CPEG655

Lab 04

Michael Hutts

## Problem 1: NVIDIA CUDA

## Task A:

### Approach

In this part, a basic implementation of matrix multiplication on GPU was implemented. It performed well and had showed no difference in results compared to the CPU implementation according to RMSE. The RMSE function was also verified for correctness by arbitrarily modifying the values of the final matrices, which did show an extremely high value, showing our metric of correctness was performing correctly and not just giving false confidence.

```
GPU time for N=16: 0.000061

CPU time for N=16: 0.000026

RMSE for N=16: 0.000000e+00

GPU time for N=32: 0.000033

CPU time for N=32: 0.000244

RMSE for N=32: 0.000000e+00
```

Figure 1: Example Run

A problem I encountered that I was unable so solve was with cudaEvent\_t. Despite it being shown as simple to implement in the slides, for reasons I can't seem to understand using it caused cascading issues in my entire codebase. For this reason I simply used gettimeofday() in place of CUDA events.

One additional decision made in this part was the initial value for threadsPerBlock(), although for part A we're limited to 1 block, the number of threads per block is unrestricted. Therefore based on my system information shown below I chose (32, 32) based on the assumption that this should maximize the capability of my GPU for any following workload.

```
Device 0: "NVIDIA GeForce MX150"
 CUDA Driver Version / Runtime Version
                                                    12.1 / 12.3
 CUDA Capability Major/Minor version number:
Total amount of global memory:
                                                    6.1
                                                    2048 MBytes (2147352576 bytes)
 (003) Multiprocessors, (128) CUDA Cores/MP:
                                                    384 CUDA Cores
 GPU Max Clock rate:
                                                    1038 MHz (1.04 GHz)
 Memory Clock rate:
                                                    2505 Mhz
                                                    64-bit
 Memory Bus Width:
 L2 Cache Size:
                                                    524288 bytes
 Maximum Texture Dimension Size (x,y,z)
                                                    1D=(131072), 2D=(131072, 65536), 3D=(16384, 16384, 16384)
 Maximum Layered 1D Texture Size, (num) layers 1D=(32768), 2048 layers
Maximum Layered 2D Texture Size, (num) layers 2D=(32768, 32768), 2048 layers
 Total amount of constant memory:
                                                    65536 bytes
 Total amount of shared memory per block:
                                                    49152 bytes
 Total shared memory per multiprocessor:
                                                    98304 bytes
 Total number of registers available per block: 65536
 Warp size:
                                                     32
 Maximum number of threads per multiprocessor:
                                                    2048
 Max dimension size of a thread block (x,y,z): (1024, 1024, 64)
 Max dimension size of a grid size (x,y,z): (2147483647, 65535, 65535)
                                                    2147483647 bytes
 Maximum memory pitch:
 Texture alignment:
                                                    512 bytes
 Concurrent copy and kernel execution:
                                                    Yes with 1 copy engine(s)
 Run time limit on kernels:
                                                    Yes
 Integrated GPU sharing Host Memory:
                                                    No
 Support host page-locked memory mapping:
                                                    Yes
 Alignment requirement for Surfaces:
                                                    Yes
 Device has ECC support:
                                                    Disabled
 Device supports Unified Addressing (UVA):
                                                    Yes
 Device supports Managed Memory:
                                                    Yes
 Device supports Compute Preemption:
                                                     Yes
 Supports Cooperative Kernel Launch:
                                                    Yes
```

Figure 3: GPU Information

#### Performance

The performance characteristics of part A showed a substantial performance difference for the two sizes of N. For a size of 8 the CPU held a small lead, most likely due to the additional overhead and complexity of a GPU implementation of such a short task, meanwhile for an N of 16 the GPU implementation pulled ahead dramatically, showing the extreme uplift CUDA provides with larger (wider) workloads that can take better advantage of concurrency.

```
Average GPU time for N=16: 0.000052
Average CPU time for N=16: 0.000028
Average GPU time for N=32: 0.000060
Average CPU time for N=32: 0.000223
```

