

Interpretable Flare Prediction with Integrated Data: SHARP parameters, Spatial Statistics Features and HMI Images¹

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¹Our submitted manuscript can be viewed [here](#), and the paper is to appear soon in *Space Weather*.

Overview

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2 Data

3 Feature Engineering

- Topological Feature
- Spatial Feature: Ripley's K Function

4 Main Results

5 Conclusions

Flare Prediction with HMI Magnetograms

- Bobra, Sun, et al. (2014) introduced the Space-weather HMI Active Region Patch (SHARP) parameters, which are derived from the HMI/SDO magnetograms and have been used frequently for solar flare prediction models in recent years (e.g. Bobra and Couvidat, 2015; Florios et al., 2018; Chen et al., 2019; Camporeale, 2019; Jiao et al., 2020).

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- There are efforts using deep neural network methods, which directly take the HMI/SDO magnetogram images to predict solar eruptions (e.g. the Long Short Term Memory network adopted by Chen et al. (2019) and Liu et al. (2019)).

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- Recent efforts (Deshmukh, Berger, Bradley, et al., 2020; Deshmukh, Berger, Meiss, et al., 2020) leverage the shape information contained in HMI magnetograms to construct interpretable and predictive new parameters for flare prediction.

Highlights of Our Work

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- ② Derive features not only from the PIL-masked HMI magnetograms but also from the spatial distribution of SHARP parameters.
- ③ Marginally but steadily improved the skill score of the classification model of strong vs. weak solar flares.

Dataset

- We use the Geostationary Operational Environmental Satellites (GOES) flare list spanning 2010/12 - 2018/06 for collecting flare events, leading to 399 M/X class flares and 1,972 B class flares coming from 487 HARP regions.

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- For each flare, we collect its corresponding high-resolution HMI magnetogram data from the JSOC at 4 time points: 1, 6, 12, 24 hours prior to the peak soft X-ray flux.
- For each flare, at all four time points, raw data of the B_r , B_p , B_t components of the magnetic field are collected.

Derive SHARP Parameter Maps

- We derive features from the B_r component of the magnetic field but also from other secondary maps derived from the B_r, B_p, B_t components, which we call *SHARP parameter maps*.

Derive SHARP Parameter Maps

Channel	Formula	Unit
Br	\mathbf{B}_z	G
GAM	$\arctan\left(\frac{\mathbf{B}_h}{\mathbf{B}_z}\right)$	Degree
GBT	$\sqrt{\left(\frac{\partial \mathbf{B}}{\partial x}\right)^2 + \left(\frac{\partial \mathbf{B}}{\partial y}\right)^2}$	$\text{G} \times \text{Mm}^{-1}$
GBH	$\sqrt{\left(\frac{\partial \mathbf{B}_h}{\partial x}\right)^2 + \left(\frac{\partial \mathbf{B}_h}{\partial y}\right)^2}$	$\text{G} \times \text{Mm}^{-1}$
GBZ	$\sqrt{\left(\frac{\partial \mathbf{B}_z}{\partial x}\right)^2 + \left(\frac{\partial \mathbf{B}_z}{\partial y}\right)^2}$	$\text{G} \times \text{Mm}^{-1}$
USJZ	$ \left(\frac{\partial \mathbf{B}_y}{\partial x} - \frac{\partial \mathbf{B}_x}{\partial y}\right) $	A
USJH	$ \mathbf{J}_z \times \mathbf{B}_z $	$\text{G}^2 \text{ m}^{-1}$
POT	$((\mathbf{B}_x - \mathbf{B}_x^{POT})^2 + (\mathbf{B}_y - \mathbf{B}_y^{POT})^2)$	erg cm^{-3}
SHR	$\arccos\left(\frac{\mathbf{B}_x^{POT} \times \mathbf{B}_x + \mathbf{B}_y^{POT} \times \mathbf{B}_y + \mathbf{B}_z^{POT} \times \mathbf{B}_z}{\sqrt{\mathbf{B}_x^{POT2} + \mathbf{B}_y^{POT2} + \mathbf{B}_z^{POT2}} \sqrt{\mathbf{B}_x^2 + \mathbf{B}_y^2 + \mathbf{B}_z^2}}\right)$	Degree

