# Report

#### **Exercise 1:**

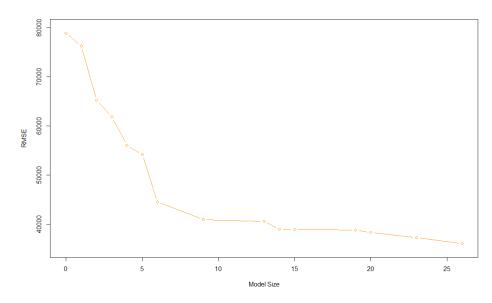
1. Use the following R code to load the Ames data, and drop the variables OverallCond and OverallQual.

```
#load the data file
rawdata=read.csv("ames.csv",header=TRUE)
#Drop the variables OverallCond and OverallQual
rawdata$OverallCond<-NULL
rawdata$OverallQual<-NULL</pre>
```

2. Using forward selection, create a series of models up to length 15. The fit\_0 model is the model with no predictors. The R code of created 15 models and their related chosen variables are shown as below:

```
# a series of models up to complexity length 15
fit_0 = lm(SalePrice \sim 1, data = data2)
fit_1 = lm(SalePrice ~ LotArea, data=data2)
fit_2 = lm(SalePrice ~ LotArea + YearRemodAdd, data=data2)
fit_3 = lm(SalePrice ~ LotArea + YearRemodAdd + BsmtFinSF1, data=data2)
fit_4 = lm(SalePrice ~ LotArea + YearRemodAdd + BsmtFinSF1 + BsmtUnfSF, data=data2)
fit_5 = lm(SalePrice ~ LotArea + YearRemodAdd + BsmtFinSF1 + BsmtUnfSF + X1stFlrSF, data=data2)
fit_6 = lm(SalePrice ~ LotArea + YearRemodAdd + BsmtFinSF1 + BsmtUnfSF + X1stFlrSF
X2ndFlrsF, data=data2)
fit_7 = lm(SalePrice ~ LotArea + YearRemodAdd + BsmtFinSF1 + BsmtUnfSF + X1stFlrSF + X2ndFlrSF +
                                                     KitchenQual, data=data2)
\texttt{fit\_8} = \texttt{lm}(\texttt{SalePrice} \sim \texttt{LotArea} + \texttt{YearRemodAdd} + \texttt{BsmtFinSF1} + \texttt{BsmtUnfSF} + \texttt{X1stFlrSF} + \texttt{X2ndFlrSF} + 
                                                     KitchenQual +GarageQual, data=data2)
\label{eq:fit_9} = \texttt{lm}(\texttt{SalePrice} \sim \texttt{LotArea} + \texttt{YearRemodAdd} + \texttt{BsmtFinSF1} + \texttt{BsmtUnfSF} + \texttt{X1stFlrSF} + \texttt{X2ndFlrSF} + \texttt{X2ndF
                                                     KitchenQual +GarageQual + YearBuilt, data=data2)
fit_10 = lm(SalePrice ~ LotArea + YearRemodAdd + BsmtFinSF1 + BsmtUnfSF + X1stFlrSF + X2ndFlrSF +
                                                         KitchenQual +GarageQual + YearBuilt +Street, data=data2)
fit_11 = lm(SalePrice ~ LotArea + YearRemodAdd + BsmtFinSF1 + BsmtUnfSF
                                                                                                                                                                                                                                                                                                        + X1stFlrSF + X2ndFlrSF +
                                                         KitchenQual +GarageQual + YearBuilt +Street +MSZoning, data=data2)
fit_12 = lm(SalePrice ~ LotArea + YearRemodAdd + BsmtFinSF1 + BsmtUnfSF + X1stFlrSF + X2ndFlrSF +
                                                         KitchenQual +GarageQual + YearBuilt +Street+MSZoning +GarageArea , data=data2)
fit_13 = lm(SalePrice ~ LotArea + YearRemodAdd + BsmtFinSF1 + BsmtUnfSF + X1stFlrSF + X2ndFlrSF
                                                         KitchenQual +GarageQual + YearBuilt +Street+MSZoning +GarageArea +ExterQual, data=data2)
fit_14 = lm(SalePrice ~ LotArea + YearRemodAdd + BsmtFinSF1 + BsmtUnfSF + X1stFlrSF + X2ndFlrSF +
                                                         KitchenQual +GarageQual + YearBuilt +Street+MSZoning +GarageArea +ExterQual+
                                                         BsmtQual, data=data2)
```

