {
44
                que.push(u->next[i]);
45
                u->next[i]->fail=u;
```

```
}
46
47
            else
                 u->next[i]=u;
48
        u->fail=NULL;
49
        while (!que.empty())
50
51
52
            u=que.front();
53
            que.pop();
54
            for (int i=0; i < CHAR; i++)
                 if (u->next[i]!=NULL)
55
56
                 {
57
                     que.push(u->next[i]);
                     u->next[i]->fail=u->fail->next[i];
58
59
                 }
60
                 else
61
                     u->next[i]=u->fail->next[i];
62
       }
63 | }
        非指针
   3.1.2
1
   struct Trie
2
   {
3
        int next[50][10],fail[50];
4
        bool end[50];
5
        int L,root;
6
7
        int newNode()
8
        {
9
            for (int i = 0; i < 10; i++)
10
                 next[L][i] = -1;
11
            end[L] = false;
12
            return L++;
13
        }
14
15
        void Init()
16
        {
17
            L = 0;
18
            root = newNode();
        }
19
20
21
        void Insert(char s[])
22
        {
23
            int now = root;
24
            for (int i = 0; s[i] != 0; i++)
25
            {
                 if (next[now][s[i]-'0'] == -1)
26
27
                     next[now][s[i]-'0'] = newNode();
28
                 now = next[now][s[i]-'0'];
29
30
            end[now] = true;
31
        }
```

```
32
33
       void Build()
34
35
            queue < int > Q;
36
            for (int i = 0; i < 10; i++)
                if (next[root][i] == -1)
37
38
                    next[root][i] = root;
39
                else
40
                {
41
                     fail[next[root][i]] = root;
42
                    Q.push(next[root][i]);
43
                }
44
            while (!Q.empty())
45
46
                int now = Q.front();
47
                Q.pop();
48
                end[now] |= end[fail[now]];
49
                for (int i = 0; i < 10; i++)
                     if (next[now][i] == -1)
50
51
                         next[now][i] = next[fail[now]][i];
52
                    else
53
                     {
54
                         fail[next[now][i]] = next[fail[now]][i];
55
                         Q.push(next[now][i]);
                    }
56
57
            }
58
       }
59 | };
   3.2
        后缀数组
   3.2.1
        DC3
   所有下标都是0 \text{ n-1},height[0]无意义。
 1 //所有相关数组都要开三倍
   const int maxn = 300010;
  \# define F(x) ((x)/3+((x)%3==1?0:tb))
  # define G(x) ((x) < tb?(x) *3+1:((x)-tb) *3+2)
   int wa[maxn * 3], wb[maxn * 3], wv[maxn * 3], ws[maxn * 3];
6
   int c0(int *r, int a, int b)
7
   {
8
       return r[a] == r[b] && r[a + 1] == r[b + 1] && r[a + 2] == r[b]
          + 2];
9
10
   int c12(int k, int *r, int a, int b)
11
   {
12
       if (k == 2) return r[a] < r[b] || r[a] == r[b] && c12(1, r, a +
           1, b + 1);
13
       else return r[a] < r[b] \mid | r[a] == r[b] && wv[a + 1] < wv[b +
          1];
14
15 | void sort(int *r, int *a, int *b, int n, int m)
```

```
16 | {
17
       int i;
18
       for (i = 0; i < n; i++) wv[i] = r[a[i]];
19
       for (i = 0; i < m; i++) ws[i] = 0;
20
       for (i = 0; i < n; i++) ws [wv[i]]++;
       for (i = 1; i < m; i++) ws[i] += ws[i - 1];
21
22
       for (i = n - 1; i \ge 0; i--) b[--ws[wv[i]]] = a[i];
23
       return;
24
   }
25
   void dc3(int *r, int *sa, int n, int m)
26
   {
27
       int i, j, *rn = r + n, *san = sa + n, ta = 0, tb = (n + 1) / 3,
           tbc = 0, p;
28
       r[n] = r[n + 1] = 0;
29
       for (i = 0; i < n; i++) if (i % 3 != 0) wa [tbc++] = i;
30
       sort(r + 2, wa, wb, tbc, m);
31
       sort(r + 1, wb, wa, tbc, m);
32
       sort(r, wa, wb, tbc, m);
       for (p = 1, rn[F(wb[0])] = 0, i = 1; i < tbc; i++)
33
           rn[F(wb[i])] = c0(r, wb[i - 1], wb[i]) ? p - 1 : p++;
34
35
       if (p < tbc) dc3(rn, san, tbc, p);
36
       else for (i = 0; i < tbc; i++) san[rn[i]] = i;
37
       for (i = 0; i < tbc; i++) if (san[i] < tb) wb[ta++] = san[i] *
          3;
       if (n \% 3 == 1) wb[ta++] = n - 1;
38
       sort(r, wb, wa, ta, m);
39
       for (i = 0; i < tbc; i++) wv[wb[i] = G(san[i])] = i;
40
41
       for (i = 0, j = 0, p = 0; i < ta && j < tbc; p++)
42
           sa[p] = c12(wb[j] \% 3, r, wa[i], wb[j]) ? wa[i++] : wb[j]
              ++];
43
       for (; i < ta; p++) sa[p] = wa[i++];
44
       for (; j < tbc; p++) sa[p] = wb[j++];
45
   }
   //str和sa也要三倍
46
47
   void da(int str[], int sa[], int rank[], int height[], int n, int m
   {
48
       for (int i = n; i < n * 3; i++)
49
50
           str[i] = 0;
       dc3 (str , sa , n + 1 , m);
51
52
       int i, j, k;
       for (i = 0; i < n; i++)
53
54
       {
55
           sa[i] = sa[i + 1];
           rank[sa[i]] = i;
56
57
       for (i = 0, j = 0, k = 0; i < n; height[rank[i ++]] = k)
58
59
           if (rank[i] > 0)
60
                for (k ? k-- : 0 , j = sa[rank[i] - 1]; i + k < n && j
                  + k < n &&
61
                        str[i + k] == str[j + k]; k ++);
```

62 | }

3.2.2 DA

这份似乎就没啥要注意的了。

```
const int maxn = 200010;
   int wx[maxn], wy[maxn], *x, *y, wss[maxn], wv[maxn];
4
   bool cmp(int *r,int n,int a,int b,int 1)
5
        return a+1 < n \&\& b+1 < n \&\& r[a] == r[b] \&\&r[a+1] == r[b+1];
6
7
8
   void da(int str[],int sa[],int rank[],int height[],int n,int m)
9
   {
10
        int *s = str;
11
        int *x=wx, *y=wy, *t, p;
12
        int i, j;
13
        for(i=0; i<m; i++)wss[i]=0;
14
        for (i=0; i < n; i++) wss [x[i]=s[i]]++;
15
        for (i=1; i < m; i++) wss [i]+= wss [i-1];
16
        for(i=n-1; i>=0; i--)sa[--wss[x[i]]]=i;
17
        for (j=1, p=1; p < n && j < n; j*=2, m=p)
18
19
            for (i=n-j, p=0; i < n; i++)y[p++]=i;
20
            for (i=0; i< n; i++) if (sa[i]-j>=0) y [p++]=sa[i]-j;
21
            for (i=0; i< n; i++) wv[i] = x[y[i]];
22
            for(i=0; i<m; i++)wss[i]=0;
23
            for(i=0; i<n; i++)wss[wv[i]]++;
24
            for(i=1; i<m; i++)wss[i]+=wss[i-1];
25
            for(i=n-1; i>=0; i--)sa[--wss[wv[i]]]=y[i];
            for(t=x,x=y,y=t,p=1,i=1,x[sa[0]]=0; i<n; i++)
26
                x[sa[i]] = cmp(y,n,sa[i-1],sa[i],j)?p-1:p++;
27
28
        }
29
        for(int i=0; i<n; i++) rank[sa[i]]=i;
        for(int i=0, j=0, k=0; i<n; height[rank[i++]]=k)
30
31
            if (rank[i] > 0)
32
                 for(k?k--:0, j=sa[rank[i]-1]; i+k < n && j+k < n && str[
                    i+k] = str[j+k]; k++);
33 | }
```

3.3 后缀三兄弟

```
1 #include <cstdio>
2 #include <cstring>
3 #include <algorithm>
4 using namespace std;
5 const int CHAR = 26;
6 const int MAXN = 100000;
7 struct SAM_Node
8 {
```

```
9
        SAM_Node *fa,*next[CHAR];
10
        int len;
11
        int id, pos;
12
        SAM_Node() {}
        SAM_Node(int _len)
13
14
15
            fa = 0;
16
            len = _len;
17
            memset(next,0,sizeof(next));
        }
18
19
   };
20
   SAM_Node SAM_node[MAXN * 2], *SAM_root, *SAM_last;
21
   int SAM_size;
22
   SAM_Node *newSAM_Node(int len)
   {
23
24
        SAM_node[SAM_size] = SAM_Node(len);
25
        SAM_node[SAM_size].id=SAM_size;
26
        return &SAM_node[SAM_size++];
27 | }
28
  |SAM_Node *newSAM_Node(SAM_Node *p)
29
   {
30
        SAM_node[SAM_size] = *p;
31
        SAM_node[SAM_size].id=SAM_size;
32
        return &SAM_node[SAM_size++];
33
34 | void SAM_init()
35
   {
36
        SAM_size = 0;
37
        SAM_root = SAM_last = newSAM_Node(0);
        SAM_node[0].pos=0;
38
39
40
   void SAM_add(int x,int len)
41
42
        SAM_Node *p = SAM_last, *np = newSAM_Node(p->len + 1);
43
        np->pos=len;
44
        SAM_last = np;
45
        for (; p \&\& !p->next[x]; p = p->fa)
            p - next[x] = np;
46
47
        if (!p)
48
        {
49
            np->fa = SAM_root;
50
            return ;
        }
51
52
        SAM_Node *q = p->next[x];
        if (q\rightarrow len == p\rightarrow len + 1)
53
54
        {
55
            np \rightarrow fa = q;
56
            return ;
57
        }
58
        SAM_Node *nq = newSAM_Node(q);
59
        nq \rightarrow len = p \rightarrow len + 1;
```

```
60
                         q \rightarrow fa = nq;
  61
                         np \rightarrow fa = nq;
  62
                         for (; p && p->next[x] == q; p = p->fa)
  63
                                      p - next[x] = nq;
  64
  65
            void SAM_build(char *s)
  66
  67
                         SAM_init();
  68
                         int l = strlen(s);
  69
                         for (int i = 0; i < 1; i++)
  70
                                       SAM_add(s[i] - 'a', i+1);
  71
           }
  72
  73
            SAM_Node * SAM_add(SAM_Node *p, int x, int len)
  74
            {
  75
                         SAM_Node *np = newSAM_Node(p->len + 1);
                         np \rightarrow pos = len;
  76
  77
                         SAM_last = np;
  78
                         for (; p \&\& !p - next[x]; p = p - fa)
  79
                                      p - next[x] = np;
                         if (!p)
  80
  81
                         {
  82
                                      np->fa = SAM_root;
  83
                                      return np;
  84
  85
                         SAM_Node *q = p->next[x];
  86
                         if (q\rightarrow len == p\rightarrow len + 1)
  87
                         {
  88
                                      np \rightarrow fa = q;
  89
                                      return np;
  90
  91
                         SAM_Node *nq = newSAM_Node(q);
  92
                         nq \rightarrow len = p \rightarrow len + 1;
  93
                         q \rightarrow fa = nq;
  94
                         np \rightarrow fa = nq;
  95
                         for (; p \&\& p - next[x] == q; p = p - fa)
  96
                                      p \rightarrow next[x] = nq;
  97
                         return np;
  98
            void SAM_build(char *s)//多串建立 注意SAM_init()的调用
  99
100
           {
                          int l = strlen(s);
101
102
                         SAM_Node *p = SAM_root;
                         for (int i = 0; i < 1; i++)
103
104
105
                                       if (!p-\next[s[i] - 'a'] \mid | !(p-\next[s[i] - 'a'] - \next[s[i] 
                                                   + 1))
106
                                                    p=SAM_add(p,s[i] - 'a', i + 1);
107
                                       else
108
                                                    p = p->next[s[i] - 'a'];
109
                         }
```

```
110
   }
111
112
    struct ST_Node
113
    {
114
        ST_Node *next[CHAR], *fa;
115
        int len, pos;
    }ST_node[MAXN*2],*ST_root;
116
117
    int Sufpos[MAXN];
118
    void ST_add(int u,int v,int chr,int len)
119
    {
120
        ST_node[u].next[chr]=&ST_node[v];
121
        ST_node[v].len=len;
122
    }
    void init(int n)
123
124
    {
125
        for (int i=0; i < n; i++)
126
        {
127
             ST_node[i].pos=-1;
128
             ST_node[i].fa=0;
129
             memset(ST_node[i].next,0,sizeof(ST_node[i].next));
        }
130
131
        ST_node[0].pos=0;
132
        ST_root=&ST_node[0];
133
134
    void ST_build(char *s)
135
136
        int n=strlen(s);
137
        reverse(s,s+n);
138
        SAM_build(s);
139
        init(SAM_size);
140
        for (int i=1;i<SAM_size;i++)</pre>
141
        {
142
             ST_add(SAM_node[i].fa->id,SAM_node[i].id,s[SAM_node[i].pos-
                SAM_node[i].fa->len-1]-'a',SAM_node[i].len-SAM_node[i].
                fa->len);
143
             if (SAM_node[i].pos==SAM_node[i].len)
144
             {
145
                 Sufpos [n-SAM_node[i].pos+1]=i;
146
                 ST_node[i].pos=n-SAM_node[i].pos+1;
147
             }
        }
148
149
    }
150
151
    int rank[MAXN],sa[MAXN+1];
152
    int height[MAXN];
153
    int L;
154
    void ST_dfs(ST_Node *p)
155
156
        if (p->pos!=-1)
157
             sa[L++]=p->pos;
158
        for (int i=0;i<CHAR;i++)
```

```
159
             if (p->next[i])
160
                 ST_dfs(p->next[i]);
161
    }
162
    char s[MAXN+1];
    int main()
163
164
        gets(s);
165
166
        ST_build(s);
167
        L=0;
168
        ST_dfs(ST_root);
169
        int n=strlen(s);
        for (int i=0; i<n; i++)
170
             sa[i] = sa[i+1] - 1;
171
172
        for (int i=0; i<n; i++)
173
             rank[sa[i]]=i;
174
        reverse(s,s+n);
175
        for (int i=0, j=0, k=0; i<n; height[rank[i++]]=k)
176
             if (rank[i])
177
                 for (k?k--:0, j=sa[rank[i]-1]; s[i+k]==s[j+k]; k++);
178 | }
          例题
    3.3.1
   #include <iostream>
 2 | #include <algorithm>
   #include <cstdio>
 3
 4 | #include <cstring>
   using namespace std;
 6
 7
    const int CHAR = 26;
 8
    const int MAXN = 100000;
 9
10
    struct SAM_Node
    {
11
12
        SAM_Node *fa,*next[CHAR];
13
        int len;
14
        int id;
15
        int mat[9];
        SAM_Node() {}
16
        SAM_Node(int _len)
17
18
        {
19
             fa = 0;
20
             len = _len;
21
             memset(mat,0,sizeof(mat));
22
             memset(next,0,sizeof(next));
23
        }
24
   };
25
    SAM_Node SAM_node[MAXN*2],*SAM_root,*SAM_last;
26
   int SAM_size;
27
   SAM_Node *newSAM_Node(int len)
28
    {
29
        SAM_node[SAM_size] = SAM_Node(len);
```

```
30
        SAM_node[SAM_size].id = SAM_size;
31
        return &SAM_node[SAM_size++];
32
33
   SAM_Node *newSAM_Node(SAM_Node *p)
34 | \{
35
        SAM_node[SAM_size] = *p;
        SAM_node[SAM_size].id = SAM_size;
36
37
        return &SAM_node[SAM_size++];
38
   }
39
   void SAM_init()
40
   {
41
        SAM_size = 0;
42
        SAM_root = SAM_last = newSAM_Node(0);
43
44
   void SAM_add(int x,int len)
45
   {
46
        SAM_Node *p = SAM_last,*np = newSAM_Node(p->len+1);
47
        SAM_last = np;
48
        for (; p&&!p->next[x]; p=p->fa)
49
            p - next[x] = np;
        if (!p)
50
51
        {
52
            np->fa = SAM_root;
53
            return;
54
55
        SAM_Node *q = p->next[x];
        if (q->len == p->len+1)
56
57
        {
58
            np->fa = q;
59
            return;
60
        }
        SAM_Node *nq = newSAM_Node(q);
61
62
        nq \rightarrow len = p \rightarrow len + 1;
63
        q \rightarrow fa = nq;
64
        np \rightarrow fa = nq;
        for (; p\&\&p->next[x] == q; p = p->fa)
65
66
            p \rightarrow next[x] = nq;
67
68
   int getid(char ch)
69
   {
70
        return ch-'a';
71
72
   void SAM_build(char *s)
73
   {
74
        SAM_init();
        int l = strlen(s);
75
        for (int i = 0; i < 1; i++)
76
            SAM_add(getid(s[i]),i+1);
77
78
79
   char s[10][MAXN+1];
80 | int ans;
```

```
81 | int head [MAXN*2];
82
    struct Edge
83
84
        int to, next;
85
   } edge[MAXN*2];
    int M;
86
87
    int n;
88
    void add_edge(int u,int v)
89
90
        edge[M].to=v;
91
        edge[M].next=head[u];
92
        head[u]=M++;
93
    }
    void dfs(int u)
94
95
96
        for (int i=head[u]; i!=-1; i=edge[i].next)
97
98
             int v=edge[i].to;
99
             dfs(v);
100
             for (int j=0; j< n-1; j++)
                 SAM_node[u].mat[j]=max(SAM_node[v].mat[j],SAM_node[u].
101
                    mat[j]);
        }
102
103
        int tmp=SAM_node[u].len;
        for (int i=0; i< n-1; i++)
104
105
             tmp=min(tmp,SAM_node[u].mat[i]);
106
        ans=max(ans,tmp);
107
108
    int main()
109
    {
110
111
        while (scanf("%s",s[n])!=EOF)
112
             n++;
113
        int L=strlen(s[0]);
114
        ans=M=0;
115
        SAM_build(s[0]);
116
        for (int j=1; j < n; j++)
117
        {
118
             int l=strlen(s[j]),len=0;
             SAM_Node *p=SAM_root;
119
             for (int i=0; i<1; i++)
120
121
122
                 if (p->next[getid(s[j][i])])
123
                 {
124
                      p=p->next[getid(s[j][i])];
125
                      p->mat[j-1]=max(p->mat[j-1],++len);
                 }
126
127
                 else
128
                 {
129
                      while (p && !p->next[getid(s[j][i])])
130
                          p=p->fa;
```

```
131
                       if (!p)
132
                       {
133
                           p=SAM_root;
134
                           len=0;
135
                      }
136
                       else
                       {
137
138
                           len=p->len+1;
139
                           p=p->next[getid(s[j][i])];
140
141
                      p\rightarrow mat[j-1]=max(p\rightarrow mat[j-1],len);
142
                  }
             }
143
         }
144
145
        memset(head, -1,4*SAM_size);
146
         for (int i=1; i<SAM_size; i++)</pre>
147
             add_edge(SAM_node[i].fa->id,i);
         dfs(0);
148
         printf("%d\n",ans);
149
150
         return 0;
151 | }
      LCS2
   #include <iostream>
    #include <algorithm>
 3
   #include <cstdio>
   #include <cstring>
 4
    using namespace std;
 6
 7
    const int CHAR = 26;
    const int MAXN = 100000;
 8
 9
10
    struct SAM_Node
11
12
         SAM_Node *fa,*next[CHAR];
13
         int len;
14
         int id;
15
         int mat[9];
16
         SAM_Node() {}
17
         SAM_Node(int _len)
18
19
             fa = 0;
             len = _len;
20
21
             memset(mat,0,sizeof(mat));
22
             memset(next,0,sizeof(next));
23
        }
24
    };
   |SAM_Node SAM_node[MAXN*2],*SAM_root,*SAM_last;
26 | int SAM_size;
27
    SAM_Node *newSAM_Node(int len)
28 | {
```

```
29
        SAM_node[SAM_size] = SAM_Node(len);
30
        SAM_node[SAM_size].id = SAM_size;
        return &SAM_node[SAM_size++];
31
32
33 | SAM_Node *newSAM_Node(SAM_Node *p)
34
35
        SAM_node[SAM_size] = *p;
36
        SAM_node[SAM_size].id = SAM_size;
37
        return &SAM_node[SAM_size++];
38
39
   void SAM_init()
40 | {
41
        SAM_size = 0;
42
        SAM_root = SAM_last = newSAM_Node(0);
43
   }
44
   void SAM_add(int x,int len)
45
   {
46
        SAM_Node *p = SAM_last,*np = newSAM_Node(p->len+1);
47
        SAM_last = np;
48
        for (; p&&!p->next[x]; p=p->fa)
49
            p->next[x] = np;
50
        if (!p)
51
        {
52
            np->fa = SAM_root;
53
            return;
        }
54
55
        SAM_Node *q = p->next[x];
56
        if (q->len == p->len+1)
        {
57
58
            np \rightarrow fa = q;
59
            return;
        }
60
61
        SAM_Node *nq = newSAM_Node(q);
62
        nq \rightarrow len = p \rightarrow len + 1;
63
        q \rightarrow fa = nq;
64
        np \rightarrow fa = nq;
65
        for (; p\&\&p->next[x] == q; p = p->fa)
66
            p - next[x] = nq;
67
68
   int getid(char ch)
69
   {
70
        return ch-'a';
71
   }
72
   void SAM_build(char *s)
73
   {
74
        SAM_init();
75
        int l = strlen(s);
        for (int i = 0; i < 1; i++)
76
77
            SAM_add(getid(s[i]),i+1);
78
79 \mid char s[MAXN+1];
```

```
80
   int ans;
    int head[MAXN*2];
81
82
   struct Edge
83
    {
84
        int to, next;
85
   } edge[MAXN*2];
    int M;
86
87
    int n;
88
    void add_edge(int u,int v)
89
    {
90
        edge[M].to=v;
91
        edge[M].next=head[u];
92
        head [u] = M++;
93
94
    void dfs(int u)
95
    {
96
        for (int i=head[u]; i!=-1; i=edge[i].next)
97
        {
98
             int v=edge[i].to;
99
             /*for (int j=0; j<n; j++)
                 SAM_node[v].mat[j]=max(SAM_node[v].mat[j],SAM_node[u].
100
                    mat[j]);*/
101
             dfs(v);
102
             for (int j=0; j < n; j++)
                 SAM_node[u].mat[j]=max(SAM_node[v].mat[j],SAM_node[u].
103
                    mat[j]);
104
        }
105
        int tmp=SAM_node[u].len;
106
        for (int i=0; i<n; i++)
107
             tmp=min(tmp,SAM_node[u].mat[i]);
108
        ans=max(ans,tmp);
109
110
    int main()
111
112
        //freopen("in.txt","r",stdin);
113
        //freopen("out.txt","w",stdout);
114
        n=0;
115
        gets(s);
116
        SAM_build(s);
117
        while (gets(s))
118
        {
119
             int l=strlen(s),len=0;
120
             SAM_Node *p=SAM_root;
121
             for (int i=0; i<1; i++)
122
123
                 if (p->next[getid(s[i])])
                 {
124
125
                      p=p->next[getid(s[i])];
126
                      p->mat[n]=max(p->mat[n],++len);
127
                 }
128
                 else
```

```
129
                  {
130
                       while (p && !p->next[getid(s[i])])
131
                           p=p->fa;
132
                       if (!p)
133
                       {
134
                           p=SAM_root;
135
                           len=0;
                      }
136
137
                       else
138
                       {
139
                           len=p->len+1;
140
                           p=p->next[getid(s[i])];
141
142
                      p->mat[n]=max(p->mat[n],len);
143
                  }
144
                  //printf("%d %d %d\n",i,len,p->id);
145
             }
146
             n++;
         }
147
        memset(head, -1,4*SAM_size);
148
         for (int i=1; i<SAM_size; i++)</pre>
149
150
             add_edge(SAM_node[i].fa->id,i);
151
         dfs(0);
        printf("%d\n",ans);
152
153
         return 0;
154 | }
```

3.4 KMP

求A[0..i]的一个后缀最多能匹配B的前缀多长。 先对B进行自匹配然后与A匹配。 KMP[i]就是对应答案,p[i]+1是B[0..i]的一个后缀最多能匹配B的前缀多长。

```
1 // 自匹配过程
  int j;
  |p[0] = j = -1;
  for ( int i = 1; i < lb; i++)
4
5
6
       while (j \ge 0 \&\& b[j + 1] != b[i]) j = p[j];
7
       if (b[j + 1] == b[i]) j ++;
8
       p[i] = j;
9
  //下面是匹配过程
10
   j = -1;
11
12
  for ( int i = 0; i < la; i++)
13
   {
14
       while (j \ge 0 \&\& b[j + 1] != a[i]) j = p[j];
15
       if (b[j + 1] == a[i]) j ++;
       KMP[i] = j + 1;
16
17 | }
```

3.5 e-KMP

求A[i..len-1]和B的最长公共前缀有多长。 先对B进行自匹配然后与A匹配。 eKMP[i]就是对应答案。p[i]是B[i..len-1]和B的最长公共前缀有多长。

```
1//自匹配过程
2
   int j = 0;
   while (j < lb \&\& b[j] == b[j + 1])
4
       j++;
   p[0] = lb, p[1] = j;
   int k = 1;
7
   for (int i = 2; i < lb; i++)
8
9
       int Len = k + p[k] - 1, L = p[i - k];
10
       if (L < Len - i + 1)
11
            p[i] = L;
12
       else
13
       {
14
            j = max(0, Len - i + 1);
            while (i + j < lb \&\& b[i + j] == b[j])
15
16
17
            p[i] = j, k = i;
18
       }
19
20
   //下面是匹配过程
21
   j = 0;
22
   while (j < la && j < lb && a[j] == b[j])
23
       j++;
   eKMP[0] = j;
24
25
   k = 0;
26
   for (int i = 1; i < la; i++)
27
28
       int Len = k + eKMP[k] - 1, L = p[i - k];
29
       if (L < Len - i + 1)
30
            eKMP[i] = L;
31
       else
32
       {
33
            j = max(0, Len - i + 1);
34
            while (i + j < la && j < lb && a[i + j] == b[j])
35
                j++;
36
            eKMP[i] = j, k = i;
37
       }
38 | }
```

3.6 *Manacher

待整理

```
1 | char s[1000],a[3000];
2 | int p[3000],len,l,pnow,pid,res,resid;
3 |
4 | int main()
5 | {
```

```
while (scanf("%s",s) != EOF)
6
7
       {
8
            len = strlen(s);
9
            1 = 0;
            a[1++] = '.';
10
            a[1++] = ',';
11
12
            for (int i = 0; i < len; i++)
13
14
                a[1++] = s[i];
15
                a[1++] = ',';
16
17
            pnow = 0;
18
            res = 0;
19
            for (int i = 1; i < 1; i++)
20
            {
21
                if (pnow > i)
22
                     p[i] = min(p[2*pid-i],pnow-i);
23
                 else
24
                     p[i] = 1;
25
                for (;a[i-p[i]] == a[i+p[i]];p[i]++);
                if (i+p[i] > pnow)
26
27
                {
28
                     pnow = i+p[i];
29
                     pid = i;
30
                }
31
                if (p[i] > res)
32
                {
33
                     res = p[i];
34
                     resid = i;
35
                }
36
            for (int i = resid-res+2; i < resid+res-1; i += 2)
37
                printf("%c",a[i]);
38
39
            printf("\n");
40
       }
41
       return 0;
42 }
        *字符串最小表示法
1 | int Gao(char a[], int len)
2
   {
3
     int i = 0, j = 1, k = 0;
4
     while (i < len && j < len && k < len)
```

int cmp = a[(j+k)%len]-a[(i+k)%len];

if (cmp == 0)

if (cmp > 0)

k++;

else

{

5

6 7

8

9

10

11

```
12
            j += k+1;
13
          else
14
            i += k+1;
          if (i == j) j++;
15
16
          k = 0;
17
       }
18
19
     return min(i,j);
20 | }
        带*通配符的匹配
   3.8
1 | #include <iostream >
2 | #include <algorithm>
3 | #include <cstdio>
4 | #include <cstring>
  using namespace std;
5
6
7
   char a[110], b[110], sp[110][110], tot, place[110];
8
   int n,la,lb,ll;
9
10
   bool check(int id,int pos)
11
   {
12
       for (int i = 0; sp[id][i] != 0; i++)
13
            if (b[pos+i] != sp[id][i])
14
                return false;
15
       return true;
16
   }
17
18
   bool check()
19
   {
20
       lb = strlen(b);
21
       int pre = 0;
22
       for (int i = 0; i < tot; i++)
23
       {
24
            bool find = false;
            for (int j = pre; j < lb; j++)
25
26
                if (check(i,j) == true)
27
                {
28
                     place[i] = j;
29
                     pre = place[i]+1;
30
                     find = true;
31
                     break;
32
33
            if (find == false)
                                 return false;
34
       }
       if (a[0] != '*')
35
36
            if (place[0] != 0)
37
                return false;
38
       if (a[la-1] != '*')
39
            if (check(tot-1,lb-ll) == false)
40
                return false;
```

```
41
        return true;
42
   }
43
44
   int main()
45
46
        while (scanf("%s",a) != EOF)
47
        {
48
            tot = 0;
49
            for (int i = 0;a[i] != 0;i++)
                 if (a[i] != '*')
50
51
                 {
52
                     int j;
53
                     for (j = i; a[j] != 0 \&\& a[j] != '*'; j++)
54
                          sp[tot][j-i] = a[j];
55
                     sp[tot++][j-i] = 0;
56
                     i = j;
                 }
57
58
            la = strlen(a);
            11 = strlen(sp[tot-1]);
59
            scanf("%d",&n);
60
            for (int i = 0; i < n; i++)
61
62
            {
63
                 scanf("%s",b);
                 if (check() == true)
64
65
                     puts(b);
            }
66
        }
67
68
        return 0;
69
   }
70
   /*
71
   Sample Input 1
72
   *.*
73
74 | main.c
75
   a.out
76 | readme
   yacc
77
78
79
   Sample Input 2
80
   *a*a*a
81
   4
82
   aaa
83 aaaaa
84
   aaaaax
85 abababa
86
87
  Sample Output 1
88
   main.c
89
   a.out
90
91 | Sample Output 2
```

- 92 | aaa
- 93 aaaaa
- 94 abababa
- 95 */

4 数学

4.1 扩展GCD

```
求ax+by=gcd(a,b)的一组解
   long long ex_gcd(long long a,long long b,long long &x,long long &y)
2
   {
3
       if (b)
4
       {
5
            long long ret = ex_gcd(b,a%b,x,y),tmp = x;
6
7
            y = tmp-(a/b)*y;
8
            return ret;
9
       }
10
       else
11
       {
12
            x = 1;
13
            y = 0;
14
            return a;
15
       }
16 }
```

4.2 模线性方程组

```
1 //有更新
2 | int m[10],a[10];//模数m 余数a
   bool solve(int &mO, int &aO, int m, int a) // 模线性方程组
3
4
   {
5
        int y,x;
6
        int g=ex_gcd(m0,m,x,y);
7
        if (abs(a-a0)%g) return 0;
8
        x*=(a-a0)/g;
9
        x\%=m/g;
10
        a0 = (x*m0+a0);
11
        m0*=m/g;
12
        a0\%=m0;
13
        if (a0 < 0) a0 + = m0;
14
        return 1;
15
   }
16
   int MLES()
17
   {
18
        bool flag=1;
19
        int m0=1, a0=0;
20
        for (int i=0; i<n; i++)
21
            if (!solve(m0,a0,m[i],a[i]))
22
            {
23
                 flag=0;
24
                 break;
25
            }
26
        if (flag)
```

```
27 | return a0;
28 | else
29 | return -1;
30 |}
```

4.3 矩阵

乘法的时候将B数组转置一下然后 $C[i][j] = \sum A[i][k] \times B[j][k]$ 会有奇效。

```
struct Matrix
2
   {
3
       int a [52] [52];
4
       Matrix operator * (const Matrix &b)const
5
       {
6
            Matrix res;
7
            for (int i = 0; i < 52; i++)
                for (int j = 0; j < 52; j++)
8
9
                {
10
                     res.a[i][j] = 0;
11
                     for (int k = 0; k < 52; k++)
12
                         res.a[i][j] += a[i][k] * b.a[k][j];
13
                }
14
            return res;
15
       }
16
       Matrix operator ^ (int y)const
17
18
            Matrix res, x;
19
            for (int i = 0; i < 52; i++)
20
21
                for (int j = 0; j < 52; j++)
22
                     res.a[i][j] = 0, x.a[i][j] = a[i][j];
23
                res.a[i][i] = 1;
24
            }
25
            for (; y; y >>= 1, x = x * x)
26
                if (y & 1)
27
                     res = res * x;
28
            return res;
29
       }
30 | };
```

4.4 康拓展开

```
1 const int PermSize = 12;
  int factory[PermSize] = {1, 1, 2, 6, 24, 120, 720, 5040, 40320,
     362880, 3628800, 39916800};
3
  int Cantor(int a[])
4
  {
5
      int i, j, counted;
6
      int result = 0;
7
      for (i = 0; i < PermSize; ++i)
8
      {
9
           counted = 0;
```

```
10
            for (j = i + 1; j < PermSize; ++j)
11
                if (a[i] > a[j])
12
                     ++counted;
13
            result = result + counted * factory[PermSize - i - 1];
       }
14
15
       return result;
16
17
18
   bool h[13];
19
20
   void UnCantor(int x, int res[])
21
22
       int i, j, l, t;
23
       for (i = 1; i \le 12; i++)
24
            h[i] = false;
25
       for (i = 1; i \le 12; i++)
26
27
            t = x / factory[12 - i];
28
            x = t * factory[12 - i];
            for (j = 1, l = 0; l \le t; j++)
29
30
                if (!h[j])1++;
31
            j--;
32
            h[j] = true;
33
            res[i - 1] = j;
34
       }
35 | }
        FFT
   4.5
   const double PI= acos(-1.0);
 2
   struct vir
3
   {
     double re,im; //实部和虚部
4
     vir(double a=0, double b=0)
5
6
7
       re=a;
8
       im=b;
9
     }
10
     vir operator +(const vir &b)
11
     {return vir(re+b.re,im+b.im);}
12
     vir operator -(const vir &b)
     {return vir(re-b.re, im-b.im);}
13
14
     vir operator *(const vir &b)
15
     {return vir(re*b.re-im*b.im , re*b.im+im*b.re);}
16
   };
17
   vir x1[200005], x2[200005];
18
   void change(vir *x,int len,int loglen)
19
20
     int i,j,k,t;
21
     for(i=0;i<len;i++)
22
     {
23
       t=i;
```

