



# Subregular Induction of Underlying Representations and a Phonological Grammar

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## Goals and Background

- Project goal: the **simultaneous inference** of URs and a grammar from SRs in a morphological paradigm.  
(Albright, 2002; Tesar, 2014)
- The **Input Strictly Local** (ISL) functions provide a structure that can solve this problem.  
(Chandlee and Heinz, 2018)

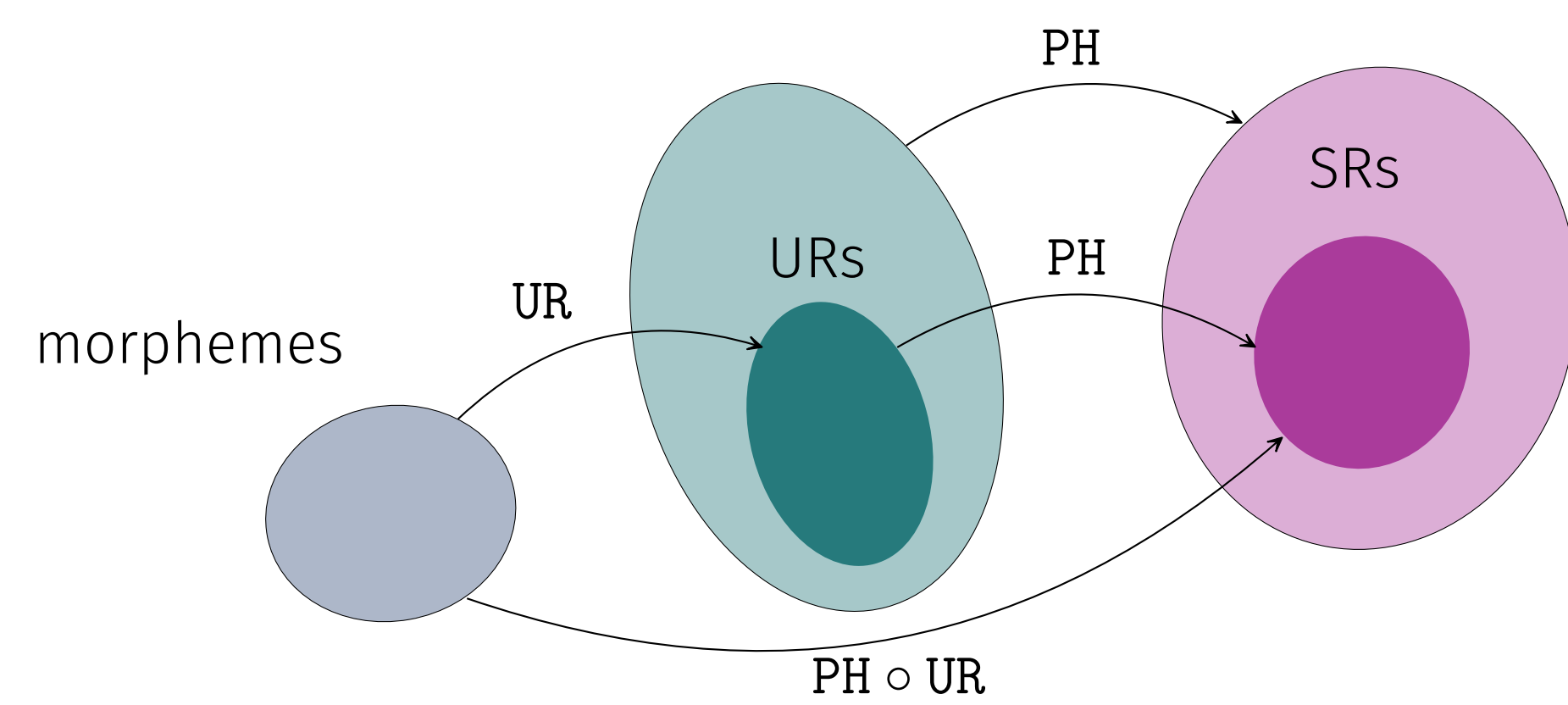
## Primary result

- The learner induces UR and phonological grammar from a range of ISL<sub>2</sub> function (ISL function for  $k = 2$ ), including progressive and regressive assimilation, deletion, epenthesis, and opacity.

