

Part 1:

I. Searching a product

```
public Iterator<E> iterator() →  $\theta(1)$ 
{
    return new Iterator<E>() {
        int current = -1; →  $\theta(1)$ 

        @Override
        public boolean hasNext() →  $\theta(1)$ 
        {
            return current < (used-1); →  $\theta(1)$ 
        }

        @Override
        public E next() →  $\theta(1)$ 
        {
            current++; →  $\theta(1)$ 
            return (E) array[current]; →  $\theta(1)$ 
        }

        @Override
        public void remove() →  $\theta(1)$ 
        {
            E element = (E)array[current]; →  $\theta(1)$ 
            MyList.this.remove(element); →  $\theta(1)$ 
        }
    };
}
```

public E find(E e) throws Exception {	→ $T_w = \theta(n), T_b = \theta(1)$	→ $O(n)$
Iterator<E> it = iterator();	→ $\theta(1)$	
while(it.hasNext())	→ $T_w = \theta(n), T_b = \theta(1)$	
{		
E element = it.next();	→ $\theta(1)$	
if(element.equals(e))	→ $T_w = \theta(1), T_b = \theta(1)$	→ $T_a = \theta(1)$
return element;	→ $\theta(1)$	
}		
throw new Exception("The given element not included");	→ $\theta(1)$	
}		

public Product getProductById(String id) throws Exception{	→ $O(n)$
Identifiable product = new Product(id) {};	→ $\theta(1)$
try {	
return products.find((Product) product);	→ $O(n)$
} catch (Exception e) {	
throw new Exception("Couldnt find the product with that id !");	→ $\theta(1)$
}	
}	

II. Add / remove product

public void addProduct(Product product) {	→ $T_w = \theta(n), T_b = \theta(1)$	→ $O(n)$
products.add(product);		
}		
public boolean add(E e)		
{		
if(capacity == used)	→ $p(T) = 1/5$ and $p(F) = 4/5$	
	→ $T_w = \theta(n), T_b = \theta(1)$	
increaseCapacity(5);	→ $\theta(n)$	
array[used] = e;	→ $\theta(1)$	
used++;	→ $\theta(1)$	
return true;	→ $\theta(1)$	
}		

private void increaseCapacity(int size)	→	$\theta(n)$
{		
int oldCapacity = capacity;	→	$\theta(1)$
Object[] temp = array;	→	$\theta(1)$
capacity += size;	→	$\theta(1)$
array = new Object[capacity];	→	$\theta(1)$
for(int i=0; i<oldCapacity; i++)	→	$\theta(n)$ (oldCapacity cant be 1)
array[i] = temp[i];	→	$\theta(1)$
}		

III. Querying the products that need to be supplied

public IContainer<Message> getProductInforms(){	→	$\theta(1)$
return repository.getMessages();	→	$\theta(1)$
}		
public IContainer<Message> getMessages() {	→	$\theta(1)$
return messages;	→	$\theta(1)$
}		

Part 2:

a) It's meaningless because big O notation is used for the worst scenario so it gives the biggest time probable.

b) The statement is false because θ is used for average case so its not maximum of $f(n)+g(n)$. Its average of $f(n)+g(n)$.

c) 1) It is true because asymptotic notations say the growing rate of the function so in first if we get n as 1 we get the result as 4, if we get n as 2 the result is 8 so the growth rate is 2^n in first statement.

2) It is false because for 2^{2n} if we get n as 1, the result is 4 and if we get n as 2, the result is 16; for 2^n if we get n as 1, the result is 2 and if we get n as 2, the result is 4 so the grow rates are not same.

3) $f(n) = O(n^2)$ so we can not know it in theta notation. It may be $\theta(n^2)$ or it may be $\theta(n)$ or smaller so according to the statement since $g(n) = \theta(n^2)$ $f(n)$ must be $\theta(n^2)$ but as I said we can not prove it is $\theta(n^2)$. It may be smaller.