Figure 4: Performance Results

## Task B:

For part B, we were no longer limited to just one thread block. This provided substantial opportunity for better performance, but with that required a bit more complexity in making the implantation threadsafe. Additionally, shared memory became a necessity to handle. Despite the

additions, the basic structured remained from part A. Additionally the kernel launching process was updated accordingly. With these improvements to concurrency and data locality, an even more extreme performance uplift was measured on a large value of N.

```
GPU time for N=2048, tile size=8: 0.000403

CPU time for N=2048: 91.076078

RMSE for N=2048, tile size=8: 0.000000e+00

GPU time for N=2048, tile size=16: 0.002118

CPU time for N=2048: 92.355528

RMSE for N=2048, tile size=16: 0.000000e+00
```

Figure 5: GPU vs CPU Performance Comparison

#### Part C

For part C, the implementation was relatively straightforward, basically just reworking main() to have modular values NB, NT, and NK as described. Disappointingly the results were not very informative. Although some basic patterns emerged, I could not seem to get consistent enough results to draw a real conclusion on the ideal values of NB and NT. My assumption was that there should be a direct correlation between higher values for both NB and NT and better performance, but not much of a difference seemed to appear.

	2	4	8	16	32	<u>NT</u>
2	0.000588	0.000594	0.000575	0.000593	0.000588	
4	0.000592	0.00059	0.000588	0.000585	0.00059	
8	0.00059	0.000587	0.00059	0.00059	0.000589	
16	0.000591	0.000585	0.000593	0.000598	0.000585	
32	0.000591	0.000586	0.000586	0.000594	0.000583	
<u>NT</u>						

Figures 6 & 7: NB/NT Benchmark (1000 Runs per Value)

1	9:32:5	5 mil	(e ~/(	docur	ments/cp	eg655/lab4 \$ ./mm_c
Α	verage	GPU	time	for	N=2048,	NB=2, NT=2: 0.000588
Α	verage	GPU	time	for	N=2048,	NB=2, NT=4: 0.000594
Α	verage	GPU	time	for	N=2048,	NB=2, NT=8: 0.000575
Α	verage	GPU	time	for	N=2048,	NB=2, NT=16: 0.000593
Α	verage	GPU	time	for	N=2048,	NB=2, NT=32: 0.000588
Α	verage	GPU	time	for	N=2048,	NB=4, NT=2: 0.000592
Α	verage	GPU	time	for	N=2048,	NB=4, NT=4: 0.000590
Α	verage	GPU	time	for	N=2048,	NB=4, NT=8: 0.000588
Α	verage	GPU	time	for	N=2048,	NB=4, NT=16: 0.000585
Α	verage	GPU	time	for	N=2048,	NB=4, NT=32: 0.000590
Α	verage	GPU	time	for	N=2048,	NB=8, NT=2: 0.000590
Α	verage	GPU	time	for	N=2048,	NB=8, NT=4: 0.000587
Α	verage	GPU	time	for	N=2048,	NB=8, NT=8: 0.000590
Α	verage	GPU	time	for	N=2048,	NB=8, NT=16: 0.000590
Α	verage	GPU	time	for	N=2048,	NB=8, NT=32: 0.000589
Α	verage	GPU	time	for	N=2048,	NB=16, NT=2: 0.000591
Α	verage	GPU	time	for	N=2048,	NB=16, NT=4: 0.000585
Α	verage	GPU	time	for	N=2048,	NB=16, NT=8: 0.000593
Α	verage	GPU	time	for	N=2048,	NB=16, NT=16: 0.000598
Α	verage	GPU	time	for	N=2048,	NB=16, NT=32: 0.000585
Α	verage	GPU	time	for	N=2048,	NB=32, NT=2: 0.000591
Α	verage	GPU	time	for	N=2048,	NB=32, NT=4: 0.000586
Α	verage	GPU	time	for	N=2048,	NB=32, NT=8: 0.000586
Α	verage	GPU	time	for	N=2048,	NB=32, NT=16: 0.000594
Α	verage	GPU	time	for	N=2048,	NB=32, NT=32: 0.000583

With a small sample size, more dramatic performance differences were shown, but with many repeated attempts thermal throttling would hit the GPU extremely fast. This seems to be a side-effect of the weak cooler on the GPU I'm using. At below 65 degrees celcius the performance

would be much better, but hard to benchmark as within a few runs the weak laptop cooler hit this limit, greatly decreasing performance.