## Learning Problem

- $M$ : finite set of morphemes  $\{\text{CAT, DOG, ..., PL}\}$   
 $\Sigma$ : finite set of segments  $\{a, b, \beta, ..., z\}$
- UR function: maps one morpheme to one UR;  
 $\text{UR} : M^* \rightarrow \Sigma^*$
- PH function: maps URs to SRs;  
 $\text{PH} : \Sigma^* \rightarrow \Sigma^*$

$\text{UR}(\text{CAT}) = \text{kæt}$      $\text{PH}(\text{kæt}) = \text{kæt}$   
 $\text{UR}(\text{PL}) = \text{z}$      $\text{PH}(\text{dɔgz}) = \text{dɔgz}$   
 $\text{UR}(\text{CAT-PL}) = \text{kætz}$      $\text{PH}(\text{kætz}) = \text{kæts}$   
 $\dots$      $\dots$      $\text{PH}(\text{bʌɪkz}) = \text{bʌɪks}$   
 $\dots$      $\dots$      $\dots$



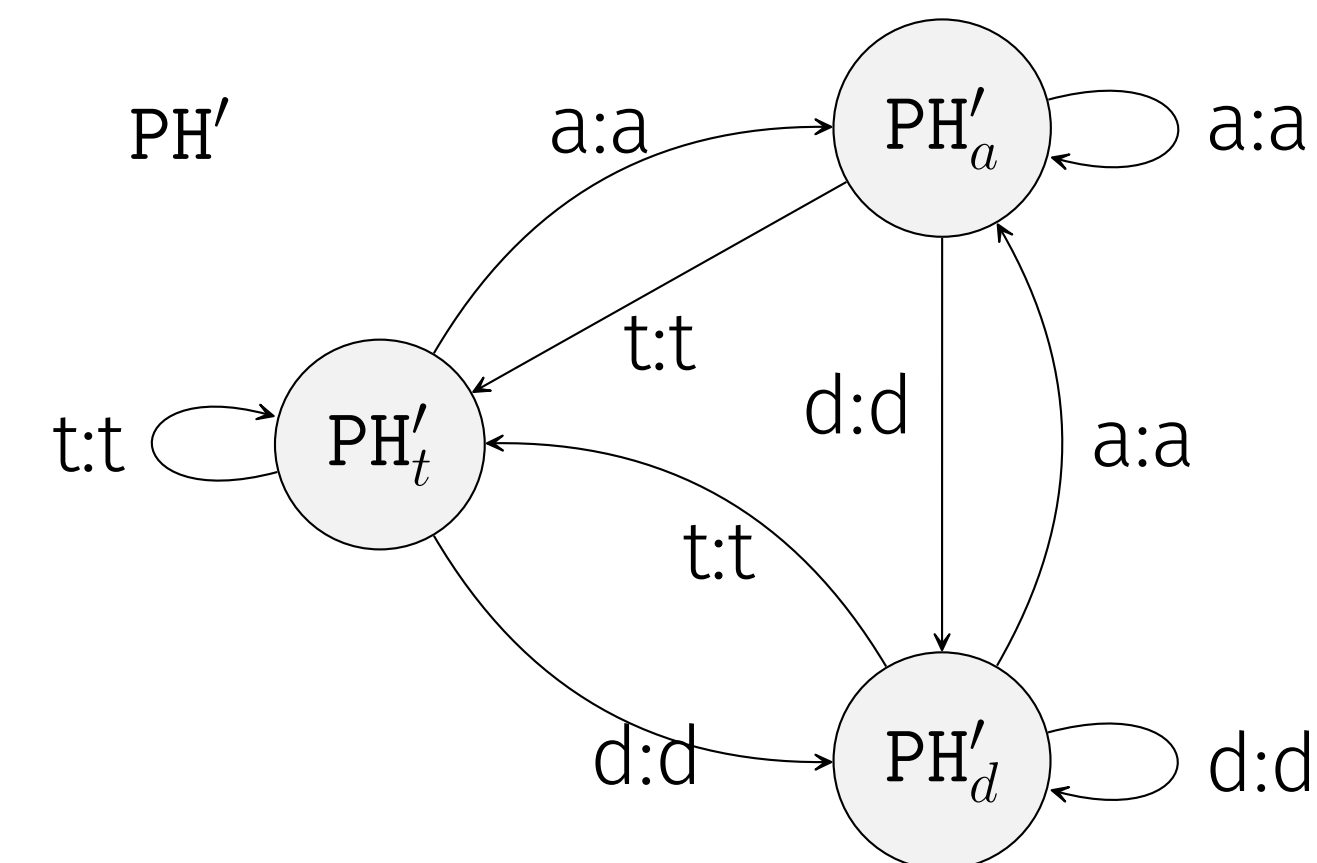
- Given a finite sample of  $\text{PH} \circ \text{UR}$ , how do we identify PH and UR?  
(CAT-PL,  $\text{kæts}$ ), (DOG-PL,  $\text{dɔgz}$ ), ..., (BOOK-PL,  $\text{bʌks}$ )