```
24
        for (j=k=0; j<loglen; j++,t>>=1)
25
          k = (k << 1) | (t & 1);
        if(k<i)
26
27
        {
28
        //
             printf("%d %d\n",k,i);
29
          vir wt=x[k];
          x[k]=x[i];
30
31
          x[i]=wt;
32
        }
33
      }
34
35
   void fft(vir *x,int len,int loglen)
36
   {
37
      int i,j,t,s,e;
38
      change(x,len,loglen);
39
      t=1;
40
      for (i=0; i<loglen; i++, t<<=1)
41
      {
42
        s=0;
43
        e=s+t;
        while(s<len)
44
45
46
          vir a,b,wo(cos(PI/t),sin(PI/t)),wn(1,0);
47
          for(j=s;j<s+t;j++)
48
          {
49
             a=x[j];
             b=x[j+t]*wn;
50
51
             x[j]=a+b;
52
             x[j+t]=a-b;
53
             wn = wn * wo;
          }
54
55
          s=e+t;
56
          e=s+t;
57
        }
      }
58
59
60
   void dit_fft(vir *x,int len,int loglen)
61
   {
62
      int i,j,s,e,t=1<<loglen;</pre>
63
      for(i=0;i<loglen;i++)
64
      {
65
        t >> = 1;
66
        s=0;
67
        e=s+t;
68
        while(s<len)
69
        {
70
          vir a,b,wn(1,0),wo(cos(PI/t),-sin(PI/t));
71
          for(j=s;j<s+t;j++)
72
73
             a=x[j]+x[j+t];
74
             b = (x[j] - x[j+t]) * wn;
```

```
x[j]=a;
75
76
             x[j+t]=b;
77
             wn = wn * wo;
           }
78
79
           s=e+t;
80
           e=s+t;
         }
81
82
      }
83
      change(x,len,loglen);
      for(i=0;i<len;i++)
84
85
         x[i].re/=len;
86
    }
87
    int main()
88
    {
89
      char a[100005],b[100005];
90
      int i,len1,len2,len,loglen;
91
      int t, over;
92
      while (scanf("%s%s",a,b)!=EOF)
93
94
         len1=strlen(a) <<1;</pre>
         len2=strlen(b) <<1;</pre>
95
96
         len=1;loglen=0;
97
         while(len<len1)
98
         {
99
           len < <=1;
                       loglen++;
         }
100
101
         while(len<len2)
102
         {
103
           len < <=1;
                       loglen++;
104
         }
105
         for(i=0;a[i];i++)
106
         {
107
           x1[i].re=a[i]-'0';
108
           x1[i].im=0;
         }
109
110
         for(;i<len;i++)
111
           x1[i].re=x1[i].im=0;
112
         for(i=0;b[i];i++)
113
         {
114
           x2[i].re=b[i]-'0';
115
           x2[i].im=0;
116
         for(;i<len;i++)
117
118
           x2[i].re=x2[i].im=0;
119
         fft(x1,len,loglen);
120
         fft(x2,len,loglen);
121
         for(i=0;i<len;i++)
122
           x1[i] = x1[i]*x2[i];
123
         dit_fft(x1,len,loglen);
124
         for (i=(len1+len2)/2-2, over=len=0; i>=0; i--)
125
         {
```

```
126
           t=(int)(x1[i].re+over+0.5);
127
           a[len++] = t%10;
           over = t/10;
128
129
         }
        while(over)
130
131
         {
132
           a[len++]=over%10;
133
           over/=10;
134
         }
         for(len--;len>=0&&!a[len];len--);
135
           if(len<0)
136
137
           putchar('0');
           else
138
             for(;len>=0;len--)
139
140
               putchar(a[len]+'0');
141
         putchar('\n');
      }
142
143
      return 0;
144 | }
```

4.6 爬山法计算器

注意灵活运用。

双目运算符在calc()中,左结合单目运算符在P()中,右结合单目运算符在 $calc_exp$ 中。(但是还没遇到过。。)

```
#include <iostream>
  #include <cstdio>
 3 | #include <cstring>
   #include <algorithm>
4
   #include <string>
 5
   using namespace std;
6
 7
8
   char s[100000];
9
   int n, cur;
10
   const string OP = "+-*";
11
12
   char next_char()
13
   {
14
       if (cur >= n) return EOF;
15
       return s[cur];
   }
16
17
   int get_priority(char ch)
18
19
   {
20
       if (ch == '*') return 2;
21
       return 1;
22
   }
23
24
   int P();
25
26 | int calc(int a, char op, int b)
```

```
27
  {
28
        if (op == '+')
29
            return a+b;
        if (op == '-')
30
31
            return a-b;
32
        if (op == '*')
33
            return a*b;
34
   }
35
36
   int calc_exp(int p)
37
   {
38
        int a = P();
39
       while ((OP.find(next_char()) != OP.npos) && (get_priority(
           next_char()) >= p))
40
        {
            char op = next_char();
41
42
            cur++;
            a = calc(a,op,calc_exp(get_priority(op)+1));
43
       }
44
45
       return a;
   }
46
47
48
   int totvar,m,var[26],varid[26];
49
   int P()
50
   {
51
52
       if (next_char() == '-')
53
        {
54
            cur++;
55
            return -P();
56
        else if (next_char() == '+')
57
        {
58
59
            cur++;
60
            return P();
        }
61
62
        else if (next_char() == '(')
63
        {
64
            cur++;
65
            int res = calc_exp(0);
66
            cur++;
67
            return res;
       }
68
69
        else
70
        {
71
            cur++;
            //cout << "getvar at " << cur << ' ' << var[varid[s[cur]-'a
72
                ']] << endl;
73
            return var[varid[s[cur-1]-'a']];
74
       }
75 | }
```

```
76
77
    int id[26], minid;
78
79
    int main()
    {
80
        while (true)
81
82
83
             scanf("%d%d",&totvar,&var[0]);
84
             if (totvar == 0 && var[0] == 0)
                                                   break;
             for (int i = 1;i < totvar;i++)</pre>
85
86
                  scanf("%d",&var[i]);
             scanf("%d",&m);
87
             scanf("%s",s);
88
             for (int i = 0; i < 26; i++)
89
90
                  id[i] = -1;
91
             minid = 0;
92
             n = strlen(s);
93
             for (int i = 0; i < n; i++)
                  if (s[i] >= 'a' && s[i] <= 'z')
94
95
                  {
                      if (id[s[i]-'a'] == -1)
96
97
                       {
98
                           id[s[i]-'a'] = minid;
99
                           minid++;
100
101
                      s[i] = 'a' + id[s[i] - 'a'];
                  }
102
103
             for (int i = 0; i < totvar; i++)
104
                  varid[i] = i;
105
             int res = 0;
106
             do
             {
107
108
                  cur = 0;
109
                  int tmp = calc_exp(0);
                  if (tmp == m)
110
111
                  {
112
                      res++;
113
                      break;
114
                  }
             }
115
116
             while (next_permutation(varid, varid+totvar));
             //puts(s);
117
             if (res > 0)
118
                  puts("YES");
119
120
             else
121
                  puts("NO");
122
         }
123
      return 0;
124 }
```

4.7 线性筛

```
int N;
2
   bool isPrime[10001];
3
  int prime [10000];
   void getPrime(int n)
5
6
        memset(isPrime,1,++n);
7
        N = 0;
8
        isPrime[0] = isPrime[1] = 0;
9
        for (int i=2; i < n; i++)
10
        {
            if (isPrime[i])
11
12
                 prime[N++]=i;
            for (int j=0; j<N \&\& prime[j]*i<n; j++)
13
14
15
                 isPrime[i*prime[j]]=0;
                 if (i%prime[j]==0)
16
17
                      break;
            }
18
19
        }
20 | }
```

4.8 线性规划

```
1 | #define MAXM 20 //max num of basic varibles
2
   #define INF 1E200
3
4 | double A[MAXM+5][MAXN+MAXM+5];
   double b[MAXM+5], c[MAXN+MAXM+5];
   int N[MAXN+5], B[MAXM+5];
6
7
   double X[MAXN+MAXM+5], V;
   int n,m,R,C,nCnt,bCnt;
9
   int v1[MAXN], v2[MAXN];
10
11
   int fcmp(double a, double b)
12
   {
13
     if(fabs(a-b)<1E-7) return 0;
14
     if(a>b) return 1;
15
     return -1;
16
   }
17
   void Pivot(int 1,int e)
18
19
     double t=A[1][e],p=c[e];
20
21
     b[1]=b[1]/t;
22
     for(int i=1;i<=C;i++)
23
       A[1][i]/=t;
24
     V = V - c[e] * b[1];
25
     for(int i=1;i<=R;i++)
26
     {
27
       if(i==1||fcmp(A[i][e],0.0)==0)
```

```
28
          continue;
29
        t=A[i][e];
        b[i]=b[i]-t*b[1];
30
31
        for(int j=1; j<=C; j++)
32
          A[i][j] = A[i][j] - t * A[1][j];
33
      }
34
      for(int i=1;i<=C;i++)
35
        c[i]=c[i]-p*A[1][i];
36
      for(int i=1;i<=nCnt;i++)</pre>
37
38
        if(N[i]==e)
39
        {
40
          N[i] = B[1];
41
          break;
42
        }
43
      }
44
      B[1] = e;
45
46
47
   bool Process(double P[])
48
   {
49
      while(true)
50
51
        int e=-1;
52
        double mV = -INF;
53
        for(int i=1;i<=nCnt;i++)</pre>
54
          if (fcmp(P[N[i]], mV) == 1)
55
             mV=P[N[i]], e=N[i];
56
57
        if (fcmp(mV, 0.0) \le 0) break;
58
        int l=-1;
59
        mV = INF;
        for(int i=1;i<=bCnt;i++)
60
61
62
          if(fcmp(A[i][e],0.0)==1)
63
          {
64
             double t=b[i]/A[i][e];
             if(fcmp(mV,t)==1||(fcmp(mV,t)==0\&\&(1==-1||B[1]>B[i])))
65
               mV=t, l=i;
66
          }
67
68
69
        if(l==-1) return false;
70
        Pivot(1,e);
      }
71
72
      return true;
73
   }
74
75
   bool initSimplex()
76
   {
77
      nCnt=bCnt=0;
78
      for(int i=1;i<=n;i++)
```

```
79
         N[++nCnt]=i;
80
      for(int i=1;i<=m;i++)</pre>
         B[++bCnt]=i+n, A[i][n+i]=1.0;
81
82
      R=bCnt, C=bCnt+nCnt;
83
      double minV=INF;
84
      int p=-1;
      for(int i=1;i<=m;i++)</pre>
85
         if (fcmp(minV,b[i]) == 1)
86
87
           minV=b[i],p=i;
      if (fcmp(minV, 0.0) >= 0)
88
89
         return true;
90
      N[++nCnt] = n+m+1; R++, C++;
      for(int i=0;i<=C;i++)
91
92
         A[R][i]=0.0;
93
      for(int i=1;i<=R;i++)
94
         A[i][n+m+1]=-1.0;
95
      Pivot(p,n+m+1);
      if(!Process(A[R])) return false;
96
97
       if(fcmp(b[R], 0.0)!=0)
         return false;
98
99
      p = -1;
100
      for (int i=1; i \le bCnt \&\&p == -1; i++)
101
         if(B[i]==n+m+1) p=i;
      if(p!=-1)
102
103
      {
104
         for(int i=1;i<=nCnt;i++)
105
106
           if (fcmp(A[p][N[i]],0.0)!=0)
107
108
              Pivot(p,N[i]);
109
              break;
110
           }
         }
111
112
      }
113
      bool f=false;
114
      for(int i=1;i<=nCnt;i++)</pre>
115
116
         if (N[i] == n+m+1) f=true;
         if (f & & i + 1 <= nCnt)
117
           N[i] = N[i+1];
118
119
      }
      nCnt --;
120
      R--, C--;
121
122
      return true;
123
    }
124
125
    //-1: no solution 1: no bound 0: has a solution -V
126
    int Simplex()
127
    {
128
      if(!initSimplex())
129
         return -1;
```

```
130
      if(!Process(c))
131
         return 1;
132
      for(int i=1;i<=nCnt;i++)</pre>
133
        X[N[i]]=0.0;
      for(int i=1;i<=bCnt;i++)</pre>
134
135
        X[B[i]]=b[i];
136
      return 0;
137
    }
138
139
    int main()
140
    {
141
         //n = 1; m=1;
142
         //V = 0.0;
         //c[1] = 1.0;
143
144
         //A[1][1] = 1.0;
145
         //b[1] = 5.0;
146
         //Simplex();
         //printf("V = %.3f\n",V);
147
148
      while(scanf("%d",&v1[1]) == 1)
149
150
             {
151
                  for(int i = 2; i <= 6; i++)
152
                       scanf("%d",&v1[i]);
153
                  n = 4; m = 6;
                  for(int i = 0; i <= m+1; i++)
154
                       for (int j=0; j \le n+m+2; j++)
155
                           A[i][j] = c[j] = 0;
156
157
                  memset(b,0,sizeof(b));
158
                  V = 0.0;
159
                  /*
                  n 为未知数个数
160
                  m 为约束个数
161
                  目标: siama(c[i]*xi)
162
                  约束: sigma(A[i][j]*xj) <=b[i]; j = 1 ... n
163
                  解存在X里面
164
165
                  */
166
                  b[1] = v1[1]; A[1][1] = 1; A[1][4] = 1;
                  b[2] = v1[2]; A[2][1] = 1; A[2][3] = 1;
167
168
                  b[3] = v1[3]; A[3][3] = 1; A[3][4] = 1;
                  b[4] = v1[4]; A[4][2] = 1; A[4][3] = 1;
169
                  b[5] = v1[5]; A[5][2] = 1; A[5][4] = 1;
170
                  b[6] = v1[6]; A[6][1] = 1; A[6][2] = 1;
171
                  c[1] = 1; c[2] = 1; c[3] = 1; c[4] = 1;
172
                  Simplex();
173
174
                  //printf("V = %.3f\n",V);
175
                  printf("\%.3f_{\perp}\%.3f_{\perp}\%.3f_{\perp}\%.3f_{n}", X[1], X[2], X[3], X[4]);
176
177
178
      return 0;
179
   }
```

4.9 分解质因数

4.9.1 米勒拉宾+分解因数

```
#include < ctime >
  #include < iostream >
 3 #define bint long long
4 using namespace std;
   const int TIME = 8;//测试次数, 够了8~10
6
   int factor [100], fac_top = -1;
7
   //计算两个数的gcd
8
9
   bint gcd(bint small, bint big)
10
        while(small)
11
12
13
            swap(small,big);
14
            small%=big;
15
        }
16
        return abs(big);
17
   }
18
   //ret = (a*b)%n (n<2^62)
19
20
   bint muti_mod(bint a, bint b, bint n)
21
22
       bint exp = a%n, res = 0;
23
       while(b)
24
25
            if(b&1)
26
            {
27
                res += exp;
28
                 if(res>n) res -= n;
29
30
            exp <<= 1;
31
            if (exp>n) exp -= n;
32
            b >> = 1;
33
        }
34
       return res;
35
   }
36
37
   // ret = (a^b)_n
38
   bint mod_exp(bint a, bint p, bint m)
39
   {
40
       bint exp=a%m, res=1; //
41
       while(p>1)
42
        {
43
            if (p&1)
44
                 res=muti_mod(res,exp,m);
45
            exp = muti_mod(exp,exp,m);
46
            p >> = 1;
47
        }
48
        return muti_mod(res,exp,m);
```

```
49
  }
50
51
   //miller-法测试素数rabin, time 测试次数
52
   bool miller_rabin(bint n, int times)
53
        if(n==2)return 1;
54
        if(n<2||!(n&1))return 0;
55
56
        bint a, u=n-1, x, y;
57
        int t=0;
58
        while (u\%2==0)
59
        {
60
            t++;
61
            u/=2;
62
        }
63
        srand(time(0));
64
        for(int i=0; i<times; i++)</pre>
65
66
            a = rand() \% (n-1) + 1;
67
            x = mod_exp(a, u, n);
            for (int j=0; j < t; j++)
68
69
            {
70
                 y = muti_mod(x, x, n);
                 if (y == 1 & x & x != 1 & x & x != n-1)
71
72
                     return false; //must not
73
                 x = y;
            }
74
75
            if( y!=1) return false;
76
77
        return true;
   }
78
79
   bint pollard_rho(bint n,int c)//找出一个因子
80
81
   {
82
        bint x, y, d, i = 1, k = 2;
        srand(time(0));
83
84
        x = rand()%(n-1)+1;
85
        y = x;
        while(true)
86
87
        {
88
            i++;
89
            x = (muti_mod(x,x,n) + c) \% n;
90
            d = gcd(y-x, n);
91
            if (1 < d && d < n) return d;
92
            if (y == x) return n;
93
            if(i == k)
94
            {
95
                 y = x;
96
                 k <<= 1;
97
            }
        }
98
99 | }
```

```
100
    void findFactor(bint n, int k)//二分找出所有质因子,存入factor
101
102
103
         if (n==1) return;
         if(miller_rabin(n, TIME))
104
105
              factor[++fac_top] = n;
106
107
              return;
         }
108
         bint p = n;
109
110
         while(p >= n)
111
              p = pollard_rho(p,k--);//值变化, 防止死循环k
112
         findFactor(p,k);
113
         findFactor(n/p,k);
114
    }
115
    int main()
116
117
    {
118
         bint cs,n,min;
119
         cin>>cs;
         while (cs--)
120
121
             cin>>n;
122
123
              fac_top = min = -1;
124
              if(miller_rabin(n,TIME)) cout << "Prime" << endl;</pre>
125
              else
126
              {
127
                   findFactor(n,107);
128
                  for(int i=0; i<=fac_top; i++)</pre>
129
                  {
130
                       if (min < 0 | | factor [i] < min)</pre>
                            min = factor[i];
131
132
                  }
133
                  cout <<min << endl;
              }
134
         }
135
136
         return 0;
   }
137
           暴力版本
    4.9.2
 1 \mid \text{int N};
    int num[30], fac[30];
 3
    void getFactor(int x)
 4
    {
 5
         N = 0;
 6
         memset(num,0,sizeof(num));
         for (int i=0; prime[i]*prime[i] <= x && i <L; i++)</pre>
 7
 8
         {
 9
              if (x\%prime[i]==0)
10
              {
11
                  while (x%prime[i]==0)
```

```
12
                {
13
                    x/=prime[i];
                    num[N]++;
14
15
                }
                fac[N++]=prime[i];
16
            }
17
       }
18
       if (x>1)
19
20
       {
            num[N]=1;
21
22
            fac[N++]=x;
23
       }
24 | }
         baby step giant step
1 #define MOD 76543
   int hs[MOD], head[MOD], next[MOD], id[MOD], top;
   void insert(int x, int y)
4
   {
5
       int k = x\%MOD;
6
       hs[top] = x, id[top] = y, next[top] = head[k], head[k] = top++;
7
8
   int find(int x)
9
   {
10
       int k = x\%MOD;
       for (int i = head[k]; i; i = next[i]) if (hs[i] == x) return id
11
          [i];
12
       return -1;
13
14
   int BSGS(int a, int b, int n)
15
   {
       memset(head, 0, sizeof(head));
16
17
       top = 1;
       if (b==1) return 0;
18
19
       int m = sqrt(n+.0), j;
20
       long long x = 1, p = 1;
21
       for (int i = 0; i < m; ++i, p = p*a%n) insert(p*b%n, i);
22
       for (long long i = m; i += m)
23
       {
            if ((j = find(x=x*p%n)) != -1) return i-j;
24
25
            if (i > n) break;
26
       }
27
       return -1;
28 | }
   4.11
         原根
1 | int getPriRoot(int p)
2
   {
 3
       if (p==2) return 1;
4
       int phi = p - 1;
```

```
getFactor(phi);
5
6
       for (int g = 2; g < p; ++g)
7
8
            bool flag=1;
9
            for (int i = 0; flag && i < N; ++i)
                if (power(g, phi/fac[i], p) == 1)
10
11
                     flag=0;
12
            if (flag)
13
                return g;
       }
14
15 | }
         逆元
   4.12
  void getInv2(int x)
2
3
       inv[1]=1;
4
       for (int i=2; i<=x; i++)
5
            inv[i] = (mod - (mod/i) * inv [mod%i] %mod) %mod;
6
7
   int getInv(int x)//为素数mod
8
9
       return power(x,mod-2);
10 | }
   4.13
         卢卡斯
   卢卡斯, num[i]阶乘也
  int comLucus(int n,int m,int p)
1
2
3
       int ans=1;
4
       for (; n && m && ans; n/=p, m/=p)
5
6
            if (n\%p>=m\%p)
7
                ans = ans*num[n%p]%p*getInv(num[m%p]%p)%p*getInv(num[n%
                   p-m%p])%p;
8
            else
9
                ans=0;
10
       }
11
       return ans;
12 | }
         欧拉函数
   4.14
   4.14.1
         分解质因数
   int getEuler(int x)
2
   {
3
       getFactor(x);
4
       int ret=x;
5
       for (int i=0; i<N; i++)
6
            ret = ret/fac[i]*(fac[i]-1);
```

```
7
       return ret;
8 | }
   4.14.2 一次预处理
  void getEuler2()
2
   {
3
       memset(euler,0,sizeof(euler));
4
       euler[1] = 1;
       for (int i = 2; i \le 3000000; i++)
5
6
       {
7
            if (!euler[i])
8
            {
9
                for (int j = i; j \le 3000000; j += i)
10
11
                     if (!euler[j])
                         euler[j] = j;
12
                     euler[j] = euler[j]/i*(i-1);
13
14
                }
15
            }
16
       }
17 | }
          费马降阶法
   4.15
   分解素数p为x^2 + y^2的费马降阶法,失败返回-1,主程序调用calcu(p,x,y)
1 | #include <stdio.h>
  #include <string.h>
3 | #include < stdlib.h>
4 | int p, expp, A, B, aa, ans, tt;
   long long M;
   long long exp(int a,int b,long long mod)
6
7
8
        long long ans=1,num=a;
9
        while (b!=0)
10
11
               if (b&1)
12
               {
                        ans=((ans%mod)*(num%mod))%mod;
13
14
               num = ((num%mod) * (num%mod)) %mod;
15
16
               b >> = 1;
17
18
        return ans;
19
20
   int calcu(int p,int &x,int &y)
21
   {
22
              if (p\%4!=1) return -1;
23
              else
24
              {
25
                   expp=(p-1)/4;
26
                  A,B;
```

```
27
                    while (1)
28
                    {
29
                         aa=rand()%p;
                         if (aa == 0) continue;
30
31
                         A=exp(aa,expp,p);
32
                         ans=(((long long)A%p)*((long long)A%p))%p;
33
                         if (ans==p-1) break;
34
                    }
35
                    B=1;
                    M=((long long)A*(long long)A+(long long)B*(long long)
36
                       B)/p;
37
                    if (M!=1) B=p;
                    while (M!=1)
38
39
40
                           if (B>A)
41
                           {tt=A; A=B; B=tt;}
42
                           tt=A;
43
                           A = B;
44
                           B = tt \%B;
45
                           M=((long long)A*(long long)A+(long long)B*(long
                                long)B)/p;
46
                    }
47
                    if (B \le A)
                    {
48
49
                               x = B;
50
                               y = A;
                    }
51
52
                    else
53
                    {
54
                       x = A;
55
                        y=B;
                    }
56
               }
57
58
   }
59
   int main()
60
   {
61
        while (scanf("%d",&p)!=EOF)
62
        {
63
               int x,y;
64
               if (calcu(p,x,y)!=-1)
65
66
        return 0;
67 | }
```

4.16 自适应simp

过了哈尔滨积分题,精度要求不高的时候可以考虑使用。暂时我只能用这个做做类似于凸函数或者凹函数的函数。

```
1 | double Simp(double 1, double r)
2 | {
3 | double h = (r-1)/2.0;
```

```
4
       return h*(calc(1)+4*calc((1+r)/2.0)+calc(r))/3.0;
5
   }
6
7
   double rSimp(double 1,double r)
8
9
       double mid = (1+r)/2.0;
10
       if (abs((Simp(1,r)-Simp(1,mid)-Simp(mid,r)))/15 < eps)
11
           return Simp(1,r);
12
       else
13
           return rSimp(1,mid)+rSimp(mid,r);
14 | }
```

4.17 组合数求模

模是质数

```
1 | #include < cstdio >
2
  #include < cstring >
3 | #include < iostream >
4 using namespace std;
5 | int mod;
   long long num[100000];
   int ni[100], mi[100];
8
   int len;
9
   void init(int p)
10
   {
11
        mod=p;
12
        num [0] = 1;
13
        for (int i=1; i<p; i++)
14
            num[i]=i*num[i-1]%p;
15
16
   void get(int n,int ni[],int p)
17
18
        for (int i = 0; i < 100; i++)
19
            ni[i] = 0;
20
        int tlen = 0;
21
        while (n != 0)
22
        {
23
            ni[tlen++] = n\%p;
24
            n /= p;
25
26
        len = tlen;
27
28
   long long power(long long x,long long y)
29
   {
30
        long long ret=1;
31
        for (long long a=x\mbox{mod}; y; y>>=1, a=a*a\mbox{mod})
32
            if (y&1)
33
                 ret=ret*a%mod;
34
        return ret;
35
36 |long long getInv(long long x)//mod为素数
```

```
37
   {
38
        return power(x, mod-2);
39
   long long calc(int n, int m, int p)//C(n, m)%p
40
   {
41
        init(p);
42
43
        long long ans=1;
        for (; n && m && ans; n/=p, m/=p)
44
45
            if (n\%p>=m\%p)
46
                 ans = ans*num[n%p]%p*getInv(num[m%p]%p)%p*getInv(num[n%
47
                    p-m%p])%p;
48
            else
49
                 ans=0;
50
        }
51
        return ans;
52
53
   int main()
   {
54
55
        int t;
        scanf("%d",&t);
56
57
        while (t--)
58
59
            int n,m,p;
            scanf("%d%d%d",&n,&m,&p);
60
            printf("%I64d\n",calc(n+m,m,p));
61
62
        }
63
        return 0;
64 }
```

4.18 其它公式

4.18.1 拉格朗日插值法

已知 $y = a_0 + a_1 x + a_2 x^2 + \dots + a_{n-1} x^{n-1}$ 曲线上的n个点 $(x_1, y_1), (x_2, y_2), (x_3, y_3) \dots (x_n, y_n)$ 用拉格朗日插值法可以不求系数可知任意x对应的y值。

$$y = y_1 \frac{(x - x_2)(x - x_3) \cdots (x - x_n)}{(x_1 - x_2)(x_1 - x_3) \cdots (x_1 - x_n)} + y_2 \frac{(x - x_1)(x - x_3) \cdots (x - x_n)}{(x_2 - x_1)(x_2 - x_3) \cdots (x_2 - x_n)} + \cdots + y_n \frac{(x - x_1)(x - x_2) \cdots (x - x_{n-1})}{(x_n - x_1)(x_n - x_2) \cdots (x_n - x_{n-1})}$$

特别的,如果 $x_1 \sim x_n$ 为 连续自然数,那么对于下一个自然数对应的y值为:

$$y_{n+1} = (-1)^{n-1}C_n^0y_1 + (-1)^{n-2}C_n^1y_2 + \dots + (-1)^0C_n^{n-1}y_n$$

这个组合系数可以通过高斯消元暴出来,前提是要猜到它满足递推关系。

4.18.2 正多面体顶点着色

正四面体:
$$N = \frac{(n^4+11\times n^2)}{12}$$
 正六面体: $N = \frac{(n^8+17\times n^4+6\times n^2)}{24}$ 正八面体: $N = \frac{(n^6+3\times n^4+12\times n^3+8\times n^2)}{24}$ 正十二面体: $N = \frac{(n^{20}+15\times n^{10}+20\times n^8+24\times n^4)}{60}$ 正二十面体: $N = \frac{(n^{12}+15\times n^6+44\times n^4)}{60}$

4.18.3 求和公式

$$\begin{array}{l} \sum k = \frac{n\times(n+1)}{2} \\ \sum 2k - 1 = n^2 \\ \sum k^2 = \frac{n\times(n+1)\times(2n+1)}{6} \\ \sum (2k-1)^2 = \frac{n\times(4n^2-1)}{3} \\ \sum k^3 = (\frac{n\times(n+1)}{2})^2 \\ \sum (2k-1)^3 = n^2 \times (2n^2-1) \\ \sum k^4 = \frac{n\times(n+1)\times(2n+1)\times(3n^2+3n-1)}{30} \\ \sum k^5 = \frac{n^2\times(n+1)^2\times(2n^2+2n-1)}{12} \\ \sum k \times (k+1) = \frac{n\times(n+1)\times(n+2)}{3} \\ \sum k \times (k+1) \times (k+2) = \frac{n\times(n+1)\times(n+2)\times(n+3)}{4} \\ \sum k \times (k+1) \times (k+2) \times (k+3) = \frac{n\times(n+1)\times(n+2)\times(n+3)\times(n+4)}{5} \end{array}$$

4.18.4 几何公式

球扇形:

全面积: $T = \pi r (2h + r_0)$, h为球冠高, r_0 为球冠底面半径体积: $V = \frac{2\pi r^2 h}{2}$

4.18.5 小公式

Pick 公式: $A = E \times 0.5 + I - 1$ (A是多边形面积,E是边界上的整点,I是多边形内部的整点) 海伦公式: $S = \sqrt{p(p-a)(p-b)(p-c)}$,其中 $p = \frac{(a+b+c)}{2}$,abc为三角形的三条边长 求 $\binom{n}{b}$ 中素因子P的个数:

- 1. 把n转化为P进制,并记它每个位上的和为S1
- 2. 把n-k, k做同样的处理, 得到S2, S3

则 $\binom{n}{k}$ 中素因子P的个数: $\frac{S2+S3-S1}{P-1}$

部分错排公式:

n+m个数中m个数必须错排 求排列数

```
1 | dp[i] = n*dp[i-1]+(i-1)*(dp[i-1]+dp[i-2]);
2 | dp[0] = n!;
3 | dp[1] = n*n!;
```

dp[m]为所求解

5 数据结构

5.1 *Splay

持续学习中。

注意节点的size值不一定是真实的值!如果有需要需要特别维护!

- 1. 旋转和Splay操作
- 2. rank操作
- 3. insert操作(。。很多题目都有)
- 4. del操作(郁闷的出纳员)
- 5. 由数组建立Splay
- 6. 前驱后继(营业额统计)
- 7. Pushdown Pushup的位置
- 8. *。。。暂时想不起了

节点定义。。

```
const int MaxN = 50003;
1
3
  struct Node
4
   {
5
       int size, key;
6
7
       Node *c[2];
8
       Node *p;
9 | mem [MaxN], *cur, *nil;
   无内存池的几个初始化函数。
  Node *newNode(int v, Node *p)
1
2
3
       cur -> c[0] = cur -> c[1] = nil, cur -> p = p;
4
       cur -> size = 1;
5
       cur -> key = v;
6
       return cur++;
7
   }
8
9
  void Init()
10
   {
11
       cur = mem;
12
       nil = newNode(0, cur);
13
       nil -> size = 0;
14 }
```

带内存池的几个函数。

```
1
   int emp[MaxN], totemp;
2
3
   Node *newNode(int v, Node *p)
4
   {
        cur = mem + emp[--totemp];
5
6
        cur -> c[0] = cur -> c[1] = nil, cur -> p = p;
7
        cur -> size = 1;
8
        cur -> key = v;
9
       return cur;
10
   }
11
12 | void Init()
13
   {
14
       for (int i = 0; i < MaxN; ++i)
15
            emp[i] = i;
16
       totemp = MaxN;
17
        cur = mem + emp[--totemp];
18
       nil = newNode(0, cur);
19
       nil->size = 0;
20
   }
21
22 | void Recycle(Node *p)
23
24
        if (p == nil)
                       return;
25
        Recycle(p \rightarrow c[0]), Recycle(p \rightarrow c[1]);
26
        emp[totemp++] = p - mem;
27 | }
   基本的Splay框架。维护序列用。
   一切下标从0开始。
   struct SplayTree
2
   {
3
       Node *root;
        void Init()
4
5
       {
6
            root = nil;
7
        }
8
        void Pushup(Node *x)
9
10
            if (x == nil)
                              return;
            Pushdown(x); Pushdown(x->c[0]); Pushdown(x->c[1]);
11
12
            x -> size = x -> c[0] -> size + x -> c[1] -> size + 1;
        }
13
14
       void Pushdown(Node *x)
15
        {
16
            if (x == nil)
                              return;
17
            //do something
18
        }
19
        void Rotate(Node *x, int f)
20
```

```
21
            if (x == nil)
                              return;
22
            Node *y = x -> p;
            y -> c[f ^1] = x -> c[f], x -> p = y -> p;
23
24
            if (x->c[f] != nil)
25
                 x->c[f]->p = y;
26
            if (y->p != nil)
27
                 y->p->c[y->p->c[1] == y] = x;
28
            x - c[f] = y, y - p = x;
29
            Pushup(y);
30
       }
31
       void Splay(Node *x, Node *f)
32
33
            while (x->p != f)
34
35
                 Node *y = x -> p;
36
                 if (y->p == f)
37
                     Rotate(x, x == y \rightarrow c[0]);
38
                 else
                 {
39
40
                     int fd = y->p->c[0] == y;
                     if (y->c[fd] == x)
41
42
                          Rotate(x, fd ^ 1), Rotate(x, fd);
43
                     else
44
                          Rotate(y, fd), Rotate(x, fd);
45
                 }
            }
46
47
            Pushup(x);
48
            if (f == nil)
49
                 root = x;
50
       }
51
       void Select(int k, Node *f)
52
        {
            Node *x = root;
53
            Pushdown(x);
54
55
            int tmp;
            while ((tmp = x->c[0]->size) != k)
56
57
58
                 if (k < tmp)
                               x = x -> c[0];
59
                 else
60
                     x = x - c[1], k -= tmp + 1;
                 Pushdown(x);
61
62
63
            Splay(x, f);
64
       }
       void Select(int 1, int r)
65
66
        {
            Select(1, nil), Select(r + 2, root);
67
68
69
        Node *Make_tree(int a[], int l, int r, Node *p)
70
        {
71
            if (1 > r) return nil;
```