3. The chart plotting the model complexity as the x-axis variable and RMSE as the y-axis variable is shown as below.



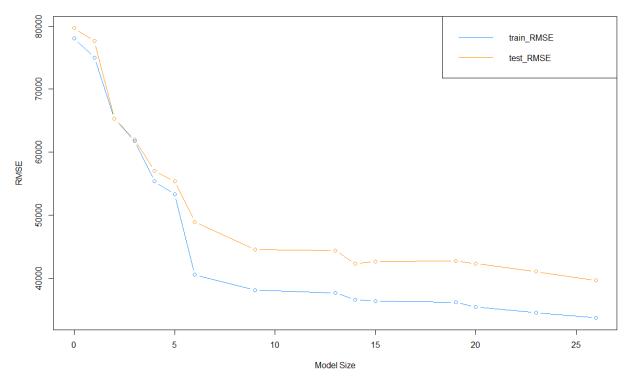
From the chart, it is observed that as model complexity rises, the RMSE of the dataset decreases. Thus, as the number of variables in the linear regression model increases, the prediction accuracy of the model improves. In conclusion, we should use the full-size model that includes all the variables. Because the full-size model has the highest prediction accuracy. The criterion we are using to make this statement is RMSE.

#### Exercise 2:

1. Use the following code to split the train dataset and test dataset. Use 50% of all the dataset as train dataset and the other 50% as test dataset.

```
set.seed(123)
num_obs = nrow(data2)
#50% of data2 as train dataset, and the other 50% as test dataset
train_index = sample(num_obs, size = trunc(0.50 * num_obs))
train_data = data2[train_index, ]
test_data = data2[-train_index, ]
```

The chart of Train and Test RMSE for the 15 models we fit in Exercise 1 is shown as below:



From the chart, it can be observed that as model complexity rises, the RMSE of the train dataset and test dataset all decrease.

2. The model we use to predict SalePrice is **Random Forest** model. We choose the following 69 variables as regressors.

```
[1] "MSSubClass"
                        "MSZoning"
                                          "LotFrontage"
                                                             "LotArea"
                                                                               "Street"
                                                                                                  "LotShape"
[7] "LotConfig"
[13] "YearBuilt"
                        "Neighborhood"
                                                             "Condition2"
                                                                               "BldgType"
                                          "Condition1"
                                                                                                  "HouseStyle"
                                                             "RoofMatl"
                        "YearRemodAdd"
                                          "RoofStyle"
                                                                               "Exterior1st"
                                                                                                  "Exterior2nd"
                                          "ExterQual"
[19] "MasVnrType"
                                                             "ExterCond"
                        "MasVnrArea"
                                                                               "Foundation"
                                                                                                  "BsmtQual"
[25] "BsmtCond"
[31] "BsmtUnfSF"
                                                             "BsmtFinSF1"
                        "BsmtExposure"
                                          "BsmtFinType1"
                                                                               "BsmtFinType2"
                                                                                                 "BsmtFinSF2"
                                                                                                  "Electrical"
                        "TotalBsmtSF"
                                          "Heating"
                                                             "HeatingQC"
                                                                               "CentralAir"
[37] "X1stFlrSF"
[43] "FullBath"
                                                             "GrLivArea"
                        "X2ndF1rSF"
                                          "LowOualFinSF"
                                                                               "BsmtFullBath"
                                                                                                  "BsmtHalfBath"
                        "HalfBath"
                                          "BedroomAbvGr"
                                                             "KitchenAbvGr"
                                                                               "KitchenQual'
                                                                                                  "TotRmsAbvGrd"
[49] "Functional"
[55] "GarageArea"
                                                                                                  "GarageCars"
                        "Fireplaces"
                                                             "GarageYrBlt"
                                                                               "GarageFinish"
                                          "GarageType"
                        "GarageQual"
                                          "GarageCond"
                                                                                                  "OpenPorchSF"
                                                             "PavedDrive"
                                                                                "WoodDeckSF"
[61] "EnclosedPorch"
[67] "YrSold"
                       "X3SsnPorch"
                                          "ScreenPorch"
                                                             "PoolArea"
                                                                               "MiscVal"
                                                                                                  "MoSold"
                        "SaleType"
                                          "SaleCondition"
```

