Generative Models for Incomplete Data Reconstruction

Elina Telesheva

Advisor: Mikhail Hushchyn

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Motivation

- Synthesizing high-quality tabular data is important for many data science tasks:
 - privacy protection
 - dataset augmentation
 - dataset enhancement
- The generation of tabular data is challenging due to varied distributions and a mixture of data types

Problem statement

 The goal is to generate synthetic data based on real data while preserving feature statistics and making it impossible to restore real data.

Real Synthetic Name Age Name Age **James Smith** 27 David Miller 19 Michael Johnson 15 Linda Moor 52 Mary Brown 72 Richard Davis 47

Figure 1: Example of real and generated data.

Previous approaches

- CTGAN and TVAE (Xu et al. 2019) are based on GAN^a and VAE^b (Goodfellow et al. 2014; Kingma and Welling 2022)
- GOOGLE (Liu et al. 2023) is based on VAE and GNN^c
- GReaT is based on auto-regressive GPT2 (Borisov et al. 2023)
- TabDDPM, TabSyn, TabDiff, STaSy, CoDi are diffusion models (Kotelnikov et al. 2022; Zhang et al. 2024; Shi et al. 2025; Kim et al. 2023; Lee et al. 2023)

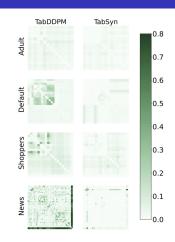


Figure 2: The value represents the absolute difference between the correlations of real and synthetic data (the lighter, the better).

 $[^]a$ Generative Adversarial Network

^bVariational autoencoder

^cGraph neural network

TabDDPM

The focus of the research is on the TabDDPM model. It uses Gaussian diffusion to model numerical features and multinomial diffusion to model categorical features.

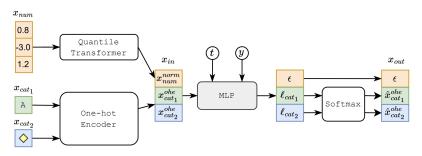


Figure 3: TabDDPM model scheme

Research question

How will the quality of the TabDDPM model change if **multinomial diffusion is excluded** from it? Let's compare the quality of the new model with the official version of TabDDPM.

Model based on TabDDPM

The multinomial diffusion part for categorical features is removed from Tab-DDPM model. Categorical features are processed using One-Hot Encoding and then passed to the model as numerical features.

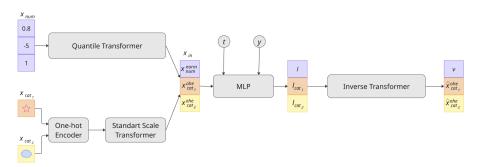


Figure 4: Considered model scheme

Metrics description

Metrics used for quality estimation of a generated dataset (Zhang et al. 2024):

- Column-wise density estimation and pair-wise column correlation estimate the density of every column and the correlation of column pairs.
- C2ST¹ evaluates if the synthetic data could be distinguished from the real data.
- $oldsymbol{lpha}$ -precision and $oldsymbol{eta}$ -recall estimate accuracy and diversity of data.
- DCR² determines the probability that the synthetic dataset is closer to the train dataset than to the test one.
- MLE³ estimates the quality of a model trained on a synthetic data.