```
72
                                                                 int mid = 1 + r >> 1;
    73
                                                                Node *x = newNode(a[mid], p);
                                                                x \rightarrow c[0] = Make_tree(a, l, mid - l, x);
    74
                                                                x \rightarrow c[1] = Make_tree(a, mid + 1, r, x);
    75
    76
                                                                Pushup(x);
    77
                                                                return x;
    78
    79
                                          void Insert(int pos, int a[], int n)
    80
    81
                                                                Select(pos, nil), Select(pos + 1, root);
    82
                                                                 root - c[1] - c[0] = Make_tree(a, 0, n - 1, root - c[1]);
                                                                 Splay(root->c[1]->c[0], nil);
    83
                                          }
    84
                                          void Insert(int v)
    85
    86
    87
                                                                Node *x = root, *y = nil;
    88
                                                                while (x != nil)
    89
                                                                 {
    90
                                                                                      y = x;
    91
                                                                                      y->size++;
    92
                                                                                      x = x - c[v >= x - key];
    93
    94
                                                                y \rightarrow c[v >= y \rightarrow key] = x = newNode(v, y);
   95
                                                                Splay(x, nil);
    96
                                          void Remove(int 1, int r)
    97
                                          {
    98
   99
                                                                Select(1, r);
100
                                                                //Recycle(root->c[1]->c[0]);
                                                                root \rightarrow c[1] \rightarrow c[0] = nil;
101
102
                                                                Splay(root->c[1], nil);
103
                                          }
104 | };
                    例题: 旋转区间赋值求和求最大子序列。
                    注意打上懒标记后立即Pushup。Pushup(root-c[1]-c[0]),Pushup(root-c[1]),Pushup(root);
        1
                               void Pushup(Node *x)
        2
        3
                                          if (x == nil) return;
        4
                                          Pushdown(x); Pushdown(x->c[0]); Pushdown(x->c[1]);
                                          x -> size = x -> c[0] -> size + x -> c[1] -> size + 1;
        5
        6
        7
                                          x -> sum = x -> c[0] -> sum + x -> c[1] -> sum + x -> key;
        8
                                         x \rightarrow lsum = max(x \rightarrow c[0] \rightarrow lsum, x \rightarrow c[0] \rightarrow sum + x \rightarrow key + max(0, x \rightarrow c[1] \rightarrow sum + x \rightarrow key + max(0, x \rightarrow c[1] \rightarrow sum + x \rightarrow key + max(0, x \rightarrow c[1] \rightarrow sum + x \rightarrow key + max(0, x \rightarrow c[1] \rightarrow sum + x \rightarrow key + max(0, x \rightarrow c[1] \rightarrow sum + x \rightarrow key + max(0, x \rightarrow c[1] \rightarrow sum + x \rightarrow key + max(0, x \rightarrow c[1] \rightarrow sum + x \rightarrow key + max(0, x \rightarrow c[1] \rightarrow sum + x \rightarrow key + max(0, x \rightarrow c[1] \rightarrow sum + x \rightarrow key + max(0, x \rightarrow c[1] \rightarrow sum + x \rightarrow key + max(0, x \rightarrow c[1] \rightarrow sum + x \rightarrow key + max(0, x \rightarrow c[1] \rightarrow sum + x \rightarrow key + max(0, x \rightarrow c[1] \rightarrow sum + x \rightarrow key + max(0, x \rightarrow c[1] \rightarrow sum + x \rightarrow key + max(0, x \rightarrow c[1] \rightarrow sum + x \rightarrow key + max(0, x \rightarrow c[1] \rightarrow sum + x \rightarrow key + max(0, x \rightarrow c[1] \rightarrow sum + x \rightarrow key + max(0, x \rightarrow c[1] \rightarrow sum + x \rightarrow key + max(0, x \rightarrow c[1] \rightarrow sum + x \rightarrow key + max(0, x \rightarrow c[1] \rightarrow sum + x \rightarrow key + max(0, x \rightarrow c[1] \rightarrow sum + x \rightarrow key + max(0, x \rightarrow c[1] \rightarrow sum + x \rightarrow key + max(0, x \rightarrow c[1] \rightarrow sum + x \rightarrow key + max(0, x \rightarrow c[1] \rightarrow sum + x \rightarrow key + max(0, x \rightarrow c[1] \rightarrow sum + x \rightarrow key + max(0, x \rightarrow c[1] \rightarrow sum + x \rightarrow key + max(0, x \rightarrow c[1] \rightarrow sum + x \rightarrow key + max(0, x \rightarrow c[1] \rightarrow sum + x \rightarrow key + max(0, x \rightarrow c[1] \rightarrow sum + x \rightarrow key + max(0, x \rightarrow c[1] \rightarrow sum + x \rightarrow key + max(0, x \rightarrow c[1] \rightarrow sum + sum +
                                                         lsum));
        9
                                          x - rsum = max(x - c[1] - rsum, x - c[1] - rsum + x - key + max(0, x - c[0] -
                                                         rsum));
    10
                                          x \rightarrow maxsum = max(max(x \rightarrow c[0] \rightarrow maxsum, x \rightarrow c[1] \rightarrow maxsum), x \rightarrow key+max
                                                          (0,x->c[0]->rsum)+max(0,x->c[1]->lsum));
    11
                               }
```

```
12
      void Pushdown(Node *x)
13
14
         if (x == nil) return;
15
         if (x->rev)
16
17
           x \rightarrow rev = 0;
           x -> c[0] -> rev ^= 1;
18
19
           x - c[1] - rev ^= 1;
20
           swap(x->c[0],x->c[1]);
21
22
           swap(x->lsum,x->rsum);
23
        }
24
        if (x->same)
25
26
           x->same = false;
27
           x \rightarrow key = x \rightarrow lazy;
           x \rightarrow sum = x \rightarrow key*x \rightarrow size;
28
29
           x \rightarrow lsum = x \rightarrow rsum = x \rightarrow maxsum = max(x \rightarrow key, x \rightarrow sum);
           x -> c[0] -> same = true, x -> c[0] -> lazy = x -> key;
30
           x - c[1] - same = true, x - c[1] - same = x - key;
31
32
         }
33
      }
34
35
   int main()
36
   {
37
      int totcas;
38
      scanf("%d",&totcas);
39
      for (int cas = 1; cas <= totcas; cas++)</pre>
40
      {
41
         Init();
42
         sp.Init();
43
        nil->lsum = nil->rsum = nil->maxsum = -Inf;
44
         sp.Insert(0);
45
         sp.Insert(0);
46
47
         int n,m;
48
         scanf("%d%d",&n,&m);
49
         for (int i = 0; i < n; i++)
           scanf("%d",&a[i]);
50
51
         sp.Insert(0,a,n);
52
53
         for (int i = 0; i < m; i++)
54
         {
55
           int pos, tot, c;
           scanf("%s",buf);
56
           if (strcmp(buf, "MAKE-SAME") == 0)
57
58
59
              scanf("%d%d%d",&pos,&tot,&c);
60
              sp.Select(pos-1,pos+tot-2);
61
              sp.root->c[1]->c[0]->same = true;
62
              sp.root -> c[1] -> c[0] -> lazy = c;
```

```
sp.Pushup(sp.root->c[1]), sp.Pushup(sp.root);
63
          }
64
          else if (strcmp(buf, "INSERT") == 0)
65
66
          {
67
            scanf("%d%d",&pos,&tot);
            for (int i = 0; i < tot; i++)
68
              scanf("%d",&a[i]);
69
70
            sp.Insert(pos,a,tot);
71
          }
          else if (strcmp(buf, "DELETE") == 0)
72
73
74
            scanf("%d%d",&pos,&tot);
75
            sp.Remove(pos-1,pos+tot-2);
76
          else if (strcmp(buf, "REVERSE") == 0)
77
78
          {
79
            scanf("%d%d",&pos,&tot);
            sp.Select(pos-1,pos+tot-2);
80
            sp.root -> c[1] -> c[0] -> rev ^= 1;
81
82
            sp.Pushup(sp.root->c[1]), sp.Pushup(sp.root);
          }
83
84
          else if (strcmp(buf, "GET-SUM") == 0)
85
86
            scanf("%d%d",&pos,&tot);
            sp.Select(pos-1,pos+tot-2);
87
            printf("%d\n", sp.root->c[1]->c[0]->sum);
88
          }
89
90
          else if (strcmp(buf, "MAX-SUM") == 0)
91
92
            sp.Select(0,sp.root->size-3);
93
            printf("%d\n",sp.root->c[1]->c[0]->maxsum);
94
          }
       }
95
96
     }
97
     return 0;
98 | }
```

维护多个序列的时候,不需要建立很多Splay。只需要记录某个点在内存池中的绝对位置就可以了。

需要操作它所在的序列时直接Splay到nil。此时Splay的root所在的Splay就是这个序列了。新建序列的时候需要多加入两个额外节点。如果某个Splay只有两个节点了需要及时回收。例题: Box(维护括号序列)

```
\\下面都是专用函数
1
      \\判断x在不在f里面
2
3
      bool Ancestor(Node *x, Node *f)
4
      {
5
          if (x == f) return true;
6
          while (x->p != nil)
7
          {
8
               if (x->p == f)
                               return true;
```

```
9
                 x = x -> p;
10
             }
11
             return false;
12
        \\把Splay v插入到pos后面,pos=nil时新开一个序列
13
        void Insert(Node *pos, Node *v)
14
        {
15
16
             int pl;
17
             if (pos == nil)
             {
18
19
                 Init();
                 Insert(0), Insert(0);
20
21
                 pl = 0;
22
             }
23
             else
24
             {
25
                  Splay(pos, nil);
26
                 pl = root -> c[0] -> size;
27
28
             Select(pl, nil), Select(pl + 1, root);
             root -> c[1] -> c[0] = v;
29
30
             v \rightarrow p = root \rightarrow c[1];
31
             Splay(v, nil);
32
        \\把[1,r]转出来(这里记录的是绝对位置)
33
34
        void Select(Node *1, Node *r)
35
        {
36
        Splay(l, nil);
             int pl = root->c[0]->size - 1;
37
38
             Splay(r, nil);
             int pr = root->c[0]->size - 1;
39
40
             Select(pl, pr);
41
        }
        \\分离[1,r]
42
43
        Node *Split(Node *1, Node *r)
44
        {
            Select(1, r);
45
            Node *res = root->c[1]->c[0];
46
47
             root \rightarrow c[1] \rightarrow c[0] = res \rightarrow p = nil;
             Splay(root->c[1], nil);
48
             if (root->size == 2)
49
50
             {
51
                 Recycle(root);
52
                 Init();
             }
53
54
             return res;
55
        }
56
57
   int main(int argc, char const *argv[])
58
   {
        freopen("P.in", "r", stdin);
59
```

```
60
        bool first = true;
61
        while (scanf("%d", &n) != EOF)
62
            if (!first) puts("");
63
             first = false;
64
             Init();
65
            for (int i = 0; i < n; i++)
66
67
             {
                 \\建立独立的N个区间,记录绝对位置
68
69
                 sp.Init();
70
                 sp.Insert(0), sp.Insert(0);
                 sp.Insert(0,i+1),sp.Insert(1,i+1);
71
                 sp.Select(0, 0), 1[i] = sp.root->c[1]->c[0];
72
                 sp.Select(1, 1), r[i] = sp.root->c[1]->c[0];
73
74
            }
75
            for (int i = 0; i < n; i++)
76
77
                 int f;
                 scanf("%d", &f);
78
79
                 if (f != 0)
80
                 {
                     \\把[1[i],r[i]]插入到1[f-1]后面
81
82
                     Node *pos = sp.Split(l[i], r[i]);
83
                     sp.Insert(l[f - 1], pos);
84
                 }
            }
85
            scanf("%d", &n);
86
            for (int i = 0; i < n; i++)
87
88
            {
89
                 scanf("%s", com);
90
                 if (com[0] == 'Q')
91
                 {
92
                     int pos;
                     scanf("%d", &pos);
93
                     \\求[1[pos-1],r[pos-1]]在哪个序列里面
94
                     sp.Splay(l[pos - 1], nil);
95
96
                     sp.Select(1, nil);
97
                     printf("%d\n", sp.root->key);
                 }
98
99
                 else
                 {
100
101
                     int u, v;
102
                     scanf("%d%d", &u, &v);
103
                     if (v == 0)
104
                          sp.Insert(nil, sp.Split(l[u-1], r[u-1]));
105
                     else
106
                     {
107
                          sp.Select(l[u-1],r[u-1]);
108
                          if (sp.Ancestor(l[v-1], sp.root->c[1]->c[0]) ==
                             false)
```

5.2 动态树

懒标记是否及时Pushdown了? 修改之后有没有及时Pushup?

5.2.1 维护点权

查询链上的最长字段和 GetRoute是用换根写的

```
1
  const int MaxN = 110000;
2
 3
   struct Node
4
5
        int size, key;
6
        bool rev;
7
8
   //
          bool same;
9
   //
          int lsum, rsum, sum, maxsum, sa;
10
11
        Node *c[2];
12
        Node *p;
   } mem[MaxN], *cur, *nil, *pos[MaxN];
13
14
15
   Node *newNode(int v, Node *p)
16
   {
17
        cur -> c[0] = cur -> c[1] = nil, cur -> p = p;
18
        cur -> size = 1;
19
        cur -> key = v;
20
        cur->rev = false;
21
22
   //
          cur->same = false;
23
   //
          cur -> sa = 0;
24
          cur->lsum = cur->rsum = cur->maxsum = 0;
   //
25
   //
          cur -> sum = v;
26
27
        return cur++;
28
   }
29
30 | void Init()
31 | {
```

```
32
          cur = mem;
33
          nil = newNode(0, cur);
34
          nil -> size = 0;
35
    }
36
37
    struct SplayTree
38
    {
39
          void Pushup(Node *x)
40
41
               if (x == nil)
                                      return;
42
               Pushdown(x); Pushdown(x->c[0]); Pushdown(x->c[1]);
43
               x -> size = x -> c[0] -> size + x -> c[1] -> size + 1;
44
45
    //
                  x -> sum = x -> c[0] -> sum + x -> c[1] -> sum + x -> key;
46
    //
                  x \rightarrow lsum = max(x \rightarrow c[0] \rightarrow lsum, x \rightarrow c[0] \rightarrow sum + x \rightarrow key + max
        (0, x->c[1]->lsum));
                  x - rsum = max(x - c[1] - rsum, x - c[1] - sum + x - key + max
47
        (0, x->c[0]->rsum));
48
    //
                  x \rightarrow \max = \max (\max (x \rightarrow c[0] \rightarrow \max , x \rightarrow c[1] \rightarrow \max ),
                        x \rightarrow key + max(0, x \rightarrow c[0] \rightarrow rsum) + max(0, x \rightarrow c[1] \rightarrow lsum
49
    //
        ));
50
51
          }
52
          void Pushdown(Node *x)
53
54
               if (x == nil)
                                      return;
               if (x->rev)
55
56
                     x \rightarrow rev = 0;
57
58
                     x -> c[0] -> rev ^= 1;
59
                     x - c[1] - rev ^= 1;
                     swap(x->c[0], x->c[1]);
60
    //注意修改与位置有关的量
61
62
    //
                        swap(x->lsum,x->rsum);
               }
63
64
    //
                  if (x->same)
65
    //
66
67
    //
                        x->same = false;
    //
68
                        x \rightarrow key = x \rightarrow sa;
   //
69
                        x \rightarrow sum = x \rightarrow sa * x \rightarrow size;
70
    //
                        x \rightarrow lsum = x \rightarrow rsum = x \rightarrow maxsum = max(0, x \rightarrow sum);
71
    //
                        if (x->c[0] != nil)
72
    //
                              x - c[0] - same = true, x - c[0] - sa = x - sa;
73
    //
                        if (x->c[1] != nil)
74
    //
                              x \rightarrow c[1] \rightarrow same = true, x \rightarrow c[1] \rightarrow sa = x \rightarrow sa;
75
                  }
    //
76
77
          bool isRoot(Node *x)
78
          {
79
               return (x == nil) \mid | (x->p->c[0] \mid = x && x->p->c[1] \mid = x);
```

```
}
80
81
         void Rotate(Node *x, int f)
82
83
             if (isRoot(x))
                                 return;
84
             Node *y = x->p;
             y -> c[f ^ 1] = x -> c[f], x -> p = y -> p;
85
              if (x->c[f] != nil)
86
87
                  x->c[f]->p = y;
88
             if (y != nil)
89
              ₹
90
                  if (y == y->p->c[1])
                       y -> p -> c[1] = x;
91
92
                  else if (y == y->p->c[0])
93
                       y - > p - > c[0] = x;
94
             }
95
             x - c[f] = y, y - p = x;
96
             Pushup(y);
97
         }
98
         void Splay(Node *x)
99
100
              static Node *stack[MaxN];
101
              int top = 0;
102
             stack[top++] = x;
103
              for (Node *y = x; !isRoot(y); y = y -> p)
                  stack[top++] = y->p;
104
             while (top)
105
106
                  Pushdown(stack[--top]);
107
108
             while (!isRoot(x))
109
             {
110
                  Node *y = x - > p;
                  if (isRoot(y))
111
                       Rotate(x, x == y -> c[0]);
112
113
                  else
                  {
114
115
                       int fd = y->p->c[0] == y;
116
                       if (y->c[fd] == x)
117
                            Rotate(x, fd ^ 1), Rotate(x, fd);
118
                       else
119
                            Rotate(y, fd), Rotate(x, fd);
120
                  }
121
122
             Pushup(x);
123
         }
124
         Node *Access(Node *u)
125
126
             Node *v = nil;
127
             while (u != nil)
128
              {
129
                  Splay(u);
130
                  v \rightarrow p = u;
```

```
131
                   u -> c[1] = v;
132
                   Pushup(u);
133
                   u = (v = u) \rightarrow p;
                   if (u == nil)
134
135
                        return v;
              }
136
         }
137
138
         Node *LCA(Node *u, Node *v)
139
140
              Access(u);
141
              return Access(v);
142
         }
         Node *Link(Node *u, Node *v)
143
144
145
              Access(u);
146
              Splay(u);
147
              u \rightarrow rev = true;
148
              u \rightarrow p = v;
         }
149
150
         void ChangeRoot(Node *u)
151
         {
152
              Access(u) \rightarrow rev ^= 1;
153
         }
         Node *GetRoute(Node *u, Node *v)
154
         {
155
156
              ChangeRoot(u);
157
              return Access(v);
158
         }
159
    };
160
161
    int n, m;
162
    SplayTree sp;
163
164
    int main(int argc, char const *argv[])
165
166
         while (scanf("%d", &n) != EOF)
167
168
              Init();
              for (int i = 0; i < n; i++)
169
170
171
                   int v;
172
                   scanf("%d", &v);
173
                   pos[i] = newNode(v, nil);
              }
174
              for (int i = 0; i < n - 1; i++)
175
176
              {
177
                   int u, v;
178
                   scanf("%d%d", &u, &v);
179
                   u--, v--;
180
                   sp.Link(pos[u], pos[v]);
              }
181
```

```
182
183
    //
               scanf("%d", &m);
184
               for (int i = 0; i < m; i++)
    //
185
    //
               {
186
    //
                    int typ, u, v, c;
187
    //
                    scanf("%d%d%d", &typ, &u, &v);
188
    //
                    u--, v--;
189
    //
                    if (typ == 1)
190
    //
                        printf("%d\n", sp.GetRoute(pos[u], pos[v])->
       maxsum);
191
    //
                    else
192
    //
                    {
193
                        scanf("%d", &c);
    //
    //
                        Node *p = sp.GetRoute(pos[u], pos[v]);
194
195
    //
                        p->same = true;
196
    //
                        p->sa = c;
197
    //
                    }
198
               }
    //
199
        }
200
        return 0;
201 | }
```

5.2.2 维护边权

刘汝佳的Happy Painting! 查询链上边的不同颜色数量 不能换根,但是可以Link和Cut

```
const int MaxN = 60000;
1
2
3
   struct Node
4
5
        int size, key;
6
7
        int msk,lazy;
8
9
        Node *c[2];
10
        Node *p;
   } mem[MaxN], *cur, *nil, *pos[MaxN];
11
12
13
   Node *newNode(int v, Node *p)
14
   {
15
        cur -> c[0] = cur -> c[1] = nil, cur -> p = p;
16
        cur -> size = 1;
17
        cur -> key = v;
18
19
        cur -> msk = 0;
20
        cur -> lazy = -1;
21
22
        return cur++;
23 | }
```

```
24
    void Init()
25
26
   {
27
         cur = mem;
28
         nil = newNode(0, cur);
29
         nil \rightarrow size = 0;
30
    }
31
32
    struct SplayTree
33
    {
34
         void Pushup(Node *x)
35
               if (x == nil) return;
36
37
               Pushdown(x);
               Pushdown (x->c[0]);
38
39
               Pushdown (x->c[1]);
40
               x -> size = x -> c[0] -> size + x -> c[1] -> size + 1;
41
42
               x \rightarrow msk = x \rightarrow c[0] \rightarrow msk \mid x \rightarrow c[1] \rightarrow msk \mid (1 << x \rightarrow key);
43
         }
         void Pushdown(Node *x)
44
45
         {
46
               if (x == nil) return;
47
48
               if (x\rightarrow lazy != -1)
               {
49
50
                    x \rightarrow key = x \rightarrow lazy;
                    x->msk = (1 << x->key);
51
52
                    x \rightarrow c[0] \rightarrow lazy = x \rightarrow c[1] \rightarrow lazy = x \rightarrow lazy;
53
                    x \rightarrow lazy = -1;
54
               }
         }
55
         bool isRoot(Node *x)
56
57
               return (x == nil) \mid | (x->p->c[0] \mid = x && x->p->c[1] \mid = x);
58
59
         }
60
         void Rotate(Node *x, int f)
61
         {
62
               if (isRoot(x)) return;
63
               Node *y = x -> p;
               y - c[f ^ 1] = x - c[f], x - p = y - p;
64
               if (x->c[f] != nil)
65
66
                    x->c[f]->p = y;
67
               if (y != nil)
68
                    if (y == y -> p -> c[1])
69
70
                          y - p - c[1] = x;
71
                    else if (y == y->p->c[0])
72
                          y - p - c[0] = x;
73
               x -> c[f] = y, y -> p = x;
74
```

```
75
             Pushup(y);
76
         }
77
         void Splay(Node *x)
78
         {
79
              static Node *stack[MaxN];
80
              int top = 0;
              stack[top++] = x;
81
82
              for (Node *y = x; !isRoot(y); y = y -> p)
83
                  stack[top++] = y->p;
84
             while (top)
85
                  Pushdown(stack[--top]);
86
87
             while (!isRoot(x))
88
89
                  Node *y = x -> p;
90
                  if (isRoot(y))
91
                       Rotate(x, x == y \rightarrow c[0]);
92
                  else
                  {
93
94
                       int fd = y->p->c[0] == y;
                       if (y->c[fd] == x)
95
96
                            Rotate(x, fd ^ 1), Rotate(x, fd);
97
                       else
98
                            Rotate(y, fd), Rotate(x, fd);
99
                  }
             }
100
101
             Pushup(x);
102
103
         Node *Access(Node *u)
104
         {
105
             Node *v = nil;
             while (u != nil)
106
              {
107
108
                  Splay(u);
                  v \rightarrow p = u;
109
110
                  u -> c[1] = v;
111
                  Pushup(u);
112
                  u = (v = u) -> p;
                  if (u == nil) return v;
113
             }
114
115
         }
116
         Node *Root(Node *u)
117
              Access(u);
118
119
             Splay(u);
120
              for (Pushdown(u); u->c[0] != nil; u = u->c[0])
121
                  Pushdown(u);
122
             Splay(u);
             return u;
123
124
         }
125
         Node *LCA(Node *u, Node *v)
```

```
126
         {
127
              if (Root(u) != Root(v))
128
                  return nil;
129
              Access(u);
              return Access(v);
130
131
         }
132
         void Cut(Node *u)
133
         {
134
              Access(u);
135
              Splay(u);
136
             u \rightarrow c[0] = u \rightarrow c[0] \rightarrow p = nil;
137
              Pushup(u);
         }
138
         void Link(Node *u, Node *v, int val)
139
140
141
              Access(u);
142
              Splay(u);
             u \rightarrow p = v;
143
144
              u \rightarrow key = val;
145
              Pushup(u);
         }
146
147
    };
148
149
    int cntbit(int x)
150
    {
         x = (x \& 0x555555555) + ((x >> 1) \& 0x555555555);
151
         x = (x \& 0x33333333) + ((x >> 2) \& 0x33333333);
152
         x = (x \& 0x0F0F0F0F) + ((x >> 4) \& 0x0F0F0F0F);
153
154
          = (x \& 0x00FF00FF) + ((x >> 8) \& 0x00FF00FF);
155
         x = (x \& 0x0000FFFF) + ((x >> 16) \& 0x0000FFFF);
156
         return x;
157
158
159
    SplayTree sp;
160
    int n,Q,f[MaxN];
161
162
    int main(int argc, char const *argv[])
163
    {
164
         while (scanf("%d%d",&n,&Q) != EOF)
165
166
              Init();
167
              for (int i = 0; i < n; i++)
168
              {
169
                   scanf("%d",&f[i]);
170
                  pos[i] = newNode(0, nil);
              }
171
172
              for (int i = 0; i < n; i++)
173
174
                   int col;
175
                  scanf("%d",&col);
176
                   if (f[i] > 0)
```

```
177
                       sp.Link(pos[i],pos[f[i]-1],col-1);
178
              }
              for (int q = 0; q < Q; q++)
179
180
              {
181
                   int typ,x,y,c;
182
                   scanf("%d%d%d",&typ,&x,&y);
183
                  x--,y--;
184
                  if (typ == 3)
185
186
                       Node *lca = sp.LCA(pos[x],pos[y]);
187
                       if (lca == nil || x == y)
188
                       {
189
                            printf("0 \sqcup 0 \backslash n");
190
                            continue;
191
                       }
192
                       int totedge = lca->c[1]->size;
193
                       int msk = lca -> c[1] -> msk;
194
195
                       if (pos[x] != lca)
196
                       {
197
                            sp.Splay(pos[x]);
198
                            totedge += pos[x]->size;
199
                            msk \mid = pos[x] \rightarrow msk;
                       }
200
201
202
                       printf("%d<sub>\\\\</sub>d\n",totedge,cntbit(msk));
                  }
203
204
                   else
205
                  {
206
                       scanf("%d",&c);
207
                       c--;
208
                       if (typ == 1)
209
                       {
210
                            if (x == y) continue;
211
212
                            Node *lca = sp.LCA(pos[x],pos[y]);
213
                            if (pos[x] == lca) continue;
214
215
                            sp.Cut(pos[x]);
216
                            sp.Link(pos[x],pos[y],c);
217
218
                       }
219
                       else
220
                       {
221
                            Node *lca = sp.LCA(pos[x],pos[y]);
222
223
                            if (lca == nil || x == y)
224
                                 continue;
225
226
                            lca -> c[1] -> lazy = c;
227
                            sp.Pushup(lca->c[1]);
```

```
228
                             sp.Pushup(lca);
229
                             if (pos[x] != lca)
230
231
                                  sp.Splay(pos[x]);
232
                                  pos[x] -> lazy = c;
233
                                  sp.Pushup(pos[x]);
234
                             }
235
                        }
                   }
236
237
              }
238
         }
239
         return 0;
240 | }
```

5.3 可持久化线段树

区间第k小数,内存压缩版,POJ2014。

```
#include <cstdio>
2
   #include <algorithm>
3
   using namespace std;
5
   const int MAXN=100000, MAXM=100000;
6
7
   struct node
8
9
       node *1,*r;
10
        int sum;
11
   tree[MAXN*4+MAXM*20];
12
13
   int N;
14
   node *newnode()
15
16
        tree[N].l=tree[N].r=NULL;
17
        tree[N].sum=0;
18
        return &tree[N++];
19
20
   node *newnode(node *x)
21
   {
22
        tree [N].l=x->l;
23
        tree [N].r=x->r;
24
        tree[N].sum=x->sum;
25
        return &tree[N++];
26
27
   node *build(int l,int r)
28
   {
29
       node *x=newnode();
30
        if (1<r)
31
        {
32
            int mid=l+r>>1;
33
            x \rightarrow l = build(l, mid);
34
            x->r=build(mid+1,r);
```

```
35
             x -> sum = x -> 1 -> sum + x -> r -> sum;
36
         }
37
         else
38
             x -> sum = 0;
39
         return x;
40
   }
   node *update(node *x,int l,int r,int p,int v)
41
42
   {
43
         if (1<r)
44
         {
45
              int mid=1+r>>1;
              node *nx=newnode(x);
46
              if (p<=mid)</pre>
47
48
49
                   node *ret=update(x->1,1,mid,p,v);
50
                   nx->l=ret;
51
              }
52
              else
              {
53
54
                   node *ret=update(x->r,mid+1,r,p,v);
55
                   nx -> r = ret;
56
57
             nx \rightarrow sum = nx \rightarrow 1 \rightarrow sum + nx \rightarrow r \rightarrow sum;
58
              return nx;
         }
59
         else
60
         {
61
62
              node *nx=newnode(x);
63
             nx -> sum += v;
64
              return nx;
65
        }
66
67
   int query(node *x1, node *x2, int 1, int r, int k)
68
         if (1<r)
69
70
         {
71
              int mid=l+r>>1;
              int lsum=x2->l->sum-x1->l->sum;
72
73
              if (lsum >= k)
74
                   return query(x1->1,x2->1,1,mid,k);
75
              else
76
                   return query(x1->r,x2->r,mid+1,r,k-lsum);
        }
77
78
         else
79
              return 1;
80
   char s[10];
81
   node *root[MAXM+1];
83
   int a[MAXN],b[MAXN];
84
   int init(int n)
85 | {
```

```
86
         for (int i=0; i < n; i++)
87
             b[i]=a[i];
         sort(b,b+n);
88
89
         int tn=unique(b,b+n)-b;
         for (int i=0; i < n; i++)
90
91
92
              int l=0, r=tn-1;
93
             while (1<r)
94
95
                  int mid=l+r>>1;
96
                  if (b[mid]>=a[i])
97
                       r=mid;
98
                  else
99
                       l=mid+1;
100
             }
101
             a[i]=1;
         }
102
103
         return tn;
104
    }
105
    int main()
106
    {
107
         int cas=1,n;
108
         while (scanf("%d",&n)!=EOF)
109
         {
110
             printf("Case \d:\n", cas++);
              for (int i=0; i < n; i++)
111
                  scanf("%d",&a[i]);
112
              int tn=init(n);
113
114
             N = 0;
115
             root [0] = build (0, tn-1);
116
             for (int i=1;i<=n;i++)
                  root[i]=update(root[i-1],0,tn-1,a[i-1],1);
117
118
              int m;
              scanf("%d",&m);
119
             for (int i=0; i < m; i++)
120
121
              {
122
                  int s,t;
                  scanf("%d%d",&s,&t);
123
124
                  printf("%d\n",b[query(root[s-1],root[t],0,tn-1,t-s])
                      +2>>1)]);
125
             }
         }
126
127
         return 0;
128 | }
```

5.4 treap正式版

支持翻转。

```
1 | #include <cstdio>
2 | #include <cstdlib>
3 | #include <algorithm>
```

```
using namespace std;
5
6
   const int MAXN = 100000;
7
   const int MAXM = 100000;
   const int inf = 0x7ffffffff;
8
   int a[MAXN];
10
   struct Treap
11
   {
12
        int N;
13
        Treap()
14
        {
15
            N = 0;
16
            root = NULL;
17
18
        void init()
19
        {
20
            N = 0;
21
            root = NULL;
22
        }
23
        struct Treap_Node
24
25
             Treap_Node *son[2];//left & right
26
             int value, fix;
            bool lazy;
27
            int size;
28
29
            Treap_Node() {}
30
            Treap_Node(int _value)
31
32
                 son[0] = son[1] = NULL;
33
                 value = _value;
34
                 fix = rand() * rand();
35
                 lazy = 0;
36
                 size = 1;
37
            }
38
            int sonSize(bool flag)
39
             {
40
                 if (son[flag] == NULL)
41
                      return 0;
42
                 else
43
                      return son[flag]->size;
44
            }
45
        } node[MAXN], *root, *pos[MAXN];
46
        void up(Treap_Node *p)
47
        {
            p\rightarrow size = p\rightarrow sonSize(0) + p\rightarrow sonSize(1) + 1;
48
49
50
        void down(Treap_Node *p)
51
52
            if (!p->lazy)
53
                 return ;
54
             for (int i = 0; i < 2; i++)
```

```
if (p->son[i])
55
                       p->son[i]->lazy = !p->son[i]->lazy;
56
57
              swap(p->son[0], p->son[1]);
             p \rightarrow lazy = 0;
58
         }
59
         Treap_Node *merge(Treap_Node *p, Treap_Node *q)
60
61
62
              if (p == NULL)
63
                  return q;
64
              else if (q == NULL)
65
                  return p;
              if (p\rightarrow fix \le q\rightarrow fix)
66
67
              {
68
                  down(p);
69
                  p \rightarrow son[1] = merge(p \rightarrow son[1], q);
70
                  up(p);
71
                  return p;
72
              }
73
              else
74
              {
75
                  down(q);
76
                  q \rightarrow son[0] = merge(p, q \rightarrow son[0]);
77
                  up(q);
78
                  return q;
79
              }
         }
80
         pair<Treap_Node *, Treap_Node *> split(Treap_Node *p, int n)
81
82
83
              if (p == NULL)
84
                  return make_pair((Treap_Node *)NULL, (Treap_Node *)NULL
              if (!n)
85
86
                  return make_pair((Treap_Node *)NULL, p);
              if (n == p -> size)
87
                  return make_pair(p, (Treap_Node *)NULL);
88
89
              down(p);
90
              if (p->sonSize(0) >= n)
91
              {
92
                  pair < Treap_Node *, Treap_Node *> ret = split(p->son[0],
                  p->son[0] = ret.second;
93
94
                  up(p);
95
                  return make_pair(ret.first, p);
              }
96
97
              else
98
              {
                  pair<Treap_Node *, Treap_Node *> ret = split(p->son[1],
99
                       n - p \rightarrow sonSize(0) - 1);
                  p->son[1] = ret.first;
100
101
                  up(p);
102
                  return make_pair(p, ret.second);
```