According to our prediction results, the Train RMSE is 13127.19 and the Test RMSE is 31998.24, as is shown below:

```
> rf_train_rmse
[1] 13127.19
> rf_test_rmse
[1] 31998.24
```

## 3. The procedure to build the **Random Forest** model is shown as below:

## (1) Data Cleaning:

Firstly, we drop the variables Id, Alley, LandContour, Utilities, LandSlope, PoolQC, Fence, MiscFeature, FireplaceQu and use the other 69 variables as regressors, as is discussed in problem 2.

Secondly, we found that there are 18% missing values in the column LotFrontage, so we fill these missing values with 0.

Thirdly, use na.omit() function to drop the rows that contain missing values. After doing this, there are 1338 rows left. And we name this dataset as data2.

#### (2) Train-Test data split

As is discussed in problem 1, we use 50% of data2 as train dataset and the other 50% as test dataset.

## (3) Build Random Forest model

Use randomForest() function to build the model. According to the results, some parameters of Random Forest model is shown as below:

```
Type of random forest: regression
Number of trees: 1000
No. of variables tried at each split: 23

Mean of squared residuals: 1034399522
% Var explained: 83.03
```

And two kinds of importance scores of the 69 regressors are shown as below. The higher the score is, the more important the variable is.

|               | %IncMSE     | IncNodePurity |
|---------------|-------------|---------------|
| GrLivArea     | 41.63509815 | 707867138974  |
| Neighborhood  | 38.96564125 | 524472933551  |
| X1stFlrSF     | 22.38672413 | 161925912834  |
| TotalBsmtSF   | 17.60193772 | 204678103922  |
| ExterQual     | 16.88226023 | 270488709774  |
| FullBath      | 16.63740045 | 129226400529  |
| GarageCars    | 14.46461917 | 578884350910  |
| GarageArea    | 13.89242932 | 223322898277  |
| KitchenQual   | 13.53909443 | 89474810663   |
| YearBuilt     | 13.28958134 | 93073011291   |
| BsmtFinSF1    | 11.58756907 | 70306125938   |
| LotArea       | 10.93328613 | 75260611773   |
|               |             | 137165086707  |
| X2ndF1rSF     | 10.78985917 |               |
| GarageType    | 10.51974988 | 18619199669   |
| YearRemodAdd  | 10.50333764 | 30888258418   |
| BsmtFinType1  | 9.93105445  | 17620743946   |
| MSZoning      | 9.89680155  | 7994949357    |
| BsmtQual      | 9.65793723  | 89623738226   |
| Fireplaces    | 9.18614212  | 19562288938   |
| MasVnrArea    | 8.39810276  | 136431328667  |
| GarageYrBlt   | 8.34854478  | 30928448786   |
| HouseStyle    | 8.33567725  | 10154806989   |
| MSSubClass    | 8.28245423  | 8740988333    |
| OpenPorchSF   | 8.21216415  | 21386849157   |
| GarageFinish  | 7.39885511  | 15792473084   |
|               |             |               |
| BsmtUnfSF     | 7.19049491  | 22205811454   |
| Exterior2nd   | 7.01399647  | 51624987344   |
| Foundation    | 6.84616666  | 6707116881    |
| HalfBath      | 6.58432145  | 5961383094    |
| BsmtFullBath  | 6.48852499  | 6439097573    |
| BedroomAbvGr  | 5.82073732  | 10407769936   |
| BldgType      | 5.43368545  | 3505099586    |
|               |             |               |
| BsmtExposure  | 5.36124517  | 14804098464   |
| Exterior1st   | 5.31161516  | 43665319592   |
| TotRmsAbvGrd  | 5.21440715  | 34473524055   |
| HeatingQC     | 5.03050032  | 8359422461    |