	2	4	8	16	32	<u>NT</u>
2	0.000415	0.000395	0.000434	0.00039	0.000416	
4	0.000394	0.000398	0.000396	0.000396	0.000397	
8	0.000448	0.000407	0.000383	0.000389	0.0004	
16	0.000407	0.000395	0.000428	0.00041	0.000425	
32	0.000371	0.0004	0.000414	0.000393	0.000405	
<u>NT</u>						

Average GPU time for N=2048, NB=2, NT=4: 0.000414 Average GPU time for N=2048, NB=2, NT=8: 0.000413 Average GPU time for N=2048, NB=2, NT=32: 0.000412 Average GPU time for N=2048, NB=2, NT=32: 0.000412 Average GPU time for N=2048, NB=4, NT=2: 0.0004123 Average GPU time for N=2048, NB=4, NT=2: 0.0004123 Average GPU time for N=2048, NB=4, NT=8: 0.0004038 Average GPU time for N=2048, NB=4, NT=16: 0.000403 Average GPU time for N=2048, NB=4, NT=16: 0.0004043 Average GPU time for N=2048, NB=8, NT=2: 0.000413 Average GPU time for N=2048, NB=8, NT=2: 0.000413 Average GPU time for N=2048, NB=8, NT=2: 0.000413 Average GPU time for N=2048, NB=8, NT=8: 0.000417 Average GPU time for N=2048, NB=8, NT=8: 0.000417 Average GPU time for N=2048, NB=8, NT=2: 0.000422 Average GPU time for N=2048, NB=16, NT=2: 0.000408 Average GPU time for N=2048, NB=16, NT=2: 0.000409 Average GPU time for N=2048, NB=16, NT=3: 0.000409 Average GPU time for N=2048, NB=16, NT=6: 0.000409 Average GPU time for N=2048, NB=16, NT=6: 0.000419 Average GPU time for N=2048, NB=16, NT=6: 0.000419 Average GPU time for N=2048, NB=32, NT=6: 0.000392 Average GPU time for N=2048, NB=32, NT=8: 0.000411	Average	GPU	time	for	N=2048,	NB=2,	NT=2:	0.000404
Average GPU time for N=2048, NB=2, NT=16: 0.000396 Average GPU time for N=2048, NB=4, NT=32: 0.000412 Average GPU time for N=2048, NB=4, NT=2: 0.000412 Average GPU time for N=2048, NB=4, NT=4: 0.000408 Average GPU time for N=2048, NB=4, NT=8: 0.000408 Average GPU time for N=2048, NB=4, NT=8: 0.000408 Average GPU time for N=2048, NB=4, NT=16: 0.0004408 Average GPU time for N=2048, NB=4, NT=2: 0.000440 Average GPU time for N=2048, NB=4, NT=2: 0.000388 Average GPU time for N=2048, NB=8, NT=2: 0.000388 Average GPU time for N=2048, NB=8, NT=3: 0.000413 Average GPU time for N=2048, NB=8, NT=3: 0.000417 Average GPU time for N=2048, NB=8, NT=32: 0.000422 Average GPU time for N=2048, NB=16, NT=1: 0.000409 Average GPU time for N=2048, NB=16, NT=1: 0.000408 Average GPU time for N=2048, NB=16, NT=1: 0.000409 Average GPU time for N=2048, NB=16, NT=1: 0.000409 Average GPU time for N=2048, NB=16, NT=1: 0.000409 Average GPU time for N=2048, NB=16, NT=12: 0.000417 Average GPU time for N=2048, NB=16, NT=3: 0.000417 Average GPU time for N=2048, NB=32, NT=16: 0.000399 Average GPU time for N=2048, NB=32, NT=16: 0.000399 Average GPU time for N=2048, NB=32, NT=8: 0.000392 Average GPU time for N=2048, NB=32, NT=8: 0.000392	Average	GPU	time	for	N=2048,	NB=2,	NT=4:	0.000414