 $^{^1\}mathrm{Classifier}$ Two Sample Test

²Distance to Closest Records

³Machine Learning Efficiency

Methods	Adult AUC ↑	Default AUC ↑	Shoppers AUC ↑	Magic AUC ↑	Beijing RMSE ↓	News RMSE ↓
Real	$.927 {\pm}.000$	$.770 {\pm}.005$	$.926 {\pm} .001$	$.946 {\pm} .001$.423±.003	.842±.002
SMOTE	.899±.007	$.741 {\pm} .009$	$.911 \scriptstyle{\pm .012}$.934±.008	.593±.011	.897±.036
CTGAN	$.886 {\pm} .002$	$.696 {\pm} .005$	$.875 {\pm} .009$	$.855 {\pm} .006$	$.902 {\pm} .019$	$.880 {\pm} .016$
TVAE	$.878 {\pm} .004$	$.724 {\pm}.005$	$.871 {\pm} .006$	$.887 {\pm}.003$	$.770 {\pm} .011$	$1.01 {\pm}.016$
GOGGLE	$.778 {\pm}.012$	$.584 {\pm} .005$	$.658 {\pm} .052$	$.654 {\pm} .024$	$1.09 {\pm}.025$	$.877 {\pm} .002$
GReaT	$.913 {\pm} .003$	$.755 {\pm} .006$	$.902 {\pm} .005$	$.888 \pm .008$	$.653 {\pm} .013$	OOM
STaSy	$.906 {\pm}.001$	$.752 {\pm} .006$	$.914 {\pm} .005$	$.934 {\pm}.003$	$.656 {\pm} .014$	$.871 {\pm} .002$
CoDi	$.871 {\pm} .006$	$.525 {\pm} .006$	$.865 {\pm} .006$	$.932 {\pm} .003$	$.818 {\pm} .021$	$1.21 {\pm}.005$
TabSyn	$.915 {\pm} .002$	$.764 {\pm} .004$	$.920 {\pm} .005$	$.938 {\pm} .002$	$.582 {\pm} .008$	$.861 {\pm} .027$
TabDDPM	$.904 {\pm} .006$	$.758 {\pm} .013$	$.916 {\pm} .003$	$.927 {\pm} .004$	$.592 {\pm} .011$	$4.86{\pm}3.04$
RESEARCH	.873 _{±0.006}	.715 _{±0.014}	.920 _{±0.005}	.925 _{±0.005}	XXX	XXX

Table 1: AUC (classification task) and RMSE (regression task) scores of Machine Learning Efficiency

Pair-wise column correlation for 'Adult'

Data Quality: Column Pair Trends (Average Score=0.98) Data Quality: Column Pair Trends (Average Score=0.96)

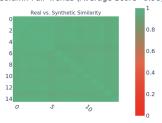


Figure 5: TabDDPM

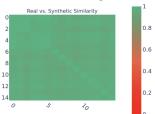


Figure 6: Our model

Conclusion

- Developed a **new method** to generate synthetic data.
- Removing the multinomial diffusion model from TabDDPM allows us to simplify the model while maintaining similar generation quality.
- Tested 5 different versions of the model, and went through more than 15 different combinations of hyperparameter settings for each version.
 - There is an impact of noise level on the quality of generation
- Studied and calculated the quality metrics.
- Figured out how the TabDDPM model works and tested it on several datasets.
- See more results in Appendix and GitHub.

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Appendix

Datasets description (1/2)

- Adult: The 'Adult Census Income' dataset contains information about demographic, educational and employment characteristics of individuals. The task is to predict whether the annual income of a person exceeds \$50,000.
- Default: The 'Default of Credit Card Clients' dataset contains data
 of customers' default payments in Taiwan. The task is to predict
 whether a client will default payment next month.
- **Shoppers**: The 'Online Shoppers Purchasing Intention Dataset' contains information about a person's web browsing activity. The task is to predict whether a session will result in shopping behavior.

Datasets description (2/2)

- Magic: The 'MAGIC Gamma Telescope' dataset contains data of the simulation of high-energy gamma-ray particles using the Cherenkov ground-based telescope. The goal is to classify these high-energy particles in the atmosphere.
- Beijing: The 'Beijing PM2.5' dataset provides hourly PM2.5 data of US Embassy in Beijing, as well as meteorological data collected at Beijing Capital International Airport. The task is to use this data to predict PM2.5 levels.
- News: The 'Online News Popularity' dataset contains a variety of features about articles published by Mashable over a two-year period. The task is to predict the number of shares in social networks.