```
103
             }
104
        }
105
        int smalls(Treap_Node *p,int value)
106
        {
107
             if (p==NULL)
108
                 return 0;
             if (p->value <= value)</pre>
109
110
                 return 1+p->sonSize(0)+smalls(p->son[1], value);
111
             else
112
                 return smalls(p->son[0], value);
113
114
        void insert(int value)
115
        {
             Treap_Node *p = &node[N++];
116
             *p = Treap_Node(value);
117
118
             pair < Treap_Node *, Treap_Node *> ret = split(root, smalls())
                root, value));
119
             root = merge(merge(ret.first, p), ret.second);
120
        }
121
        void remove(int value)
122
123
             pair < Treap_Node *, Treap_Node *> ret = split(root, smalls())
                root, value) - 1);
             root = merge(ret.first, split(ret.second, 1).second);
124
125
126
        Treap_Node *build(int s, int t)
127
        {
128
             int idx = t + s >> 1;
129
             Treap_Node *p = &node[N++];
130
             *p = Treap_Node(a[idx]);
131
             pos[a[idx]] = p;
             if (idx > s)
132
133
                 p = merge(build(s, idx - 1), p);
             if (idx < t)
134
                 p = merge(p, build(idx + 1, t));
135
136
             up(p);
             return p;
137
138
        void build(int n)
139
140
141
             root = build(0, n - 1);
142
143
        void *reverse(int s, int t)
144
        {
             pair<Treap_Node *, Treap_Node *> tmp1, tmp2;
145
             tmp1 = split(root, s - 1);
146
             tmp2 = split(tmp1.second, t - s + 1);
147
             tmp2.first->lazy = !tmp2.first->lazy;
148
149
             root = merge(tmp1.first, merge(tmp2.first, tmp2.second));
150
        }
151 | };
```

```
152
   Treap treap;
153
    int main()
154
    {
155
        treap.init();
156
        int n;
157
        scanf("%d", &n);
158
        for (int i = 0; i < n; i++)
159
             scanf("%d", &a[i]);
160
        treap.build(n);
161 }
```

5.5 树链剖分

5.5.1 点权

```
1 | #include <cstdio>
2 | #include <cstring>
3 | #include <cstdlib>
4 | #include <algorithm>
5
   using namespace std;
6 \mid const int MAX = 12000;
7
   const int LOG = 15;
   const int oo = 0x3f3f3f3f;
9
   struct Edge
10
11
            int to, w, id;
12
            Edge* next;
13
   } memo[MAX << 1], *cur, *g[MAX], *pree[MAX], *solid[MAX], *valid[</pre>
14
   int dp[MAX][LOG], pos[MAX], lst[MAX], dep[MAX], cnt[MAX], h[MAX], K
      , n;
15
   void init()
16
   {
17
       for (int i = 1; i <= n; i++)
18
19
            g[i] = NULL;
20
            valid[i] = NULL;
21
            solid[i] = NULL;
22
            pree[i] = NULL;
23
       }
24
       for (int i = 0; i < LOG; i++)
25
       {
26
            dp[1][i] = 1;
27
28
       cur = memo;
29
       K = 0;
30
31
   void add(int u, int v, int w, int id)
32
33
       cur -> to = v;
34
       cur -> w = w;
```

```
35
        cur -> id = id;
36
        cur->next = g[u];
37
       g[u] = cur++;
38
39
   void dfsLCA(int d, int u, int f)
40
41
       dep[u] = d;
42
        dp[u][0] = f;
43
        cnt[u] = 1;
44
        for (int i = 1; i < LOG; i++)
45
        {
            dp[u][i] = dp[dp[u][i - 1]][i - 1];
46
47
        }
48
        for (Edge* it = g[u]; it; it = it->next)
49
            int v = it -> to;
50
51
            if (v != f)
52
            {
53
                 pree[v] = it;
54
                 valid[it->id] = it;
                 dfsLCA(d + 1, v, u); //RE
55
56
                 cnt[u] += cnt[v];
57
                 if (solid[u] == NULL || cnt[solid[u]->to] < cnt[v])</pre>
58
                 {
59
                     solid[u] = it;
                 }
60
61
            }
       }
62
63
   }
64
   void dfsChain(int u, int head)
65
66
       h[u] = head;
67
        if (solid[u])
68
69
            lst[pos[u] = K++] = u;
70
            dfsChain(solid[u]->to, head);
71
        }
72
        else
73
        for (Edge* it = g[u]; it; it = it->next)
74
75
            int v = it -> to;
76
            if (it != solid[u] && v != dp[u][0])
77
            {
78
                 dfsChain(v, v);
79
            }
80
       }
81
82
   int getLCA(int u, int v)
83
   {
84
        if (dep[u] < dep[v])
85
            swap(u, v);
```

```
for (int st = 1 << (LOG - 1), i = LOG - 1; i >= 0; i--, st >>=
86
           1)
        {
87
             if (st \le dep[u] - dep[v])
88
89
90
                 u = dp[u][i];
             }
91
92
        }
93
        if (u == v)
94
             return u;
95
        for (int i = LOG - 1; i >= 0; i--)
96
97
             if (dp[u][i] != dp[v][i])
98
99
                 u = dp[u][i];
100
                 v = dp[v][i];
101
             }
102
103
        return dp[u][0];
104
105
    struct Node
106
    {
107
             int l, r, ma, mi;
108
             bool rev;
    } seg[MAX << 2];</pre>
109
110
    void reverse(int k)
111
    {
112
        seg[k].mi *= -1;
113
        seg[k].ma *= -1;
        seg[k].rev ^= 1;
114
115
        swap(seg[k].mi, seg[k].ma);
116
117
    void pushdown(int k)
118
119
        if (seg[k].rev)
120
        {
121
             reverse(k << 1);
122
             reverse(k << 1 | 1);
123
             seg[k].rev = false;
        }
124
125
126
    void update(int k)
127
128
        seg[k].mi = min(seg[k << 1].mi, seg[k << 1 | 1].mi);
129
        seg[k].ma = max(seg[k << 1].ma, seg[k << 1 | 1].ma);
130
131
    void init(int k, int l, int r)
132
    {
133
        seg[k].l = 1;
134
        seg[k].r = r;
135
        seg[k].rev = false;
```

```
136
        if (1 == r)
137
        {
138
             seg[k].mi = seg[k].ma = solid[lst[1]]->w; //solid WA
139
             return;
        }
140
141
        int mid = 1 + r >> 1;
        init(k << 1, 1, mid);</pre>
142
143
        init(k << 1 | 1, mid + 1, r);
144
        update(k);
145
146
    void update(int k, int id, int v)
147
        if (seg[k].l == seg[k].r)
148
149
150
             seg[k].mi = seg[k].ma = solid[lst[id]] -> w = v;
151
             return;
152
        }
153
        pushdown(k);
        int mid = seg[k].l + seg[k].r >> 1;
154
155
        if (id <= mid)</pre>
156
             update(k << 1, id, v);
157
        else
158
             update(k << 1 | 1, id, v);
159
        update(k);
160
    void reverse(int k, int l, int r)
161
162
    {
163
        if (seg[k].l > r || seg[k].r < l)
164
             return;
165
        if (seg[k].l >= l \&\& seg[k].r <= r)
166
        {
167
             reverse(k);
168
             return;
169
170
        pushdown(k);
171
        reverse(k << 1, 1, r);
172
        reverse(k << 1 | 1, 1, r);
173
        update(k);
174
175
    int read(int k, int l, int r)
176
    {
177
        if (seg[k].l > r || seg[k].r < l)
178
             return -oo;
179
        if (seg[k].l >= l \&\& seg[k].r <= r)
             return seg[k].ma;
180
181
        pushdown(k);
182
        return max(read(k << 1, 1, r), read(k << 1 | 1, 1, r));
183
184
    void setEdge(int id, int v)
185
    {
186
        Edge* it = valid[id];
```

```
187
         if (h[it->to] != it->to)
188
         {
189
             update(1, pos[dp[it->to][0]], v);
190
         }
191
         else
192
         {
193
             it -> w = v;
194
         }
195
    }
196
    void negateLCA(int t, int u)
197
198
         while (t != u)
199
         {
200
             int tmp = h[u];
201
             if (dep[tmp] < dep[t])
202
                  tmp = t;
             if (h[u] == u)
203
204
             {
205
                  pree[u] -> w *= -1;
                  u = dp[u][0];
206
             }
207
208
             else
209
             {
                  reverse(1, pos[tmp], pos[dp[u][0]]);
210
211
                  u = tmp;
212
             }
213
         }
214
215
    void negate(int u, int v)
216
    {
217
         int t = getLCA(u, v);
218
         negateLCA(t, u);
219
         negateLCA(t, v);
220
    }
221
    int maxLCA(int t, int u)
222
    {
223
         int ret = -00;
224
         while (t != u)
225
         {
226
             int tmp = h[u];
227
             if (dep[tmp] < dep[t])</pre>
228
                  tmp = t;
229
             if (h[u] == u)
230
             {
231
                  ret = max(ret, pree[u]->w);
232
                  u = dp[u][0];
             }
233
234
             else
235
             {
236
                  ret = max(ret, read(1, pos[tmp], pos[dp[u][0]]));
237
                  u = tmp;
```

```
238
              }
239
         }
240
         return ret;
241
242
    int query(int u, int v)
243
         int t = getLCA(u, v);
244
245
         return max(maxLCA(t, u), maxLCA(t, v));
246
    }
247
    int main()
248
    {
249
         int T;
250
         int u, v, w;
251
         char op [15];
252
         scanf("%d", &T);
253
         while (T--)
254
         {
255
              scanf("%d", &n);
256
              init();
              for (int i = 1; i < n; i++)
257
258
259
                   scanf("%d%d%d", &u, &v, &w);
260
                  add(u, v, w, i);
261
                  add(v, u, w, i);
262
263
              dfsLCA(0, 1, 1);
264
              dfsChain(1, 1);
265
              init(1, 0, K - 1);
266
              while (scanf("%s", op), op[0] != 'D')
267
              {
268
                  scanf("%d%d", &u, &v);
                  if (op[0] == 'C')
269
270
                  {
271
                       setEdge(u, v);
272
                  }
273
                  else if (op[0] == 'N')
274
275
                       negate(u, v);
276
                  }
277
                  else
278
                  {
279
                       printf("%d\n", query(u, v));
280
                  }
281
              }
282
         }
283
         return 0;
284 | }
    5.5.2
          边权
  1 | #include <cstdio>
 2 \mid \texttt{\#include} \mid \texttt{<iostream>}
```

```
#include <cstdlib>
4 | #include <algorithm>
5 | #include <cmath>
6 | #include <cstring>
7 using namespace std;
8 | int n,m,sum,pos;
9 | int head [50005], e;
10 \mid \text{int s} [50005], \text{from} [50005];
11 | int fa[50005][20], deep[50005], num[50005];
   int solid[50005],p[50005],fp[50005];
12
13
   struct N
14 | {
15
     int 1, r, mid;
16
     int add, w;
17 | \rangle nod [50005*4];
18
   struct M
19
20
     int v, next;
21
   }edge[100005];
22
   void addedge(int u,int v)
23
   {
24
     edge[e].v=v;
25
     edge[e].next=head[u];
     head[u]=e++;
26
27
28
     edge[e].v=u;
29
     edge[e].next=head[v];
     head[v]=e++;
30
31
  }
32
   void LCA(int st,int f,int d)
33
34
     deep[st]=d;
35
     fa[st][0]=f;
36
     num[st]=1;
37
     int i, v;
     for(i=1;i<20;i++)
38
39
        fa[st][i]=fa[fa[st][i-1]][i-1];
40
     for(i=head[st];i!=-1;i=edge[i].next)
41
42
        v=edge[i].v;
        if (v!=f)
43
44
          LCA(v,st,d+1);
45
46
          num[st]+=num[v];
          if(solid[st] == -1 | | num[v] > num[solid[st]])
47
            solid[st]=v;
48
        }
49
     }
50
51
52
  void getpos(int st,int sp)
53 | {
```

```
from[st]=sp;
54
55
      if(solid[st]!=-1)
56
         p[st]=pos++;
57
         fp[p[st]]=st;
58
         getpos(solid[st],sp);
59
      }
60
61
      else
62
      {
         p[st]=pos++;
63
64
         fp[p[st]]=st;
65
         return;
      }
66
67
      int i, v;
68
      for(i=head[st];i!=-1;i=edge[i].next)
69
70
         v=edge[i].v;
         if (v!=solid[st]&&v!=fa[st][0])
71
72
           getpos(v,v);
      }
73
74
75
    int getLCA(int u,int v)
76
77
      if (deep[u] < deep[v])</pre>
78
         swap(u,v);
79
       int d=1 << 19, i;
      for (i=19; i>=0; i--)
80
81
82
         if (d<=deep[u]-deep[v])</pre>
83
           u=fa[u][i];
84
         d>>=1;
85
      }
      if(u==v)
86
87
         return u;
88
      for (i=19; i>=0; i--)
89
         if(fa[u][i]!=fa[v][i])
90
91
           u=fa[u][i];
92
           v=fa[v][i];
93
94
      return fa[u][0];
95
96
    void init(int p,int l,int r)
97
    {
98
      nod[p].1=1;
      nod[p].r=r;
99
100
      nod[p].mid=(l+r)>>1;
      nod[p].add=0;
101
      if(l==r)
102
103
         nod[p].w=s[fp[1]];
104
       else
```

```
105
      {
106
         init(p<<1,1,nod[p].mid);</pre>
         init(p<<1|1,nod[p].mid+1,r);</pre>
107
108
      }
109
    }
110
    void lazy(int p)
111
112
      if (nod [p].add!=0)
113
114
         nod[p<<1].add+=nod[p].add;
115
         nod[p<<1|1].add+=nod[p].add;
116
         nod[p].add=0;
      }
117
118
119
    void update(int p,int l,int r,int v)
120
121
      if (nod[p].l==1&&nod[p].r==r)
122
      {
123
         nod[p].add+=v;
124
         return;
      }
125
126
      lazy(p);
127
      if(nod[p].mid<1)</pre>
128
         update(p<<1|1,1,r,v);
129
      else if(nod[p].mid>=r)
130
         update(p<<1,1,r,v);
131
      else
132
      {
133
         update(p<<1,1,nod[p].mid,v);
134
         update(p<<1|1,nod[p].mid+1,r,v);
135
      }
136
137
    int read(int p,int l,int r)
138
139
      if (nod [p].l==1&&nod [p].r==r)
140
         return nod[p].w+nod[p].add;
141
      lazy(p);
142
      if(nod[p].mid<1)</pre>
143
         return read(p<<1|1,1,r);
144
       else if(nod[p].mid>=r)
145
         return read(p<<1,1,r);</pre>
146
147
    void jump(int st,int ed,int val)
148
149
      while (deep[st]>=deep[ed])
150
      {
         int tmp=from[st];
151
         if (deep[tmp] < deep[ed])</pre>
152
153
           tmp=ed;
154
         update(1,p[tmp],p[st],val);
155
         st=fa[tmp][0];
```

```
156
      }
157
    }
158
    void change(int st,int ed,int val)
159
160
      int lca=getLCA(st,ed);
161
      jump(st,lca,val);
162
      jump(ed,lca,val);
163
      jump(lca,lca,-val);
164
    }
165
    int main()
166
    {
      while (scanf("%d%d%d",&n,&m,&sum)==3)
167
168
      {
169
         int i;
170
         s[0]=0; pos=0; deep[0]=-1;
171
         memset(fa,0,sizeof(fa));
172
         for(i=1;i<=n;i++)
         {
173
174
           solid[i] = -1;
175
           scanf("%d",&s[i]);
         }
176
177
         memset(head, -1, sizeof(head));
178
         e=0;
179
         for (i=0; i < m; i++)
         {
180
181
           int a,b;
182
           scanf("%d%d",&a,&b);
183
           addedge(a,b);
184
         }
         LCA(1,0,0);
185
         getpos(1,1);
186
187
         init(1,0,pos-1);
         for(i=0;i<sum;i++)
188
189
190
           char que [5];
           scanf("%s",que);
191
192
           if (que [0]!='Q')
193
           {
194
              int a,b,c;
195
              scanf("%d%d%d",&a,&b,&c);
              if(que[0]=='D')
196
197
                c = -c;
198
              change(a,b,c);
           }
199
200
           else
201
           {
202
              int a;
203
              scanf("%d",&a);
204
              printf("%d\n", read(1, p[a], p[a]));
205
           }
         }
206
```

```
207
      }
208
      return 0;
209
   }
          划分树
    5.6
    int n,m;
    struct elem
 3
    {
 4
         int v,index;
 5
    }a[120000];
 6
    int d[30][120000];
 7
    int s[30][120000];
 8
 9
    bool cmp(elem a, elem b)
 10
    {
         if (a.v == b.v)
 11
 12
             return a.index <= b.index;</pre>
 13
         return a.v < b.v;
 14
    }
 15
 16
    void build(int depth,int l,int r)
 17
    {
 18
         if (1 == r)
 19
             return;
 20
         int mid = (1+r)/2;
 21
         int tl, tr;
 22
         tl = tr = 0;
         for (int i = 1; i \le r; i++)
 23
 24
         {
 25
             if (cmp(a[d[depth][i]],a[mid]))
 26
             {
 27
                  d[depth+1][l+tl] = d[depth][i];
 28
                  tl++;
             }
 29
 30
             else
 31
             {
 32
                  d[depth+1][mid+1+tr] = d[depth][i];
 33
                  tr++;
 34
             s[depth][i] = tl;
 35
 36
 37
        build(depth+1,1,mid);
 38
        build(depth+1, mid+1, r);
 39
    }
 40
 41
    int find(int depth, int dl, int dr, int fl, int fr, int k)
 42
    {
 43
         if (fl == fr)
 44
             return a[d[depth][f1]].v;
 45
         int ls,rs;
 46
         int mid = (dl+dr)/2;
```

```
47
       ls = (fl == dl)? 0 : s[depth][fl-1];
48
       rs = s[depth][fr];
49
       return (rs-ls < k)? find(depth+1, mid+1, dr, mid+fl-dl-ls+1, mid+fr
           -dl-rs+1, k-(rs-ls)): find(depth+1,dl,mid,dl+ls,dl+rs-1,k);
50
   }
51
52
   int main()
53
   {
54
       while (scanf("%d%d",&n,&m) != EOF)
55
       {
            for (int i = 1; i \le n; i++)
56
57
58
                 scanf("%d",&a[i].v);
                 a[i].index = i;
59
60
61
            sort(a+1,a+n+1,cmp);
62
            for (int i = 1; i \le n; i++)
                 d[0][a[i].index] = i;
63
            build(0,1,n);
64
65
            int l,r,k;
            for (int i = 1; i \le m; i++)
66
67
            {
68
                 scanf("%d%d%d",&1,&r,&k);
69
                 printf("%d\n",find(0,1,n,l,r,k));
            }
70
71
       }
72
       return 0;
73 | }
   5.7
         树状数组
   int read(int k)
1
2
3
       int sum = 0;
       for (; k; k^=k\&-k)
4
5
            sum+=tree[k];
6
       return sum;
7
8
   void update(int k, int v)
9
   {
10
       for (; k \le MaxN; k + = k\&-k)
11
            tree[k]+=v;
12
   }
   int find_Kth(int k)
13
14
15
       int idx = 0;
16
        for(int i=20; i>=0; i--)
17
        {
18
            idx | = 1 << i;
19
            if(idx <= MaxN && tree[idx] < k)</pre>
20
                 k -= tree[idx];
21
                   idx ^= 1 << i;
            else
```

```
22 | }
23 | return idx + 1;
24 |}
```

6 图论

6.1 优先队列优化的dijkstra

```
#include < cstdio >
  #include < cstring >
 3 | #include < iostream >
4 | #include < algorithm >
 5 | #include < queue >
6
   #include < vector >
7
  using namespace std;
   const int MAXN=100;
   const int MAXM=1000;
10 | int N,L;
11
   int head[MAXN];
12
   struct edges
13
   {
14
        int to, next, cost;
15
   } edge[MAXM];
16
   int dist[MAXN];
17
   class states
18
19
   public:
20
        int cost, id;
21
   };
22
   class cmp
23
24
   public:
25
        bool operator ()(const states &i,const states &j)
26
27
            return i.cost>j.cost;
28
        }
29
   };
30
   void init(int n)
31
32
       N=n;
33
       L=0;
34
        for (int i=0; i<n; i++)
35
            head[i]=-1;
36
37
   void add_edge(int x,int y,int cost)
38
   {
39
        edge[L].to=y;
40
        edge[L].cost=cost;
41
        edge[L].next=head[x];
42
        head[x]=L++;
43
   }
44
   int dijkstra(int s,int t)
45
   {
        memset(dist,63,sizeof(dist));
46
47
        states u;
```

```
48
       u.id=s;
49
       u.cost=0;
50
        dist[s]=0;
51
        priority_queue < states , vector < states > , cmp > q;
52
       q.push(u);
        while (!q.empty())
53
        {
54
55
            u=q.top();
56
            q.pop();
            if (u.id==t) return dist[t];
57
            if (u.cost!=dist[u.id]) continue;
58
            for (int i=head[u.id]; i!=-1; i=edge[i].next)
59
            {
60
61
                 states v=u;
62
                 v.id=edge[i].to;
63
                 if (dist[v.id]>dist[u.id]+edge[i].cost)
64
                 {
                     v.cost=dist[v.id]=dist[u.id]+edge[i].cost;
65
66
                     q.push(v);
                 }
67
            }
68
69
       }
70
       return -1;
71
72
   int main()
73
74
        int n,m;
75
        scanf("%d%d",&n,&m);
76
        init(n);
77
        for (int i=0; i<m; i++)
78
        {
79
            int x,y,z;
80
            scanf("%d%d%d",&x,&y,&z);
81
            add_edge(x,y,z);
82
            add_edge(y,x,z);
83
        }
84
        int s,t;
        scanf("%d%d",&s,&t);
85
        printf("%d\n",dijkstra(s,t));
86
87
        return 0;
88
  }
   6.2
         SAP四版
 1 const int MAXEDGE=20400;
2 \mid const int MAXN = 400;
   const int inf=0x3fffffff;
 4
   struct edges
5
 6
        int cap, to, next, flow;
 7
   } edge[MAXEDGE+100];
  struct nodes
```

```
9
   {
10
        int head, label, pre, cur;
11
   } node[MAXN+100];
   int L,N;
12
   int gap[MAXN+100];
13
   void init(int n)
14
15
16
       L=0:
17
       N=n;
18
       for (int i=0; i<N; i++)
19
            node[i].head=-1;
20
   }
21
   void add_edge(int x,int y,int z,int w)
22
23
       edge[L].cap=z;
24
        edge[L].flow=0;
25
        edge[L].to=y;
26
        edge[L].next=node[x].head;
27
       node[x].head=L++;
28
        edge[L].cap=w;
29
        edge[L].flow=0;
30
        edge[L].to=x;
31
        edge[L].next=node[y].head;
32
       node[y].head=L++;
33
34
   int maxflow(int s,int t)
35
   {
36
       memset(gap,0,sizeof(gap));
37
       gap[0]=N;
38
        int u,ans=0;
39
       for (int i=0; i<N; i++)
40
       {
41
            node[i].cur=node[i].head;
42
            node[i].label=0;
       }
43
44
       u=s;
45
       node[u].pre=-1;
46
       while (node[s].label < N)
47
       {
48
            if (u==t)
49
            {
50
                 int min=inf;
51
                 for (int i=node[u].pre; i!=-1; i=node[edge[i^1].to].pre
                   )
52
                     if (min > edge[i].cap-edge[i].flow)
53
                         min=edge[i].cap-edge[i].flow;
54
                 for (int i=node[u].pre; i!=-1; i=node[edge[i^1].to].pre
55
                {
56
                     edge[i].flow+=min;
57
                     edge[i^1].flow-=min;
```

```
}
58
59
                u=s;
60
                ans+=min;
61
                continue;
            }
62
63
            bool flag=false;
64
            int v;
65
            for (int i=node[u].cur; i!=-1; i=edge[i].next)
66
67
                v=edge[i].to;
68
                if (edge[i].cap-edge[i].flow && node[v].label+1==node[u
                   ].label)
                {
69
70
                     flag=true;
71
                    node[u].cur=node[v].pre=i;
72
                     break;
73
                }
74
            }
75
            if (flag)
76
            {
77
                u = v;
78
                continue;
79
            node[u].cur=node[u].head;
80
            int min=N;
81
82
            for (int i=node[u].head; i!=-1; i=edge[i].next)
                if (edge[i].cap-edge[i].flow && node[edge[i].to].label <
83
                   min)
84
                    min=node[edge[i].to].label;
85
            gap[node[u].label]--;
            if (!gap[node[u].label]) return ans;
86
            node[u].label=min+1;
87
            gap[node[u].label]++;
88
89
            if (u!=s) u=edge[node[u].pre^1].to;
90
       }
91
       return ans;
92 | }
        费用流三版
   6.3
   T了可以改成栈。
1 const int MAXM=60000;
2
   const int MAXN=400;
 3
   const int inf=0x3fffffff;
 4
   int L,N;
   int K;
6
   struct edges
7
8
       int to,next,cap,flow,cost;
9
   } edge[MAXM];
10 struct nodes
```

```
11
  {
12
        int dis, pre, head;
13
       bool visit;
14
   } node[MAXN];
   void init(int n)
15
16
17
       N=n;
18
       L=0;
19
       for (int i=0; i<N; i++)
20
            node[i].head=-1;
21
22
   void add_edge(int x,int y,int cap,int cost)
23
   {
24
       edge[L].to=y;
25
        edge[L].cap=cap;
26
        edge[L].cost=cost;
27
        edge[L].flow=0;
28
        edge[L].next=node[x].head;
29
       node[x].head=L++;
30
        edge[L].to=x;
31
        edge [L] . cap=0;
32
        edge[L].cost=-cost;
33
        edge[L].flow=0;
34
        edge[L].next=node[y].head;
       node[y].head=L++;
35
36
   }
37
   bool spfa(int s,int t)
38
   {
39
       queue <int> q;
40
       for (int i=0; i<N; i++)
41
42
            node[i].dis=0x3fffffff;
            node[i].pre=-1;
43
            node[i].visit=0;
44
45
46
       node[s].dis=0;
47
       node[s].visit=1;
48
       q.push(s);
49
       while (!q.empty())
50
            int u=q.front();
51
52
            node[u].visit=0;
            for (int i=node[u].head; i!=-1; i=edge[i].next)
53
54
            {
55
                 int v=edge[i].to;
                if (edge[i].cap>edge[i].flow &&
56
57
                         node[v].dis>node[u].dis+edge[i].cost)
                {
58
59
                     node[v].dis=node[u].dis+edge[i].cost;
60
                     node[v].pre=i;
61
                     if (!node[v].visit)
```

```
62
                     {
63
                          node[v].visit=1;
                          q.push(v);
64
                     }
65
                 }
66
            }
67
68
            q.pop();
69
70
        if (node[t].pre==-1)
71
            return 0;
72
        else
73
            return 1;
74
75
   int mcmf(int s,int t,int &cost)
76
   {
77
        int flow=0;
78
        while (spfa(s,t))
        {
79
80
            int max=inf;
            for (int i=node[t].pre; i!=-1; i=node[edge[i^1].to].pre)
81
82
83
                 if (max>edge[i].cap-edge[i].flow)
84
                     max = edge[i].cap - edge[i].flow;
85
            }
            for (int i=node[t].pre; i!=-1; i=node[edge[i^1].to].pre)
86
87
88
                 edge[i].flow+=max;
89
                 edge[i^1].flow-=max;
90
                 cost+=edge[i].cost*max;
91
            }
92
            flow+=max;
93
94
        return flow;
95 | }
```

6.4 匈牙利

6.4.1 新版,隐式图可解

```
bool check(int u)
1
2
   {
3
       for (int i=head[u]; i!=-1; i=edge[i].next)
4
5
            int v=edge[i].to;
            if (matc[v]==u) continue;
6
7
            if (!use[v])
            {
8
9
                use[v]=1;
10
                if (matc[v] == -1 || check(matc[v]))
11
                {
12
                     matc[v]=u;
```

```
13
                      matc[u]=v;
14
                      return 1;
                 }
15
16
            }
        }
17
18
        return 0;
19
20
   int match()
21
   {
22
        int ret=0;
23
        memset(matc,-1,sizeof(matc));
24
        for (int u=0; u<N; u++)
25
        {
26
            if (matc[u]!=-1) continue;
27
            memset(use,0,sizeof(use));
28
            if (check(u))
29
                 ret++;
30
        }
31
        return ret;
32 | }
         邻接矩阵
   6.4.2
   bool check(int u)
2
   {
3
        for (int v=0; v<N; v++)
4
            if (am[u][v] && !use[v])
            {
5
6
                 use[v]=1;
7
                 if (pre[v] == -1 || check(pre[v]))
8
                 {
9
                      pre[v]=u;
10
                      return 1;
11
                 }
12
13
        return 0;
14
   }
15
   int match()
16
   {
17
        int ret=0;
18
        memset(pre,-1,sizeof(pre));
        for (int u=0; u<N; u++)
19
20
        {
21
            memset(use,0,sizeof(use));
22
            if (check(u))
23
                 ret++;
        }
24
25
        return ret;
26 | \}
         邻接表
   6.4.3
1 | bool check(int u)
```

```
2
   {
3
       for (int i=head[u]; i!=-1; i=edge[i].next)
4
            int v=edge[i].to;
5
6
            if (!use[v])
7
            {
8
                use [v]=1;
9
                if (pre[v] == -1 || check(pre[v]))
10
                {
11
                     pre[v]=u;
12
                     return 1;
                }
13
            }
14
       }
15
16
       return 0;
17
   }
18
   int match()
19
   {
20
       int ret=0;
21
       memset(pre,-1,sizeof(pre));
       for (int u=1; u \le N; u++)
22
23
       {
24
            memset(use,0,sizeof(use));
25
            if (check(u))
26
                ret++;
27
       }
28
       return ret;
29 | }
        一般图匹配带花树
   6.5
  const int MaxN = 222;
1
   int N;
   bool Graph[MaxN+1][MaxN+1];
3
   int Match[MaxN+1];
   bool InQueue [MaxN+1], InPath [MaxN+1], InBlossom [MaxN+1];
6
   int Head, Tail;
7
   int Queue[MaxN+1];
8
   int Start, Finish;
   int NewBase;
   int Father[MaxN+1], Base[MaxN+1];
10
11
   int Count;
12
   void CreateGraph()
13
   {
14
       int u, v;
15
       memset(Graph, false, sizeof(Graph));
16
       scanf("%d",&N);
17
       while (scanf("%d%d",&u,&v) != EOF)
18
            Graph[u][v] = Graph[v][u] = true;
19
20
   void Push(int u)
21
  {
```

```
22
       Queue[Tail] = u;
23
       Tail++;
24
        InQueue[u] = true;
25
26
   int Pop()
27
   {
28
       int res = Queue[Head];
29
       Head++;
30
       return res;
31
32
   int FindCommonAncestor(int u,int v)
33
34
       memset(InPath, false, sizeof(InPath));
       while (true)
35
36
       {
37
            u = Base[u];
38
            InPath[u] = true;
            if (u == Start) break;
39
40
            u = Father[Match[u]];
       }
41
42
       while (true)
43
       {
44
            v = Base[v];
45
            if (InPath[v]) break;
            v = Father[Match[v]];
46
       }
47
48
       return v;
49
50
   void ResetTrace(int u)
51
   {
52
       int v;
53
       while (Base[u] != NewBase)
54
        {
55
            v = Match[u];
56
            InBlossom[Base[u]] = InBlossom[Base[v]] = true;
57
            u = Father[v];
58
            if (Base[u] != NewBase) Father[u] = v;
       }
59
60
   void BlossomContract(int u,int v)
61
62
   {
63
       NewBase = FindCommonAncestor(u,v);
64
       memset(InBlossom, false, sizeof(InBlossom));
65
       ResetTrace(u);
66
       ResetTrace(v);
        if (Base[u] != NewBase) Father[u] = v;
67
        if (Base[v] != NewBase) Father[v] = u;
68
69
        for (int tu = 1; tu <= N; tu++)
70
            if (InBlossom[Base[tu]])
71
            {
                Base[tu] = NewBase;
72
```

```
if (!InQueue[tu]) Push(tu);
73
             }
74
75
    void FindAugmentingPath()
76
77
78
        memset(InQueue, false, sizeof(InQueue));
        memset(Father, 0, size of (Father));
79
        for (int i = 1; i <= N; i++)
80
81
             Base[i] = i;
82
        Head = Tail = 1;
83
        Push(Start);
84
        Finish = 0;
85
        while (Head < Tail)
86
87
             int u = Pop();
88
             for (int v = 1; v \le N; v++)
89
                  if (Graph[u][v] && (Base[u] != Base[v]) && (Match[u] !=
                      v))
                  {
90
                      if ((v == Start) || ((Match[v] > 0) && (Father[
91
                         Match[v]] > 0)))
92
                           BlossomContract(u,v);
93
                      else if (Father[v] == 0)
94
                      {
95
                           Father[v] = u;
                           if (Match[v] > 0)
96
97
                               Push(Match[v]);
98
                           else
99
                           {
100
                               Finish = v;
101
                               return;
                           }
102
                      }
103
104
                  }
105
        }
106
107
    void AugmentPath()
108
109
        int u, v, w;
110
        u = Finish;
        while (u > 0)
111
112
             v = Father[u];
113
114
             w = Match[v];
             Match[v] = u;
115
116
             Match[u] = v;
117
             u = w;
        }
118
119
120
    void Edmonds()
121 | {
```

