A Statistical Approach to Detecting Polarity Inversion Lines

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- ▶ Background and motivation
- ► Algorithm for finding Polarity Inversion Line(PIL)
- ► Potential Application
- ▶ Limitation of the algorithm



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Background: predict solar flares

Data source: Space-Weather HMI-Active Region Patch (SHARP) data files

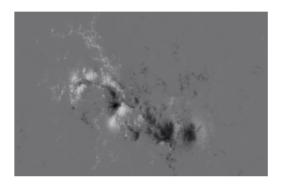


Figure: B-z Component, HARP377, 2011-02-17 14:00:00TAI



Input into LSTM Model

Physical quantities for each HMI-Active Region Patch(HARP):

- ► Total unsigned flux
- ► Total unsigned current helicity
- Mean shear angle
- **.**.



Input Time Series

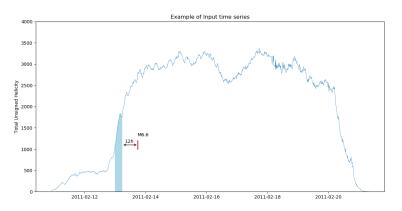


Figure: HARP377 Total Unsigned Helicity Series



Machine Learning Task

Task: With all physical quantities' time series as input, classify whether the flare 12 hours later is an M-X class flare or a B-class flare.



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Class/Year	2010	2011	2012	2013	2014	2015	2016	2017	2018	Total
X	0	9	7	12	16	2	0	4	0	50
M	0	106	124	97	194	128	15	37	0	701
\mathbf{C}	1	1002	1115	1197	1626	1275	294	229	11	6750
В	19	665	475	469	184	446	757	620	207	3842

Figure: Flare Data Summary



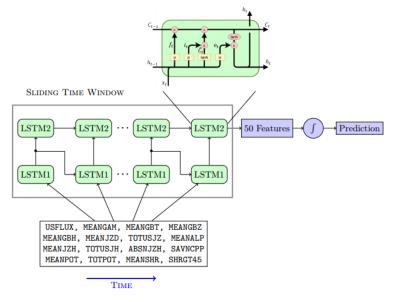
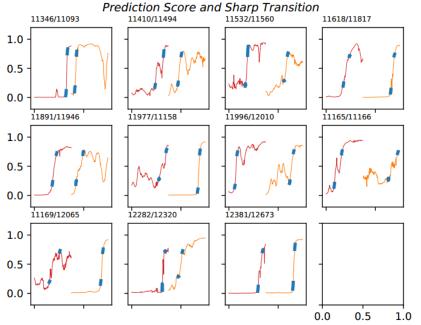


Figure: LSTM Model







LSTM Model Variable Importance

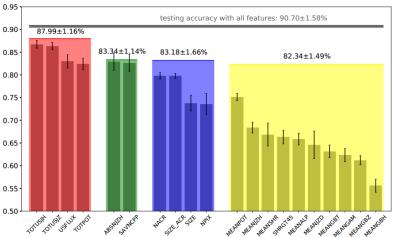


Figure: Feature Importance in trained LSTM Model (Chen et al. 2019)



Motivation

Finding: Many variables are able to single-handedly classfify MX flares against B flares.

But what is the underlying mechanism? Physical quantities in SHARP data are computed using **the whole HARP region** magnetic field...



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Find Polarity Inversion Line

Previous methods (Falconer et al. 2002, Bokenkemp 2007) are modeling the spatial distribution of magnetic vector field.

Here we provide an alternative statistical method that does not model the distribution of polars but work on **pixels of the magnetogram** directly.



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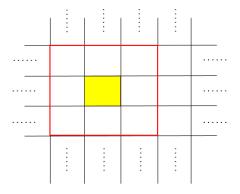


Figure: A pixel's neighborhood, 3×3 window



Data Type: Magnetogram with 200,000+ pixels.

In every pixel's neighborhood, we check if there is both a strong positive polar and a strong negative polar. (default threshold $\pm 100 {\rm Gauss}$)



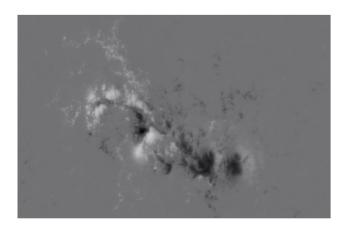


Figure: B-z Component, HARP377, 2011-02-17 14:00:00TAI





Figure: Pixels remained after neighborhood check $(5 \times 5 \text{ window})$



- ▶ Having shape of multiple PIL segments
- ▶ Having miscellaneous clusters of pixels not of our interest
- Pixels on the same PIL are not linked well
- ▶ The PILs seem to be too thick.



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Use Prewitt filter to calculate local B-z gradient for each of the pixel:

$$\mathbf{G_x} = \begin{bmatrix} +1 & 0 & -1 \\ +1 & 0 & -1 \\ +1 & 0 & -1 \end{bmatrix} * \mathbf{A} \quad \text{and} \quad \mathbf{G_y} = \begin{bmatrix} +1 & +1 & +1 \\ 0 & 0 & 0 \\ -1 & -1 & -1 \end{bmatrix} * \mathbf{A}$$

With both G_x and G_y , we could calculate the direction of the gradient by $\arctan(\frac{G_y}{G_x})$.

And with the direction of the gradient, we could define the adjacent pixels along the gradient direction of any pixel with non-zero gradient.



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Figure: Adjacent pixels along gradient direction

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Now we only retain the pixels whose gradient norm is local maxima along it gradient direction.



Figure: Thin Edges after Non-maxima Suppression



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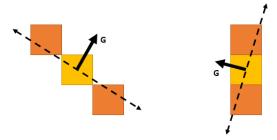


Figure: PIL extension direction



Figure: More connected PILs



Such an extension would add more connectivity to each PIL, but will add many pixels with small B-z gradients into the PIL.

Optionally, one could only extend on points with large gradients, and this extension can be conducted **recursively**.



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How to classify PIL pixels into several clusters?

- ► Connected-component analysis
- ▶ Density-based clustering algorithm



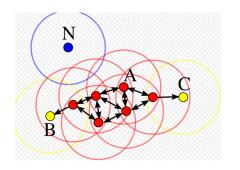
Density-based spatial clustering of applications with noise (DBSCAN)

- Locate some "core" points as the seed for a cluster
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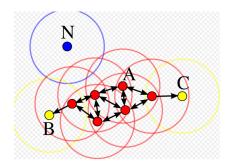






Figure: More connected PILs





Figure: PILs left after deleting small clusters



Potential Application



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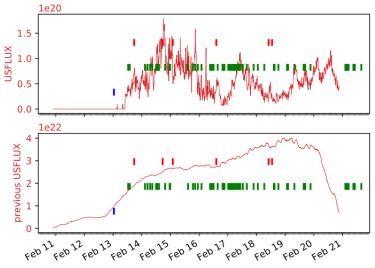


Figure: Recalculate USFLUX for HARP377



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