Average GPU time for N=2048, NB=2, NT=32: 0.000412 Average GPU time for N=2048, NB=4, NT=2: 0.000412 Average GPU time for N=2048, NB=4, NT=2: 0.000423 Average GPU time for N=2048, NB=4, NT=4: 0.000438 Average GPU time for N=2048, NB=4, NT=8: 0.000438 Average GPU time for N=2048, NB=4, NT=16: 0.000443 Average GPU time for N=2048, NB=4, NT=2: 0.000440 Average GPU time for N=2048, NB=8, NT=2: 0.000388 Average GPU time for N=2048, NB=8, NT=2: 0.000413 Average GPU time for N=2048, NB=8, NT=4: 0.000413 Average GPU time for N=2048, NB=8, NT=16: 0.000419 Average GPU time for N=2048, NB=8, NT=32: 0.000422 Average GPU time for N=2048, NB=16, NT=2: 0.000425 Average GPU time for N=2048, NB=16, NT=1: 0.000409 Average GPU time for N=2048, NB=16, NT=1: 0.000409 Average GPU time for N=2048, NB=16, NT=8: 0.000409 Average GPU time for N=2048, NB=16, NT=2: 0.000419 Average GPU time for N=2048, NB=16, NT=2: 0.000419 Average GPU time for N=2048, NB=16, NT=2: 0.000409 Average GPU time for N=2048, NB=32, NT=16: 0.000399 Average GPU time for N=2048, NB=32, NT=8: 0.000399	Average	GPU	time	for	N=2048,	NB=2,	NT=8:	0.000413
Average GPU time for N=2048, NB=4, NT=2: 0.0004/23 Average GPU time for N=2048, NB=4, NT=4: 0.0004/08 Average GPU time for N=2048, NB=4, NT=4: 0.0004/08 Average GPU time for N=2048, NB=4, NT=3: 0.0004/08 Average GPU time for N=2048, NB=4, NT=16: 0.0004/43 Average GPU time for N=2048, NB=8, NT=2: 0.0004/40 Average GPU time for N=2048, NB=8, NT=2: 0.0004/40 Average GPU time for N=2048, NB=8, NT=4: 0.0004/17 Average GPU time for N=2048, NB=8, NT=8: 0.0004/17 Average GPU time for N=2048, NB=8, NT=8: 0.0004/17 Average GPU time for N=2048, NB=8, NT=3: 0.0004/22 Average GPU time for N=2048, NB=16, NT=2: 0.0004/08 Average GPU time for N=2048, NB=16, NT=2: 0.0004/09 Average GPU time for N=2048, NB=16, NT=8: 0.0004/09 Average GPU time for N=2048, NB=16, NT=16: 0.0004/28 Average GPU time for N=2048, NB=16, NT=2: 0.0004/28 Average GPU time for N=2048, NB=32, NT=8: 0.0003/99	Average	GPU	time	for	N=2048,	NB=2,	NT=16:	0.000396
Average GPU time for N=2048, NB=4, NT=4: 0.000408 Average GPU time for N=2048, NB=4, NT=8: 0.000438 Average GPU time for N=2048, NB=4, NT=8: 0.000438 Average GPU time for N=2048, NB=4, NT=3: 0.0004408 Average GPU time for N=2048, NB=4, NT=2: 0.000440 Average GPU time for N=2048, NB=8, NT=2: 0.000388 Average GPU time for N=2048, NB=8, NT=2: 0.000388 Average GPU time for N=2048, NB=8, NT=8: 0.000417 Average GPU time for N=2048, NB=8, NT=16: 0.000409 Average GPU time for N=2048, NB=8, NT=32: 0.000422 Average GPU time for N=2048, NB=16, NT=2: 0.000428 Average GPU time for N=2048, NB=16, NT=4: 0.000495 Average GPU time for N=2048, NB=16, NT=4: 0.000495 Average GPU time for N=2048, NB=16, NT=16: 0.0004409 Average GPU time for N=2048, NB=16, NT=16: 0.000420 Average GPU time for N=2048, NB=16, NT=3: 0.000361 Average GPU time for N=2048, NB=32, NT=16: 0.000399 Average GPU time for N=2048, NB=32, NT=8: 0.000399	Average	GPU	time	for	N=2048,	NB=2,	NT=32:	0.000412