## Initialization

- Running example  $D \subset \text{PH} \circ \text{UR}(M^*)$

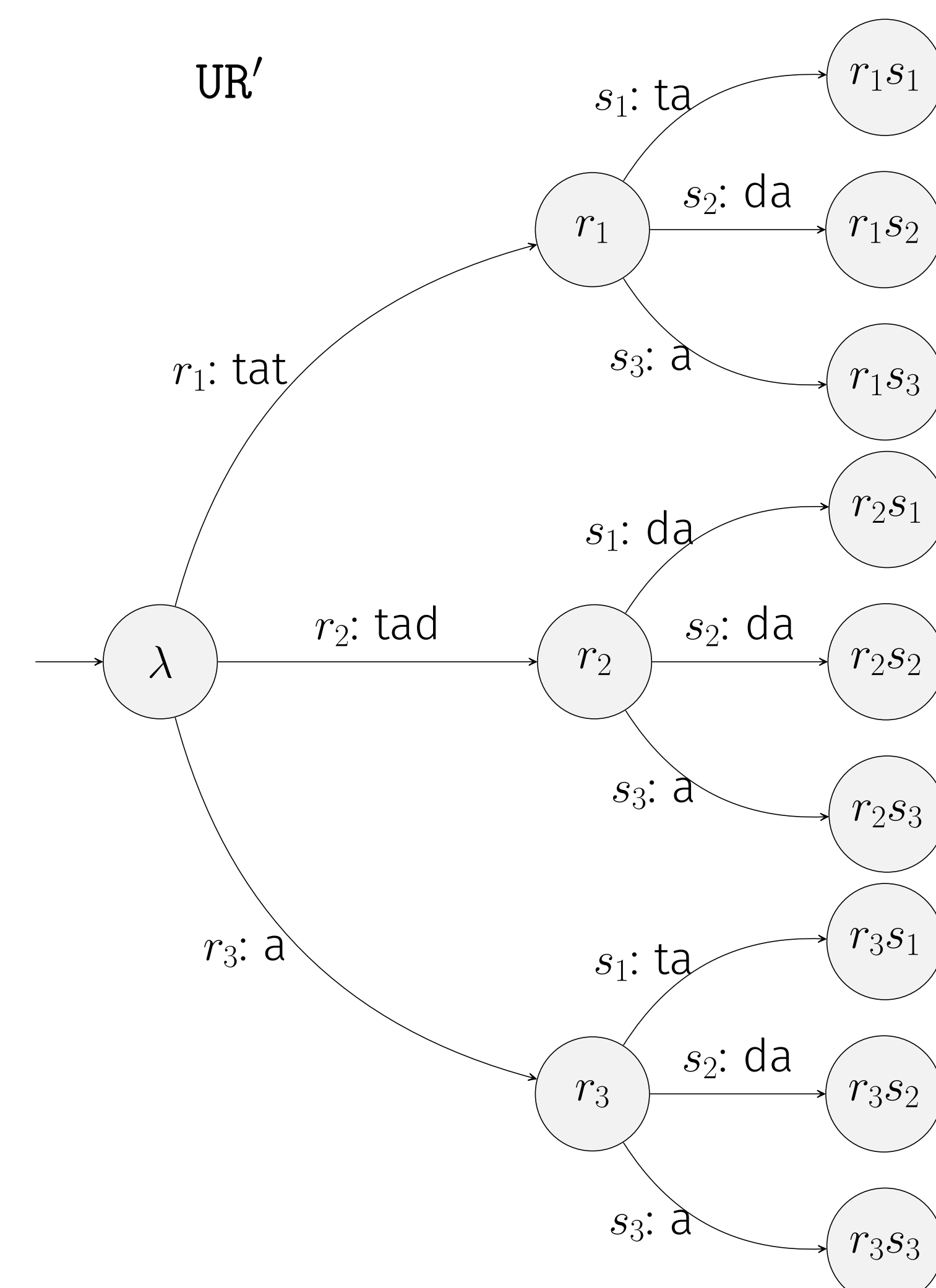
Sample of $\text{PH} \circ \text{UR}$ (PROG. ASSIMILATION)					
$w$	$\text{PH}(\text{UR}(w))$	$w$	$\text{PH}(\text{UR}(w))$	$w$	$\text{PH}(\text{UR}(w))$
$r_1 s_1$	tatta	$r_2 s_1$	tadda	$r_3 s_1$	ata
$r_1 s_2$	tatda	$r_2 s_2$	tadda	$r_3 s_2$	ada
$r_1 s_3$	tata	$r_2 s_3$	tada	$r_3 s_3$	aa