Method	Adult	Default	Shoppers	Magic	Beijing	News
SMOTE	$1.60{\pm0.23}$	1.48 ± 0.15	2.68 ± 0.19	$0.91{\scriptstyle\pm0.05}$	$1.85{\scriptstyle\pm0.21}$	5.31 ± 0.46
CTGAN	$16.84{\scriptstyle\pm0.03}$	$16.83{\pm0.04}$	$21.15{\scriptstyle\pm0.10}$	$9.81{\scriptstyle\pm0.08}$	$21.39{\scriptstyle\pm0.05}$	$16.09{\scriptstyle\pm0.02}$
TVAE	$14.22{\pm0.08}$	$10.17{\pm0.05}$	$24.51{\pm0.06}$	$8.25{\pm0.06}$	$19.16{\scriptstyle\pm0.06}$	$16.62{\pm0.03}$
GOGGLE	16.97	17.02	22.33	1.90	16.93	25.32
GReaT	$12.12{\pm0.04}$	$19.94{\scriptstyle\pm0.06}$	$14.51{\scriptstyle\pm0.12}$	$16.16{\scriptstyle\pm0.09}$	$8.25{\scriptstyle\pm0.12}$	OOM
STaSy	$11.29{\pm0.06}$	$5.77{\pm0.06}$	$9.37{\scriptstyle\pm0.09}$	$6.29{\pm0.03}$	$6.71{\scriptstyle\pm0.03}$	$6.89{\scriptstyle\pm0.03}$
CoDi	$21.38{\pm0.06}$	$15.77{\pm0.06}$	$31.84{\scriptstyle\pm0.05}$	$11.56{\pm0.26}$	$16.94{\scriptstyle\pm0.02}$	$32.27{\pm0.04}$
TabSyn	$0.58{\scriptstyle\pm0.06}$	$0.85{\pm0.04}$	$1.43{\pm0.24}$	$0.88{\scriptstyle\pm0.09}$	$1.12{\pm0.05}$	$1.64{\pm}0.04$
TabDDPM	$1.18{\pm0.66}$	$1.45{\pm0.58}$	$2.92{\pm}1.10$	$1.040{\pm0.40}$	$1.30{\pm0.03}$	$78.75{\scriptstyle\pm0.01}$
RESEARCH	$1.57_{\pm 0.98}$	$1.42_{\pm 0.57}$	$1.59_{\pm 0.76}$	$0.905_{\pm0.29}$	XXX	XXX

Table 2: Error rate (%) of column-wise density estimation

Method	Adult	Default	Shoppers	Magic	Beijing	News
SMOTE	$3.28{\scriptstyle\pm0.29}$	8.41±0.38	$3.56{\pm0.22}$	$3.16{\scriptstyle\pm0.41}$	$2.39{\scriptstyle\pm0.35}$	$5.38{\pm0.76}$
CTGAN	$20.23{\scriptstyle\pm1.20}$	$26.95{\scriptstyle\pm0.93}$	$13.08{\scriptstyle\pm0.16}$	$7.00{\scriptstyle\pm0.19}$	$22.95{\scriptstyle\pm0.08}$	$5.37{\pm0.05}$
TVAE	$14.15{\pm0.88}$	$19.50{\scriptstyle\pm0.95}$	$18.67{\pm0.38}$	$5.82{\pm0.49}$	$18.01{\pm0.08}$	$6.17{\pm0.09}$
GOGGLE	45.29	21.94	23.90	9.47	45.94	23.19
GReaT	$17.59{\scriptstyle\pm0.22}$	$70.02{\scriptstyle\pm0.12}$	$45.16{\scriptstyle\pm0.18}$	$10.23{\pm0.40}$	$59.60{\scriptstyle \pm 0.55}$	OOM
STaSy	$14.51{\pm0.25}$	$5.96{\scriptstyle\pm0.26}$	$8.49{\scriptstyle\pm0.15}$	$6.61{\scriptstyle\pm0.53}$	$8.00{\pm0.10}$	$3.07{\pm0.04}$
CoDi	$22.49{\scriptstyle\pm0.08}$	$68.41{\scriptstyle\pm0.05}$	$17.78{\scriptstyle\pm0.11}$	$6.53{\scriptstyle\pm0.25}$	$7.07{\pm0.15}$	$11.10{\scriptstyle\pm0.01}$
TabSyn	$1.54{\pm}0.27$	$2.05{\pm0.12}$	$2.07{\pm0.21}$	$1.06{\scriptstyle\pm0.31}$	$2.24{\pm0.28}$	1.44 ± 0.03
TabDDPM	$2.16{\scriptstyle\pm1.11}$	$2.91{\pm}2.94$	$9.06{\pm}8.33$	$0.746{\scriptstyle\pm0.76}$	$2.71{\pm0.09}$	$13.16{\scriptstyle\pm0.11}$
RESEARCH	$3.00_{\pm 1.59}$	$2.21_{\pm 1.38}$	$2.39_{\pm 1.39}$	$1.15_{\pm 2.13}$	XXX	XXX