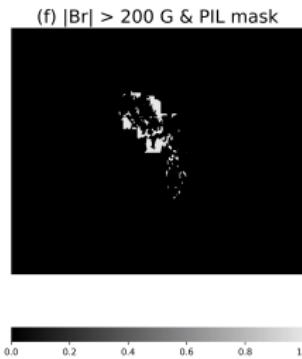
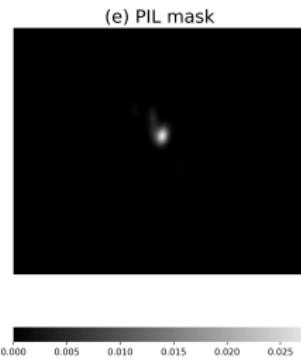
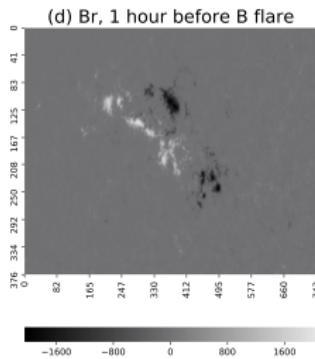
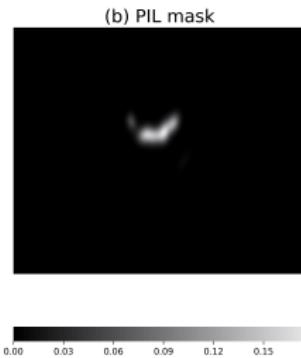
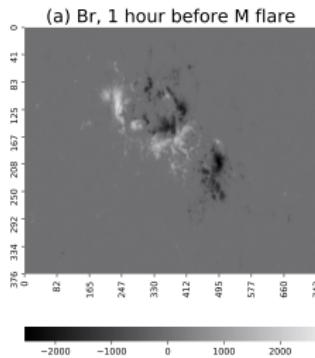
Table 1. SHARP parameter mask, formula applied to every pixel of the HMI magnetogram. Here, \mathbf{B}_x , \mathbf{B}_y , \mathbf{B}_z are the x , y , z components of the magnetic field and \mathbf{B}_x^{POT} , \mathbf{B}_y^{POT} the potential field components respectively. Detailed definition of the parameters can be found in Table 3 of Bobra et al. (2014).



Derive the Polarity Inversion Line (PIL)

- We focus specifically on the area adjacent to the polarity inversion line (PIL) by constructing the PIL mask.

Derive the Polarity Inversion Line (PIL)



