

# Parallel Programming Principle and Practice

---

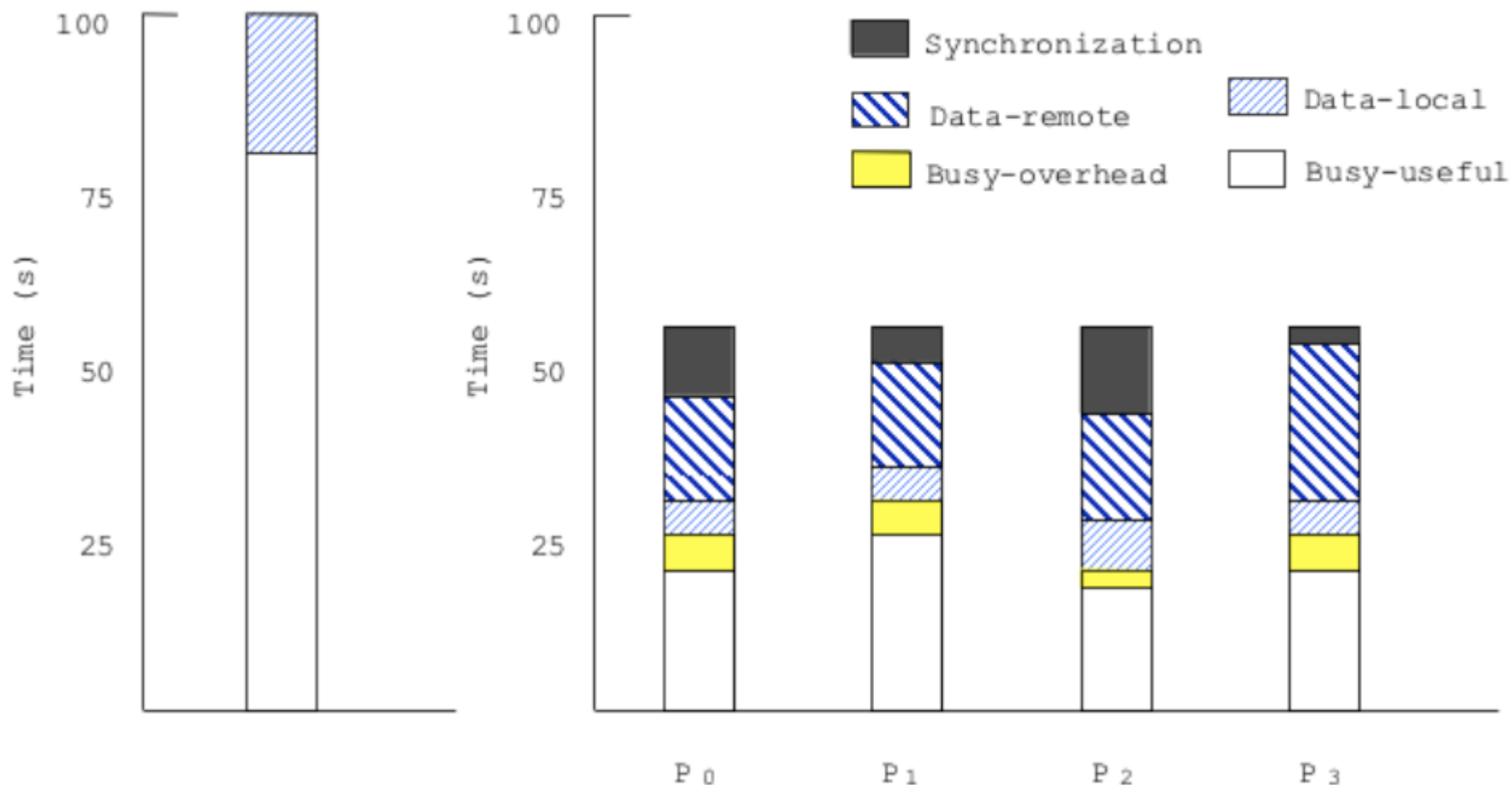
## **Lecture 5 — Parallel Programming: Performance**

# Outline

---

- Components of execution time as seen by processor
- Partitioning for performance
- Relationship of communication, data locality and architecture
- Orchestration for performance

# Processor-Centric Perspective



# Outline

---

- ❑ Components of execution time as seen by processor
- ❑ Partitioning for performance
- ❑ Relationship of communication, data locality and architecture
- ❑ Orchestration for performance