```
122
         memset(Match,0,sizeof(Match));
123
         for (int u = 1; u <= N; u++)
             if (Match[u] == 0)
124
125
             {
126
                  Start = u;
127
                  FindAugmentingPath();
128
                  if (Finish > 0) AugmentPath();
             }
129
130
    }
131
    void PrintMatch()
132
         for (int u = 1; u \le N; u++)
133
134
             if (Match[u] > 0)
135
                  Count++;
136
         printf("%d\n",Count);
137
         for (int u = 1; u \le N; u++)
             if (u < Match[u])</pre>
138
139
                  printf("%d<sub>□</sub>%d\n",u,Match[u]);
140
    }
141
    int main()
142
143
         CreateGraph();
144
         Edmonds();
145
         PrintMatch();
146 }
          KM
    6.6
```

6.6.1 最大加权匹配

```
1 | bool visx[N], visy[N]; //x, y中的点是否被访问
   int lx[N], ly[N]; //x, y中的点的标号
2
   int matchy[N];//y中各点匹配状态
   int map[N][N];//二分图描述[x][y]
   bool find(int x)
5
6
7
     visx[x]=true;
8
9
     for (int y=0; y < y < t; y++)
10
11
       if (!visy[y])
12
       {
13
         t=lx[x]+ly[y]-map[x][y];
14
         if (t==0)
15
16
            visy[y]=true;
17
            if (matchy[y] == -1 || find(matchy[y]))
            {
18
19
              matchy[y]=x;
20
              return true;
21
            }
22
         }
```

```
23
          else if (lack>t) lack=t;
24
       }
     }
25
26
     return false;
27
   }
28
   void KM()
29
   {
30
     memset(lx,0,sizeof(lx));
31
     memset(ly,0,sizeof(ly));
32
     memset(matchy,-1,sizeof(matchy));
33
     for (int i=0;i<xcnt;i++)</pre>
       for (int j=0; j < ycnt; j++)
34
35
          if (map[i][j]>lx[i])
            lx[i]=map[i][j];
36
37
     for (int x=0; x<xcnt; x++)
38
39
       while (true)
40
       {
          memset(visx,false,sizeof(visx));
41
42
          memset(visy,false,sizeof(visy));
43
          lack=INFI;
44
          if (find(x)) break;
45
          for (int i=0;i<xcnt;i++)</pre>
46
          {
47
            if (visx[i]) lx[i]-=lack;
            if (visy[i]) ly[i]+=lack;
48
49
          }
50
       }
51
     }
52
     int cost=0;
53
     for (int i=0;i<ycnt;i++)</pre>
        cost+=map[matchy[i]][i];
54
55 }
   6.6.2
         自认为正确的Kuhn_Munkras
   未验证
1 #include <cstdio>
2 | #include < cstring >
  #include <algorithm >
  using namespace std;
4
   const int MAXN=100;
5
6
   const int inf=0x3f3f3f3f;
   bool visitx[MAXN], visity[MAXN];
   int labx[MAXN],laby[MAXN],matx[MAXN],maty[MAXN],slack[MAXN];
8
   int ma[MAXN][MAXN];
   bool check(int x,int n)
10
11
   {
12
       visitx[x]=1;
13
       for (int i=0; i<n; i++)
14
            if (!visity[i])
15
                 if (labx[x]+laby[i] == ma[x][i])
```

```
{
16
17
                     visity[i]=1;
                     if (maty[i] == -1 || check(maty[i],n))
18
19
                     {
20
                          matx[x]=i;
21
                          maty[i]=x;
22
                          return 1;
23
                     }
                 }
24
25
                 else
26
                     slack[i]=min(slack[i], labx[x]+laby[i]-ma[x][i]);
27
28
       return 0;
29
30
   void maintain(int n)
31
   {
32
        int diff=inf;
33
        for (int i=0; i<n; i++)
34
            if (!visity[i])
                 diff=min(diff,slack[i]);
35
        for (int i=0; i<n; i++)
36
37
        {
38
            if (visitx[i])
39
                 labx[i]-=diff;
40
            if (visity[i])
                 laby[i]+=diff;
41
42
            else
43
                 slack[i]-=diff;
44
       }
45
   }
46
   int Kuhn_Munkras(int n)
47
   {
        for (int i=0; i<n; i++)
48
49
            labx[i]=-inf;
50
            for (int j=0; j < n; j++)
51
52
                 labx[i]=max(labx[i],ma[i][j]);
53
        }
       memset (laby, 0,4*n);
54
55
       memset(matx,-1,4*n);
       memset (maty, -1, 4*n);
56
        for (int i=0; i<n; i++)
57
        {
58
59
            memset(visitx,0,n);
            memset(visity,0,n);
60
            memset(slack,63,4*n);
61
            while (!check(i,n))
62
63
64
                 maintain(n);
65
                 memset(visitx,0,n);
66
                 memset(visity,0,n);
```

```
67
             }
68
        }
69
        int ret=0;
70
        for (int i=0;i<n;i++)</pre>
71
             ret += labx[i] + laby[i];
72
        return ret;
73
74
   int main()
75
   {
76
        int n,m;
77
        scanf("%d%d",&m,&n);
78
        for (int i=m; i<n; i++)
79
             for (int j=0; j < n; j++)
                  ma[i][j]=0;
80
        for (int i=0; i<m; i++)
81
82
             for (int j=0; j < n; j++)
                  scanf("%d",&ma[i][j]);
83
84
        printf("%d\n",Kuhn_Munkras(n));
        printf("%d", matx[0]+1);
85
        for (int i=1;i<m;i++)</pre>
86
             printf("\( \' \) \( \) matx[i]+1);
87
88
        puts("");
89
        return 0;
90 | \}
```

6.7 *二维平面图的最大流

待整理

```
1 | #include <iostream >
2
  #include <algorithm>
3 | #include <cstdio>
4 | #include <cstring>
  #include <vector>
  #include <cmath>
6
7
   #include <map>
  #include <queue>
8
9
   using namespace std;
10
11
   const int maxn = 100100;
   const int inf = 0x3f3f3f3f;
12
13
   struct Point
14
   {
15
       int x,y,id;
16
       double theta;
17
       Point() {}
18
       Point(int _x,int _y)
19
       {
20
            x = _x;
21
            y = y;
22
       }
```

```
23
       Point(Point _s,Point _e,int _id)
24
       {
            id = _id;
25
26
            x = _s.x-_e.x;
27
            y = _s.y-_e.y;
28
            theta = atan2(y,x);
29
30
       bool operator < (const Point &b)const</pre>
31
32
            return theta < b.theta;
       }
33
34
   };
35
36
   map<pair<int,int>,int > idmap;
37
   struct Edge
38
   {
39
       int from, to, next, cap, near, mark;
40
   };
   Edge edge[maxn*2];
41
   int head[maxn],L;
42
   int cntd[maxn];
43
44
   void addedge(int u,int v,int cap)
45
       cntd[u]++;
46
47
       cntd[v]++;
        idmap[make_pair(u,v)] = L;
48
49
        edge[L].from = u;
50
        edge[L].to = v;
51
        edge[L].cap = cap;
52
       edge[L].next = head[u];
53
       edge[L].mark = -1;
54
       head[u] = L++;
   }
55
56
57
   int rtp[maxn];
   Point p[maxn], tp[maxn];
58
59
   int n,m,S,T;
   int vid;
60
61
62
   struct Edge2
63
   {
64
       int to, next, dis;
   } edge2[maxn*2];
65
66
   int head2[maxn],L2;
67
68
   void addedge2(int u,int v,int dis)
   {
69
70
       edge2[L2].to = v;
71
        edge2[L2].dis = dis;
72
        edge2[L2].next = head2[u];
73
       head2[u] = L2++;
```

```
74
   }
75
76
    int dist[maxn];
    bool inq[maxn];
77
    int SPFA(int s,int t)
78
79
80
        queue < int > Q;
81
        memset(inq,false,sizeof(inq));
82
        memset(dist,63,sizeof(dist));
83
        Q.push(s);
        dist[s] = 0;
84
85
        while (!Q.empty())
86
        {
87
             int now = Q.front();
88
             Q.pop();
89
             for (int i = head2[now]; i != -1; i = edge2[i].next)
90
                 if (dist[edge2[i].to] > dist[now]+edge2[i].dis)
                 {
91
92
                      dist[edge2[i].to] = dist[now]+edge2[i].dis;
                      if (inq[edge2[i].to] == false)
93
94
                      {
95
                          inq[edge2[i].to] = true;
96
                          Q.push(edge2[i].to);
97
                      }
98
99
             inq[now] = false;
100
        }
101
        return dist[t];
102
    }
103
    int main()
104
105
    {
106
        int totcas;
        scanf("%d",&totcas);
107
        for (int cas = 1; cas <= totcas; cas++)</pre>
108
109
        {
110
             idmap.clear();
             L = 0;
111
             scanf("%d%d",&n,&m);
112
113
             S = T = 0;
             for (int i = 0; i < n; i++)
114
115
116
                 head[i] = -1;
117
                 scanf("%d%d",&p[i].x,&p[i].y);
118
                 if (p[S].x > p[i].x)
119
                      S = i;
120
                 if (p[T].x < p[i].x)
121
                      T = i;
122
                 cntd[i] = 0;
123
             }
124
             //源汇中间加入一个特殊节点
```

```
125
            head[n] = -1;
126
            n ++;
127
             addedge(S,n-1,inf);
128
             addedge(n-1,S,inf);
             addedge(T,n-1,inf);
129
130
             addedge(n-1,T,inf);
131
132
            for (int i = 0; i < m; i++)
133
            {
134
                 int u, v, cap;
135
                 scanf("%d%d%d",&u,&v,&cap);
136
137
                 v--;
138
                 addedge(u,v,cap);
139
                 addedge(v,u,cap);
            }
140
141
142
            for (int i = 0; i < n; i++)
143
            {
144
                 int tot = 0;
                 //源点汇点连到特殊点的方向需要特别考虑一下
145
146
                 if (i == S)
147
                     tp[tot++] = Point(Point(0,0), Point(-1,0), n-1);
                 else if (i == T)
148
149
                     tp[tot++] = Point(Point(0,0), Point(1,0), n-1);
150
                 else if (i == n-1)
                 {
151
152
                     tp[tot++] = Point(Point(0,0), Point(1,0),S);
153
                     tp[tot++] = Point(Point(0,0), Point(-1,0),T);
                 }
154
155
                 if (i < n-1)
156
                 {
157
                     for (int j = head[i]; j != -1; j = edge[j].next)
158
159
                          if (i == S \&\& edge[j].to == n-1)
                                                               continue;
                          if (i == T && edge[j].to == n-1) continue;
160
161
                          tp[tot++] = Point(p[i],p[edge[j].to],edge[j].to
                            );
162
                     }
                 }
163
                 sort(tp,tp+tot);
164
165
                 for (int j = 0; j < tot; j++)
166
                     rtp[tp[j].id] = j;
167
                 for (int j = head[i]; j != -1; j = edge[j].next)
168
                     edge[j].near = tp[(rtp[edge[j].to]+1)%tot].id;
169
            }
170
171
            vid = 0;
             for (int i = 0;i < L;i++)
172
173
                 if (edge[i].mark == -1)
174
                 {
```

```
175
                      int now = edge[i].from;
176
                      int eid = i;
177
                      int to = edge[i].to;
178
                      while (true)
179
                      {
180
                          edge[eid].mark = vid;
181
                          eid ^= 1;
182
                          now = to;
183
                          to = edge[eid].near;
184
                          eid = idmap[make_pair(now,to)];
185
186
                          if (now == edge[i].from)
                                                         break;
                     }
187
188
                     vid++;
                 }
189
190
             L2 = 0;
191
192
             for (int i = 0; i < vid; i++)
                 head2[i] = -1;
193
194
             for (int i = 0; i < L; i++)
                 addedge2(edge[i].mark,edge[i^1].mark,edge[i].cap);
195
196
             printf("%d\n",SPFA(edge[0].mark,edge[1].mark));
197
        }
198
        return 0;
199 }
```

6.8 强联通

```
int dfsnum[2000];
 2
   int low[2000];
   int stack [2000];
 3
   int top;
 5
   int ans;
6
   int an;
7
   int be[2000];
8
   int flag[2000];
   void dfs(int x)
9
10
   {
       dfsnum[x] = low[x] = ans++;
11
12
       stack[++top] = x;
13
       flag[x] = 1;
14
       for (int i = head[x]; i != -1; i = edge[i].next)
15
       {
16
            int y = edge[i].to;
17
            if (dfsnum[y] == -1)
18
            {
19
                dfs(y);
20
                low[x] = min(low[x], low[y]);
21
22
            else if (flag[y] == 1)
23
                low[x] = min(low[x],dfsnum[y]);
```

```
24
        }
25
        if (dfsnum[x] == low[x])
26
27
            while (stack[top] != x)
28
            {
29
                 flag[stack[top]] = 0;
                 be[stack[top]] = an;
30
31
                 top--;
32
            }
33
            flag[x] = 0;
            be[x] = an++;
34
35
            top--;
36
        }
37 | }
   调用:
   void SC()
2
   {
 3
        memset(dfsnum,-1,sizeof(dfsnum));
 4
        memset(flag,0,sizeof(flag));
 5
        top = 0;
 6
        an = 0;
 7
        ans = 0;
8
        for (int i = 0; i < n; i++)
9
            if (dfsnum[i] == -1)
10
                 dfs(i);
11 | }
```

6.9 最大团以及相关知识

- **独立集:** 独立集是指图的顶点集的一个子集,该子集的导出子图不含边.如果一个独立集不是任何一个独立集的子集,那么称这个独立集是一个极大独立集.一个图中包含顶点数目最多的独立集称为最大独立集。最大独立集一定是极大独立集,但是极大独立集不一定是最大的独立集。
- **支配集**: 与独立集相对应的就是支配集,支配集也是图顶点集的一个子集,设S是图G的一个支配集,则对于图中的任意一个顶点u,要么属于集合s,要么与s中的顶点相邻。在s中除去任何元素后s不再是支配集,则支配集s是极小支配集。称G的所有支配集中顶点个数最少的支配集为最小支配集,最小支配集中的顶点个数成为支配数。
- **最小点的覆盖**: 最小点的覆盖也是图的顶点集的一个子集,如果我们选中一个点,则称这个 点将以他为端点的所有边都覆盖了。将图中所有的边都覆盖所用顶点数最少,这个集合就 是最小的点的覆盖。
- **最大团**: 图G的顶点的子集,设D是最大团,则D中任意两点相邻。若u, v是最大团,则u,v有 边相连,其补图u,v没有边相连,所以图G的最大团=其补图的最大独立集。给定无 向图G=(V,E),如果U属于V,并且对于任意u,v包含于U 有< u,v >包含于U ,则 称U是U0 完全子图,U0 份元全子图,U0 份元全子图,U0 日本日本的一个 图中,U0 日本日本的一个 图中,U0 日本日本的一个 图中,U0 日本日本的一个 图中,U0 日本日本的一个 图中,U0 日本日本的一个 图,U0 中本的一个 U0 中本的一个

一**些性质:** 最大独立集+最小覆盖集=V,最大团=补图的最大独立集,最小覆盖集=最大匹配

```
#include <cstdio>
   bool am [100] [100];
3
   int ans;
4
   int c[100];
   int U[100][100];
   int n;
 7
   bool dfs(int rest,int num)
8
9
        if (!rest)
10
        {
11
            if (num >= ans)
                 return 1;
12
13
            else
14
                 return 0;
        }
15
16
        int pre=-1;
17
        for (int i=0;i<rest && rest-i+num>=ans;i++)
18
19
            int idx=U[num][i];
            if (num+c[idx] < ans)</pre>
20
21
                 return 0:
22
            int nrest=0;
            for (int j=i+1; j < rest; j++)
23
24
                 if (am[idx][U[num][j]])
25
                     U[num+1][nrest++]=U[num][j];
26
            if (dfs(nrest,num+1))
27
                 return 1:
28
29
        return 0;
30
   }
31
   int main()
32
33
        while (scanf("%d",&n),n)
34
35
            for (int i=0; i < n; i++)
36
                 for (int j=0; j< n; j++)
37
                      scanf("%d",&am[i][j]);
38
            ans=0;
39
            for (int i=n-1; i>=0; i--)
40
41
                 int rest=0;
42
                 for (int j=i+1; j < n; j++)
43
                      if (am[i][j])
44
                          U[0][rest++]=j;
45
                 ans+=dfs(rest,0);
46
                 c[i] = ans;
47
            }
48
            printf("%d\n",ans);
```

```
49 | }
50 | return 0;
51 |}
```

6.10 双连通分量

标号从0起

```
1 #include < cstdio >
 2 | #include < cstring >
 3 | #include < stack >
 4 | #include < queue >
   #include <algorithm >
   using namespace std;
   const int MAXN=100000*2;
8
   const int MAXM=200000;
9
   struct edges
10
   {
11
        int to, next;
12
        bool cut, visit;
13
   } edge[MAXM<<1];</pre>
   int head[MAXN],low[MAXN],dpt[MAXN],L;
14
   bool visit[MAXN], cut[MAXN];
15
16
   void init(int n)
17
   {
18
        L=0;
19
        memset (head, -1, 4*n);
20
        memset(visit,0,n);
21
   }
22
   void add_edge(int u,int v)
23
   {
24
        edge[L].cut=edge[L].visit=0;
25
        edge[L].to=v;
26
        edge[L].next=head[u];
27
        head [u] = L++;
28
   }
29
   int idx;
30 | stack < int > st;
31
   int bcc[MAXM];
   void dfs(int u,int fu,int deg)
32
33
   {
34
        cut[u]=0;
35
        visit[u]=1;
        low[u]=dpt[u]=deg;
36
37
        int tot=0;
38
        for (int i=head[u]; i!=-1; i=edge[i].next)
39
        {
40
            int v=edge[i].to;
41
            if (edge[i].visit)
42
                 continue;
43
            st.push(i/2);
44
            edge[i].visit=edge[i^1].visit=1;
```

```
if (visit[v])
45
46
             {
                 low[u] = dpt[v] > low[u] ? low[u] : dpt[v];
47
48
                 continue;
            }
49
50
            dfs(v,u,deg+1);
51
             edge[i].cut=edge[i^1].cut=(low[v]>dpt[u] || edge[i].cut);
             if (u!=fu) cut[u]=low[v]>=dpt[u]?1:cut[u];
52
53
             if (low[v] >= dpt[u] \mid | u==fu)
             {
54
55
                 while (st.top()!=i/2)
                 {
56
                      int x=st.top()*2, y=st.top()*2+1;
57
58
                      bcc[st.top()]=idx;
59
                      st.pop();
                 }
60
61
                 bcc[i/2]=idx++;
62
                 st.pop();
            }
63
            low[u] = low[v] > low[u] ? low[u] : low[v];
64
65
            tot++;
66
        }
67
        if (u==fu && tot>1) cut[u]=1;
68
   }
   int main()
69
70
   {
71
        int n,m;
72
        while (scanf("%d%d",&n,&m)!=EOF)
73
        ₹
74
             init(n);
75
            for (int i=0; i<m; i++)
             {
76
77
                 int u, v;
                 scanf("%d%d",&u,&v);
78
                 add_edge(u,v);
79
80
                 add_edge(v,u);
81
            }
82
             idx=0;
83
             for (int i=0; i<n; i++)
84
                 if (!visit[i])
85
                      dfs(i,i,0);
86
        }
87
        return 0;
88 | }
```

6.11 割点与桥

```
1 #include < cstdio >
2 #include < cstring >
3 const int MAXN = 10000;
4 struct edges
```

```
{
 5
6
        int to, next;
7
        bool cut, visit;
8
        int from;
   } edge[MAXN-1<<1];</pre>
9
   int head[MAXN],low[MAXN],dfn[MAXN],L;
   bool visit[MAXN], cut[MAXN];
   void init(int n)
12
13
14
       L=0;
15
       memset (head, -1, 4*n);
16
       memset(cut, 0, 4*n);
17
       memset(visit,0,4*n);
18
19
   void add_edge(int u,int v)
20
   {
21
        edge[L].from=u;
22
        edge[L].cut=edge[L].visit=0;
23
        edge[L].to=v;
24
        edge[L].next=head[u];
25
        head [u]=L++;
26
   }
27
   int idx;
28
   void dfs(int u,int fu)
29
   {
30
        visit[u]=1;
        low[u]=dfn[u]=idx++;
31
32
        int tot=0;
33
        for (int i=head[u]; i!=-1; i=edge[i].next)
34
        {
35
            int v=edge[i].to;
            if (edge[i].visit)
36
37
                 continue;
38
            edge[i].visit=edge[i^1].visit=1;
            if (visit[v])
39
40
            {
41
                 low[u]=dfn[v]>low[u]?low[u]:dfn[v];
42
                 continue;
43
            }
44
            dfs(v,u);
45
            edge[i].cut=edge[i^1].cut=low[v]>dfn[u] || edge[i].cut;
            if (u!=fu) cut[u]=low[v]>=dfn[u]?1:cut[u];
46
            low[u] = low[v] > low[u] ? low[u] : low[v];
47
48
            tot++;
49
        if (u==fu && tot>1) cut[u]=1;
50
51
   }
52
   int main()
53
54
        int t;
55
        scanf("%d",&t);
```

```
while (t--)
56
57
        {
58
            int n,m;
59
            scanf("%d%d",&n,&m);
60
            init(n);
            for (int i=0; i<m; i++)
61
            {
62
63
                 int u,v;
64
                 scanf("%d%d",&u,&v);
65
                 add_edge(--u,--v);
66
                 add_edge(v,u);
            }
67
            for (int i=0; i<n; i++)
68
                 if (!visit[i])
69
70
                 {
71
                     idx=0;
72
                     dfs(i,i);
                 }
73
74
        }
75
        return 0;
76 | }
          LCA
   6.12
   在线LCA, bfs
 1 | #include < cstdio >
2 | #include < cstring >
3 | #include < queue >
4 using namespace std;
5
   const int NSIZE = 50000;
6
   const int DEG = 20;
7
   struct trees
8
9
10
        int fa[DEG];
11
        int head, deg;
12
   } tree[NSIZE];
13 struct edges
14
15
        int to , next;
16
   } edge[NSIZE];
17
   struct states
18
   {
19
        int u,fu,deg;
20
   };
21
   int L;
22
   void add_edge(int x, int y)
23
24
        edge[L].to = y;
25
        edge[L].next = tree[x].head;
26
        tree[x].head = L++;
```

27 | }

```
28
  int Root;
29
   void BFS(int s)
30
   {
31
       queue < states > que;
32
        states st;
33
        st.deg=0;
34
        st.fu=st.u=s;
35
       que.push(st);
36
       while(!que.empty())
37
       {
38
            states st=que.front();
39
            que.pop();
            tree[st.u].deg = st.deg;
40
            tree[st.u].fa[0] = st.fu;
41
            for (int i=1;i<DEG;i++)</pre>
42
43
                tree[st.u].fa[i]=s;
44
            for (int tmp=st.fu,num=1;tree[tmp].deg;tmp=tree[st.u].fa[
               num++])
45
                 tree[st.u].fa[num]=tree[tmp].fa[num-1];
            for(int i = tree[st.u].head ; i != -1; i = edge[i].next)
46
47
48
                int v = edge[i].to;
49
                if (v == st.fu) continue;
50
                states nst;
                nst.u=v;
51
52
                nst.fu=st.u;
53
                nst.deg=st.deg+1;
                que.push(nst);
54
55
            }
56
       }
57
   int LCA(int x, int y)
58
59
        if(tree[x].deg > tree[y].deg) swap(x,y);
60
        int hx=tree[x].deg,hy=tree[y].deg;
61
62
        int tx=x,ty=y;
63
        for (int det=hy-hx, i=0; det; det>>=1, i++)
64
            if (det&1)
65
                ty=tree[ty].fa[i];
66
        if(tx == ty) return tx;
       for (int i=DEG-1; i>=0; i--)
67
68
       {
            if(tree[tx].fa[i] == tree[ty].fa[i])
69
70
                 continue;
            tx = tree[tx].fa[i];
71
72
            ty = tree[ty].fa[i];
73
       }
74
       return tree[tx].fa[0];
75
76
  int main()
77
  | {
```

```
78
        int t;
79
         scanf("%d",&t);
        while(t--)
80
81
        {
82
             int n;
             scanf("%d",&n);
83
             L = 0;
84
85
             for(int i = 0; i < n; i++)
86
                  tree[i].head = -1;
             for(int i = 0; i < n-1; i++)
87
88
             {
89
                  int a,b;
                  scanf("%d%d",&a ,&b);
90
91
                  add_edge(a-1,b-1);
92
                  add_edge(b-1,a-1);
             }
93
94
             Root = 0;
95
             BFS(Root);
96
             int a,b;
             scanf("%d%d",&a,&b);
97
98
             int lca=LCA(a-1,b-1)+1;
99
             printf("%d\n",lca);
100
        }
101
        return 0;
102 }
```

6.13 最优比例生成树

```
1 #include < stdio.h>
 2 | #include < string . h >
 3 | #include < math.h >
4 struct
5
   {
6
        int x,y;
7
        double z;
8
   } node[1100];
9
   struct
10
   {
11
        double 1,c;
12
   } map[1100][1100];
   int n,1,f[1100],pre[1100];
   double dis[1100];
14
15
   double mst(double x)
16
   {
17
        int i,j,tmp;
18
        double min, s=0, t=0;
19
        memset(f,0,sizeof(f));
20
        f[1]=1;
21
        for (i=2; i \le n; i++)
22
        {
23
            dis[i]=map[1][i].c-map[1][i].l*x;
```

```
24
            pre[i]=1;
25
        }
        for (i=1; i<n; i++)
26
27
        {
28
            min=1e10;
29
            for (j=1; j \le n; j++)
                 if (!f[j] && min>dis[j])
30
31
                 {
32
                     min=dis[j];
33
                     tmp=j;
34
                 }
35
            f[tmp]=1;
            t+=map[pre[tmp]][tmp].1;
36
37
            s+=map[pre[tmp]][tmp].c;
38
            for (j=1; j \le n; j++)
39
                 if (!f[j] && map[tmp][j].c-map[tmp][j].l*x<dis[j])</pre>
40
                     dis[j]=map[tmp][j].c-map[tmp][j].l*x;
41
42
                     pre[j]=tmp;
                 }
43
44
        }
45
        return s/t;
46
   }
47
   int main()
48
   {
49
        int i,j;
50
        double a,b;
        scanf("%d",&n);
51
52
        while (n)
53
        {
54
            for (i=1; i<=n; i++)
55
                 scanf("%d%d%lf",&node[i].x,&node[i].y,&node[i].z);
            for (i=1; i<=n; i++)
56
                 for (j=i+1; j \le n; j++)
57
                 {
58
59
                     map[j][i].l=map[i][j].l=sqrt(1.0*(node[i].x-node[j
                        ].x)*(node[i].x-node[j].x)+(node[i].y-node[j].y)
                        *(node[i].y-node[j].y));
                     map[j][i].c=map[i][j].c=fabs(node[i].z-node[j].z);
60
                 }
61
62
            a=0, b=mst(a);
            while (fabs(b-a)>1e-8)
63
64
            {
65
                 a=b;
66
                 b=mst(a);
67
68
            printf("%.3f\n",b);
69
            scanf("%d",&n);
70
       }
71 | }
```

6.14 全局最小割

```
1 #include <iostream>
2
   using namespace std;
3
   const int maxn=510;
   int map[maxn][maxn];
   int n;
6
   void contract(int x,int y)
7
8
       int i,j;
9
       for (i=0; i< n; i++)
10
            if (i!=x) map[x][i]+=map[y][i],map[i][x]+=map[i][y];
11
       for (i=y+1; i < n; i++) for (j=0; j < n; j++)
12
13
                map[i-1][j]=map[i][j];
14
                map[j][i-1]=map[j][i];
15
            }
16
       n--;
17
   }
18
   int w[maxn],c[maxn];
19
   int sx,tx;
20
   int mincut()
21
   {
22
       int i,j,k,t;
23
       memset(c,0,sizeof(c));
24
       c[0]=1;
25
       for (i=0; i< n; i++) w[i]=map[0][i];
26
       for (i=1; i+1 < n; i++)
27
       {
28
            t = k = -1;
29
            for (j=0; j< n; j++) if (c[j]==0\&\&w[j]>k)
30
                     k=w[t=j];
31
            c[sx=t]=1;
32
            for (j=0; j< n; j++) w[j]+=map[t][j];
33
34
       for (i=0; i< n; i++) if (c[i]==0) return w[tx=i];
35
   }
36
   int main()
37
   {
38
       int i,j,k,m;
39
       while (scanf("%d%d",&n,&m)!=EOF)
40
41
            memset(map,0,sizeof(map));
42
            while (m--)
43
            {
44
                 scanf("%d%d%d",&i,&j,&k);
45
                map[i][j]+=k;
46
                map[j][i]+=k;
47
48
            int mint = 999999999;
49
            while (n>1)
```

```
{
50
51
                 k=mincut();
52
                 if (k<mint) mint=k;</pre>
                 contract(sx,tx);
53
             }
54
55
            printf("%d\n",mint);
56
57
        return 0;
58 | }
          欧拉路
   6.15
           有向图
   6.15.1
   void solve(int x)
1
2
3
        int i;
4
        if (!match[x])
5
        {
6
            path[++1] = x;
7
             return ;
8
        }
        for (i=1; i<=n; i++)
9
             if (b[x][i])
10
11
             {
12
                 b[x][i]--;
13
                 match[x]--;
14
                 solve(i);
15
16
        path[++1] = x;
17 | }
          无向图
   6.15.2
   void solve(int x)
2
   {
3
        int i;
4
        if (!match[x])
 5
        {
6
            path[++1]=x;
7
             return ;
8
        for (i=1; i<=n; i++)
9
             if (b[x][i])
10
11
12
                 b[x][i]--;
                 b[i][x]--;
13
14
                 match[x]--;
15
                 match[i]--;
16
                 solve(i);
17
             }
18
        path[++1] = x;
```

19 }

6.15.3 混合图

```
zju1992
   int in [MAXN+100], out [MAXN+100];
 2
   int main()
3
   {
4
        int t;
5
        scanf("%d",&t);
        while (t--)
6
7
        {
8
            int n,m;
            scanf("%d%d",&n,&m);
9
10
            N=n+2; L=-1;
11
            for (int i=0; i<N; i++)
12
                 head[i]=-1;
            memset(in,0,sizeof(in));
13
14
            memset(out,0,sizeof(out));
15
16
            for (int i=0; i < m; i++)
17
            {
18
                 int x,y,z;
19
                 scanf("%d%d%d",&x,&y,&z);
20
                 in[y]++; out[x]++;
21
                 if (!z)
22
                     add_edge(x,y,1);
            }
23
24
            int flag=1;
25
            for (int i=1;i<=n;i++)
26
            {
27
                 if (in[i]-out[i]>0)
28
                     add_edge(i,n+1,(in[i]-out[i])/2);
29
                 else
                 if (out[i]-in[i]>0)
30
                     add_edge(0,i,(out[i]-in[i])/2);
31
                 //printf("%d %d %d\n",i,out[i],in[i]);
32
                 if ((in[i]+out[i])&1)
33
34
35
                     flag=0;
36
                     break;
                 }
37
38
            }
39
            maxflow(0,n+1);
40
            for (int i=head[0];i!=-1;i=edge[i].next)
                 if (edge[i].cap>0 && edge[i].cap>edge[i].flow)
41
42
                 {
43
                     flag=0;
44
                     break;
45
                 }
46
            if (flag)
47
                 puts("possible");
48
            else
```

```
49 puts("impossible");
50 }
51 return 0;
52 }
```

6.16 K短路

```
1 #include < cstdio >
2 | #include < cstring >
3
  #include < queue >
 4 \mid \text{using namespace std};
 5
   int K;
   class states
6
7
   public:
8
9
        int cost, id;
10
   };
11
   int dist[1000];
12
   class cmp
13
14
   public:
15
        bool operator ()(const states &i,const states &j)
16
        {
17
            return i.cost>j.cost;
18
        }
19
   };
20
   class cmp2
21
   {
22
   public:
23
        bool operator ()(const states &i,const states &j)
24
        {
25
            return i.cost+dist[i.id]>j.cost+dist[j.id];
26
        }
27
   };
28
   struct edges
29
   {
30
        int to,next,cost;
31
   } edger[100000], edge[100000];
   int headr [1000], head [1000], Lr, L;
32
33
   void dijkstra(int s)
34
35
        states u;
36
        u.id=s;
37
        u.cost=0;
38
        dist[s]=0;
39
        priority_queue < states , vector < states > , cmp > q;
40
        q.push(u);
        while (!q.empty())
41
42
        {
43
            u=q.top();
44
            q.pop();
```

```
if (u.cost!=dist[u.id]) continue;
45
46
            for (int i=headr[u.id]; i!=-1; i=edger[i].next)
47
48
                 states v=u;
49
                 v.id=edger[i].to;
                 if (dist[v.id]>dist[u.id]+edger[i].cost)
50
                 {
51
52
                     v.cost=dist[v.id]=dist[u.id]+edger[i].cost;
53
                     q.push(v);
                 }
54
            }
55
       }
56
57
   }
58
   int num [1000];
59
   void init(int n)
60
   {
61
       Lr=L=0;
62
       memset (head, -1, 4*n);
63
       memset(headr,-1,4*n);
64
       memset(dist,63,4*n);
65
        memset(num,0,4*n);
66
67
   void add_edge(int u,int v,int x)
68
   {
69
        edge[L].to=v;
70
        edge[L].cost=x;
71
        edge[L].next=head[u];
        head[u]=L++;
72
73
        edger[Lr].to=u;
74
        edger[Lr].cost=x;
75
        edger[Lr].next=headr[v];
        headr[v]=Lr++;
76
77
   }
78
   int a_star(int s,int t)
79
   {
        if (dist[s]==0x3f3f3f3f)
80
81
            return -1;
82
        priority_queue < states , vector < states > , cmp2 > q;
83
        states tmp;
84
        tmp.id=s;
        tmp.cost=0;
85
86
        q.push(tmp);
        while (!q.empty())
87
88
        {
89
            states u=q.top();
90
            q.pop();
            num [u.id]++;
91
92
            if (num[t] == K)
93
                 return u.cost;
94
            for (int i=head[u.id]; i!=-1; i=edge[i].next)
95
```