Part 3:

- | | |
|--------------------|--|
| 0) 3^n | $\lim_{n \rightarrow \infty} 3^n / n2^n = \infty$ so 3^n is bigger |
| 1) $n2^n$ | $\lim_{n \rightarrow \infty} n2^{2n} / 2^{n+1} = \infty$ so $n2^n$ is bigger |
| 2) 2^{n+1} | since $\log_2 n$ is very lower than n |
| 3) $5^{\log_2 n}$ | |
| 4) 2^n | 2^n is bigger than $n \log^2 n$ because exponential bigger than linear |
| 5) $n \log^2 n$ | $\lim_{n \rightarrow \infty} n \log^2 n / (\log n)^3 = \infty$ so $n \log^2 n$ is bigger |
| 6) $(\log n)^3$ | let say $n=8$ then $(\log n)^3 = 9$ but $n^{1.01} =$ about 8. |
| 7) $n^{1.01}$ | $\sqrt{n} = n^{1/2}$ so $n^{1.01}$ is bigger |
| 8) \sqrt{n} | $\sqrt{n} = n^{1/2}$ logarithmic is slower than exponential |
| 9) $\log n$ | |

Part 4:

min(elements)	$\rightarrow \theta(n)$
min = elements.get(0)	$\rightarrow \theta(1)$
for i to n	$\rightarrow \theta(n)$
if(min >= elements.get(i))	$\rightarrow p(T) = 1/2$ and $p(F) = 1/2$
	$\rightarrow T_w = \theta(1), T_b = \theta(1)$
	$\rightarrow \theta(1)$
min = elements.get(i)	$\rightarrow \theta(1)$
return min	$\rightarrow \theta(1)$

median(elements)	$\rightarrow \theta(n^2)$
medianIndex = n / 2	$\rightarrow \theta(1)$
for i to medianIndex	$\rightarrow \theta(n^2)$
min = min(elements)	$\rightarrow \theta(n)$
elements.remove(min)	$\rightarrow \theta(n)$
median = min(elements)	$\rightarrow \theta(n)$
return median	$\rightarrow \theta(1)$

twoElements(number) $\rightarrow \theta(1)$
 first = Math.random() * number $\rightarrow \theta(1)$
 second = number – first $\rightarrow \theta(1)$

ArrayList mergeList(list1, list2) $\rightarrow O((m+n)*\max(m,n))$

index1 = 0 $\rightarrow \theta(1)$
 index2 = 0 $\rightarrow \theta(1)$

ArrayList myList $\rightarrow \theta(1)$

T_{all}

```

while ( index1< list1.size && index2<list2.size )
    if(list1.get(index1) < list2.get(index2))  $\rightarrow O(m)$ 
        myList.add(list1.get(index1++))  $\rightarrow T_w = \theta(m), T_b = \theta(1) \rightarrow O(m)$ 
    else  $\rightarrow O(n)$ 
        myList.add(list2.get(index2++))  $\rightarrow T_w = \theta(n), T_b = \theta(1) \rightarrow O(n)$ 

while ( index1< list1.size )  $\rightarrow O(m)$ 
    myList.add(list1.get(index1++))  $\rightarrow T_w = \theta(m), T_b = \theta(1) \rightarrow O(m)$ 

while( index2 < list2.size )  $\rightarrow O(n)$ 
    myList.add(list2.get(index2++))  $\rightarrow T_w = \theta(n), T_b = \theta(1) \rightarrow O(n)$ 

return myList
  
```

There are two case of T_{all} . If list1(m) is bigger than list2(n) and list2(n) is bigger than list1(m)

$T_{all-1} = O((m+n)* m)$ $T_{all-2} = O((m+n)* n)$

$T_{all} = O((m+n)*\max(m,n))$

Part 5:

- a) `int p_1 (int array[]):` → $T=\theta(1)$, $S=\theta(1)$
 {
 return array[0] * array[2]) → $T=\theta(1)$, $S=\theta(1)$
 }
- b) `int p_2 (int array[], int n):` → $T=\theta(n)$, $S=\theta(1)$
 {
 Int sum = 0 → $T=\theta(1)$
 for (int i = 0; i < n; i=i+5) → $T=\theta(n)$
 sum +=array[i] * array[i]) → $T=\theta(1)$
 return sum → $T=\theta(1)$
 }
- c) `void p_3(int array[], int n):` → undefined , $S=\theta(1)$
 {
 for (int i = 0; i < n; i++) → $T=\theta(n)$
 for (int j = 0; j < i; j=j*2) → undefined(infinity loop)
 printf("%d", array[i] * array[j]) → $T=\theta(1)$
 }
- d) `void p_4(int array[], int n):` → $T=O(n) + \max(O(n), a)$, $S=\theta(1)$
 {
 → $T=\theta(n)$
 If (p_2(array, n))> 1000 → $T_w=\theta(n) + \max(\theta(n), a)$
 , $T_b=\theta(n) + \min(\theta(n), a)$
 p_3(array, n) → undefined → let say x
 else
 printf("%d", p_1(array)*p_2(array, n)) → $T=\theta(n)$
 }