# Partitioning for Performance

---

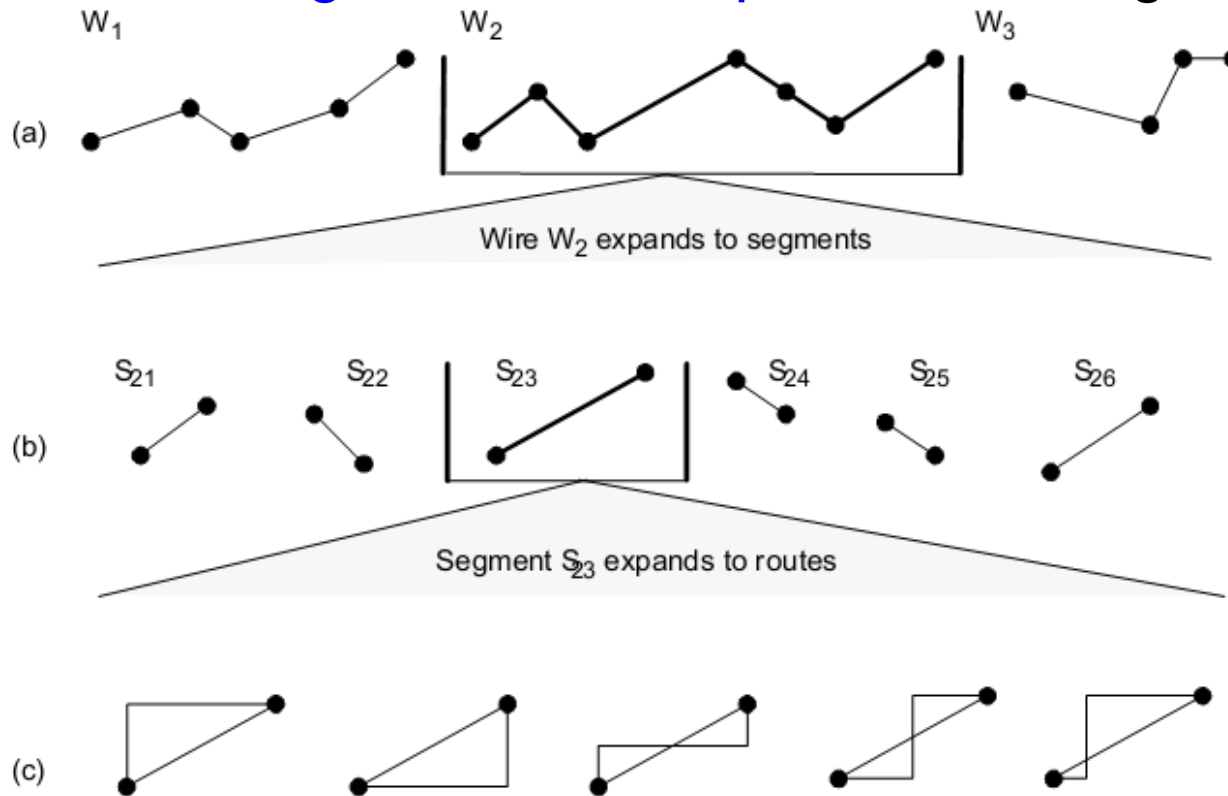
- Balancing the workload and reducing wait time at synch points
- Reducing inherent communication
- Reducing extra work

# Load Balance and Synch Wait Time

- Limit on speedup:  $Speedup_{problem}(p) \leq \frac{\text{Sequential Work}}{\text{Max Work on any Processor}}$ 
  - Work includes data access and other costs
  - Not just equal work, but must be busy at same time
  
- Four parts to load balance and reducing synch wait time
  - Identify enough concurrency
  - Decide how to manage it
  - Determine the granularity at which to exploit it
  - Reduce serialization and cost of synchronization

# Identifying Concurrency

- ❑ Techniques seen for equation solver
  - Loop structure, fundamental dependences, new algorithms
- ❑ *Data Parallelism* versus *Function Parallelism*
- ❑ Often see *orthogonal levels of parallelism*; e.g. VLSI routing



# Identifying Concurrency

## □ Function parallelism

- focuses on distributing execution processes (threads) across different parallel computing nodes
- entire large tasks (procedures) that can be done in parallel on same or different data
  - e.g. different independent grid computations in Ocean
  - e.g. pipelining, as in video encoding /decoding, or polygon rendering
- degree usually modest and does not grow with input size
- difficult to load balance
- often used to reduce synch between data parallel phases



# Identifying Concurrency

□ Most scalable programs data parallel

□ Data parallelism

- Focuses on distributing the data across different parallel computing nodes
- Similar parallel operation sequences performed on elements of large data structures
  - e.g ocean equation solver, pixel-level image processing
- Such as resulting from parallelization of loops
- Usually easy to load balance (e.g ocean equation solver)
- Degree of concurrency usually increase with input or problem size.  
e.g  $O(n^2)$  in equation solver example

# Load Balance and Synch Wait Time

- Limit on speedup:  $Speedup_{problem}(p) \leq \frac{\text{Sequential Work}}{\text{Max Work on any Processor}}$ 
  - Work includes data access and other costs
  - Not just equal work, but must be busy at same time
  
- Four parts to load balance and reducing synch wait time
  - Identify enough concurrency
  - Decide how to manage it
  - Determine the granularity at which to exploit it
  - Reduce serialization and cost of synchronization

# Decide How to Manage Concurrency

❑ *Static* versus *Dynamic* techniques

❑ **Static**

- Algorithmic assignment based on input; will not change
- Low runtime overhead
- Computation must be predictable
- Preferable when applicable (except in multiprogrammed or heterogeneous environment)

❑ **Dynamic**

- Adapt at runtime to balance load
- Can increase communication and reduce locality
- Can increase task management overheads

# Dynamic Assignment

## □ Profile-based (semi-static)

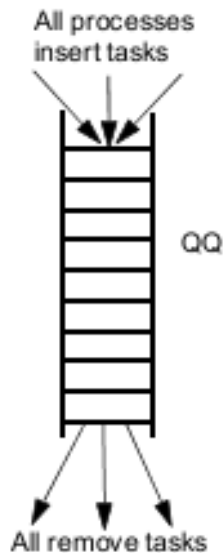
- Profile work distribution at runtime, and repartition dynamically
- Applicable in many computations, e.g. some graphics