```
96
                  int v=edge[i].to;
97
                  tmp.id=v;
98
                  tmp.cost=u.cost+edge[i].cost;
99
                  q.push(tmp);
             }
100
         }
101
102
         return -1;
103
    }
104
    int main()
105
    {
106
         int n,m;
         scanf("%d%d",&n,&m);
107
         init(n);
108
         for (int i=0; i<m; i++)
109
110
111
             int u, v, x;
112
             scanf("%d%d%d",&u,&v,&x);
113
             add_edge(u-1,v-1,x);
         }
114
115
         int s,t;
116
         scanf("%d%d%d",&s,&t,&K);
117
         if (s==t)
118
             K++;
119
         dijkstra(t-1);
120
         printf("%d\n",a_star(s-1,t-1));
121
   }
```

6.17 稳定婚姻

假定有n个男生和M个女生,理想的拍拖状态就是对于每对情侣(a,b),找不到另一对情侣(c,d)使得c更喜欢b,b也更喜欢c,同理,对a来说也没有(e,f)使得a更喜欢e而e更喜欢a,当然最后会有一些人落单。这样子一个状态可以称为理想拍拖状态,它也有一个专业的名词叫稳定婚姻。求解这个问题可以用一个专有的算法,延迟认可算法,其核心就是让每个男生按自己喜欢的顺序逐个向女生表白,例如leokan向一个女生求爱,这个过程中,若这个女生没有男朋友,那么这个女生就暂时成为leokan的女朋友,或这个女生喜欢她现有男朋友的程度没有喜欢leokan高,这个女生也暂时成为leokan的女朋友,而她原有的男朋友则再将就找下一个次喜欢的女生来当女朋友。

```
1 | #include < string . h >
2
   #include < stdio.h>
   #define N 1050
4
   int boy[N][N];
   int girl[N][N];
6
   int ans[N];
7
   int cur[N];
8
   int n;
9
   void getMarry(int g)
10
11
     for (int i=ans[g]+1;i<n;i++)
12
13
        int b=girl[g][i]-1;
14
        if (cur[b]<0)
15
        {
```

```
16
          ans[g]=i;
17
          cur[b]=g;
18
          return;
19
        }
20
        int og=cur[b];
        if (boy[b][og] > boy[b][g])
21
22
23
          cur[b]=g;
24
          ans[g]=i;
          getMarry(og);
25
26
          return;
27
        }
28
     }
29
   };
30
   int main()
31
   {
32
     int t,a;
33
     scanf("%d",&t);
     while(t--)
34
35
        memset(girl,0,sizeof(girl));
36
37
        memset(boy,0,sizeof(boy));
38
        scanf("%d",&n);
39
        for (int i=0; i < n; i++)
          for (int j=0; j < n; j++)
40
            scanf("%d",&girl[i][j]);
41
42
        for (int i=0; i < n; i++)
43
          for (int j=0; j < n; j++)
44
          {
45
            scanf("%d",&a);
46
            boy[i][a-1]=j;
47
          }
        memset(cur,0xff,sizeof(cur));
48
49
        memset(ans,0xff,sizeof(ans));
        for (int i=0; i < n; i++)
50
          getMarry(i);
51
52
        for (int i=0;i<n;i++)
53
          printf("%d\n",girl[i][ans[i]]);
54
     }
55
     return 0;
56 | }
```

6.18 最小树形图

```
1 const int inf = 19921005;
2 int n,m,u,v,cost,dis[1001][1001],L;
3 
4 void init(int n)
5 {
6     L = 0;
7     for (int i = 0; i < n; i++)</pre>
```

```
8
            for (int j = 0; j < n; j++)
9
                dis[i][j] = inf;
10
   }
11
12 struct Edge
13
14
       int u,v,cost;
15
   };
16
17
   Edge e[1001*1001];
18
19
   int pre[1001], id[1001], visit[1001], in[1001];
20
21
   int zhuliu(int root,int n,int m,Edge e[])
22
   {
23
       int res = 0,u,v;
24
       while (true)
25
       {
26
            for (int i = 0; i < n; i++)
27
                in[i] = inf;
            for (int i = 0; i < m; i++)
28
29
                if (e[i].u != e[i].v && e[i].cost < in[e[i].v])</pre>
30
31
                     pre[e[i].v] = e[i].u;
32
                     in[e[i].v] = e[i].cost;
                }
33
34
            for (int i = 0; i < n; i++)
35
                if (i != root)
36
                     if (in[i] == inf) return -1;
37
            int tn = 0;
38
            memset(id,-1,sizeof(id));
39
            memset(visit,-1,sizeof(visit));
            in[root] = 0;
40
            for (int i = 0; i < n; i++)
41
42
43
                res += in[i];
44
                v = i;
45
                while (visit[v] != i \&\& id[v] == -1 \&\& v != root)
46
                {
47
                     visit[v] = i;
48
                     v = pre[v];
49
                if(v != root && id[v] == -1)
50
51
                {
52
                     for(int u = pre[v] ; u != v ; u = pre[u])
53
                         id[u] = tn;
54
                     id[v] = tn++;
                }
55
56
57
            if(tn == 0)
                            break;
58
            for (int i = 0; i < n; i++)
```

```
59
                 if (id[i] == -1)
60
                      id[i] = tn++;
             for (int i = 0; i < m;)
61
62
             {
63
                 int v = e[i].v;
                 e[i].u = id[e[i].u];
64
                 e[i].v = id[e[i].v];
65
                 if (e[i].u != e[i].v)
66
                      e[i++].cost -= in[v];
67
68
                 else
69
                      swap(e[i],e[--m]);
70
             }
71
             n = tn;
72
             root = id[root];
73
        }
74
        return res;
75
   }
76
77
    int main()
78
    {
        freopen("in.txt","r",stdin);
79
80
        while (scanf("%d%d",&n,&m) != EOF)
81
        {
82
             init(n);
83
             for (int i = 0; i < m; i++)
84
85
                 scanf("%d%d%d",&u,&v,&cost);
                 if (u == v) continue;
86
87
                 dis[u][v] = min(dis[u][v],cost);
88
             }
             L = 0;
89
             for (int i = 0; i < n; i++)
90
                 for (int j = 0; j < n; j++)
91
92
                      if (dis[i][j] != inf)
93
                      {
94
                          e[L].u = i;
95
                          e[L].v = j;
96
                          e[L++].cost = dis[i][j];
97
98
             printf("%d\n",zhuliu(0,n,L,e));
99
        }
100
        return 0;
101 | }
```

7 计算几何

7.1 基本函数

7.1.1 Point定义

15

```
struct Point
1
2
3
       double x, y;
4
       Point() {}
5
       Point(double _x, double _y)
6
       {
7
           x = _x, y = _y;
8
       }
9
       Point operator -(const Point &b)const
10
11
            return Point(x - b.x, y - b.y);
12
       }
13
       double operator *(const Point &b)const
14
15
            return x * b.y - y * b.x;
16
       }
17
       double operator &(const Point &b)const
18
       {
19
           return x * b.x + y * b.y;
20
       void transXY(double B)
21
22
23
            double tx = x, ty = y;
24
           x = tx*cos(B) - ty*sin(B);
           y = tx*sin(B) + ty*cos(B);
25
26
       }
27 | };
   7.1.2 Line定义
1 struct Line
2
   {
3
       Point s, e;
4
       double k;
5
       Line() {}
6
       Line(Point _s, Point _e)
7
       {
8
            s = _s, e = _e;
9
           k = atan2(e.y - s.y, e.x - s.x);
10
11
       Point operator &(const Line &b)const
12
       {
13
            Point res = s;
            //注意: 有些题目可能会有直线相交或者重合情况
14
```

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//可以把返回值改成pair<Point,int>来返回两直线的状态。

```
double t = ((s - b.s) * (b.s - b.e)) / ((s - e) * (b.s - b.
16
              e));
17
           res.x += (e.x - s.x) * t;
18
           res.y += (e.y - s.y) * t;
19
           return res;
20
       }
21 | };
   7.1.3 距离: 两点距离
1 double dist2(Point a, Point b)
2
3
       return (a.x - b.x) * (a.x - b.x) + (a.y - b.y) * (a.y - b.y);
4 | }
   7.1.4 距离:点到直线距离
   result:点到直线最近点
1 | Point NPT(Point P, Line L)
2
   {
3
       Point result;
4
       double a, b, t;
5
6
       a = L.p2.x - L.p1.x;
7
       b = L.p2.y - L.p1.y;
8
       t = ((P.x - L.p1.x) * a + (P.y - L.p1.y) * b) / (a * a + b *
9
10
       result.x = L.p1.x + a * t;
11
       result.y = L.p1.y + b * t;
12
       return dist2(P, result);
13 | }
        距离: 点到线段距离
   7.1.5
   res: 点到线段最近点
  double dist2(Point p1, Point p2, Point p)
2
   {
3
       Point res;
4
       double a, b, t;
5
       a = p2.x - p1.x;
6
       b = p2.y - p1.y;
7
       t = ((p.x - p1.x) * a + (p.y - p1.y) * b) / (a * a + b * b);
       if (t >= 0 \&\& t <= 1)
8
9
       {
10
           res.x = p1.x + a * t;
11
           res.y = p1.y + b * t;
12
       }
13
       else
14
       {
15
           if (dist2(p, p1) < dist2(p, p2))
16
               res = p1;
```

```
17
           else
18
               res = p2;
19
20
       return dist2(p, res);
21 | }
   旧版
  double CalcDis(Point a, Point s, Point e) //点到线段距离
2
3
       if (pmult(Point(s,e),Point(s,a)) < 0 || pmult(Point(e,s),Point(
          e,a)) < 0)
4
           return min(CalcDis(a,s),CalcDis(a,e));
5
       return abs(xmult(Point(a,s),Point(a,e)))/CalcDis(s,e);
6
  }
        面积: 多边形
   7.1.6
   点按逆时针排序。
  double CalcArea(Point p[], int n)
2
   {
3
       double res = 0;
4
       for (int i = 0; i < n; i++)
5
           res += (p[i] * p[(i + 1) % n]) / 2;
6
       return res;
7
  }
   7.1.7
        判断:线段相交
  bool inter(Line 11, Line 12)
1
2
   {
3
       return (\max(11.s.x,11.e.x) >= \min(12.s.x,12.e.x) \&\&
4
               \max(12.s.x, 12.e.x) >= \min(11.s.x, 11.e.x) &&
               \max(11.s.y, 11.e.y) >= \min(12.s.y, 12.e.y) &&
5
6
               \max(12.s.y, 12.e.y) >= \min(11.s.y, 11.e.y) &&
7
                ((12.s-11.s)*(11.e-11.s))*((12.e-11.s)*(11.e-11.s)) <=
8
                ((11.s-12.s)*(12.e-12.s))*((11.e-12.s)*(12.e-12.s)) <=
                  0);
9 }
   7.2
        圆
   7.2.1
       面积:两圆相交
   圆不可包含
1 double dis(int x, int y)
2
   {
3
       return sqrt((double)(x*x+y*y));
4
5
  double area(int x1,int y1,int x2,int y2,double r1,double r2)
6
  | {
```

```
7
       double s=dis(x2-x1,y2-y1);
8
       if (r1+r2 < s) return 0;
9
       else if(r2-r1>s) return PI*r1*r1;
       else if(r1-r2>s) return PI*r2*r2;
10
       double q1=acos((r1*r1+s*s-r2*r2)/(2*r1*s));
11
12
       double q2=acos((r2*r2+s*s-r1*r1)/(2*r2*s));
       return (r1*r1*q1+r2*r2*q2-r1*s*sin(q1));
13
14 | }
         三角形外接圆
   7.2.2
   void CircumscribedCircle()
2
   {
3
       for (int i = 0; i < 3; i++)
4
            scanf("%lf%lf",&p[i].x,&p[i].y);
5
       tp = Point((p[0].x+p[1].x)/2,(p[0].y+p[1].y)/2);
6
       1[0] = Line(tp, Point(tp.x-(p[1].y-p[0].y), tp.y+(p[1].x-p[0].x))
          );
7
       tp = Point((p[0].x+p[2].x)/2,(p[0].y+p[2].y)/2);
8
       1[1] = Line(tp, Point(tp.x-(p[2].y-p[0].y), tp.y+(p[2].x-p[0].x))
          );
9
       tp = LineToLine(1[0],1[1]);
       r = Point(tp,p[0]).Length();
10
11
       printf("(\%.6f,\%.6f,\%.6f)\n",tp.x,tp.y,r);
12 | }
   7.2.3 三角形内切圆
   void InscribedCircle()
2
   {
3
       for (int i = 0; i < 3; i++)
4
            scanf("%lf%lf",&p[i].x,&p[i].y);
       if (xmult(Point(p[0],p[1]),Point(p[0],p[2])) < 0)</pre>
5
6
           swap(p[1],p[2]);
7
       for (int i = 0; i < 3; i++)
8
            len[i] = Point(p[i],p[(i+1)%3]).Length();
       tr = (len[0]+len[1]+len[2])/2;
9
       r = sqrt((tr-len[0])*(tr-len[1])*(tr-len[2])/tr);
10
11
       for (int i = 0; i < 2; i++)
12
       {
           v = Point(p[i], p[i+1]);
13
           tv = Point(-v.y,v.x);
14
15
           tr = tv.Length();
           tv = Point(tv.x*r/tr,tv.y*r/tr);
16
17
           tp = Point(p[i].x+tv.x,p[i].y+tv.y);
18
           l[i].s = tp;
19
           tp = Point(p[i+1].x+tv.x,p[i+1].y+tv.y);
20
           l[i].e = tp;
21
       }
22
       tp = LineToLine(1[0],1[1]);
23
       printf("(\%.6f,\%.6f,\%.6f)\n",tp.x,tp.y,r);
24 | }
```

7.2.4 点对圆的两个切点

```
void calc_qie(Point poi,Point o,double r,Point &result1,Point &
      result2) {
2
       double line=sqrt((poi.x-o.x)*(poi.x-o.x)+(poi.y-o.y)*(poi.y-o.y
3
       double angle=acos(r/line);
4
       Point unitvector, lin;
5
       lin.x=poi.x-o.x;
6
       lin.y=poi.y-o.y;
7
       unitvector.x=lin.x/sqrt(lin.x*lin.x+lin.y*lin.y)*r;
8
       unitvector.y=lin.y/sqrt(lin.x*lin.x+lin.y*lin.y)*r;
9
       result1=Rotate(unitvector, -angle);
10
       result2=Rotate(unitvector, angle);
11
       result1.x+=o.x;
12
       result1.y+=o.y;
       result2.x+=o.x;
13
14
       result2.y+=o.y;
15
       return;
16 }
         两圆公切点
   7.2.5
  void Gao()
2
   {
3
       tn = 0;
4
       Point a,b,vab;
5
       double tab, tt, dis, theta;
6
       for (int i = 0; i < tc; i++)
7
           for (int j = 0; j < tc; j++)
8
                if (i != j)
9
                {
10
                    a = c[i];
                    b = c[j];
11
12
                    vab = Point(a,b);
                    tab = atan2(vab.y,vab.x);
13
14
                    dis = sqrt(vab.x*vab.x+vab.y*vab.y);
15
                    if (b.r > a.r)
                        tt = asin((b.r-a.r)/dis);
16
17
                    else
                        tt = -asin((a.r-b.r)/dis);
18
                    theta = tab+pi/2+tt;
19
20
                    tp[tn++] = Point(a.x+a.r*cos(theta),a.y+a.r*sin(
21
                    tp[tn++] = Point(b.x+b.r*cos(theta),b.y+b.r*sin(
                       theta));
22
                }
23 | }
```

7.3 矩阵

7.3.1 基本矩阵

按向量(x,y,z)平移:

$$\begin{pmatrix} 1 & 0 & 0 & x \\ 0 & 1 & 0 & y \\ 0 & 0 & 1 & z \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

按比例(x,y,z)缩放:

$$\begin{pmatrix} x & 0 & 0 & 0 \\ 0 & y & 0 & 0 \\ 0 & 0 & z & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

绕向量(x, y, z)旋转angle角度:

$$\begin{pmatrix} x^2\times (1-c)+c & x\times y\times (1-c)-z\times s & x\times z\times (1-c)+y\times s & 0\\ y\times x\times (1-c)+z\times s & y^2\times (1-c)+c & y\times z\times (1-c)-x\times s & 0\\ x\times z\times (1-c)-y\times s & y\times z\times (1-c)+x\times s & z^2\times (1-c)+c & 0\\ 0 & 0 & 1 \end{pmatrix} \begin{cases} s=sin(angle)\\ c=cos(angle)\end{cases}$$

7.3.2 刘汝佳的几何教室

```
const double pi = acos(-1.0);
1
2
3 \mid \text{int n,m,q};
4
   struct Point
5
6
       double a,b,c,d;
7
   Point p[50000],f[50000];
8
9
10
   double a,b,c,theta,mt[4][4],tmp[4][4],tmt[4][4],rmt[4][8];
   char com [20];
11
12
13
   void TRANSLATE()
14
   {
15
       memset(tmt,0,sizeof(tmt));
       tmt[0][0] = tmt[1][1] = tmt[2][2] = tmt[3][3] = 1;
16
17
       tmt[3][0] = a;
       tmt[3][1] = b;
18
19
       tmt[3][2] = c;
20
       memset(tmp,0,sizeof(tmp));
       for (int i = 0; i < 4; i++)
21
            for (int j = 0; j < 4; j++)
22
                for (int k = 0; k < 4; k++)
23
24
                    tmp[i][j] += mt[i][k]*tmt[k][j];
25
       for (int i = 0; i < 4; i++)
26
            for (int j = 0; j < 4; j++)
```

```
27
                mt[i][j] = tmp[i][j];
28
   }
29
30
   void ROTATE()
31
32
       theta = -theta*pi/180;
33
       memset(tmt,0,sizeof(tmt));
34
       tmt[3][3] = 1;
35
       tmt[0][0] = cos(theta)+(1-cos(theta))*a*a;
       tmt[1][0] = (1-cos(theta))*a*b+c*sin(theta);
36
37
       tmt[2][0] = (1-cos(theta))*a*c-b*sin(theta);
38
       tmt[0][1] = (1-cos(theta))*a*b-c*sin(theta);
39
       tmt[1][1] = cos(theta) + (1-cos(theta))*b*b;
       tmt[2][1] = (1-cos(theta))*b*c+a*sin(theta);
40
41
       tmt[0][2] = (1-cos(theta))*a*c+b*sin(theta);
42
       tmt[1][2] = (1-cos(theta))*b*c-a*sin(theta);
43
       tmt[2][2] = cos(theta) + (1-cos(theta))*c*c;
44
       memset(tmp,0,sizeof(tmp));
       for (int i = 0; i < 4; i++)
45
            for (int j = 0; j < 4; j++)
46
                for (int k = 0; k < 4; k++)
47
48
                    tmp[i][j] += mt[i][k]*tmt[k][j];
49
       for (int i = 0; i < 4; i++)
            for (int j = 0; j < 4; j++)
50
                mt[i][j] = tmp[i][j];
51
52
   }
53
54
   void SCALE()
55
   {
56
       memset(tmt,0,sizeof(tmt));
       tmt[0][0] = a;
57
58
       tmt[1][1] = b;
59
       tmt[2][2] = c;
60
       tmt[3][3] = 1;
       memset(tmp,0,sizeof(tmp));
61
       for (int i = 0; i < 4; i++)
62
63
            for (int j = 0; j < 4; j++)
64
                for (int k = 0; k < 4; k++)
65
                    tmp[i][j] += mt[i][k]*tmt[k][j];
       for (int i = 0; i < 4; i++)
66
            for (int j = 0; j < 4; j++)
67
                mt[i][j] = tmp[i][j];
68
69
   }
70
71
   void solvep(Point p)
72
   {
73
       memset(tmt,0,sizeof(tmt));
74
       tmt[0][0] = p.a;
75
       tmt[0][1] = p.b;
76
       tmt[0][2] = p.c;
77
       tmt[0][3] = 1;
```

```
78
        memset(tmp,0,sizeof(tmp));
79
         for (int i = 0; i < 1; i++)
             for (int j = 0; j < 4; j++)
80
81
                  for (int k = 0; k < 4; k++)
82
                      tmp[i][j] += tmt[i][k]*mt[k][j];
83
        printf("%.2f_{\perp}%.2f_{\parallel}%.2f_{\parallel}, tmp[0][0], tmp[0][1], tmp[0][2]);
    }
84
85
    void solvef(Point f)
86
87
    {
88
        memset(tmt,0,sizeof(tmt));
        tmt[0][0] = f.a;
89
        tmt[1][0] = f.b;
90
        tmt[2][0] = f.c;
91
92
        tmt[3][0] = 0;
93
        memset(tmp,0,sizeof(tmp));
        for (int i = 0; i < 4; i++)
94
95
             for (int j = 0; j < 1; j++)
                 for (int k = 0; k < 4; k++)
96
                      tmp[i][j] += mt[i][k]*tmt[k][j];
97
98
         tmp[3][0] += f.d;
99
         double kk = tmp[0][0]*tmp[0][0]+tmp[1][0]*tmp[1][0]+tmp[2][0]*
            tmp[2][0];
100
        kk = sqrt(1/kk);
         for (int i = 0; i < 4; i++)
101
             printf("%.2f",tmp[i][0]*kk);
102
        printf("\n");
103
104
    }
105
106
    void solvermt()
107
        memset(rmt,0,sizeof(rmt));
108
        for (int i = 0; i < 4; i++)
109
             for (int j = 0; j < 4; j++)
110
                  rmt[i][j] = mt[i][j];
111
112
        rmt[0][4] = rmt[1][5] = rmt[2][6] = rmt[3][7] = 1;
113
        for (int i = 0; i < 4; i++)
114
        {
115
             for (int j = i; j < 4; j++)
116
                  if (fabs(rmt[j][i]) > 1e-8)
117
                  {
118
                      for (int k = i; k < 8; k++)
                           swap(rmt[i][k],rmt[j][k]);
119
120
                      break;
121
                 }
122
             double tt = rmt[i][i];
123
             for (int j = i; j < 8; j++)
124
                 rmt[i][j] /= tt;
125
             for (int j = 0; j < 4; j++)
126
                 if (i != j)
127
                  {
```

```
128
                     tt = rmt[j][i];
129
                      for (int k = i; k < 8; k++)
                          rmt[j][k] -= rmt[i][k]*tt;
130
131
                 }
132
        for (int i = 0; i < 4; i++)
133
             for (int j = 0; j < 4; j++)
134
135
                 mt[i][j] = rmt[i][4+j];
136
    }
137
138
    int main()
139
140
        scanf("%d%d%d",&n,&m,&q);
        for (int i = 0; i < n; i++)
141
142
             scanf("%lf%lf%lf",&p[i].a,&p[i].b,&p[i].c);
143
        for (int i = 0; i < m; i++)
144
             scanf("%lf%lf%lf%lf",&f[i].a,&f[i].b,&f[i].c,&f[i].d);
        memset(mt,0,sizeof(mt));
145
        mt[0][0] = mt[1][1] = mt[2][2] = mt[3][3] = 1;
146
147
        for (int i = 0; i < q; i++)
148
        {
149
             scanf("%s",com);
150
             if (strcmp(com, "TRANSLATE") == 0)
151
             {
152
                 scanf("%lf%lf%lf",&a,&b,&c);
153
                 TRANSLATE();
154
             }
155
             else if (strcmp(com, "ROTATE") == 0)
156
157
                 scanf("%lf%lf%lf%lf",&a,&b,&c,&theta);
                 ROTATE();
158
             }
159
             else if (strcmp(com, "SCALE") == 0)
160
161
162
                 scanf("%lf%lf%lf",&a,&b,&c);
163
                 SCALE();
164
             }
165
        }
      //处理点
166
167
        for (int i = 0; i < n; i++)
168
             solvep(p[i]);
      //处理面
169
170
        solvermt();
        for (int i = 0; i < m; i++)
171
172
             solvef(f[i]);
173
        return 0;
174 | }
         重心
    7.4
 1 | Point CenterOfPolygon(Point poly[],int n)
 2 | {
```

```
3
       Point p, p0, p1, p2, p3;
4
       double m, m0;
5
       p1 = poly[0];
6
       p2 = poly[1];
7
       p.x = p.y = m = 0;
       for (int i = 2; i < n; i++)
8
9
10
     p3 = poly[i];
11
     p0.x = (p1.x + p2.x + p3.x) / 3.0;
     p0.y = (p1.y + p2.y + p3.y) / 3.0;
12
     m0 = p1.x * p2.y + p2.x * p3.y + p3.x * p1.y - p1.y * p2.x - p2.y
13
         * p3.x - p3.y * p1.x;
     if (cmp(m + m0, 0.0) == 0)
14
         m0 += eps;
15
16
     p.x = (m * p.x + m0 * p0.x) / (m + m0);
17
     p.y = (m * p.y + m0 * p0.y) / (m + m0);
18
     m = m + m0;
19
     p2 = p3;
20
21
       return p;
22 | \}
```

7.5 KD树

查找某个点距离最近的点,基本思想是每次分治把点分成两部分,建议按照坐标规模决定是垂直划分还是水平划分,查找时先往分到的那一部分查找,然后根据当前最优答案决定是否去另一个区间查找。

```
1 | bool Div[MaxN];
   void BuildKD(int deep,int 1, int r, Point p[]) \\记得备份一下P
3
4
       if (1 > r) return;
       int mid = 1 + r >> 1;
5
6
       int minX, minY, maxX, maxY;
7
       minX = min_element(p + 1, p + r + 1, cmpX) -> x;
8
       minY = min_element(p + 1, p + r + 1, cmpY) -> y;
9
       maxX = max_element(p + 1, p + r + 1, cmpX) -> x;
       maxY = max_element(p + l, p + r + 1, cmpY) \rightarrow y;
10
11
       Div[mid] = (maxX - minX >= maxY - minY);
12
       nth_element(p + 1, p + mid, p + r + 1, Div[mid] ? cmpX : cmpY);
13
       BuildKD(1, mid - 1, p);
14
       BuildKD(mid + 1, r, p);
15
   }
16
17
   long long res;
18
   void Find(int 1, int r, Point a, Point p[])\\ 查找
19
   {
20
       if (1 > r) return;
21
       int mid = 1 + r >> 1;
22
       long long dist = dist2(a, p[mid]);
23
       if (dist > 0)//如果有重点不能这样判断
24
           res = min(res, dist);
25
       long long d = Div[mid]? (a.x - p[mid].x): (a.y - p[mid].y);
```

```
26
       int 11, 12, r1, r2;
27
       11 = 1, 12 = mid + 1;
28
       r1 = mid - 1, r2 = r;
29
        if (d > 0)
30
            swap(11, 12), swap(r1, r2);
31
       Find(l1, r1, a, p);
32
        if (d * d < res)
33
            Find(12, r2, a, p);
34 | }
```

7.5.1 例题

查询一个点为中心的给定正方形内所有点并删除(2012金华网赛A)

```
1 | #include <iostream >
 2 | #include <cstdio>
3 | #include <cstring>
4 | #include <algorithm>
5
   #include <cmath>
6 | #include <queue>
7
   using namespace std;
8
9
  const int MaxN = 100000;
10 | struct Point
11
12
     int x,y,r;
13
     int id;
14
     bool del;
15
   };
16
17
   int cmpTyp;
18
   bool cmp(const Point& a,const Point& b)
19
   {
20
     if (cmpTyp == 0)
21
       return a.x < b.x;
22
     else
23
       return a.y < b.y;
24 }
25
26
   int cnt[MaxN];
27 | bool Div[MaxN];
   int minX[MaxN], minY[MaxN], maxX[MaxN], maxY[MaxN];
28
29
   void BuildKD(int 1,int r,Point p[])
30
   {
31
     if (1 > r)
                  return;
32
     int mid = 1+r>>1;
33
     cmpTyp = 0;
34
     minX[mid] = min_element(p+1,p+r+1,cmp)->x;
35
     maxX[mid] = max_element(p+1,p+r+1,cmp)->x;
36
     cmpTyp = 1;
37
     minY[mid] = min_element(p+1,p+r+1,cmp)->y;
```

```
38
     maxY[mid] = max_element(p+1,p+r+1,cmp)->y;
39
     cnt[mid] = r-l+1;
40
41
     cmpTyp = Div[mid] = (maxX[mid]-minX[mid] < maxY[mid]-minY[mid]);</pre>
     nth_element(p+l,p+mid,p+r+1,cmp);
42
43
     BuildKD(1,mid-1,p);
44
     BuildKD(mid+1,r,p);
45
   }
46
47
   queue < int > Q;
48
   int Find(int 1,int r,Point a,Point p[])
49
50
     if (1 > r) return 0;
51
     int mid = 1+r>>1;
     if (cnt[mid] == 0) return 0;
52
53
     if (maxX[mid] < a.x-a.r ||</pre>
54
          minX[mid] > a.x+a.r ||
55
          maxY[mid] < a.y-a.r ||</pre>
56
          minY[mid] > a.y+a.r)
57
       return 0;
58
59
60
     int totdel = 0;
61
62
     if (p[mid].del == false)
       if (abs(p[mid].x-a.x) \le a.r \&\& abs(p[mid].y-a.y) \le a.r)
63
64
       {
65
          p[mid].del = true;
          Q.push(p[mid].id);
66
67
          totdel++;
68
       }
69
70
     totdel += Find(l,mid-1,a,p);
     totdel += Find(mid+1,r,a,p);
71
72
73
     cnt[mid] -= totdel;
74
75
     return totdel;
76
   }
77
   Point p[MaxN], tp[MaxN];
78
79
   int n;
80
   int main()
81
82
83
     int cas = 1;
     while (true)
84
85
86
       scanf("%d",&n);
87
       if (n == 0) break;
88
```

```
89
        for (int i = 0; i < n; i++)
90
91
           p[i].id = i;
92
           int tx, ty;
           scanf("%d%d%d",&tx,&ty,&p[i].r);
93
           p[i].x = tx-ty;
94
           p[i].y = tx+ty;
95
96
           p[i].del = false;
97
           tp[i] = p[i];
         }
98
99
         BuildKD(0,n-1,tp);
100
101
        printf("Case<sub>□</sub>#%d:\n",cas++);
102
         int q;
103
         scanf("%d",&q);
104
         for (int i = 0; i < q; i++)
105
106
           int id;
           scanf("%d",&id);
107
108
           int res = 0;
109
           id--;
110
           Q.push(id);
111
           while (!Q.empty())
112
           {
             int now = Q.front();
113
114
             Q.pop();
115
             if (p[now].del == true) continue;
116
             p[now].del = true;
117
             res += Find(0,n-1,p[now],tp);
118
           }
119
           printf("%d\n",res);
        }
120
121
      }
122
      return 0;
123 | }
    7.6
          半平面交
```

直线左边代表有效区域。

```
bool HPIcmp(Line a, Line b)
1
2
  {
3
       if (fabs(a.k - b.k) > eps)
                                   return a.k < b.k;
       return ((a.s - b.s) * (b.e-b.s)) < 0;
4
5
  }
6
   Line Q[100];
8
   void HPI(Line line[], int n, Point res[], int &resn)
9
   {
10
       int tot = n;
11
       sort(line, line + n, HPIcmp);
12
       tot = 1;
```

```
13
       for (int i = 1; i < n; i++)
14
           if (fabs(line[i].k - line[i - 1].k) > eps)
                line[tot++] = line[i];
15
       int head = 0, tail = 1;
16
       Q[0] = line[0];
17
       Q[1] = line[1];
18
       resn = 0;
19
20
       for (int i = 2; i < tot; i++)
21
22
           if (fabs((Q[tail].e-Q[tail].s) * (Q[tail - 1].e-Q[tail -
              1].s)) < eps ||
23
                    fabs((Q[head].e-Q[head].s) * (Q[head + 1].e-Q[head
                       + 1].s)) < eps)
24
                return;
25
           while (head < tail && (((Q[tail]&Q[tail - 1]) - line[i].s)
              * (line[i].e-line[i].s)) > eps)
26
                tail--;
27
           while (head < tail && (((Q[head]&Q[head + 1]) - line[i].s)
              * (line[i].e-line[i].s)) > eps)
28
                head++;
29
           Q[++tail] = line[i];
30
31
       while (head < tail && (((Q[tail]&Q[tail - 1]) - Q[head].s) * (Q
          [head].e-Q[head].s)) > eps)
32
           tail--;
       while (head < tail && (((Q[head]&Q[head + 1]) - Q[tail].s) * (Q
33
          [tail].e-Q[tail].s)) > eps)
           head++;
34
35
       if (tail <= head + 1) return;</pre>
36
       for (int i = head; i < tail; i++)
37
           res[resn++] = Q[i] & Q[i + 1];
38
       if (head < tail + 1)
39
           res[resn++] = Q[head] & Q[tail];
40 | }
        凸包
   7.7
   得到的凸包按照逆时针方向排序。
1 | bool GScmp(Point a, Point b)
2
   {
3
       if (fabs(a.x - b.x) < eps)
4
           return a.y < b.y - eps;
5
       return a.x < b.x - eps;
6
   }
7
8
   void GS(Point p[], int n, Point res[], int &resn)
9
10
       resn = 0;
11
       int top = 0;
```

12

13

sort(p, p + n, GScmp);
for (int i = 0; i < n;)</pre>

```
if (resn < 2 || (res[resn - 1] - res[resn - 2]) * (p[i] -
14
               res[resn - 1]) > eps)
                res[resn++] = p[i++];
15
16
            else
17
                --resn;
18
       top = resn - 1;
       for (int i = n - 2; i >= 0;)
19
20
            if (resn < top + 2 || (res[resn - 1] - res[resn - 2]) * (p[
               i] - res[resn - 1]) > eps)
                res[resn++] = p[i--];
21
22
            else
23
                --resn;
24
       resn--;
25
       if (resn < 3)
                        resn = 0;
26 \mid \}
```

7.8 直线与凸包求交点

复杂度 $O(\log n)$ 。 需要先预处理几个东西。

```
|//二分[la,lb]这段区间那条边与line相交
   int Gao(int la,int lb,Line line)
3
   {
4
       if (la > lb)
5
           1b += n;
6
       int l = la, r = lb, mid;
7
       while (l < r)
8
9
           mid = 1+r+1>>1;
10
           if (cmp((line.e-line.s)*(p[la]-line.s),0)*cmp((line.e-line.
              s)*(p[mid]-line.s),0) >= 0)
11
                1 = mid;
12
           else
13
               r = mid-1;
14
15
       return 1%n;
16
   //求1与凸包的交点
17
18
   //先调用Gettheta预处理出凸包每条边的斜率,然后处理成升序排列
19
20
   double theta[maxn];
21
22
   void Gettheta()
23
   {
24
       for (int i = 0; i < n; i++)
25
       {
26
           Point v = p[(i+1)%n]-p[i];
27
           theta[i] = atan2(v.y,v.x);
28
29
       for (int i = 1; i < n; i++)
```