Table 3: Error rate (%) of pair-wise column correlation score

Methods	Adult AUC ↑	Default AUC ↑	Shoppers AUC ↑	Magic AUC ↑	Beijing RMSE ↓	News RMSE ↓
Real	$.927 {\pm} .000$	$.770 {\pm}.005$	$.926 {\pm} .001$	$.946 {\pm} .001$	$.423 {\pm} .003$	$.842 {\pm} .002$
SMOTE	.899±.007	.741±.009	.911±.012	.934±.008	.593±.011	.897±.036
CTGAN	$.886 {\pm} .002$	$.696 {\pm} .005$	$.875 {\pm} .009$	$.855 {\pm} .006$	$.902 {\pm} .019$	$.880 {\pm} .016$
TVAE	$.878 {\pm} .004$	$.724 {\pm}.005$	$.871 {\pm} .006$	$.887 {\pm}.003$	$.770 {\pm} .011$	$1.01 {\pm}.016$
GOGGLE	$.778 {\pm}.012$	$.584 {\pm} .005$	$.658 {\pm} .052$	$.654 {\pm} .024$	$1.09 {\scriptstyle \pm .025}$	$.877 {\pm} .002$
GReaT	$.913 {\pm}.003$	$.755 {\pm} .006$	$.902 {\pm} .005$	$.888 \pm .008$	$.653 {\pm} .013$	OOM
STaSy	$.906 {\pm}.001$	$.752 {\pm} .006$	$.914 {\pm} .005$	$.934 {\pm}.003$	$.656 {\pm} .014$	$.871 {\pm} .002$
CoDi	$.871 {\pm} .006$	$.525 {\pm} .006$	$.865 {\pm} .006$	$.932 {\pm} .003$	$.818 {\pm} .021$	$1.21 {\pm}.005$
TabSyn	$.915 {\pm}.002$	$.764 {\pm} .004$	$.920 {\pm} .005$	$.938 {\pm} .002$	$.582 {\pm} .008$	$.861 {\pm} .027$
TabDDPM	$.904 {\pm} .006$	$.767 {\pm} .008$	$.916 {\pm} .003$	$.927 {\pm} .004$	$.592 {\pm} .011$	$4.86{\pm}3.04$
RESEARCH	.873 _{±0.006}	.765 _{±0.008}	.920 _{±0.005}	.925 _{±0.005}	XXX	XXX

Table 4: AUC (classification task) and RMSE (regression task) scores of Machine Learning Efficiency

Methods	Adult	Default	Shoppers	Magic	Beijing	News
CTGAN	77.74±0.15	62.08±0.08	76.97±0.39	86.90±0.22	96.27±0.14	96.96±0.17
TVAE	$98.17{\scriptstyle\pm0.17}$	$85.57{\pm0.34}$	$58.19{\scriptstyle\pm0.26}$	$86.19{\pm0.48}$	$97.20{\scriptstyle\pm0.10}$	$86.41{\scriptstyle\pm0.17}$
GOGGLE	50.68	68.89	86.95	90.88	88.81	86.41
GReaT	$55.79{\scriptstyle\pm0.03}$	$85.90{\scriptstyle\pm0.17}$	$78.88{\scriptstyle\pm0.13}$	$85.46{\scriptstyle\pm0.54}$	$98.32{\scriptstyle\pm0.22}$	_
STaSy	$82.87{\pm0.26}$	$90.48{\scriptstyle\pm0.11}$	$89.65{\scriptstyle\pm0.25}$	$86.56{\scriptstyle\pm0.19}$	$89.16{\scriptstyle\pm0.12}$	$94.76{\scriptstyle\pm0.33}$
CoDi	$77.58{\scriptstyle\pm0.45}$	$82.38{\scriptstyle\pm0.15}$	$94.95{\scriptstyle\pm0.35}$	$85.01{\pm0.36}$	$98.13{\scriptstyle\pm0.38}$	$87.15{\scriptstyle\pm0.12}$
TabSyn	$99.52{\scriptstyle\pm0.10}$	$99.26{\scriptstyle\pm0.27}$	$99.16{\scriptstyle\pm0.22}$	$99.38{\scriptstyle\pm0.27}$	$98.47{\scriptstyle\pm0.10}$	$96.80{\scriptstyle\pm0.25}$
TabDDPM	$95.15{\scriptstyle\pm0.20}$	$97.76{\scriptstyle\pm0.36}$	$95.14{\scriptstyle\pm0.68}$	$98.11{\scriptstyle\pm0.17}$	$97.93{\scriptstyle\pm0.30}$	$0.00{\pm}0.00$
RESEARCH	94.61±0.22	97.63±0.29	95.37±0.64	$99.41_{\pm 0.51}$	XXX	XXX