## □ Dynamic Tasking

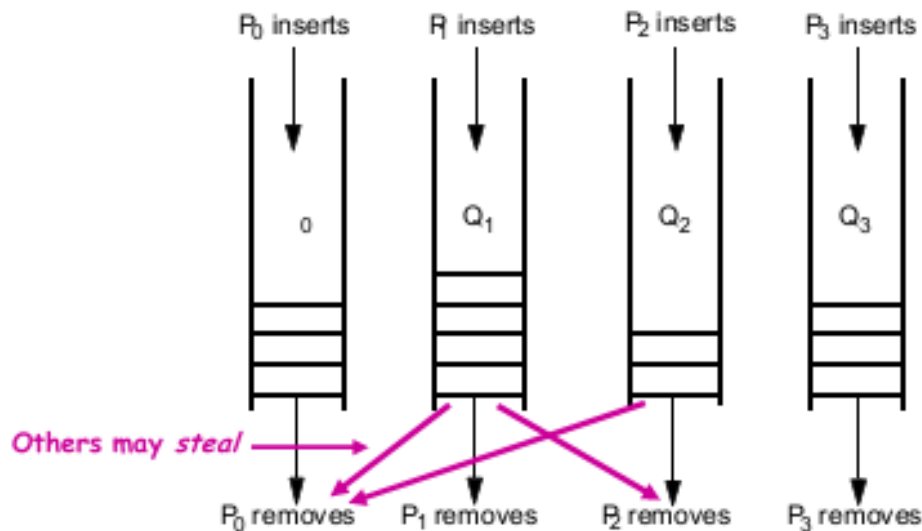
- Deal with unpredictability in program or environment (e.g. Raytrace)
  - computation, communication, and memory system interactions
  - multiprogramming and heterogeneity
  - used by runtime systems and OS too
- Pool of tasks; take and add tasks until done
- e.g. “self-scheduling” of loop iterations (shared loop counter)

# Dynamic Tasking with Task Queues

- Centralized versus distributed queues
- Task stealing with distributed queues
  - Can compromise communication and locality, and increase synchronization
  - Whom to steal from, how many tasks to steal, ...
  - Termination detection
  - Maximum imbalance related to size of task



(a) Centralized task queue



(b) Distributed task queues (one per process)

# Load Balance and Synch Wait Time

- Limit on speedup:  $Speedup_{problem}(p) \leq \frac{\text{Sequential Work}}{\text{Max Work on any Processor}}$ 
  - Work includes data access and other costs
  - Not just equal work, but must be busy at same time
  
- Four parts to load balance and reducing synch wait time
  - Identify enough concurrency
  - Decide how to manage it
  - Determine the granularity at which to exploit it
  - Reduce serialization and cost of synchronization

# Determining Task Granularity

- Task granularity: amount of work associated with a task
- General rule
  - Coarse-grained => often less load balance
  - Fine-grained => more overhead; often more communication & contention
- Communication & contention actually affected by assignment, not size
  - Overhead by size itself too, particularly with task queues

# Load Balance and Synch Wait Time

- Limit on speedup:  $Speedup_{problem}(p) \leq \frac{\text{Sequential Work}}{\text{Max Work on any Processor}}$ 
  - Work includes data access and other costs
  - Not just equal work, but must be busy at same time
  
- Four parts to load balance and reducing synch wait time
  - Identify enough concurrency
  - Decide how to manage it
  - Determine the granularity at which to exploit it
  - Reduce serialization and cost of synchronization



# Reducing Serialization

- ❑ Careful about assignment and orchestration (including scheduling)
- ❑ Event synchronization
  - Reduce use of conservative synchronization
    - e.g. point-to-point instead of barriers, or granularity of pt-to-pt
  - But fine-grained synch more difficult to program, more synch ops.
- ❑ Mutual exclusion
  - Separate locks for separate data
    - e.g. locking records in a database: lock per process, record, or field
    - lock per task in task queue, not per queue
    - finer grain => less contention/serialization, more space, less reuse
  - Smaller, less frequent critical sections
    - Do not do reading/testing in critical section, only modification
    - e.g. searching for task to dequeue in task queue, building tree
  - Stagger critical sections in time

# Partitioning for Performance

---

- ☐ Balancing the workload and reducing wait time at synch points
- ☐ Reducing inherent communication
- ☐ Reducing extra work

# Reducing Inherent Communication

- ❑ Communication is expensive!
- ❑ Measure: communication to computation ratio
- ❑ Focus here on inherent communication
  - Determined by assignment of tasks to processes
  - Later see that actual communication can be greater
- ❑ Assign tasks that access same data to same process
- ❑ Solving communication and load balance NP-hard in general case
- ❑ But simple heuristic solutions work well in practice
  - Applications have structure

# Implications of Communication-to-Computation Ratio

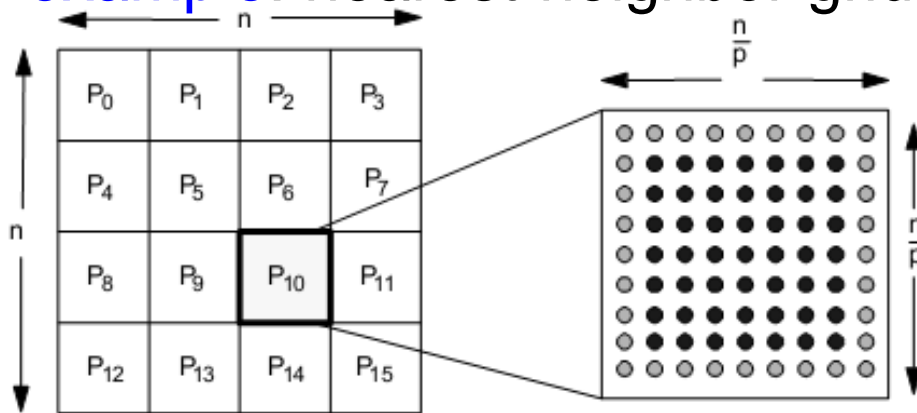
- If denominator is **execution time**, ratio gives **average bandwidth needs**
- If denominator is **operation count**, gives **extremes in impact of latency and bandwidth**
  - **Latency**: assume no latency hiding
  - **Bandwidth**: assume all latency hidden
- Actual impact of communication depends on structure & cost as well

$$\text{Speedup} \leq \frac{\text{Sequential Work}}{\text{Max}(\text{Work} + \text{Synch Wait Time} + \text{Comm Cost})}$$