Average GPU time for N=2048, NB=4, NT=8: 0.000438 Average GPU time for N=2048, NB=4, NT=16: 0.000443 Average GPU time for N=2048, NB=4, NT=32: 0.000443 Average GPU time for N=2048, NB=8, NT=2: 0.000388 Average GPU time for N=2048, NB=8, NT=2: 0.000433 Average GPU time for N=2048, NB=8, NT=4: 0.000433 Average GPU time for N=2048, NB=8, NT=16: 0.000417 Average GPU time for N=2048, NB=8, NT=32: 0.000429 Average GPU time for N=2048, NB=16, NT=32: 0.000422 Average GPU time for N=2048, NB=16, NT=2: 0.000428 Average GPU time for N=2048, NB=16, NT=8: 0.000499 Average GPU time for N=2048, NB=16, NT=8: 0.000499 Average GPU time for N=2048, NB=16, NT=8: 0.000428 Average GPU time for N=2048, NB=16, NT=26: 0.000428 Average GPU time for N=2048, NB=32, NT=8: 0.000399	Average	GPU	time	for	N=2048,	NB=4,	NT=2:	0.000423
Average GPU time for N=2048, NB=4, NT=16: 0.000443 Average GPU time for N=2048, NB=4, NT=32: 0.000440 Average GPU time for N=2048, NB=8, NT=2: 0.000440 Average GPU time for N=2048, NB=8, NT=2: 0.000433 Average GPU time for N=2048, NB=8, NT=4: 0.000417 Average GPU time for N=2048, NB=8, NT=8: 0.000417 Average GPU time for N=2048, NB=8, NT=16: 0.000409 Average GPU time for N=2048, NB=8, NT=32: 0.000422 Average GPU time for N=2048, NB=16, NT=2: 0.000408 Average GPU time for N=2048, NB=16, NT=2: 0.000409 Average GPU time for N=2048, NB=16, NT=8: 0.000428 Average GPU time for N=2048, NB=16, NT=16: 0.000428 Average GPU time for N=2048, NB=16, NT=2: 0.000312 Average GPU time for N=2048, NB=32, NT=1: 0.000399 Average GPU time for N=2048, NB=32, NT=8: 0.000399	Average	GPU	time	for	N=2048,	NB=4,	NT=4:	0.000408
Average GPU time for N=2048, NB=4, NT=32: 0.000440 Average GPU time for N=2048, NB=8, NT=2: 0.000388 Average GPU time for N=2048, NB=8, NT=2: 0.000388 Average GPU time for N=2048, NB=8, NT=8: 0.000417 Average GPU time for N=2048, NB=8, NT=16: 0.000409 Average GPU time for N=2048, NB=8, NT=16: 0.000422 Average GPU time for N=2048, NB=16, NT=2: 0.000422 Average GPU time for N=2048, NB=16, NT=2: 0.000425 Average GPU time for N=2048, NB=16, NT=8: 0.000409 Average GPU time for N=2048, NB=16, NT=8: 0.000409 Average GPU time for N=2048, NB=16, NT=16: 0.000428 Average GPU time for N=2048, NB=32, NT=16: 0.000361 Average GPU time for N=2048, NB=32, NT=16: 0.000399 Average GPU time for N=2048, NB=32, NT=16: 0.000399 Average GPU time for N=2048, NB=32, NT=16: 0.000392 Average GPU time for N=2048, NB=32, NT=16: 0.000420	Average	GPU	time	for	N=2048,	NB=4,	NT=8:	0.000438