- Initialize  $\text{PH}'$  to the identity function  
 $\text{PH}'(\text{tatta}) = \text{tatta}$ ,  $\text{PH}'(\text{tatda}) = \text{tatda}$ , etc.



- Initialize  $\text{UR}'$  to a **prefix tree transducer** representing  $D$ : segmentation based on **longest common prefix (lcp)**.

$\text{lcp}(\{\text{tatta}, \text{tatda}, \text{tata}\}) = \text{tat}$   
 $\text{lcp}(\{\text{tadda}, \text{tada}\}) = \text{tad}$



## Inconsistency detection

If a morpheme is mapped to multiple SRs, the learner detects this inconsistency.

$r_1$ : tat     $r_2$ : tad     $r_3$ : a  
 $s_1$ : ta, da     $s_2$ : da     $s_3$ : a

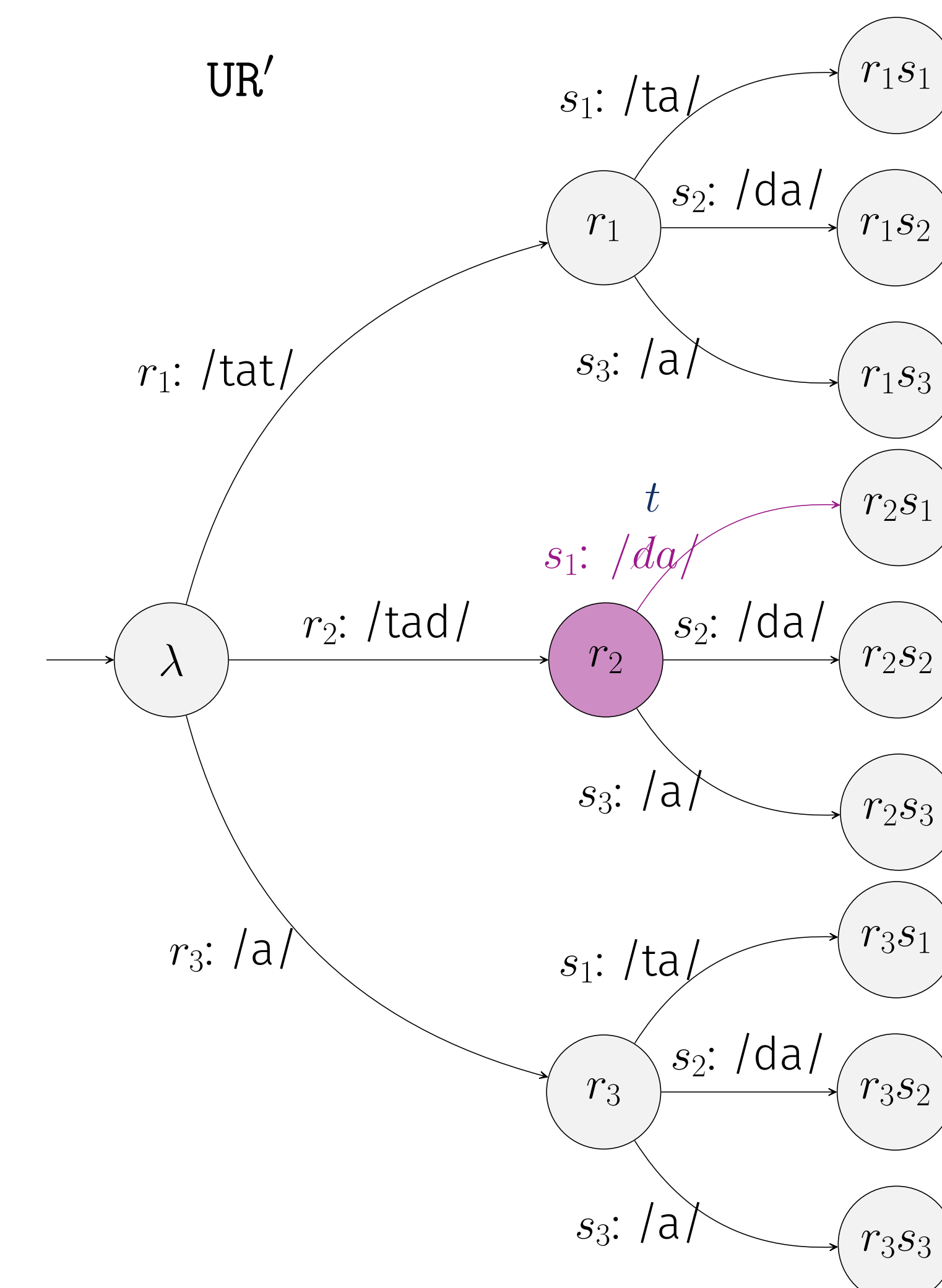
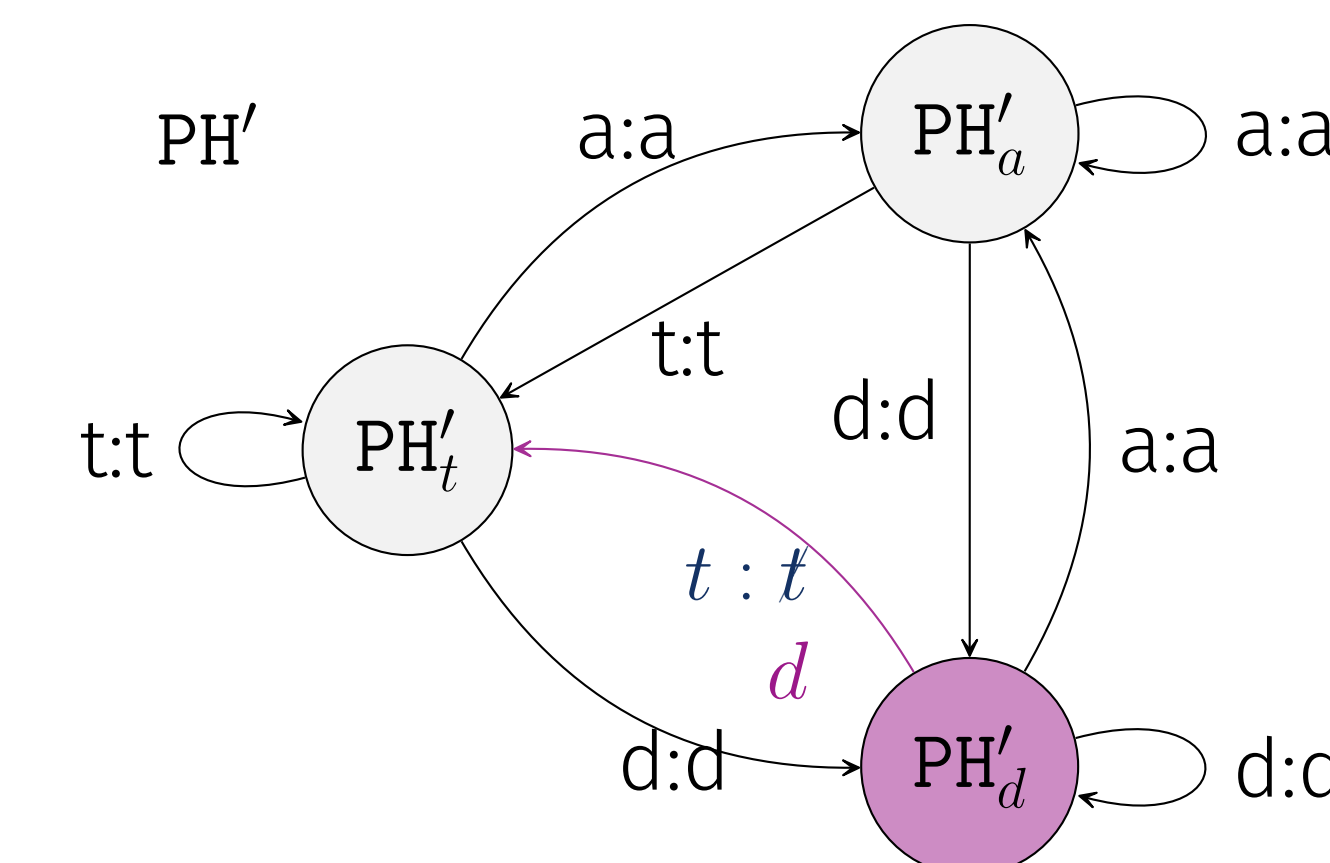
## Environment collection

- ISL provides environment information
- $t$  is the most **informative** form  $\rightarrow$  UR.

$ws_1$	env.	$s_1$
$r_1 s_1$	tat	ta
$r_3 s_1$	a	ta
$r_2 s_1$	tad	da

## Modification

Change  $\text{UR}'$ , making the opposite change in  $\text{PH}'$



## Take-home message

From an **abstract** and **principled** perspective, learning is possible given the basic principles:

- a restrictive, structured hypothesis space
- complementarily distributed allomorphs
- a surface-driven set of URs
- One morpheme  $\rightarrow$  one UR

## Future work

- Long-distance processes can be captured by different classes of subsequential functions with a similar structure;
- One example: output strictly-local class also has a restricted state structure;  
(Chandlee et al., 2015)
- Abstract URs may be learnable when input alphabet is larger than output alphabet (and thus allows larger categories).

## Selected References

Albright, Adam C (2002). *The identification of bases in morphological paradigms*. PhD thesis, University of California, Los Angeles.

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Chandlee, Jane and Heinz, Jeffrey (2018). Strict locality and phonological maps. *Linguistic Inquiry*, 49(1):23–60.

Tesar, Bruce (2014). *Output-driven phonology: Theory and learning*. Cambridge University Press.

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