- Need to keep communication balanced across processors as well

# Domain Decomposition

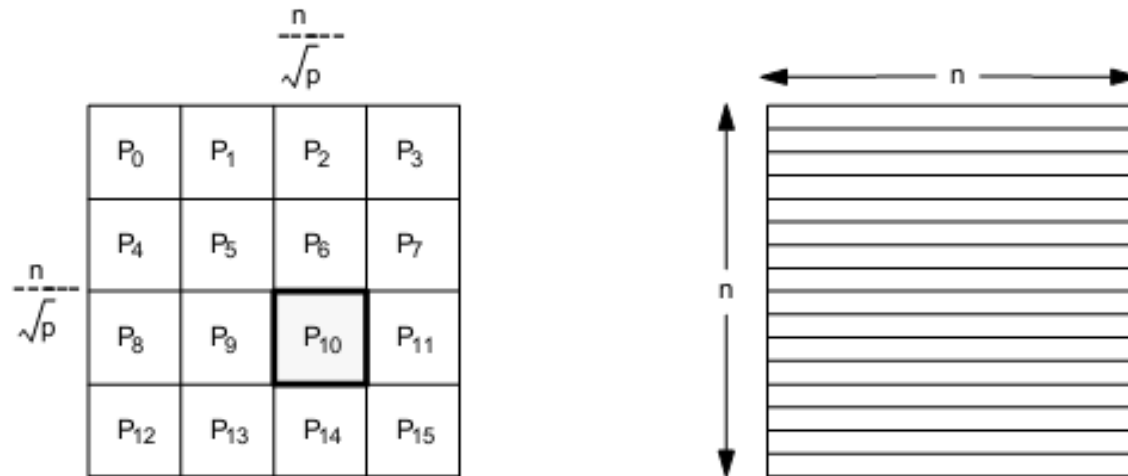
- ❑ Works well for scientific, engineering, graphics, ...applications
- ❑ Exploits local-biased nature of physical problems
  - Information requirements often short-range  
Or long-range but fall off with distance
- ❑ Simple example: nearest-neighbor grid computation



- Depends on  $n, p$ : decreases with  $n$ , increases with  $p$

# Domain Decomposition

- Best domain decomposition depends on information requirements
- Nearest neighbor example: **block** versus **strip** decomposition



- Comm to comp:  $\frac{4\sqrt{p}}{n}$  for **block**,  $\frac{2\sqrt{p}}{n}$  for **strip**
  - Retain block from here on
- Application dependent: strip may be better in other cases
  - E.g. particle flow in tunnel

# Finding a Domain Decomposition

## □ Static, by inspection

- Must be **predictable**: grid example above, and Ocean

## □ Static, but not by inspection

- **Input-dependent**, require analyzing input structure
- e.g. sparse matrix computations, data mining

## □ Semi-static (periodic repartitioning)

- Characteristics **change but slowly**; e.g. Barnes-Hut

## □ Static or semi-static, with dynamic task stealing

- Initial decomposition, but **highly unpredictable**; e.g. ray tracing

# Relation to Load Balance

- ❑ Scatter Decomposition, e.g. initial partition in Raytrace

12	
3	4

Domain decomposition

12		12		12		12	
3	4	3	4	3	4	3	4
12		12		12		12	
3	4	3	4	3	4	3	4
12		12		12		12	
3	4	3	4	3	4	3	4
12		12		12		12	
3	4	3	4	3	4	3	4

Scatter decomposition

Preserve locality in task stealing

- Steal large tasks for locality, steal from same queues, ...



# Partitioning for Performance

---

- ☐ Balancing the workload and reducing wait time at synch points
- ☐ Reducing inherent communication
- ☐ Reducing extra work

# Reducing Extra Work

## □ Common sources of extra work

- Computing a good partition
  - e.g. partitioning in Barnes-Hut or sparse matrix
- Using redundant computation to avoid communication
- Task, data and process management overhead
  - applications, languages, runtime systems, OS
- Imposing structure on communication
  - coalescing messages, allowing effective naming

## □ Architectural Implications

- Reduce need by making communication and orchestration efficient

$$\text{Speedup} \leq \frac{\text{Sequential Work}}{\text{Max}(\text{Work} + \text{Synch Wait Time} + \text{Comm Cost} + \text{Extra Work})}$$

# Outline

---

- ❑ Components of execution time as seen by processor
- ❑ Partitioning for performance
- ❑ Relationship of communication, data locality and architecture
- ❑ Orchestration for performance

# Limitations of Algorithm Analysis

- ❑ Inherent communication in parallel algorithm is not all
  - **artifactual communication** caused by program implementation and architectural interactions can even dominate
  - thus, amount of communication not dealt with adequately
- ❑ Cost of communication determined not only by amount
  - also how communication is structured
  - and cost of communication in system
- ❑ Both **architecture-dependent**, and addressed in orchestration step
- ❑ To understand techniques, first **look at system interactions**

# Memory-Oriented View

- ❑ Multiprocessor as extended memory hierarchy
  - as seen by a given processor
- ❑ Levels in extended hierarchy
  - Registers, caches, local memory, remote memory (topology)
  - Glued together by communication architecture
  - Levels communicate at a certain granularity of data transfer
- ❑ Need to exploit spatial and temporal locality in hierarchy
  - Otherwise extra communication may also be caused
  - Especially important since communication is expensive

# Extended Hierarchy

- ❑ Idealized view: local cache hierarchy + single main memory
- ❑ But reality is more complex
  - Centralized Memory: caches of other processors
  - Distributed Memory: some local, some remote; + network topology
  - Management of levels
    - caches managed by hardware
    - main memory depends on programming model
      - ✓ SAS: data movement between local and remote transparent
      - ✓ message passing: explicit
  - Levels closer to processor are lower latency and higher bandwidth
  - Improve performance through architecture or program locality
  - Tradeoff with parallelism; need good node performance and parallelism