Table 5: Comparison of α -Precision scores

Methods	Adult	Default	Shoppers	Magic	Beijing	News
CTGAN	30.80 ± 0.20	$18.22{\scriptstyle\pm0.17}$	$31.80{\scriptstyle\pm0.35}$	$11.75{\pm0.20}$	34.80 ± 0.10	$24.97{\scriptstyle\pm0.29}$
TVAE	$38.87{\scriptstyle\pm0.31}$	$23.13{\scriptstyle\pm0.11}$	$19.78{\scriptstyle\pm0.10}$	$32.44{\pm0.35}$	$28.45{\scriptstyle\pm0.08}$	$29.66{\scriptstyle\pm0.21}$
GOGGLE	8.80	14.38	9.79	9.88	19.87	2.03
GReaT	$49.12{\scriptstyle\pm0.18}$	42.04 ± 0.19	$44.90{\scriptstyle\pm0.17}$	$34.91{\scriptstyle\pm0.28}$	$43.34{\scriptstyle\pm0.31}$	_
STaSy	$29.21{\pm0.34}$	$39.31{\scriptstyle\pm0.39}$	$37.24{\scriptstyle\pm0.45}$	$53.97{\pm0.57}$	$54.79{\scriptstyle\pm0.18}$	$39.42{\scriptstyle\pm0.32}$
CoDi	$9.20{\scriptstyle\pm0.15}$	$19.94{\scriptstyle\pm0.22}$	$20.82{\scriptstyle\pm0.23}$	$50.56{\scriptstyle\pm0.31}$	$52.19{\scriptstyle\pm0.12}$	34.40 ± 0.31
TabSyn	$47.56{\scriptstyle\pm0.22}$	$48.00{\scriptstyle\pm0.35}$	$48.95{\scriptstyle\pm0.28}$	$48.03{\scriptstyle\pm0.23}$	$55.84{\scriptstyle\pm0.19}$	$45.04{\scriptstyle\pm0.34}$
TabDDPM	$49.76{\scriptstyle\pm0.25}$	$47.25{\scriptstyle\pm0.35}$	$49.76{\scriptstyle\pm0.25}$	$47.96{\scriptstyle\pm0.42}$	$56.92{\scriptstyle\pm0.13}$	$0.00{\pm}0.00$
RESEARCH	48.28±0.25	46.69±0.31	51.06±0.30	$49.36_{\pm0.12}$	XXX	XXX

Table 6: Comparison of β -Recall scores

Method	Adult	Default	Shoppers	Magic	Beijing	News
SMOTE	0.9710	0.9274	0.9086	0.9961	0.9888	0.9344
CTGAN	0.5949	0.4875	0.7488	0.6728	0.7531	0.6947
TVAE	0.6315	0.6547	0.2962	0.7706	0.8659	0.4076
GOGGLE	0.1114	0.5163	0.1418	0.9526	0.4779	0.0745
GReaT	0.5376	0.4710	0.4285	0.4326	0.6893	_
STaSy	0.4054	0.6814	0.5482	0.6939	0.7922	0.5287
CoDi	0.2077	0.4595	0.2784	0.7206	0.7177	0.0201
TabSyn	0.9986	0.9870	0.9740	0.9732	0.9603	0.9749
TabDDPM	0.9530	0.9834	0.8666	0.9998	0.9513	0.0002
RESEARCH	0.9350	0.9653	0.9300	0.9998	XXX	XXX

Table 7: Detection score (C2ST) using logistic regression classifier. Higher scores indicate better performance.

Appendix

Method	Default	Shoppers
SMOTE	91.41%±3.42	96.40%±4.70
STaSy	$50.23\% \pm 0.09$	$51.53\% \pm 0.16$
CoDi	$51.82\% \pm 0.26$	$51.06\% \pm 0.18$
TabSyn	$51.20\% \pm 0.18$	$52.90\% \pm 0.22$
TabDDPM	$50.17\% \pm 1.20$	$52.42\% \pm 0.25$
RESEARCH	$51.59\% \pm 1.26$	51.07%±1.01

Table 8: DCR score