Topological Feature: Betti Numbers

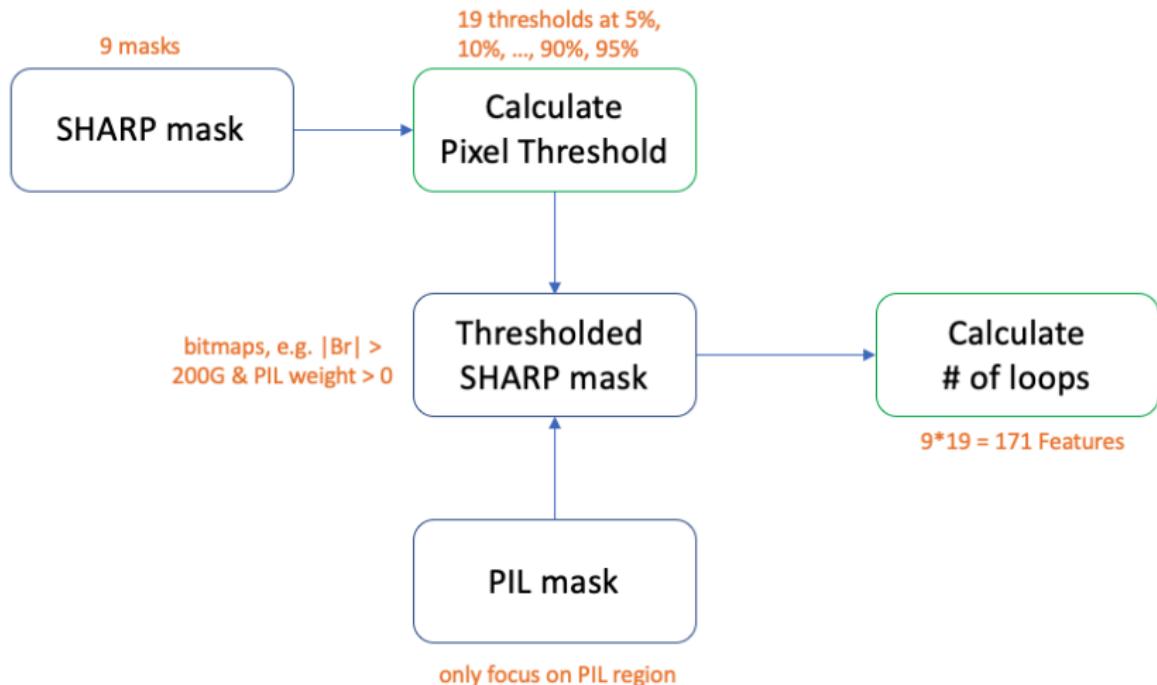
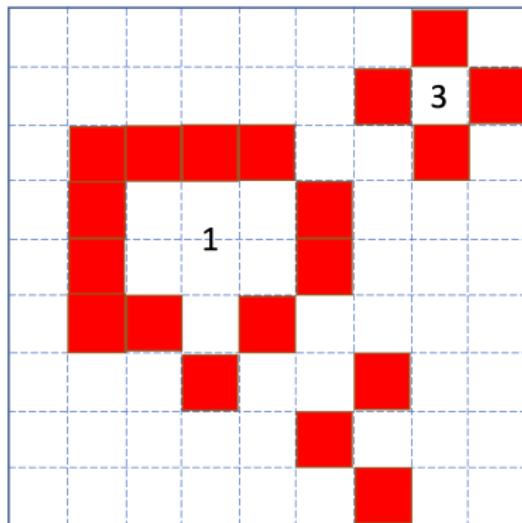


Figure: Feature Engineering Pipeline of Topological Features

Topological Feature: Betti Numbers

(a) Low Threshold



(b) High Threshold

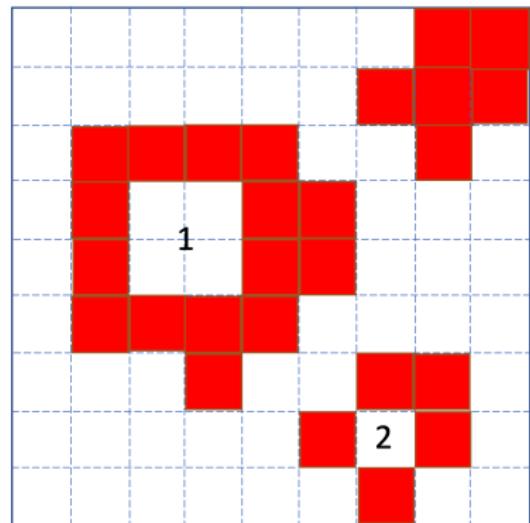


Figure: What is a loop?