# Artifactual Communication in Extended Hierarchy

- Accesses not satisfied in local portion cause communication
  - Inherent communication, implicit or explicit, causes transfers
    - determined by program
  - Artifactual communication
    - determined by program implementation and architecture interactions
    - poor allocation of data across distributed memories
    - unnecessary data in a transfer
    - unnecessary transfers due to system granularities
    - redundant communication of data
    - finite replication capacity (in cache or main memory)
  - Inherent communication assumes unlimited capacity, small transfers, perfect knowledge of what is needed

# Outline

---

- ❑ Components of execution time as seen by processor
- ❑ Partitioning for performance
- ❑ Relationship of communication, data locality and architecture
- ❑ Orchestration for performance



# Orchestration for Performance

- ❑ Reducing amount of communication
  - **Artifactual:** exploit spatial, temporal locality in extended hierarchy
  - **Inherent:** change logical data sharing patterns in algorithm
- ❑ Structuring communication to reduce cost
- ❑ Let's examine techniques for both

# Reducing Artifactual Communication

## □ Message passing model

- Communication and replication are both explicit
- Even artifactual communication is in explicit messages

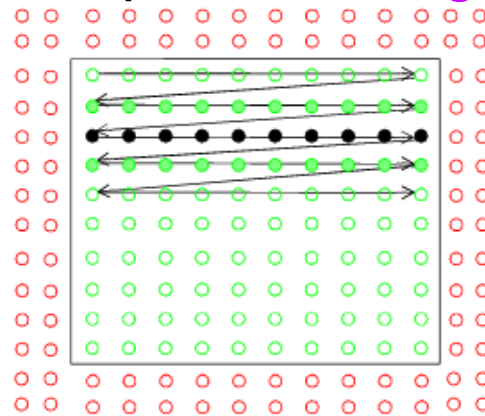
## □ Shared address space model

- More interesting from an architectural perspective
- Occurs transparently due to interactions of program and system
  - sizes and granularities in extended memory hierarchy

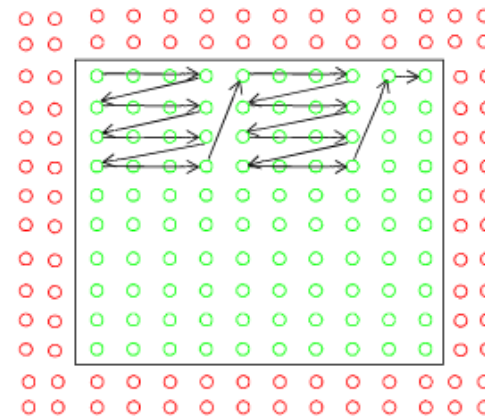
## □ Use shared address space to illustrate issues

# Exploiting Temporal Locality

- Structure algorithm so that working sets map well to hierarchy
  - often techniques to reduce inherent communication do well here
  - schedule tasks for data reuse once assigned
- Multiple data structures in same phase
  - e.g. database records: local versus remote
- Solver example: **blocking**



(a) Unblocked access pattern in a sweep



(b) Blocked access pattern with  $B = 4$

- More useful when  $O(n^{k+1})$  computation on  $O(n^k)$  data
  - many linear algebra computations (factorization, matrix multiply)

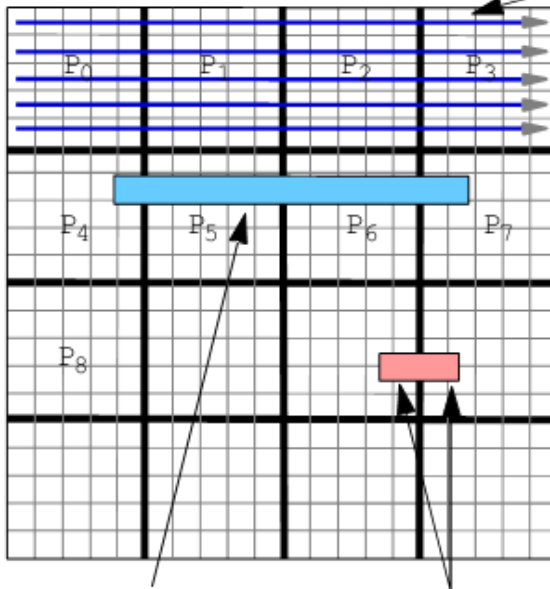
# Exploiting Spatial Locality

- Besides capacity, granularities are important
  - Granularity of allocation
  - Granularity of communication or data transfer
  - Granularity of coherence
- Major spatial-related causes of artifactual communication
  - Conflict misses
  - Data distribution/layout (allocation granularity)
  - Fragmentation (communication granularity)
  - False sharing of data (coherence granularity)
- All depend on how spatial access patterns interact with data structures
  - Fix problems by modifying data structures, or layout/alignment
- Examine later in context of architectures
  - one simple example here: data distribution in SAS solver

# Spatial Locality Example

- Repeated sweeps over 2-d grid, each time adding 1 to elements
- Natural 2-d versus higher-dimensional array representation

