

(Group: 4)

(Introduction to Data Science)

< Assignment-5 >

Q:1

S1 = "sunshine state enjoy sunshine"

S2 = "brown fox jump high, brown fox run"

S3 = "sunshine state fox run fast"

BOW Model:-

Unique words:

sunshine, state, enjoy, brown, fox, jump, high, run, fast.

	sunshine	state	enjoy	brown	fox	jump	high	run	fast	Total length
S1	2	1	1	0	0	0	0	0	0	4
S2	0	0	0	2	2	1	1	1	0	7
S3	1	1	0	0	1	0	0	1	1	5

vector S1 : [2, 1, 1, 0, 0, 0, 0, 0, 0]

vector S2 : [0, 0, 0, 2, 2, 1, 1, 1, 0]

vector S3 : [1, 1, 0, 0, 1, 0, 0, 1, 1]

TF Model :-

	sunshine	state	enjoy	brown	fox	jump	high	run	fast
tf-S1	1/2	1/4	1/4	0	0	0	0	0	0
tf-S2	0	0	0	2/7	2/7	1/7	1/7	1/7	0
tf-S3	1/5	1/5	0	0	1/5	0	0	1/5	1/5

IDF Model:-

$$IDF = \log \left[\frac{\text{total number of documents}}{\text{number of documents containing current term}} \right]$$

	IDF
sunshine	0.17
state	0.17
enjoy	0.47
brown	0.47
fox	0.17
jump	0.47
high	0.47
run	0.17
fast	0.47

TF.IDF values:-

$$tf.idf = tf_{i,d} \times idf_i$$

	tf.idf -(S1)	tf.idf -(S2)	tf.idf -(S3)
sunshine	0.085	0	0.034
state	0.0425	0	0.034
enjoy	0.1175	0	0
brown	0	0.134	0
fox	0	0.048	0.034
jump	0	0.067	0
high	0	0.067	0
run	0	0.024	0.034
fast	0	0	0.094

Q.2

Cosine similarity between $S1$ & $S3$:-

$$\cos(S1, S3) = \frac{(S1 \cdot S3)}{|S1| \cdot |S3|}$$

$$S1 = [0.085, 0.042, 0.117, 0, 0, 0, 0, 0, 0]$$

$$S3 = [0.034, 0.034, 0, 0, 0.034, 0, 0, 0.034, 0.094]$$

$$\begin{aligned} S1 \cdot S3 = & (0.085 \times 0.034) + (0.042 \times 0.034) + \\ & (0.117 \times 0) + (0 \times 0) + (0 \times 0) + (0 \times 0.034) + \\ & (0 \times 0) + (0 \times 0) + (0 \times 0.034) + (0 \times 0.094) \end{aligned}$$

$$S1 \cdot S3 = 0.0043$$

$$\begin{aligned} |S1| = & [(0.085 \times 0.085) + (0.042 \times 0.042) + (0.117 \times \\ & 0.117) + (0 \times 0) + (0 \times 0) + (0 \times 0) + (0 \times 0) + (0 \times 0) + (0 \times 0)]^{1/2} \\ |S1| = & 0.15 \end{aligned}$$

$$\begin{aligned} |S3| = & [(0.034 \times 0.034) + (0.034 \times 0.034) + (0 \times 0) + \\ & (0 \times 0) + (0.034 \times 0.034) + (0 \times 0) + (0 \times 0) \\ & (0.034 \times 0.034) + (0.094 \times 0.094)]^{1/2} \\ |S3| = & 0.11 \end{aligned}$$

$$\cos(S1, S3) = \frac{(S1 \cdot S3)}{|S1| \cdot |S3|} \Rightarrow \frac{0.0043}{(0.15)(0.11)}$$

$$\boxed{\cos(S1, S3) = 0.2606}$$