| CentralAir    | 4.07708524  | 3663757410    |
| WoodDeckSF    | 3.96013963  | 15439328117   |
| ScreenPorch   | 3.09798741  | 4726763767    |
| RoofStyle     | 3.07068364  | 9278109571    |
| MasVnrType    | 2.61681634  | 6630322115    |
| BsmtFinSF2    | 2.52548514  | 2997954594    |
|               |             |               |
| KitchenAbvGr  | 2.47203972  | 1149035560    |
| SaleCondition | 2.39887616  | 7249080934    |
| Functional    | 2.26598562  | 3667722557    |
| SaleType      | 2.02189162  | 3923647166    |
| BsmtCond      | 1.82246827  | 2146451346    |
| LotFrontage   | 1.78538240  | 16944289413   |
| EnclosedPorch | 1.45333704  | 3392179877    |
| LotConfig     | 1.25767666  | 12700781647   |
| Heating       | 1.25052494  | 976561971     |
| YrSold        | 1.14669331  | 6466151554    |
| PavedDrive    | 0.92307804  | 764312215     |
| MiscVal       | 0.86960683  | 268091097     |
| BsmtHalfBath  | 0.70634127  | 7242289193    |
| GarageCond    | 0.66330197  | 703041617     |
| ExterCond     | 0.59314937  | 2758468097    |
|               |             |               |
| GarageQual    | 0.58809113  | 4030307485    |
| Condition1    | 0.58446233  | 5336238774    |
| RoofMatl      | 0.05018633  | 11097139607   |
| Street        | 0.00000000  | 109367386     |
| PoolArea      | 0.00000000  | 42922887      |
| LotShape      | -0.31010169 | 10144405756   |
| X3SsnPorch    | -0.50070934 | 104352716     |
| LowQualFinSF  | -0.55788930 | 2618222454    |
| Electrical    | -0.72318737 | 914373677     |
| MoSold        | -0.95372896 | 15403087913   |
| BsmtFinType2  | -1.39112732 | 2476316330    |
| Condition2    | -2.44126746 | 1341054044    |
| COLLETE TOTAL | 22207 10    | 15.1051074    |
|               |             |               |

## (4) Predict and calculate the Train and Test RMSE

After building the Random Forest model, use the following code to predict the SalePrice on the train dataset and test dataset. And calculate the Train and Test RMSE.

```
pred_rf=predict(rf_fit,newdata = test_data)
pred_rf_train=predict(rf_fit,newdata = train_data)

rf_train_rmse=rmse(train_data$SalePrice,pred_rf_train)
rf_train_rmse

rf_test_rmse=rmse(test_data$SalePrice,pred_rf)
rf_test_rmse

As is discussed in Problem 2, the Train RMSE is 13127.19 and the Test RMSE is 31998.24, as is shown below:

> rf_train_rmse
[1] 13127.19

> rf_test_rmse
[1] 31998.24
```

## The advantages of the Random Forest model:

A random forest is an ensemble learning approach to supervised learning. Multiple predictive models are developed, and the results are aggregated to improve classification rates.

The algorithm for a random forest involves sampling cases and variables to create a large number of decision trees. Each case is classified by each decision tree. The most common classification for that case is then used as the outcome.

Random forests tend to be very accurate compared with other classification methods. Additionally, they can handle large problems (many observations and variables), can handle large amounts of missing data in the training set, and can handle cases in which the number of variables is much greater than the number of observations. The provision of OOB error rates and measures of variable importance are also significant advantages.