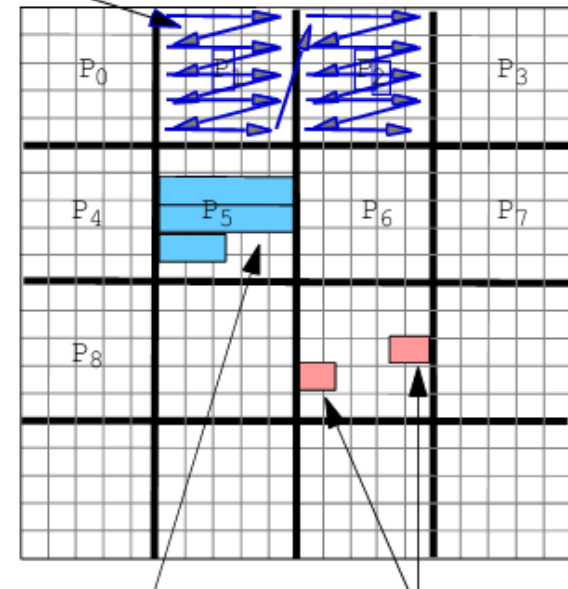
Contiguity in memory layout



Page straddles  
partition boundaries:  
difficult to distribute  
memory well

Cache block  
straddles partition  
boundary

(a) Two-dimensional array



Page does not  
straddle partition  
boundary

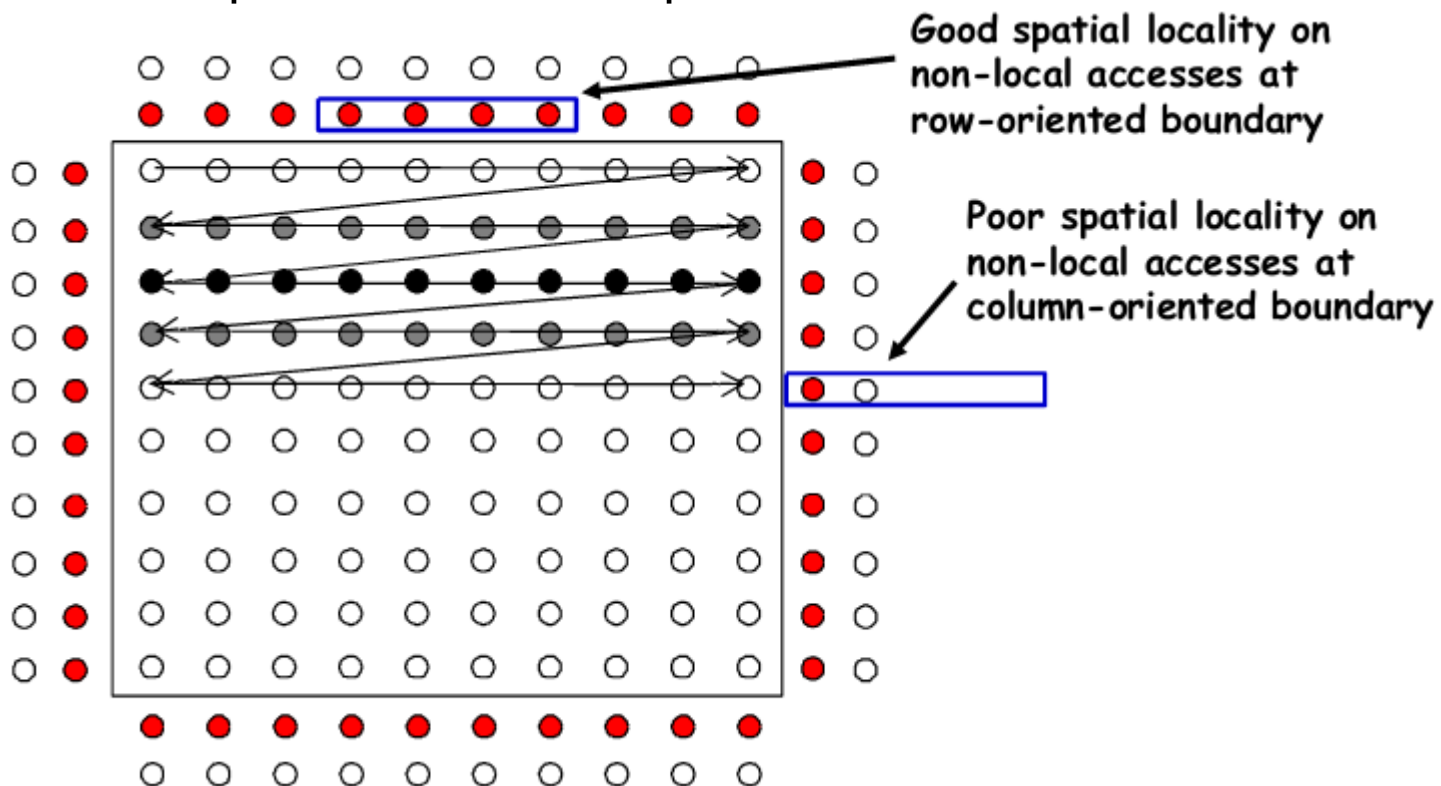
Cache block is  
within a partition

(b) Four-dimensional array

# Tradeoffs with Inherent Communication

## □ Partitioning grid solver: blocks versus rows

- **Blocks** still have a **spatial locality problem on remote data**
- **Rows** can perform better despite worse inherent c-to-c ratio



# Structuring Communication

□ Given amount of communication, goal is to reduce cost

□ Cost of communication as seen by process

$$C = f * (o + l + \frac{n_c/m}{B} + t_c - \text{overlap})$$

- $f$  = frequency of messages
  - $o$  = overhead per message (at both ends)
  - $l$  = network delay per message
  - $n_c$  = total data sent
  - $m$  = number of messages
  - $B$  = bandwidth along path (determined by network, NI, assist)
  - $t_c$  = cost induced by content  $i$  on per message
  - $\text{overlap}$  = amount of latency hidden by overlap with comp. or comm.
- Portion in parentheses is cost of a message (as seen by processor)
- That portion, ignoring overlap, is **latency** of a message
- **Goal: reduce terms in latency and increase overlap**