Topological Feature: Betti Numbers

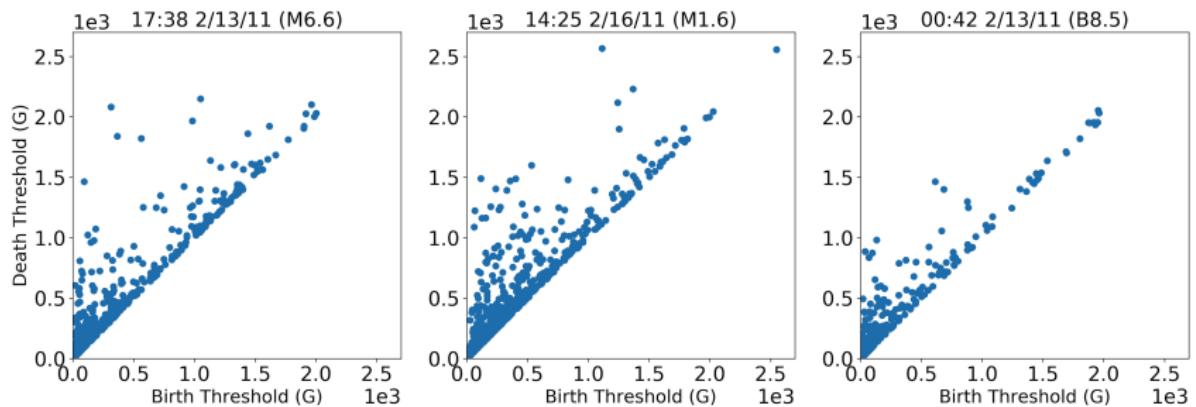
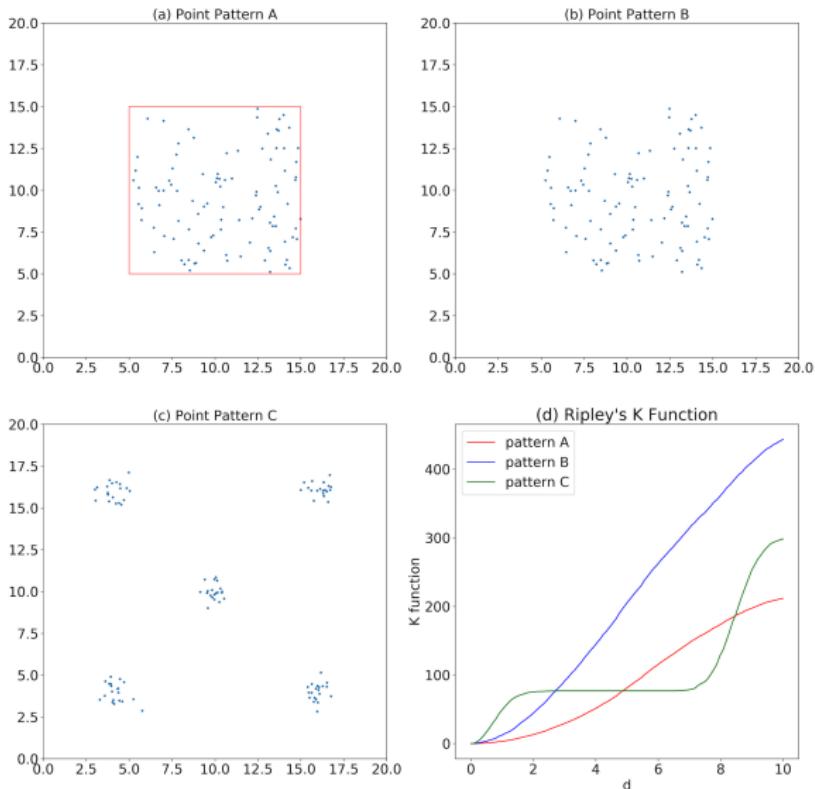


Figure: Final Topological Feature in Persistence Diagram

Spatial Feature I: Ripley's K Function



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- For the thresholded B_r mask, we randomly pick 500 pixels, with sampling probability proportional to $|B_r|$, to construct a point cloud. Each picked pixel has a pair of (x, y) pixel coordinates in the 2D pixel grid.
- Ripley's K function:

$$L(d) = \sqrt{\frac{A \sum_{i=1}^n \sum_{j=1, j \neq i}^n k_{i,j}}{\pi n(n-1)}},$$

where $k_{i,j} = 1$ if the i -th and j -th pixel are within distance d , and $n = 500$ in our case. A is the area size and is defined as the number of PIL pixels in our study.