```
30
           if (theta[i-1] > theta[i]+eps)
31
                theta[i] += 2*pi;
32
   }
33
34
   double Calc(Line 1)
35
36
       double tnow;
37
       Point v = l.e-l.s;
38
       tnow = atan2(v.y,v.x);
       if (cmp(tnow,theta[0]) < 0)</pre>
39
                                      tnow += 2*pi;
       int pl = lower_bound(theta, theta+n, tnow)-theta;
40
       tnow = atan2(-v.y,-v.x);
41
42
       if (cmp(tnow,theta[0]) < 0)</pre>
                                       tnow += 2*pi;
       int pr = lower_bound(theta, theta+n, tnow)-theta;
43
44
       //pl和pr是在l方向上距离最远的点对
       pl = pl%n;
45
       pr = pr%n;
46
47
       if (cmp(v*(p[pl]-l.s),0)*cmp(v*(p[pr]-l.s),0) >= 0)
48
49
           return 0.0;
50
       int xa = Gao(pl,pr,l);
51
52
       int xb = Gao(pr,pl,l);
53
54
       if (xa > xb)
                        swap(xa,xb);
55
       //与[xa,xa+1]和[xb,xb+1]这两条线段相交
56
57
       if (cmp(v*(p[xa+1]-p[xa]),0) == 0)
                                              return 0.0;
       if (cmp(v*(p[xb+1]-p[xb]),0) == 0)
58
                                              return 0.0;
59
       Point pa, pb;
60
       pa = Line(p[xa], p[xa+1]) &1;
61
62
       pb = Line(p[xb], p[xb+1]) &1;
       //题目: 求直线切凸包得到的两部分的面积
63
64
       double area0 = sum[xb]-sum[xa+1]+(pa*p[xa+1])/2.0+(p[xb]*pb)
          /2.0+(pb*pa)/2.0;
       double area1 = sum[xa+n] - sum[xb+1] + (pb*p[xb+1])/2.0 + (p[xa]*pa)
65
          /2.0+(pa*pb)/2.0;
66
67
       return min(area0, area1);
68 | }
        三维凸包
   7.9
```

暴力写法

```
1 #define eps 1e-7
2 #define MAXV 505
3
4 struct pt
5 {
```

```
6
       double x, y, z;
7
       pt() {}
8
       pt(double _x, double _y, double _z): x(_x), y(_y), z(_z) {}
9
       pt operator - (const pt p1)
10
       {
11
            return pt(x - p1.x, y - p1.y, z - p1.z);
12
13
       pt operator * (pt p)
14
       {
15
            return pt(y*p.z-z*p.y, z*p.x-x*p.z, x*p.y-y*p.x);
16
17
       double operator ^ (pt p)
18
       {
19
            return x*p.x+y*p.y+z*p.z;
20
       }
21
   };
22
   struct _3DCH
23
   {
24
       struct fac
25
26
            int a, b, c;
27
            bool ok;
28
       };
29
       int n;
30
       pt P[MAXV];
31
       int cnt;
32
       fac F[MAXV*8];
33
       int to[MAXV][MAXV];
34
       double vlen(pt a)
35
       {
36
            return sqrt(a.x*a.x+a.y*a.y+a.z*a.z);
37
38
       double area(pt a, pt b, pt c)
39
            return vlen((b-a)*(c-a));
40
41
       double volume(pt a, pt b, pt c, pt d)
42
43
       {
44
            return (b-a)*(c-a)^(d-a);
45
       }
46
       double ptof(pt &p, fac &f)
47
48
            pt m = P[f.b]-P[f.a], n = P[f.c]-P[f.a], t = p-P[f.a];
            return (m * n) ^ t;
49
50
51
       void deal(int p, int a, int b)
52
53
            int f = to[a][b];
54
            fac add;
55
            if (F[f].ok)
56
```

```
if (ptof(P[p], F[f]) > eps)
57
                      dfs(p, f);
58
59
                 else
                 {
60
61
                      add.a = b, add.b = a, add.c = p, add.ok = 1;
62
                      to[p][b] = to[a][p] = to[b][a] = cnt;
                     F[cnt++] = add;
63
64
                 }
65
             }
66
        }
67
        void dfs(int p, int cur)
68
             F[cur].ok = 0;
69
             deal(p, F[cur].b, F[cur].a);
70
71
             deal(p, F[cur].c, F[cur].b);
72
             deal(p, F[cur].a, F[cur].c);
73
74
        bool same(int s, int t)
75
             pt &a = P[F[s].a], &b = P[F[s].b], &c = P[F[s].c];
76
77
             return fabs(volume(a, b, c, P[F[t].a])) < eps && fabs(
                volume(a, b, c,
78
                     P[F[t].b])) < eps && fabs(volume(a, b, c, P[F[t].c))
                        ])) < eps;
79
80
        void construct()
81
        {
82
             cnt = 0;
83
             if (n < 4)
84
                 return;
85
             bool sb = 1;
             for (int i = 1; i < n; i++)
86
87
             {
88
                 if (vlen(P[0] - P[i]) > eps)
89
                 {
90
                      swap(P[1], P[i]);
91
                      sb = 0;
92
                     break;
93
                 }
             }
94
95
             if (sb)return;
96
             sb = 1;
97
             for (int i = 2; i < n; i++)
98
             {
99
                 if (vlen((P[0] - P[1]) * (P[1] - P[i])) > eps)
                 {
100
101
                      swap(P[2], P[i]);
102
                      sb = 0;
103
                     break;
104
                 }
             }
105
```

```
106
             if (sb)return;
107
             sb = 1;
             for (int i = 3; i < n; i++)
108
109
             {
110
                  if (fabs((P[0] - P[1]) * (P[1] - P[2]) ^ (P[0] - P[i]))
                      > eps)
                  {
111
112
                      swap(P[3], P[i]);
113
                      sb = 0;
114
                      break;
115
                  }
             }
116
117
             if (sb)return;
118
             fac add;
119
             for (int i = 0; i < 4; i++)
120
             {
                  add.a = (i+1)\%4, add.b = (i+2)\%4, add.c = (i+3)\%4, add.
121
                     ok = 1;
122
                  if (ptof(P[i], add) > 0)
123
                      swap(add.b, add.c);
                  to[add.a][add.b] = to[add.b][add.c] = to[add.c][add.a]
124
                     = cnt;
125
                  F[cnt++] = add;
             }
126
127
             for (int i = 4; i < n; i++)
128
129
                  for (int j = 0; j < cnt; j++)
130
                  {
131
                      if (F[j].ok \&\& ptof(P[i], F[j]) > eps)
132
                      {
133
                           dfs(i, j);
134
                           break;
                      }
135
136
                  }
             }
137
138
             int tmp = cnt;
139
             cnt = 0;
140
             for (int i = 0; i < tmp; i++)
141
             {
142
                  if (F[i].ok)
                  {
143
                      F[cnt++] = F[i];
144
145
                  }
146
             }
147
        }
    //表面积
148
149
         double area()
150
151
             double ret = 0.0;
152
             for (int i = 0; i < cnt; i++)
153
```

```
154
                 ret += area(P[F[i].a], P[F[i].b], P[F[i].c]);
155
             }
156
             return ret / 2.0;
157
    //体积
158
        double volume()
159
160
        {
161
             pt 0(0, 0, 0);
162
             double ret = 0.0;
163
             for (int i = 0; i < cnt; i++)
164
165
                 ret += volume(0, P[F[i].a], P[F[i].b], P[F[i].c]);
166
167
             return fabs(ret / 6.0);
168
        }
    //表面三角形数
169
170
        int facetCnt_tri()
171
        {
172
             return cnt;
173
        }
    //表面多边形数
174
        int facetCnt()
175
176
177
             int ans = 0;
178
             for (int i = 0; i < cnt; i++)
179
180
                 bool nb = 1;
181
                 for (int j = 0; j < i; j++)
182
183
                      if (same(i, j))
184
                      {
185
                          nb = 0;
186
                          break;
187
188
                 }
189
                 ans += nb;
190
             }
191
             return ans;
192
        }
193
194
        pt Fc[MAXV*8];
195
        double V[MAXV*8];
        pt Center()//重心
196
197
        {
198
             pt O(0,0,0);
199
             for (int i = 0; i < cnt; i++)
200
                 Fc[i].x = (0.x+P[F[i].a].x+P[F[i].b].x+P[F[i].c].x)
201
                    /4.0;
202
                 Fc[i].y = (0.y+P[F[i].a].y+P[F[i].b].y+P[F[i].c].y)
                    /4.0;
```

```
203
                 Fc[i].z = (0.z+P[F[i].a].z+P[F[i].b].z+P[F[i].c].z)
                    /4.0;
204
                 V[i] = volume(0,P[F[i].a],P[F[i].b],P[F[i].c]);
205
             }
206
             pt res = Fc[0], tmp;
             double m = V[0];
207
             for (int i = 1; i < cnt; i++)
208
209
             {
210
                 if (fabs(m+V[i]) < eps)
211
                     V[i] += eps;
212
                 tmp.x = (m*res.x+V[i]*Fc[i].x)/(m+V[i]);
                 tmp.y = (m*res.y+V[i]*Fc[i].y)/(m+V[i]);
213
214
                 tmp.z = (m*res.z+V[i]*Fc[i].z)/(m+V[i]);
215
                 m += V[i];
216
                 res = tmp;
             }
217
218
             return res;
219
        }
220
    };
221
222
    _3DCH hull;
223
    int main()
224
225
    {
226
        while (scanf("%d",&hull.n) != EOF)
227
228
             for (int i = 0; i < hull.n; i++)
229
                 scanf("%lf%lf%lf",&hull.P[i].x,&hull.P[i].y,&hull.P[i].
                    z);
230
             hull.construct();
231
        }
232
        return 0;
233 | }
```

7.10 旋转卡壳

"对踵"

7.10.1 单个凸包

```
1
   void solve(Point p[],int n)
2
   {
3
       Point v;
4
        int cur = 1;
       for (int i = 0; i < n; i++)
5
6
        {
7
            v = p[i]-p[(i+1)%n];
            while (v*(p[(cur+1)%n]-p[cur]) < 0)
8
9
                 cur = (cur + 1) %n;
10
            //p[cur] -> p[i]
```

7.10.2 两个凸包

注意初始点的选取,代码只是个示例。 有时候答案需要取solve(p0,n,p1,m)和solve(p1,m,p0,n)的最优值。 何老鱼说我的是错的。。

```
1
   void solve(Point p0[],int n,Point p1[],int m)
2
   {
3
       Point v;
4
       int cur = 0;
5
       for (int i = 0; i < n; i++)
6
       {
7
            v = p0[i]-p0[(i+1)%n];
8
            while (v*(p1[(cur+1)%m]-p1[cur]) < 0)
9
                 cur = (cur + 1) \%m;
10
            //p1[cur] -> p0[i]
            //p1[cur] -> p0[i+1]
11
12
            //p1[cur] -> (p0[i],p0[i+1])
13
       }
14 | }
```

7.10.3 外接矩形

```
void solve()
1
2
   {
3
       resa = resb = 1e100;
4
       double dis1, dis2;
5
       Point xp[4];
6
       Line 1[4];
7
       int a,b,c,d;
8
       int sa, sb, sc, sd;
9
       a = b = c = d = 0;
10
       sa = sb = sc = sd = 0;
11
       Point va, vb, vc, vd;
12
       for (a = 0; a < n; a++)
13
       {
14
            va = Point(p[a],p[(a+1)%n]);
15
            vc = Point(-va.x,-va.y);
16
            vb = Point(-va.y,va.x);
            vd = Point(-vb.x,-vb.y);
17
            if (sb < sa)
18
            {
19
20
                b = a;
21
                sb = sa;
22
23
            while (xmult(vb, Point(p[b], p[(b+1)%n])) < 0)
```

```
24
            {
25
                b = (b+1) \%n;
26
                sb++;
27
            }
            if (sc < sb)
28
29
            {
30
                c = b;
31
                sc = sb;
32
            }
            while (xmult(vc, Point(p[c], p[(c+1)%n])) < 0)
33
34
35
                c = (c+1) \%n;
36
                sc++;
37
38
            if (sd < sc)
39
            {
40
                d = c;
41
                sd = sc;
42
            while (xmult(vd, Point(p[d], p[(d+1)%n])) < 0)
43
44
45
                d = (d+1) \%n;
46
                sd++;
            }
47
48
            //卡在p[a],p[b],p[c],p[d]上
49
50
            sa++;
       }
51
52 | }
          三角形内点个数
   7.11
          无三点共线
   7.11.1
  Point p[1000], tp[2000], base;
1
2
   bool cmp(const Point &a, const Point &b)
3
4
5
     return a.theta < b.theta;
   }
6
7
8
   int cnt[1000][1000];
9
   int cntleft[1000][1000];
10
   int n, m;
11
12
   int calc(int a, int b, int c)
13
14
       Point p1 = p[b] - p[a], p2 = p[c] - p[a];
15
        if (atan2(p1.y, p1.x) > atan2(p2.y, p2.x))
16
            swap(b, c);
17
        if ((p[b] - p[a]) * (p[c] - p[a]) > 0)
```

return cnt[a][c] - cnt[a][b] - 1;

18

```
19
       else
20
            return n - 3 - (cnt[a][c] - cnt[a][b] - 1);
21
   }
22
23
   int main(int argc, char const *argv[])
24
25
       int totcas;
26
       scanf("%d", &totcas);
27
       for (int cas = 1; cas <= totcas; ++cas)</pre>
28
       {
29
            scanf("%d", &n);
30
            for (int i = 0; i < n; ++i)
            {
31
32
                scanf("%11d%11d", &p[i].x, &p[i].y);
33
                p[i].id = i;
34
            }
35
            for (int i = 0; i < n; ++i)
36
            {
37
                m = 0;
38
                base = p[i];
39
                for (int j = 0; j < n; ++ j)
40
                     if (i != j)
41
                     {
42
                         tp[m] = p[j];
43
                         Point v = tp[m]-base;
44
                         tp[m++].theta = atan2(v.y,v.x);
                     }
45
46
47
                sort(tp, tp + m, cmp);
48
                for (int j = 0; j < m; ++ j)
49
                     tp[m + j] = tp[j];
50
                //calc cnt
51
52
                for (int j = 0; j < m; ++ j)
53
                     cnt[i][tp[j].id] = j;
54
55
                //calc cntleft
                for (int j = 0, k = 0, tot = 0; j < m; ++j)
56
                {
57
                     while (k == j \mid | (k < j + m && (tp[j] - base) * (tp
58
                        [k] - base) > 0))
                         k++, tot++;
59
60
                     cntleft[i][tp[j].id] = --tot;
                }
61
62
            }
63
64
            printf("Case \d:\n", cas);
65
            int q;
66
            scanf("%d", &q);
67
            for (int i = 0; i < q; ++i)
68
```

```
69
                int x, y, z;
70
                scanf("%d%d%d", &x, &y, &z);
71
                if ((p[z] - p[x]) * (p[y] - p[x]) > 0)
72
                     swap(y, z);
73
                int res = cntleft[x][z] + cntleft[z][y] + cntleft[y][x
                res += calc(x, y, z) + calc(y, z, x) + calc(z, x, y);
74
75
                res -= 2 * (n - 3);
76
                printf("%d\n", res);
            }
77
78
       }
79
       return 0;
80 | }
   7.11.2
         有三点共线且点有类别之分
   int n, n0, n1, m;
   Point p[3000], tp[3000], base;
2
3
   bool cmp(const Point &a, const Point &b)
5
   {
6
       if ((a-base)*(b-base) == 0)
7
       {
8
            return (a-base).getMol() < (b-base).getMol();</pre>
9
       }
10
       return a.theta < b.theta;
11
   }
12
13
   int cnt[100][100];
14
   int cntleft[100][100];
15
16
   int calc(int a,int b,int c)
17
18
       Point p1 = p[b]-p[a], p2 = p[c]-p[a];
19
       if (atan2(1.0*p1.y,1.0*p1.x) > atan2(1.0*p2.y,1.0*p2.x))
20
            swap(b,c);
21
       int res = cnt[a][c]-cnt[a][b];
22
       if ((p[b]-p[a])*(p[c]-p[a]) > 0)
23
            return res;
24
       else
25
            return n1-res;
26
  }
27
28
   int main()
29
   {
30
       int cas = 0;
31
       while (scanf("%d%d",&n0,&n1) != EOF)
32
       {
33
            n = n1+n0;
34
            for (int i = 0; i < n; i++)
35
            {
36
                scanf("%I64d%I64d",&p[i].x,&p[i].y);
```

```
37
                p[i].id = i;
38
            }
39
            for (int i = 0; i < n0; ++i)
40
            {
41
                m = 0;
42
                base = p[i];
43
                for (int j = 0; j < n; ++ j)
44
                     if (i != j)
45
                     {
46
                         tp[m] = p[j];
47
                         Point v = tp[m]-base;
48
                         tp[m++].theta = atan2(1.0*v.y,1.0*v.x);
                     }
49
50
51
                sort(tp, tp + m, cmp);
52
                for (int j = 0; j < m; ++ j)
53
                     tp[m + j] = tp[j];
54
55
                for (int j = 0, tot = 0; j < m; ++ j)
56
                {
57
                     if (tp[j].id < n0)
58
                          cnt[i][tp[j].id] = tot;
59
                     else
60
                         tot++;
                }
61
62
63
                for (int j = 0, k = 0, tot = 0; j < m; ++j)
64
                {
65
                     while (k == j \mid | (k < j + m && (tp[j] - base) * (tp
                        [k] - base) > 0))
                     {
66
67
                         if (tp[k].id >= n0)
68
                              tot++;
69
                         k++;
70
                     }
71
                     if (tp[j].id >= n0)
72
                         tot--;
73
                     else
74
                          cntleft[i][tp[j].id] = tot;
                }
75
            }
76
77
            int ans = 0;
78
            for (int i = 0; i < n0; i++)
79
80
                 for (int j = i+1; j < n0; j++)
81
                     for (int k = j+1; k < n0; k++)
82
                     {
83
                          int x = i, y = j, z = k;
84
85
                          if ((p[z] - p[x]) * (p[y] - p[x]) > 0)
86
                              swap(y, z);
```

```
ACM Template
                         int res = cntleft[x][z] + cntleft[z][y] +
87
                            cntleft[y][x];
88
89
                         res += calc(x, y, z) + calc(y, z, x) + calc(z,
                            x, y);
90
91
                         res -= 2 * n1;
92
93
                         //printf("%d %d %d %d\n",x,y,z,res);
94
95
                         if (res \%2 == 1)
96
                             ans++;
97
                     }
            printf("Case \( \) \%d\n",++cas,ans);
98
99
100
        return 0;
101 | }
          最近点对
   7.12
   7.12.1
          类快排算法
   double calc_dis(Point &a ,Point &b) {
        return sqrt((a.x-b.x)*(a.x-b.x) + (a.y-b.y)*(a.y-b.y));
 3
   //别忘了排序
 4
```

```
bool operator < (const Point &a ,const Point &b) {</pre>
       if(a.y != b.y) return a.x < b.x;</pre>
6
7
       return a.x < b.x;
8
   }
9
   double Gao(int 1 ,int r ,Point pnts[]) {
10
       double ret = inf;
11
       if(l == r) return ret;
12
       if(1+1 ==r) {
            ret = min(calc_dis(pnts[l],pnts[l+1]) ,ret);
13
14
            return ret;
       }
15
16
       if(1+2 ==r) {
            ret = min(calc_dis(pnts[l],pnts[l+1]) ,ret);
17
            ret = min(calc_dis(pnts[1],pnts[1+2]) ,ret);
18
            ret = min(calc_dis(pnts[l+1],pnts[l+2]) ,ret);
19
20
            return ret;
21
       }
22
23
       int mid = 1+r>>1;
24
       ret = min (ret ,Gao(l ,mid,pnts));
25
       ret = min (ret , Gao(mid+1, r,pnts));
26
27
       for(int c = 1; c<=r; c++)
28
            for(int d = c+1; d <= c+7 && d <= r; d++) {
29
                ret = min(ret , calc_dis(pnts[c],pnts[d]));
30
            }
```

```
31
       return ret;
32 | }
          随机增量法
   7.12.2
 1 | #include <iostream >
  #include <cstdio>
3 | #include <cstring>
4 | #include <map>
5 #include <vector>
6 | #include <cmath>
7 | #include <algorithm>
  |#define Point pair < double , double >
9
   using namespace std;
10
11
  |const int step[9][2] =
      {{-1,-1},{-1,0},{-1,1},{0,-1},{0,0},{0,1},{1,-1},{1,0},{1,1}};
12 \mid \text{int n,x,y,nx,ny};
13 | map < pair < int , int > , vector < Point > > g;
14 | vector < Point > tmp;
15 | Point p[20000];
16
   double tx, ty, ans, nowans;
17 | vector < Point >::iterator it, op, ed;
18
  pair < int , int > gird;
19
  bool flag;
20
21
   double Dis(Point p0, Point p1)
22
   {
23
        return sqrt((p0.first-p1.first)*(p0.first-p1.first)+
24
                     (p0.second-p1.second)*(p0.second-p1.second));
25
   }
26
27
   double CalcDis(Point p0, Point p1, Point p2)
28
   {
29
       return Dis(p0,p1)+Dis(p0,p2)+Dis(p1,p2);
30
   }
31
32
   void build(int n,double w)
33
34
       g.clear();
35
        for (int i = 0; i < n; i++)
36
            g[make_pair((int)floor(p[i].first/w),(int)floor(p[i].second
               /w))].push_back(p[i]);
37
   }
38
39
   int main()
40
   {
41
        int t;
42
        scanf("%d",&t);
        for (int ft = 1;ft <= t;ft++)
43
44
        {
45
            scanf("%d",&n);
```

```
46
            for (int i = 0; i < n; i++)
47
            {
                scanf("%lf%lf",&tx,&ty);
48
49
                p[i] = make_pair(tx,ty);
            }
50
51
            random_shuffle(p,p+n);
52
            ans = CalcDis(p[0],p[1],p[2]);
53
            build(3, ans/2.0);
            for (int i = 3; i < n; i++)
54
55
            {
56
                x = (int)floor(2.0*p[i].first/ans);
                y = (int)floor(2.0*p[i].second/ans);
57
                tmp.clear();
58
                for (int k = 0; k < 9; k++)
59
60
                {
61
                     nx = x+step[k][0];
62
                     ny = y + step[k][1];
63
                     gird = make_pair(nx,ny);
64
                     if (g.find(gird) != g.end())
65
66
                         op = g[gird].begin();
67
                         ed = g[gird].end();
68
                         for (it = op; it != ed; it++)
69
                              tmp.push_back(*it);
                     }
70
                }
71
72
                flag = false;
73
                for (int j = 0; j < tmp.size(); j++)
74
                     for (int k = j+1; k < tmp.size(); k++)
75
                     {
76
                         nowans = CalcDis(p[i],tmp[j],tmp[k]);
77
                         if (nowans < ans)
78
79
                              ans = nowans;
80
                              flag = true;
                         }
81
82
                     }
83
                if (flag == true)
84
                     build(i+1, ans/2.0);
85
                else
                     g[make_pair((int)floor(2.0*p[i].first/ans),(int)
86
                        floor(2.0*p[i].second/ans))].push_back(p[i]);
            }
87
88
            printf("%.3f\n",ans);
89
       }
90 | }
```

7.13 多圆面积并

7.13.1 去重

有时候可能需要去掉不需要的圆

```
for (int i = 0; i < n; i++)
2
   {
3
       scanf("%lf%lf%lf",&c[i].c.x,&c[i].c.y,&c[i].r);
4
       del[i] = false;
   }
5
6
   for (int i = 0; i < n; i++)
7
       if (del[i] == false)
8
       {
9
            if (c[i].r == 0.0) del[i] = true;
10
            for (int j = 0; j < n; j++)
                if (i != j)
11
12
                     if (del[j] == false)
                         if (cmp(Point(c[i].c,c[j].c).Len()+c[i].r,c[j].
13
                            r) \ll 0
14
                             del[i] = true;
15
       }
   tn = n;
16
17
   n = 0;
18
   for (int i = 0; i < tn; i++)
19
       if (del[i] == false)
20
            c[n++] = c[i];
   7.13.2 圆并
   ans[i]表示被覆盖i次的面积
1 \mid const double pi = acos(-1.0);
2 const double eps = 1e-8;
   struct Point
3
4
   {
5
       double x,y;
6
       Point(){}
7
       Point(double _x,double _y)
8
            {
9
                x = _x;
10
                y = y;
11
       double Length()
12
13
            {
14
                return sqrt(x*x+y*y);
15
            }
16 | };
17
   struct Circle
18
   {
19
       Point c;
20
       double r;
21
   };
22
   struct Event
23
   {
24
       double tim;
25
       int typ;
26
       Event(){}
```

```
27
       Event(double _tim,int _typ)
28
            {
                tim = _tim;
29
30
                typ = _typ;
            }
31
32
   };
33
34
   int cmp(const double& a,const double& b)
35
36
       if (fabs(a-b) < eps)
                                  return 0;
37
       if (a < b)
                     return -1;
38
       return 1;
39
   }
40
41
   bool Eventcmp(const Event& a,const Event& b)
42
   {
43
       return cmp(a.tim,b.tim) < 0;
44
   }
45
46
   double Area(double theta, double r)
47
   {
48
       return 0.5*r*r*(theta-sin(theta));
49
   }
50
51
   double xmult(Point a, Point b)
52
53
       return a.x*b.y-a.y*b.x;
54
   }
55
56
   int n, cur, tote;
   Circle c[1000];
57
   double ans [1001], pre [1001], AB, AC, BC, theta, fai, a0, a1;
58
   Event e[4000];
59
   Point lab;
60
61
62
   int main()
63
   {
64
       while (scanf("%d",&n) != EOF)
65
       {
66
            for (int i = 0; i < n; i++)
                 scanf("%lf%lf%lf",&c[i].c.x,&c[i].c.y,&c[i].r);
67
68
            for (int i = 1; i \le n; i++)
                 ans[i] = 0.0;
69
            for (int i = 0; i < n; i++)
70
71
            {
72
                tote = 0;
73
                e[tote++] = Event(-pi,1);
74
                e[tote++] = Event(pi,-1);
75
                for (int j = 0; j < n; j++)
76
                     if (j != i)
77
                     {
```

```
lab = Point(c[j].c.x-c[i].c.x,c[j].c.y-c[i].c.y
78
                             );
79
                          AB = lab.Length();
80
                          AC = c[i].r;
                          BC = c[j].r;
81
82
                          if (cmp(AB+AC,BC) \le 0)
83
84
                              e[tote++] = Event(-pi,1);
85
                              e[tote++] = Event(pi,-1);
86
                              continue;
87
                          }
                          if (cmp(AB+BC,AC) <= 0) continue;</pre>
88
89
                          if (cmp(AB,AC+BC) > 0)
                                                    continue;
                          theta = atan2(lab.y,lab.x);
90
91
                          fai = acos((AC*AC+AB*AB-BC*BC)/(2.0*AC*AB));
92
                          a0 = theta-fai;
93
                          if (cmp(a0,-pi) < 0)
                                                    a0 += 2*pi;
94
                          a1 = theta+fai;
95
                          if (cmp(a1,pi) > 0)
                                                    a1 -= 2*pi;
                          if (cmp(a0,a1) > 0)
96
97
98
                              e[tote++] = Event(a0,1);
99
                              e[tote++] = Event(pi,-1);
                              e[tote++] = Event(-pi,1);
100
                              e[tote++] = Event(a1,-1);
101
                          }
102
103
                          else
104
105
                              e[tote++] = Event(a0,1);
                              e[tote++] = Event(a1,-1);
106
107
                          }
108
                     }
109
                 sort(e,e+tote,Eventcmp);
110
                 cur = 0;
                 for (int j = 0; j < tote; j++)
111
112
                 {
                     if (cur != 0 && cmp(e[j].tim,pre[cur]) != 0)
113
114
                      {
115
                          ans[cur] += Area(e[j].tim-pre[cur],c[i].r);
116
                          ans[cur] += xmult(Point(c[i].c.x+c[i].r*cos(pre
                             [cur]),c[i].c.y+c[i].r*sin(pre[cur])),
                                                Point(c[i].c.x+c[i].r*cos(e
117
                                                   [j].tim),c[i].c.y+c[i].r
                                                   *sin(e[j].tim)))/2.0;
                     }
118
119
                      cur += e[j].typ;
120
                     pre[cur] = e[j].tim;
                 }
121
122
123
             for (int i = 1; i < n; i++)
124
                 ans[i] -= ans[i+1];
```

```
125 | for (int i = 1; i <= n; i++)

126 | printf("[%d]_=_%.3f\n",i,ans[i]);

127 | }

128 | return 0;

129 |}
```

7.14 一个圆与多边形面积交

```
1 | bool InCircle(Point a, double r)
2
  {
       return cmp(a.x*a.x+a.y*a.y,r*r) <= 0; //这里判断的时候EPS一定不要太
3
          小!!
  }
4
5
6
  double CalcArea(Point a, Point b, double r)
7
   {
8
       Point p[4];
9
       int tot = 0;
10
       p[tot++] = a;
11
12
       Point tv = Point(a,b);
13
       Line tmp = Line(Point(0,0), Point(tv.y,-tv.x));
14
       Point near = LineToLine(Line(a,b),tmp);
       if (cmp(near.x*near.x+near.y*near.y,r*r) <= 0)</pre>
15
16
       {
17
           double A,B,C;
18
           A = near.x*near.x+near.y*near.y;
19
           C = r;
20
           B = C*C-A;
           double tvl = tv.x*tv.x+tv.y*tv.y;
21
           double tmp = sqrt(B/tvl); //这样做只用一次开根
22
23
           p[tot] = Point(near.x+tmp*tv.x,near.y+tmp*tv.y);
           if (OnSeg(Line(a,b),p[tot]) == true)
24
25
           p[tot] = Point(near.x-tmp*tv.x,near.y-tmp*tv.y);
26
           if (OnSeg(Line(a,b),p[tot]) == true)
27
       }
       if (tot == 3)
28
29
       {
30
            if (cmp(Point(p[0],p[1]).Length(),Point(p[0],p[2]).Length()
              ) > 0)
31
                swap(p[1],p[2]);
32
33
       p[tot++] = b;
34
35
       double res = 0.0, theta, a0, a1, sgn;
36
       for (int i = 0; i < tot-1; i++)
37
38
           if (InCircle(p[i],r) == true && InCircle(p[i+1],r) == true)
39
           {
                res += 0.5*xmult(p[i],p[i+1]);
40
```

```
}
41
42
           else
43
           ₹
44
                a0 = atan2(p[i+1].y,p[i+1].x);
                a1 = atan2(p[i].y,p[i].x);
45
46
                if (a0 < a1)
                                a0 += 2*pi;
                theta = a0-a1;
47
48
                if (cmp(theta,pi) >= 0) theta = 2*pi-theta;
                sgn = xmult(p[i],p[i+1])/2.0;
49
                if (cmp(sgn,0) < 0) theta = -theta;
50
                res += 0.5*r*r*theta;
51
52
           }
53
       }
54
       return res;
55 }
   调用
1 | area2 = 0.0;
  |for (int i = 0;i < resn;i++) //遍历每条边, 按照逆时针
       area2 += CalcArea(p[i],p[(i+1)%resn],r);
```

7.15 精度问题

7.15.1 浮点数为啥会有精度问题

浮点数(以C/C++为准),一般用的较多的是float、double。

	占字节数	数值范围	一十进制精度位数
float	4	$-3.4e - 38 \sim 3.4e38$	$6 \sim 7$
double	8	$-3.4e - 38 \sim 3.4e38$ $-1.7e - 308 \sim 1.7e308$	$14 \sim 15$

如果内存不是很紧张或者精度要求不是很低,一般选用double。14位的精度(是有效数字位,不是小数点后的位数)通常够用了。注意,问题来了,数据精度位数达到了14位,但有些浮点运算的结果精度并达不到这么高,可能准确的结果只有10~12位左右。那低几位呢?自然就是不可预料的数字了。这给我们带来这样的问题:即使是理论上相同的值,由于是经过不同的运算过程得到的,他们在低几位有可能(一般来说都是)是不同的。这种现象看似没太大的影响,却会一种运算产生致命的影响:==。恩,就是判断相等。注意,C/C++中浮点数的==需要完全一样才能返回true。

7.15.2 eps

eps缩写自epsilon,表示一个小量,但这个小量又要确保远大于浮点运算结果的不确定量。eps最常见的取值是1e-8左右。引入eps后,我们判断两浮点数a、b相等的方式如下:

1 | int sgn(double a) {return a < -eps ? -1 : a < eps ? 0 : 1;}

这样,我们才能把相差非常近的浮点数判为相等;同时把确实相差较大(差值大于eps)的数判为不相等。

养成好习惯,尽量不要再对浮点数做==判断。

7.15.3 eps带来的函数越界

如果sqrt(a), asin(a), acos(a) 中的a是你自己算出来并传进来的,那就得小心了。如果a本来应该是0的,由于浮点误差,可能实际是一个绝对值很小的负数(比如-1e-12),这样sqrt(a)应得0的,直接因a不在定义域而出错。

类似地,如果a本来应该是±1,则asin(a)、acos(a)也有可能出错。

因此,对于此种函数,必需事先对a进行校正。

7.15.4 输出陷阱I

现在考虑一种情况,题目要求输出保留两位小数。有个case的正确答案的精确值是0.005,按理应该输出0.01,但你的结果可能是0.005000000001(恭喜),也有可能是0.004999999999(悲剧),如果按照printf("%.2lf", a)输出,那你的遭遇将和括号里的字相同。

解决办法是,如果a为正,则输出a + eps,否则输出a - eps

7.15.5 输出陷阱II

ICPC题目输出有个不成文的规定(有时也成文),不要输出:-0.000那我们首先要弄清,什么时候按printf("%.3lf",a)输出会出现这个结果。直接给出结果好了: $a \in (-0.000499999 \cdots, -0.000 \cdots 1)$

所以,如果你发现a落在这个范围内,请直接输出0.000。更保险的做法是用sprintf直接判断输出结果是不是-0.000再予处理。

7.15.6 范围越界

请注意,虽然double可以表示的数的范围很大,却不是不穷大,上面说过最大是1e308。所以有些时候你得小心了,比如做连乘的时候,必要的时候要换成对数的和。

7.15.7 关于set

经观察,set不是通过==来判断相等的,是通过<来进行的,具体说来,只要a < b 和b < a都不成立,就认为a和b相等,可以发现,如果将小于定义成:

1 | bool operator < (const Dat dat)const{return val < dat.val - eps;} 就可以解决问题了。(基本类型不能重载运算符,所以封装了下)

7.15.8 输入值波动过大

这种情况不常见,不过可以帮助你更熟悉eps。假如一道题输入说,给一个浮点数a, 1e-20 < a < 1e20。那你还敢用1e-8做eps么?合理的做法是把eps按照输入规模缩放到合适大小。

7.15.9 一些建议

容易产生较大浮点误差的函数有asin、 acos。欢迎尽量使用atan2。

另外,如果数据明确说明是整数,而且范围不大的话,使用int或者long long代替double都是极佳选择,因为就不存在浮点误差了

8 搜索

8.1 Dancing Links

8.1.1 估价函数