# Reducing Overhead

- ❑ Can reduce # of messages  $m$  or overhead per message  $o$
- ❑  $o$  is usually determined by hardware or system software
  - Program should try to reduce  $m$  by coalescing messages
  - More control when communication is explicit
- ❑ Coalescing data into larger messages
  - Easy for regular, coarse-grained communication
  - Can be difficult for irregular, naturally fine-grained communication
    - may require changes to algorithm and extra work
      - ✓ coalescing data and determining what and to whom to send



# Reducing Network Delay

□ Network delay component =  $f * h * t_h$

- $h$  = number of hops traversed in network
- $t_h$  = link + switch latency per hop

□ Reducing  $f$ : communicate less, or make messages larger

□ Reducing  $h$

➤ Map communication patterns to network topology

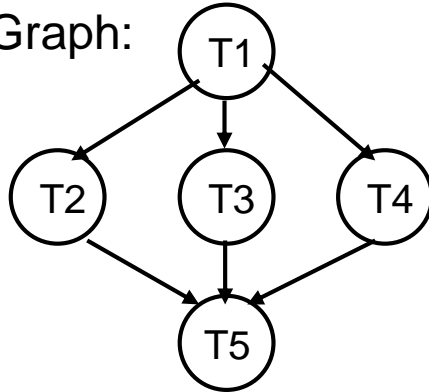
- e.g. nearest-neighbor on mesh and ring; all-to-all

➤ How important is this?

- used to be major focus of parallel algorithms
- depends on number of processors, how  $t_h$ , compares with other components
- less important on modern machines
  - ✓ overheads, processor count, multiprogramming

# Mapping of Task Communication Patterns to Topology

Task Graph:

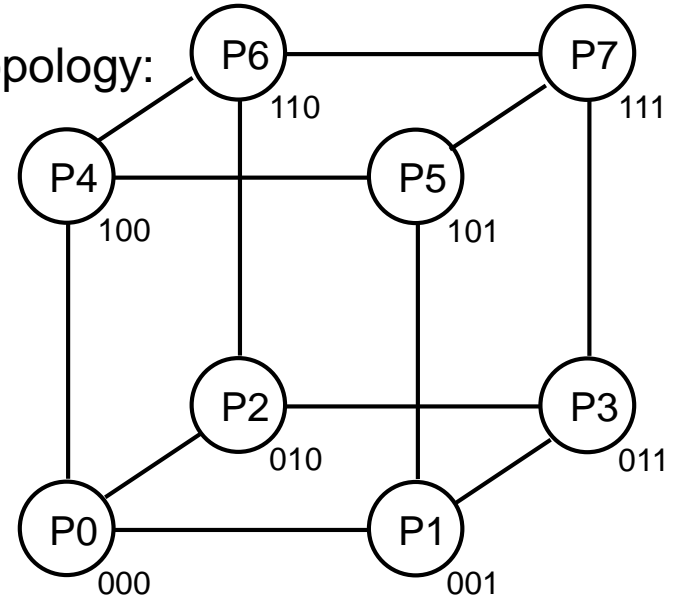


Poor Mapping:

T1 runs on P0  
 T2 runs on P5  
 T3 runs on P6  
 T4 runs on P7  
 T5 runs on P0

- Communication from T1 to T2 requires 2 hops  
 Route: P0-P1-P5
- Communication from T1 to T3 requires 2 hops  
 Route: P0-P2-P6
- Communication from T1 to T4 requires 3 hops  
 Route: P0-P1-P3-P7
- Communication from T2, T3, T4 to T5
  - similar routes to above reversed (2-3 hops)

Parallel System Topology:  
 3D Binary Hypercube



Better Mapping:

T1 runs on P0  
 T2 runs on P1  
 T3 runs on P2  
 T4 runs on P4  
 T5 runs on P0

- Communication between any two communicating (dependant) tasks requires just 1 hop

# Reducing Contention

## □ All resources have nonzero occupancy

- Memory, communication controller, network link, etc.
- Can only handle so many transactions per unit time

## □ Effects of contention

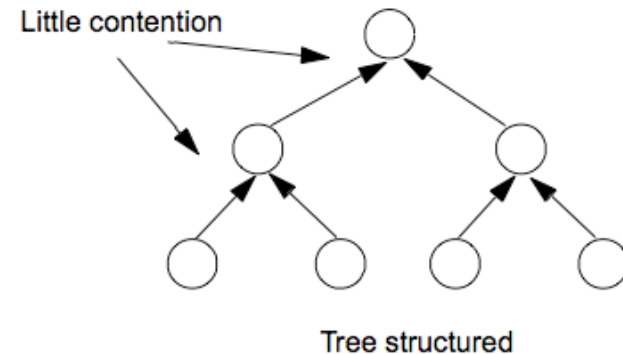
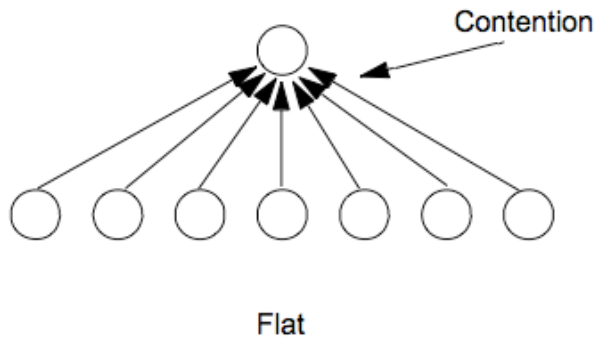
- Increased end-to-end cost for messages
- Reduced available bandwidth for individual messages
- Causes imbalances across processors

## □ Particularly insidious performance problem

- Easy to ignore when programming
- Slow down messages that don't even need that resource
  - by causing other dependent resources to also congest
- Effect can be devastating: *Don't flood a resource!*