Spatial Feature I: Ripley's K Function

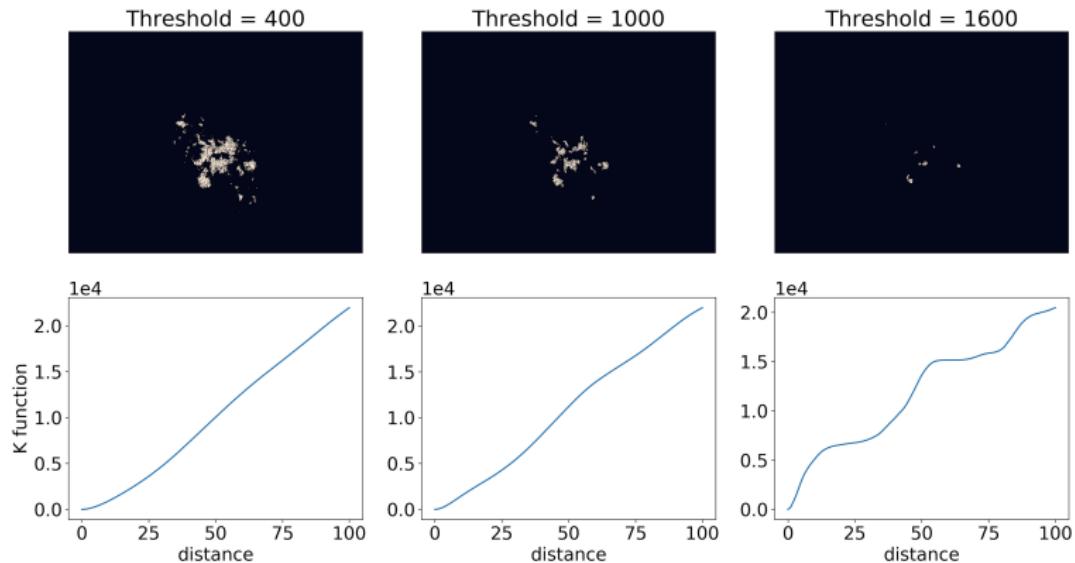
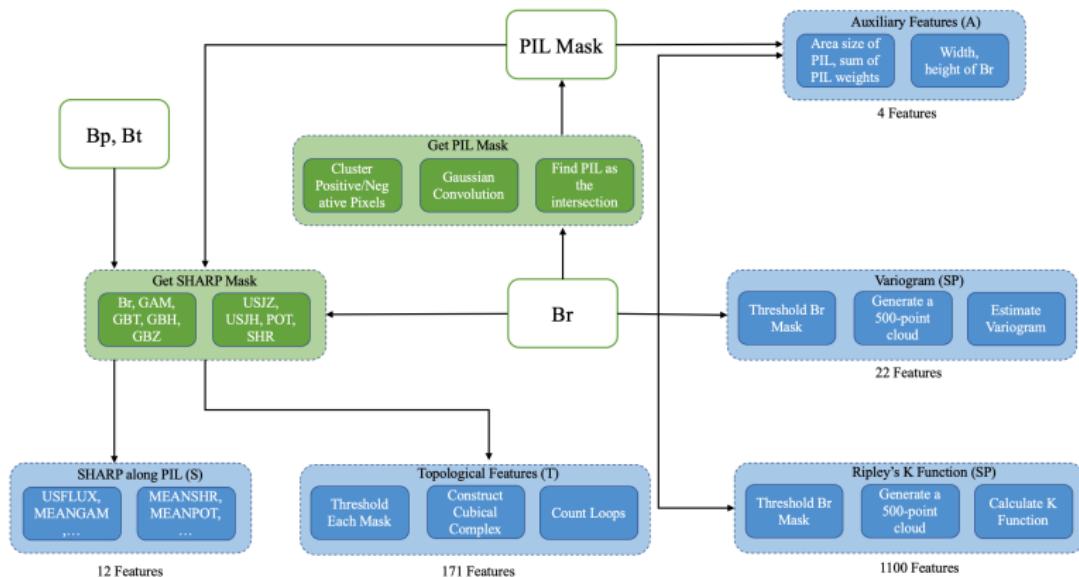


Figure: Point cloud and the corresponding Ripley's K function for the B_r mask collected from HARP 377, 1 hour before the M flare peaked at 2011.02.13 17:38. The top row includes 3 point clouds generated by 3 thresholds at 400G, 1000G, 1600G. The bottom row shows the 3 corresponding Ripley's K functions.