```
int h()
 1
2
   {
3
        bool vis[100];
4
        memset(vis,false,sizeof(vis));
5
        int i,j,k,res=0,mi,col;
6
        while(1)
 7
        {
8
            mi=inf;
9
            for(i=R[head]; i!=head&&i<=2*n; i=R[i])
10
                 if (mi > nk [i] & & ! vis [i])
11
12
                     mi=nk[i];
13
                     col=i;
14
                 }
15
            if(mi==inf)
16
                 break;
17
            res++;
            vis[col]=true;
18
19
            for(j=D[col]; j!=col; j=D[j])
20
                 for(k=R[j]; k!=j; k=R[k])
                 {
21
22
                     if(C[k]>2*n)
23
                          continue;
24
                     vis[C[k]]=true;
                 }
25
26
        }
27
        return res;
28 | }
   8.1.2 DLX
  void remove1(int col)
2
   {
 3
        int i,j;
4
        L[R[col]]=L[col];
        R[L[col]]=R[col];
5
6
        for(i=D[col];i!=col;i=D[i])
7
8
            L[R[i]]=L[i];
9
            R[L[i]]=R[i];
10
        }
11
12
   void remove2(int col)
13
   {
14
        int i,j;
        L[R[col]]=L[col];
15
```

```
16
        R[L[col]] = R[col];
17
        for(i=D[col];i!=col;i=D[i])
18
19
            for(j=R[i];j!=i;j=R[j])
20
            {
21
                 U[D[j]]=U[j];
22
                 D[U[j]]=D[j];
23
                 --nk[C[j]];
24
            }
25
        }
26
27
   void resume1(int col)
28
   {
29
        int i,j;
30
        for(i=U[col];i!=col;i=U[i])
31
        {
32
            L[R[i]]=i;
33
            R[L[i]]=i;
        }
34
35
        L[R[col]]=col;
        R[L[col]] = col;
36
37
38
   void resume2(int col)
39
   {
40
        int i,j;
        for(i=U[col];i!=col;i=U[i])
41
42
43
            for(j=L[i];j!=i;j=L[j])
44
            {
45
                 ++nk[C[j]];
46
                 U[D[j]]=j;
47
                 D[U[j]]=j;
            }
48
49
50
        L[R[col]] = col;
51
        R[L[col]] = col;
52
   }
   int h()
53
54
   {
55
     bool vis[100];
56
     memset(vis,false,sizeof(vis));
57
     int i,j,k,res=0,mi,col;
     while(1)
58
59
     {
60
        mi=inf;
        for(i=R[head];i!=head&&i<=2*n;i=R[i])
61
          if (mi>nk[i]&&!vis[i])
62
63
64
            mi=nk[i];
65
            col=i;
66
          }
```

```
67
         if(mi==inf)
68
           break;
         res++; vis[col]=true;
69
70
         for(j=D[col]; j!=col; j=D[j])
71
           for(k=R[j];k!=j;k=R[k])
72
             if(C[k]>2*n)
73
74
                continue;
75
             vis[C[k]]=true;
           }
76
77
      }
78
      return res;
79
    }
80
    bool DLX(int d, int deep)
81
    {
82
      if(d+h()>deep) return false;
         if (R[head] == head | | R[head] > 2*n)
83
84
           return true;
85
         if(d>=deep)
86
           return false;
         int col,ma=inf;
87
88
         int i,j;
89
         for(i=R[head];i!=head&&i<=2*n;i=R[i])
             if(nk[i]<ma)
90
             {
91
92
                  col=i;
93
                  ma=nk[i];
94
95
         remove1(col);
96
         for(i=D[col];i!=col;i=D[i])
97
98
             int flag=1;
99
             for(j=R[i];;j=R[j])
100
101
                  if (j == R[i] & &! flag)
102
                       break;
103
                  U[D[j]]=U[j];
104
                  D[U[j]]=D[j];
105
                  if(C[j]>2*n)
106
                       remove2(C[j]);
107
                  else
108
                       remove1(C[j]);
109
                  flag=0;
             }
110
111
             if(DLX(d+1,deep))
112
                return true;
113
             flag=1;
114
             for(j=L[i];;j=L[j])
115
116
                  if(j==L[i]&&!flag)
117
                       break;
```

```
118
                  if(C[j]>2*n)
119
                      resume2(C[j]);
120
                  else
                      resume1(C[j]);
121
                 U[D[j]]=j;
122
123
                 D[U[j]]=j;
                  flag=0;
124
             }
125
        }
126
         resume1(col);
127
         return false;
128
129 }
```

9 动态规划

9.1 斜率优化

```
#include < cstdio >
1
  #include <algorithm >
3 using namespace std;
  int a[1000], sum[1001], dp[1000][1000];
4
   int deque [1000];
   const int inf=0x7fffffff;
6
7
   int N,s,t;
   int calc(int i,int l,int j)//决策值计算
9
   {
10
       return dp[j][1-1]-(sum[i]-sum[j])*(sum[N]-sum[i]);
11
   }
12
   bool check(int i,int 1)//尾端判断
13
   {
14
       int k1=deque[t-1], k2=deque[t-2];
       return (long long)(dp[k1][l]-dp[k2][l])*(sum[i]-sum[k1])>(long
15
          long)(dp[i][1]-dp[k1][1])*(sum[k1]-sum[k2]);
16
   }
17
   int main()
18
   {
19
       int n,m;
20
       while (scanf("%d%d",&n,&m),n)
21
22
           for (int i=0; i<n; i++)
23
                scanf("%d",&a[i]);
24
           N=n;
25
            sum[0]=0;
26
           for (int i=0; i<n; i++)
27
                sum[i+1] = sum[i]+a[i];
28
           dp[0][0]=0;
29
            for (int i=0; i<n; i++)
                for (int j=i+1; j<n; j++)
30
31
                    dp[0][0]+=a[i]*a[i];
32
           for (int i=1; i<n; i++)
33
                dp[i][0]=inf;
           for (int i=1; i<n; i++)
34
35
            {
36
                dp[i][1]=inf;
                for (int j=0; j < i; j++)
37
38
                    dp[i][1]=min(dp[i][1],calc(i,1,j));
39
           }
40
           for (int 1=2; 1<=m; 1++)
41
42
                s=t=0;//双端队列清空
43
                for (int i=1; i<n; i++)
44
45
                    while (t-s>1 && check(i-1,l-1)) t--;
                    deque[t++]=i-1;//决策加入
46
```

```
while (t-s>1 && calc(i,l,deque[s])>calc(i,l,deque[s
47
                        +1])) s++;
                     dp[i][1]=calc(i,1,deque[s]);
48
49
                 }
            }
50
51
            int ans=0x7fffffff;
52
            for (int i=m; i<n; i++)
53
                 ans=min(ans,dp[i][m]);
54
            printf("%d\n",ans);
        }
55
        return 0;
56
57 | }
        RMQ二版
   9.2
   void init()
2
   {
3
        int i,j;
4
        int n=N, k=1, l=0;
        for (i=0; i< n; i++)
 5
6
7
            f[i][0]=ele[i].num;
8
            if (i+1>k*2)
9
            ₹
10
                 k * = 2;
11
                 1++;
12
            lent[i+1]=1;
13
14
15
        for (j=1; (1<< j)-1< n; j++)
16
            for (i=0; i+(1<< j)-1< n; i++)
17
                 f[i][j]=max(f[i][j-1],f[i+(1<<(j-1))][j-1]);
18
19
   int fint(int x, int y)
20
21
        int k=lent[y-x+1];
22
        return \max(f[x][k], f[y-(1 << k)+1][k]);
23 | }
         二维LIS
   9.3
 1 #include <cstdio>
2 | #include < map >
3 using namespace std;
4 | map < int , int > mp [100001];
   bool check(int idx,int x,int y)
 5
6
7
        if (!idx) return 1;
        if (mp[idx].begin()->first>=x) return 0;
8
9
       map<int,int> ::iterator it=mp[idx].lower_bound(x);
10
        it--;
11
        if (it->second<y) return 1;</pre>
```

```
12
       else return 0;
13
   }
14
   int main()
15
   {
16
        int n;
17
        scanf("%d",&n);
18
        int 1=0, r=0;
19
       for (int i=0; i<n; i++)
20
       {
21
            int x,y;
22
            scanf("%d%d",&x,&y);
            int tl=1,tr=r;
23
24
            while (tl<tr)
25
26
                int mid=(tl+tr+1)/2;
27
                if (check(mid,x,y))
28
                     tl=mid;
29
                else
30
                     tr=mid-1;
            }
31
            if (tl==r) r++;
32
33
            int idx=tl+1;
34
            map<int,int> ::iterator itl=mp[idx].lower_bound(x),itr=itl;
            while (itr!=mp[idx].end() && itr->second>y) itr++;
35
            if (mp[idx].find(x)!=mp[idx].end())
36
                y=min(y,mp[idx][x]);
37
            if (itl!=itr) mp[idx].erase(itl,itr);
38
            if (mp[idx].find(x) == mp[idx].end() || mp[idx][x]>y)
39
40
                mp[idx][x]=y;
41
42
       printf("%d\n",r);
43
       return 0;
44 | }
```

9.4 插头DP

Tower Defence独立插头+构造解构造解的时候保存的是在hash_map的ele数组的下标位置没想清楚千万别去写

```
int bit [12];
1
2
3
  inline int getbit(long long sta,int pos)
4
   {
       return sta/bit[pos]%bit[1];
5
6
   }
8
   inline long long setbit(long long sta, int pos, int val)
9
   {
10
       return sta/bit[pos+1]*bit[pos+1]+val*bit[pos]+sta%bit[pos];
11
12
```

```
13 | int n,m,mp[30][10];
14
   char buf [30] [10];
15
   hash_map dp[2];
   bool flag;
16
17
   int key,val,upd,l,u,res,msk,cov,now,pr,resnow,resmsk,pru;
   int w[15],s[15],top;
18
   int pre[210][10007], preuse[210][10007];
19
20
21
   void decode(int msk,int& key,int& cov)
22
   {
23
       int tmp;
24
       key = cov = 0;
25
       for (int i = 0; i < m+1; i++)
26
27
            tmp = getbit(msk,i);
28
            if (tmp > 0)
29
            {
30
                key = setbit(key,i,tmp-1);
31
                cov = setbit(cov,i,1);
32
            }
       }
33
34
   }
35
36
   int encode(int key,int cov)
37
   {
38
       int res = 0, tmp;
       for (int i = 0; i < m+1; i++)
39
40
41
            tmp = getbit(cov,i);
42
            if (tmp > 0)
43
            {
44
                tmp = getbit(key,i);
45
                res = setbit(res,i,tmp+1);
46
            }
       }
47
48
       return res;
49
   }
50
51
   void update(int a,int key,int cov,int val)
52
53
       int msk = encode(key,cov);
54
       int pos;
       if (dp[a][msk] < val)
55
56
       {
57
            dp[a][msk] = val;
            pos = dp[a].fint(msk);
58
            pre[now][pos] = pr;
59
60
            preuse[now][pos] = pru;
       }
61
62
   }
63
```

```
int count3(int sta)
64
65
    {
66
        int res = 0;
67
        for (int i = 0; i < m+1; i++)
             if (getbit(sta,i) == 3)
68
69
                 res++;
70
        return res;
71
   }
72
73
    void expand(int sta)
74
    {
75
        top = 0;
76
        for (int i = 0; i < m+1; i++)
             if (getbit(sta,i) == 1)
77
78
                 s[top++] = i;
79
             else if (getbit(sta,i) == 2)
80
             {
81
                 w[s[top-1]] = i;
82
                 w[i] = s[top-1];
83
                 top--;
             }
84
85
    }
86
87
    int main()
    {
88
89
        //freopen("TD.in","r",stdin);
        //freopen("TDM.out","w",stdout);
90
91
        bit[0] = 1;
92
        for (int i = 1; i < 12; i++) bit[i] = bit[i-1]*5;
93
        int t;
94
        scanf("%d",&t);
        dp[0].init();
95
        dp[1].init();
96
        for (int ft = 1; ft <= t; ft++)
97
98
        {
99
             scanf("%d%d",&n,&m);
100
             res = 0;
101
             memset(mp,0,sizeof(mp));
             memset(pre,0,sizeof(pre));
102
103
             memset(preuse,0,sizeof(preuse));
             for (int i = 0; i < n; i++)
104
105
                 scanf("%s",buf[i]);
106
107
                 for (int j = 0; j < m; j++)
108
                      if (buf[i][j] == '.')
109
                          mp[i][j] = 1;
110
                      else if (buf[i][j] != 'B')
111
                          mp[i][j] = 2;
112
113
             dp[0].clear();
114
             dp[1].clear();
```

```
115
            flag = 0;
116
             dp[flag][0] = 0;
             int res = 0;
117
118
            now = 0;
119
             for (int i = 0; i < n; i++)
120
121
                 for (int j = 0; j < m; j++)
122
                 {
123
                     dp[!flag].clear();
                     for (int k = 0; k < dp[flag].N; k++)
124
125
126
                          msk = dp[flag].ele[k].key;
127
                          pr = k;
128
                          val = dp[flag].ele[k].val;
                          decode(msk,key,cov);
129
130
                          l = getbit(key,j);
131
                          u = getbit(key, j+1);
132
                          if (mp[i][j] == 0)//是障碍
133
                          {
134
                              if (1 == 0 \&\& u == 0)
135
                              {
136
                                   pru = 0;
137
                                   update(!flag,key,setbit(setbit(cov,j,0)
                                      ,j+1,0),val);
                              }
138
                          }
139
140
                          else
141
                              if (mp[i][j] == 1 && 1 == 0 && u == 0)// \pi
142
                                 要插头
                              {
143
144
                                   pru = 1;
145
                                   update(!flag,key,setbit(setbit(cov,j,0)
                                      ,j+1,0),val);
                              }
146
147
                              if (getbit(cov,j) == 1 && 1 == 0)
                                 continue://不可以在这里搞插
                                 头
                              if (getbit(cov, j+1) == 1 \&\& u == 0)
148
                                 continue;
                              cov = setbit(setbit(cov,j,1),j+1,1);//更新覆
149
150
                              upd = setbit(setbit(key,j,0),j+1,0);
151
                              pru = 2;
152
                              if (mp[i][j] == 2)
153
                              {
                                   if (1 == 0 \&\& u == 0)
154
155
                                   {
                                       if (count3(key) < 2)//可以新建独立插头
156
157
                                       {
158
                                            if (mp[i][j+1] != 0)
```

```
159
                                                update(!flag,setbit(setbit(
                                                   key, j, 0), j+1, 3), cov, val
                                                   +1);
160
                                            if (mp[i+1][j] != 0)
161
                                                update(!flag,setbit(setbit(
                                                   key, j, 3), j+1, 0), cov, val
                                                   +1);
162
                                       }
163
                                   }
164
                                   else if (1 == 0 || u == 0)
165
                                   {
                                       if (1+u < 3 && count3(key) < 2)//可
166
                                          以用一个独立插头来结束这条路径
167
                                       {
168
                                            expand(key);
                                            if (1 > 0)
169
170
                                                update(!flag,setbit(upd,w[j
                                                   ],3),cov,val+1);
171
                                            else
172
                                                update(!flag,setbit(upd,w[j
                                                   +1],3),cov,val+1);
173
                                       }
174
                                       else if (1+u == 3 \&\& upd == 0)//B
                                          径的一端
                                       {
175
176
                                            if (res < val+1)
177
                                            {
178
                                                res = val+1;
179
                                                resnow = now-1;
180
                                                resmsk = k;
181
                                            }
                                       }
182
183
                                   }
                              }
184
185
                              else if (1 == 0 \&\& u == 0)
186
                              {
                                   if (mp[i][j+1] != 0 \&\& mp[i+1][j] != 0)
187
                                      //可以新建插
188
                                       update(!flag,setbit(setbit(key,j,1)
                                          ,j+1,2),cov,val+1);
189
                              }
190
                              else if (1 == 0 || u == 0)
191
                              {
192
                                   if (mp[i][j+1] != 0)//可以延续插头
193
                                       update(!flag,setbit(upd,j+1,l+u),
                                          cov, val+1);
194
                                   if (mp[i+1][j] != 0)//可以延续插头
                                       update(!flag,setbit(upd,j,l+u),cov,
195
                                          val+1);
196
                              }
```

```
197
                               else if (1 == u)
198
                                   if (1 < 3) //合并两个相同的括号
199
200
                                   {
201
                                       expand(key);
202
                                       if (1 == 1)
203
                                            update(!flag,setbit(upd,w[j
                                               +1],1),cov,val+1);
204
                                       else
205
                                            update(!flag,setbit(upd,w[j],2)
                                               ,cov,val+1);
206
                                   }
                                   else if (upd == 0)//合并两个独立插头
207
208
                                   {
209
                                       if (res < val+1)
210
                                       {
211
                                            res = val+1;
212
                                            resnow = now-1;
213
                                            resmsk = k;
214
                                       }
215
                                   }
                               }
216
                               else if (1 == 3 || u == 3)//合并独立插头与括号
217
218
                               {
219
                                   expand(key);
220
                                   if (1 == 3)
221
                                       update(!flag,setbit(upd,w[j+1],3),
                                          cov, val+1);
222
                                   else
223
                                       update(!flag,setbit(upd,w[j],3),cov
                                           , val+1);
224
                               }
225
                               else if (1 == 2 || u == 1) //合并)(
226
                                   update(!flag,upd,cov,val+1);
227
                          }
228
                      }
229
                      flag = !flag;
230
                      now++;
                 }
231
232
                 if (i+1 == n)
                                   break;
233
234
                 dp[!flag].clear();
235
                 for (int k = 0; k < dp[flag].N; k++)
                 {
236
237
                      msk = dp[flag].ele[k].key;
238
                      pr = k;
239
                      val = dp[flag].ele[k].val;
240
                      pru = 0;
241
                      decode (msk, key, cov);
242
                      update(!flag,key*bit[1],cov*bit[1],val);
243
                 }
```

```
244
                  now++;
245
                  flag = !flag;
246
             }
247
248
             printf("Case_{\sqcup}%d:_{\sqcup}%d\n",ft,res);
249
             for (int i = resnow; i \ge 0; i--)
250
251
                  if (preuse[i][resmsk] == 1)
                       buf [i/(m+1)][i\%(m+1)] = 'W';
252
253
                  resmsk = pre[i][resmsk];
254
             for (int i = 0; i < n; i++)
255
256
                  printf("%s\n",buf[i]);
             printf("\n");
257
258
         }
259
         return 0;
260 }
```

10 杂物

10.1 高精度数

支持乘以整数和加法。

```
1 struct BigInt
2
3
       const static int mod = 100000000;
       int a[600], len;
4
       BigInt (){}
5
6
       BigInt (int v)
7
       {
8
            len = 0;
9
            do
10
            ₹
11
                a[len++] = v\%mod;
12
                v /= mod;
13
            }while(v);
14
15
       BigInt operator *(const int& b) const
16
       {
17
            BigInt res;
            res.len = len;
18
19
            for (int i = 0; i \le len; ++i)
20
                res.a[i] = 0;
21
            for (int i = 0; i < len; ++i)
22
            {
23
                res.a[i] += a[i]*b;
24
                res.a[i+1] += res.a[i]/mod;
25
                res.a[i] %= mod;
26
            }
27
            if (res.a[len] > 0) res.len++;
28
            return res;
29
       }
30
       BigInt operator +(const BigInt& b) const
31
32
            BigInt res;
            res.len = max(len,b.len);
33
            for (int i = 0; i \le res.len; ++i)
34
35
                res.a[i] = 0;
36
            for (int i = 0; i < res.len; ++i)
37
                res.a[i] += ((i < len)?a[i]:0)+((i < b.len)?b.a[i]:0);
38
39
                res.a[i+1] += res.a[i]/mod;
40
                res.a[i] %= mod;
            }
41
42
            if (res.a[res.len] > 0) res.len++;
43
            return res;
44
       }
45
       void output()
```

```
{
46
47
            printf("%d",a[len-1]);
            for (int i = len-2; i >= 0; --i)
48
49
                printf("%08d",a[i]);
            printf("\n");
50
51
       }
52 | };
         整数外挂
   10.2
   int wg;
2
   char ch;
3
   bool ng;
5
   inline int readint()
6
   {
7
       ch = getchar();
8
       while (ch != '-' && (ch < '0' || ch > '9')) ch = getchar();
9
       if (ch == '-')
10
       {
11
            ng = true;
12
            ch = getchar();
13
       }
14
       else
15
            ng = false;
16
       wg = ch - '0';
17
       ch = getchar();
18
       while (ch >= '0' && ch <= '9')
19
       {
20
            wg = wg*10+ch-'0';
21
            ch = getchar();
22
       }
23
       if (ng == true) wg = -wg;
24
       return wg;
25 | }
   10.3
          Java
         文件操作
   10.3.1
1 | import java.io.*;
   import java.util.*;
2
   import java.math.*;
4
   import java.text.*;
5
6
   public class Main
7
   {
8
9
       public static void main(String args[]) throws
```

Scanner sc = new Scanner(new FileReader("a.in"));

FileNotFoundException, IOException

10

11

{

```
12
           PrintWriter pw = new PrintWriter(new FileWriter("a.out"));
13
           int n,m;
           n=sc.nextInt();//读入下一个INT
14
15
           m=sc.nextInt();
16
17
           for(ci=1; ci<=c; ++ci)
18
19
               pw.println("Case_#"+ci+": _easy_for_output");
20
21
           pw.close();//关闭流并释放,这个很重要,否则是没有输出的
22
           sc.close();//关闭流并释放
23
24
       }
25 | \}
         优先队列
   10.3.2
1
  | PriorityQueue queue = new PriorityQueue( 1, new Comparator()
2
3
       public int compare( Point a, Point b )
4
5
     if (a.x < b.x | | a.x == b.x && a.y < b.y)
         return -1;
6
7
     else if( a.x == b.x && a.y == b.y)
8
         return 0;
9
     else
10
         return 1;
       }
11
12 | });
   10.3.3
        Map
1 Map map = new HashMap();
2 | map.put("sa","dd");
  String str = map.get("sa").toString;
3
4
5
  for(Object obj : map.keySet()){
6
       Object value = map.get(obj);
7
  }
   10.3.4 sort
   static class cmp implements Comparator
2
3
       public int compare(Object o1,Object o2)
4
5
     BigInteger b1=(BigInteger)o1;
     BigInteger b2=(BigInteger)o2;
6
     return b1.compareTo(b2);
7
8
       }
9
10 | public static void main(String[] args) throws IOException
11 | {
```

```
12
       Scanner cin = new Scanner(System.in);
13
        int n;
14
       n=cin.nextInt();
15
       BigInteger[] seg = new BigInteger[n];
       for (int i=0;i<n;i++)</pre>
16
17
     seg[i]=cin.nextBigInteger();
18
        Arrays.sort(seg,new cmp());
19 | }
   10.4
          hashmap
   struct hash_map
2
   {
3
        const static int mod=10007;
4
        int head[mod];
5
        struct hash_tables
6
        {
7
            int key;
8
            int val;
9
            int next;
10
       } ele[10007];
11
       int N;
12
        int getHash(int x)
13
       {
14
            return x%mod;
15
       void init()
16
17
18
            memset(head, 255, sizeof(head));
19
            N = 0;
20
       }
21
       void clear()
22
            for (int i = 0; i < N; i++)
23
24
                head[getHash(ele[i].key)] = -1;
25
            N = 0;
26
       int fint(int x)
27
28
29
            for (int i=head[getHash(x)]; i!=-1; i=ele[i].next)
                 if (ele[i].key==x) return i;
30
31
            return -1;
32
       }
33
       void insert(int x)
34
35
            int tmp=getHash(x);
            ele[N].key=x;
36
37
            ele[N].val=0;
38
            ele[N].next=head[tmp];
39
            head[tmp]=N++;
40
       }
41
        int& operator [](int x)
```

```
42
       {
43
            int tmp=fint(x);
            if (tmp==-1)
44
45
           {
46
                insert(x);
                return ele[N-1].val;
47
           }
48
49
           else
50
                return ele[tmp].val;
51
       }
52 | };
         C++&STL常用函数
   10.5
   10.5.1
         lower_bound/upper_bound
   不解释
1 | iterator lower_bound(const key_type &key ) \\返回一个迭代器, 指向键值>=
     key的第一个元素。
2 | iterator upper_bound(const key_type &key ) \ \返回一个迭代器, 指向键值>
      key的第一个元素。
3
   #include <iostream>
4
   #include <algorithm>
5
   #include <vector>
6
   using namespace std;
7
8
9
   int main () {
10
     int myints[] = \{10,20,30,30,20,10,10,20\};
11
     vector < int > v(myints, myints + 8);
                                                  // 10 20 30 30 20 10 10
12
     vector < int > :: iterator low, up;
13
     sort (v.begin(), v.end());
14
                                                  // 10 10 10 20 20 20 30
         30
15
     low=lower_bound (v.begin(), v.end(), 20); //
16
17
     up= upper_bound (v.begin(), v.end(), 20); //
18
19
     cout << "lower_bound_at_position_" << int(low- v.begin()) << endl
20
     cout << "upper_bound_at_position_" << int(up - v.begin()) << endl
21
22
     return 0;
23 | }
   Output:
1 lower_bound at position 3
2 upper_bound at position 6
```

10.5.2 rotate

把数组后一半搬到前面

```
template <class ForwardIterator>
     void rotate ( ForwardIterator first, ForwardIterator middle,
2
3
                     ForwardIterator last );
   10.5.3
         nth_{-}element
   template <class RandomAccessIterator>
1
2
     void nth_element ( RandomAccessIterator first,
        RandomAccessIterator nth,
3
                          RandomAccessIterator last );
4
5
   template <class RandomAccessIterator, class Comapre>
6
     void nth_element ( RandomAccessIterator first,
        RandomAccessIterator nth,
7
                          RandomAccessIterator last, Compare comp );
   10.5.4
          bitset
   取用
1 | bitset <4> mybits;
2
3 | mybits [1] = 1;
                              // 0010
4 \mid mybits[2] = mybits[1];
                              // 0110
   翻转
1 | bitset <4> mybits (string("0001"));
2
3 | cout << mybits.flip(2) << endl;
                                          // 0101
4 | cout << mybits.flip() << endl;
                                          // 1010
   运算
1 | bitset <4> first (string("1001"));
   bitset<4> second (string("0011"));
3
   cout << (first^=second) << endl;</pre>
4
                                                  // 1010 (XOR, assign)
   cout << (first&=second) << endl;</pre>
                                                 // 0010 (AND, assign)
   cout << (first|=second) << endl;</pre>
                                                  // 0011 (OR, assign)
6
7
   cout << (first <<=2) << endl;</pre>
                                                 // 1100 (SHL, assign)
9
   cout << (first>>=1) << endl;</pre>
                                                  // 0110 (SHR, assign)
10
11 | cout << (~second) << endl;
                                                 // 1100 (NOT)
   cout << (second <<1) << endl;</pre>
12
                                                 // 0110 (SHL)
13
   cout << (second>>1) << endl;</pre>
                                                  // 0001 (SHR)
14
```

```
// false (0110==0011)
15
  cout << (first==second) << endl;</pre>
16
   cout << (first!=second) << endl;</pre>
                                                 // true
                                                           (0110! = 0011)
17
18 cout << (first&second) << endl;
                                                 // 0010
19 | cout << (first|second) << endl;
                                                 // 0111
20 | cout << (first^second) << endl;
                                                 // 0101
   10.5.5
          multimap
   遍历
   multimap < char, int > mymm;
 2 | multimap < char, int > :: iterator it;
   char c;
 3
 4
 5 \mid mymm.insert(pair < char, int > ('x', 50));
   mymm.insert(pair<char,int>('y',100));
6
   mymm.insert(pair<char,int>('y',150));
   mymm.insert(pair<char,int>('y',200));
8
   mymm.insert(pair<char,int>('z',250));
9
   mymm.insert(pair<char,int>('z',300));
10
11
12
   for (c='x'; c<='z'; c++)
13
14
     cout << "There are " << (int) mymm.count(c);</pre>
     cout << "uelementsuwithukeyu" << c << ":";
15
     for (it=mymm.equal_range(c).first; it!=mymm.equal_range(c).second
16
        ; ++it)
17
       cout << "" << (*it).second;
18
     cout << endl;</pre>
   }
19
20
   /*
21
   Output:
22
23
   There are 1 elements with key x: 50
   There are 3 elements with key y: 100 150 200
25
   There are 2 elements with key z: 250 300
26 | */
   二分查找
  multimap < char, int > mymultimap;
   multimap < char, int > :: iterator it, itlow, itup;
3
4 | mymultimap.insert(pair<char,int>('a',10));
   mymultimap.insert(pair<char,int>('b',121));
   mymultimap.insert(pair<char,int>('c',1001));
7
   mymultimap.insert(pair<char,int>('c',2002));
   mymultimap.insert(pair<char,int>('d',11011));
8
   mymultimap.insert(pair<char,int>('e',44));
10
```

```
itlow=mymultimap.lower_bound ('b'); // itlow points to b
12
   itup=mymultimap.upper_bound ('d'); // itup points to e (not d)
13
14
   // print range [itlow,itup):
15
   for ( it=itlow ; it != itup; it++ )
     cout << (*it).first << "_{\sqcup}=>_{\sqcup}" << (*it).second << endl;
16
17
18
   /*
19
   Output:
20
21
   b => 121
22 c => 1001
23
  c => 2002
24 \mid d => 11011
25 | */
   删除
   multimap < char, int > mymultimap;
2
   multimap < char, int > :: iterator it;
3
4 // insert some values:
   mymultimap.insert(pair<char,int>('a',10));
6 | mymultimap.insert(pair<char,int>('b',20));
   mymultimap.insert(pair<char,int>('b',30));
7
   mymultimap.insert(pair<char,int>('c',40));
   mymultimap.insert(pair<char,int>('d',50));
9
   mymultimap.insert(pair < char, int > ('d',60));
10
   mymultimap.insert(pair<char,int>('e',70));
11
12
   mymultimap.insert(pair<char,int>('f',80));
13
14 | it=mymultimap.find('b');
15 | mymultimap.erase (it);
                                                  // erasing by iterator
      (1 element)
16
17
  mymultimap.erase ('d');
                                                  // erasing by key (2
      elements)
18
19
   it=mymultimap.find ('e');
20
   mymultimap.erase ( it, mymultimap.end() ); // erasing by range
21
22
   // show content:
23
   for ( it=mymultimap.begin() ; it != mymultimap.end(); it++ )
24
     cout << (*it).first << "_{\sqcup} = >_{\sqcup}" << (*it).second << endl;
25
26
   /*
27
   Output:
28
29 a => 10
30 | b = > 30
31
   c => 40
32 | */
```

10.6 位运算

10.6.1 基本操作

注意括号

功能	示例	位运算
去掉最后一位	$(101101 \to 10110)$	x shr 1
在最后加一个0	$(101101 \rightarrow 1011010)$	x shl 1
在最后加一个1	$(101101 \rightarrow 1011011)$	x shl 1+1
把最后一位变成1	$(101100 \rightarrow 101101)$	x or 1
把最后一位变成0	$(101101 \rightarrow 101100)$	x or 1-1
最后一位取反	$(101101 \rightarrow 101100)$	x xor 1
把右数第 k 位变成 1	$(101001 \to 101101, k = 3)$	x or (1 shl (k-1))
把右数第 k 位变成 0	$(101101 \to 101001, k = 3)$	x and not $(1 shl (k-1))$
右数第k位取反	$(101001 \to 101101, k = 3)$	x xor (1 shl (k-1))
取末三位	$(1101101 \to 101)$	x and 7
取末 k 位	$(1101101 \to 1101, k = 5)$	\mathbf{x} and (1 shl k-1)
取右数第 k 位	$(1101101 \rightarrow 1, k = 4)$	x shr (k-1) and 1
把末 k 位变成 1	$(101001 \to 101111, k = 4)$	x or (1 shl k-1)
末k位取反	$(101001 \to 100110, k = 4)$	x xor (1 shl k-1)
把右边连续的1变成0	$ (1001011111 \rightarrow 100100000) $	x and $(x+1)$
把右起第一个0变成1	$(1001011111 \rightarrow 1001111111)$	x or (x+1)
把右边连续的0变成1	$(11011000 \rightarrow 11011111)$	x or (x-1)
取右边连续的1	$(1001011111 \to 1111)$	(x xor (x+1)) shr 1
去掉右起第一个1的左边	$(100101000 \to 1000)$	\mid x and (x xor (x-1))

10.6.2 枚举长为*n*含*k*个1的01串

```
1 | int n = 5, k = 3;
  for (int s = (1 << k)-1, u = 1 << n; s < u;)
2
3
  {
4
       for (int i = 0; i < n; i++)
5
           printf("%d",(((s>>(n-1-i))&1) == 1));
6
       printf("\n");
7
8
       int b = s \& -s;
       s = (s+b) | (((s^(s+b))>>2)/b);
9
10 }
```

10.7 其它

10.7.1 对跑脚本

```
1 while true; do
2    ./gen > input
3    ./sol < input > output.sol
4    ./bf < input > output.bf
5    ./
6    diff output.sol output.bf
```

```
7 \mid \text{if [ \$? -ne 0 ] ; then break; fi} \\ 8 \mid \text{done}
```