# Types of Contention

- ❑ Network contention and end-point contention (*hot-spots*)
- ❑ *Location* and *Module* hot-spots
- ❑ *Location*: e.g. accumulating into global variable barrier
  - solution: tree-structured communication



- In general, reduce burstiness; may conflict with making messages
- ❑ *Module*: all-to-all personalized comm. in matrix transpose
  - solution: stagger access by different processors to same node temporally

# Overlapping Communication

- ❑ Cannot afford to stall for high latencies
  - even on uniprocessors!
- ❑ Overlap with computation or communication to hide latency
- ❑ Requires extra concurrency (*slackness*), higher bandwidth
- ❑ Techniques
  - Prefetching
  - Block data transfer
  - Proceeding past communication
  - Multithreading

# Summary of Tradeoffs

## □ Different goals often have conflicting demands

### ➤ Load Balance

- fine-grain tasks
- random or dynamic assignment

### ➤ Communication

- usually coarse grain tasks
- decompose to obtain locality: not random/dynamic

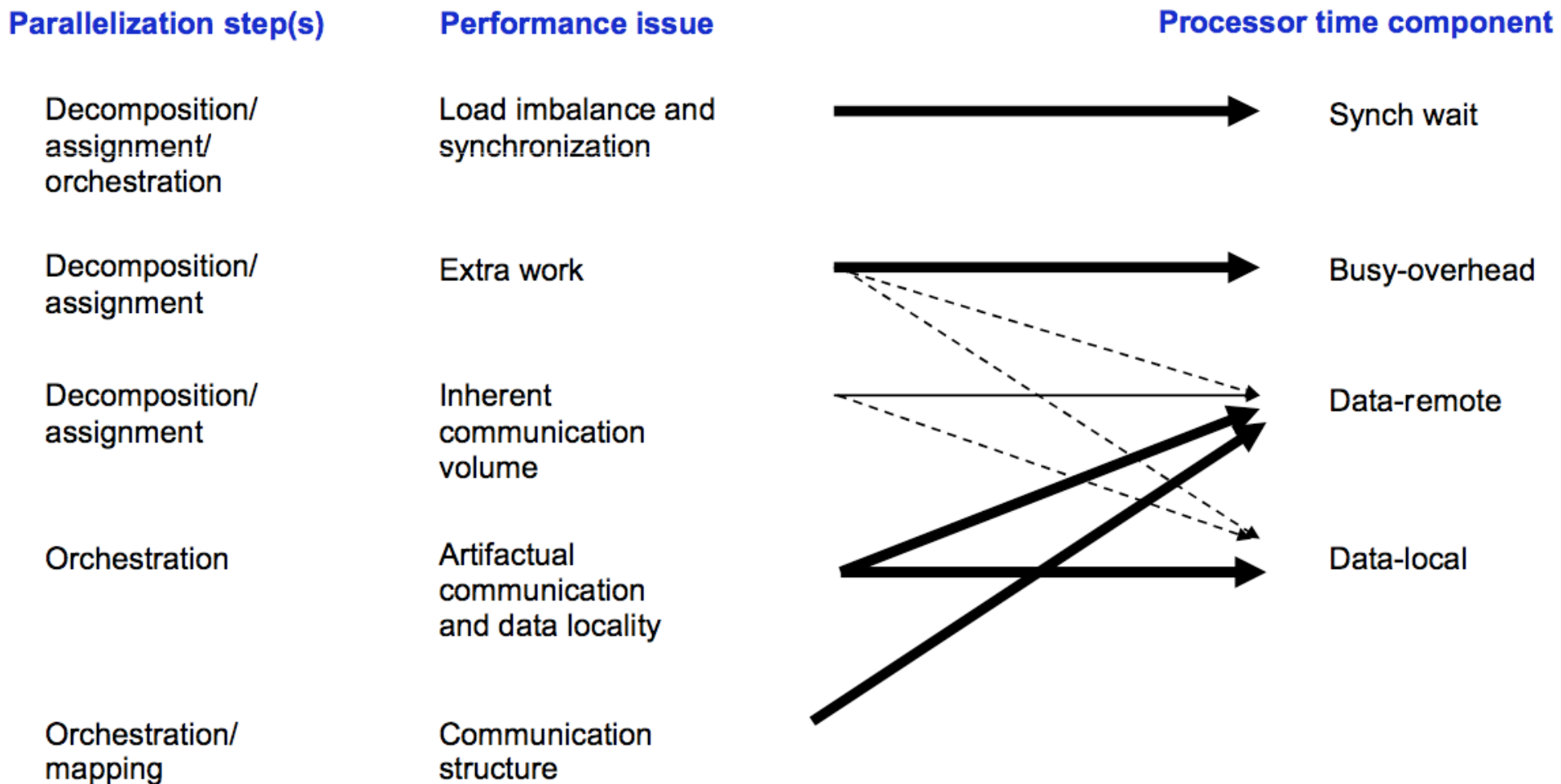
### ➤ Extra Work

- coarse grain tasks
- simple assignment

### ➤ Communication Cost

- big transfers: amortize overhead and latency
- small transfers: reduce contention

# Relationship between Perspectives



# Summary

$$Speedup_{prob}(p) = \frac{Busy(1) + Data(1)}{Busy_{useful}(p) + Data_{local}(p) + Synch(p) + Data_{remote}(p) + Busy_{overhead}(p)}$$

- Goal is to reduce denominator components
- Both programmer and system have role to play
- Architecture cannot do much about load imbalance or too much communication
- But it can
  - reduce incentive for creating ill-behaved programs (efficient naming, communication and synchronization)
  - reduce artifactual communication
  - provide efficient naming for flexible assignment
  - allow effective overlapping of communication