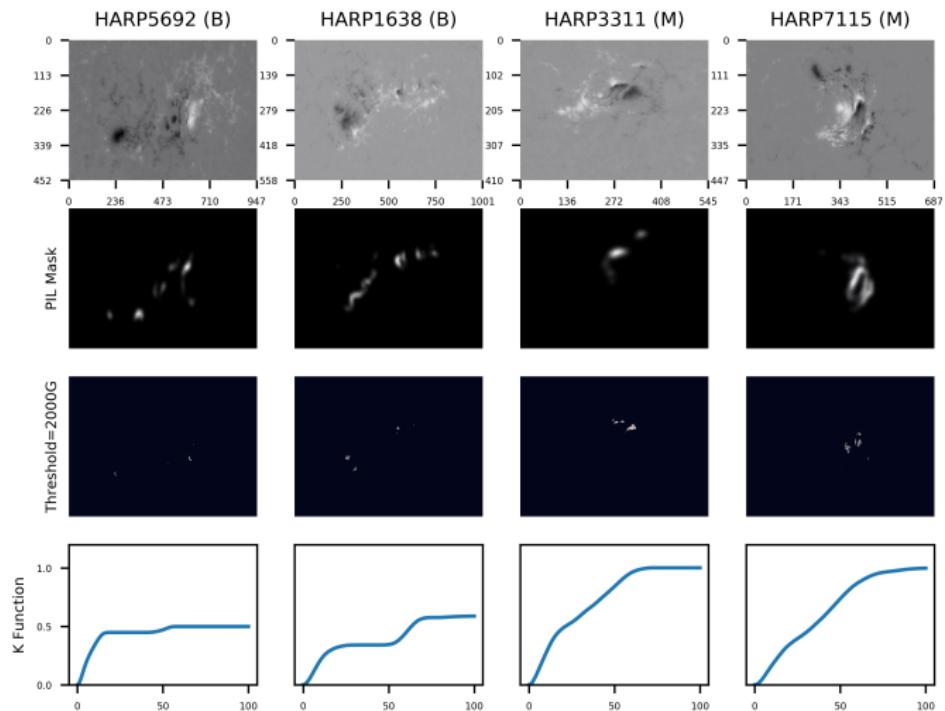
Feature Pipeline Summary



Result: True Skill Score for Xgboost Model

Feature Combination	Prediction Time (hour)			
	1	6	12	24
S	0.553 (0.075)	0.555 (0.071)	0.539 (0.068)	0.489 (0.077)
T	0.548 (0.069)	0.575 (0.071)	0.561 (0.063)	0.525 (0.069)
SP	0.558 (0.066)	0.578 (0.076)	0.546 (0.071)	0.528 (0.072)
S+T	0.578 (0.071)	0.581 (0.072)	0.554 (0.057)	0.536 (0.052)
S+SP	0.56 (0.059)	0.58 (0.073)	0.538 (0.078)	0.533 (0.074)
S+T+SP	0.586 (0.077)	0.599 (0.068)	0.558 (0.08)	0.57 (0.06)
S+T_PC+SP_PC	0.554 (0.075)	0.561 (0.077)	0.53 (0.082)	0.533 (0.076)
S+T+SP+A	0.587 (0.071)	0.605 (0.063)	0.551 (0.077)	0.55 (0.059)
S+T_PC+SP_PC+A	0.578 (0.068)	0.561 (0.071)	0.533 (0.076)	0.521 (0.089)

Result: Example of the Ripley's K function



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- Engineered interpretable and predictive features summarizing the spatial variation, dispersion patterns of various SHARP quantities, especially the B_r component, using tools from TDA and spatial statistics.
- Obtained marginal but steady improvement on the solar flare classification task.
- The spatial features derived solely from the B_r component are as good or better for flare prediction than full vector SHARP parameters. Theoretically interesting and important for future missions.

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