Average GPU time for N=2048, NB=8, NT=2: 0.000388 Average GPU time for N=2048, NB=8, NT=4: 0.000433 Average GPU time for N=2048, NB=8, NT=4: 0.000433 Average GPU time for N=2048, NB=8, NT=3: 0.000449 Average GPU time for N=2048, NB=8, NT=32: 0.000422 Average GPU time for N=2048, NB=16, NT=2: 0.000409 Average GPU time for N=2048, NB=16, NT=2: 0.000408 Average GPU time for N=2048, NB=16, NT=8: 0.000409 Average GPU time for N=2048, NB=16, NT=8: 0.000409 Average GPU time for N=2048, NB=16, NT=32: 0.000417 Average GPU time for N=2048, NB=32, NT=2: 0.000361 Average GPU time for N=2048, NB=32, NT=8: 0.000399 Average GPU time for N=2048, NB=32, NT=8: 0.000392 Average GPU time for N=2048, NB=32, NT=8: 0.000392	Average	GPU	time	for	N=2048,	NB=4,	NT=16:	0.000443
Average GPU time for N=2048, NB=8, NT=4: 0.000433 Average GPU time for N=2048, NB=8, NT=8: 0.000417 Average GPU time for N=2048, NB=8, NT=16: 0.000419 Average GPU time for N=2048, NB=8, NT=32: 0.000422 Average GPU time for N=2048, NB=16, NT=2: 0.000408 Average GPU time for N=2048, NB=16, NT=2: 0.000408 Average GPU time for N=2048, NB=16, NT=8: 0.000409 Average GPU time for N=2048, NB=16, NT=8: 0.000409 Average GPU time for N=2048, NB=16, NT=2: 0.000417 Average GPU time for N=2048, NB=32, NT=16: 0.000399 Average GPU time for N=2048, NB=32, NT=8: 0.000399 Average GPU time for N=2048, NB=32, NT=8: 0.000399 Average GPU time for N=2048, NB=32, NT=8: 0.000399 Average GPU time for N=2048, NB=32, NT=16: 0.000392	Average	GPU	time	for	N=2048,	NB=4,	NT=32:	0.000440
Average GPU time for N=2048, NB=8, NT=8: 0.000417 Average GPU time for N=2048, NB=8, NT=16: 0.000409 Average GPU time for N=2048, NB=8, NT=16: 0.000409 Average GPU time for N=2048, NB=16, NT=2: 0.000402 Average GPU time for N=2048, NB=16, NT=2: 0.000408 Average GPU time for N=2048, NB=16, NT=8: 0.000409 Average GPU time for N=2048, NB=16, NT=8: 0.000409 Average GPU time for N=2048, NB=16, NT=32: 0.000417 Average GPU time for N=2048, NB=32, NT=2: 0.000361 Average GPU time for N=2048, NB=32, NT=4: 0.000399 Average GPU time for N=2048, NB=32, NT=8: 0.000399 Average GPU time for N=2048, NB=32, NT=8: 0.000399 Average GPU time for N=2048, NB=32, NT=8: 0.000399	Average	GPU	time	for	N=2048,	NB=8,	NT=2:	0.000388
Average GPU time for N=2048, NB=8, NT=16: 0.000409 Average GPU time for N=2048, NB=8, NT=32: 0.000422 Average GPU time for N=2048, NB=16, NT=2: 0.000422 Average GPU time for N=2048, NB=16, NT=4: 0.000425 Average GPU time for N=2048, NB=16, NT=8: 0.000409 Average GPU time for N=2048, NB=16, NT=16: 0.000428 Average GPU time for N=2048, NB=16, NT=32: 0.000417 Average GPU time for N=2048, NB=32, NT=2: 0.000361 Average GPU time for N=2048, NB=32, NT=18: 0.000399 Average GPU time for N=2048, NB=32, NT=8: 0.000399 Average GPU time for N=2048, NB=32, NT=8: 0.000399 Average GPU time for N=2048, NB=32, NT=16: 0.000420	Average	GPU	time	for	N=2048,	NB=8,	NT=4:	0.000433
Average GPU time for N=2048, NB=8, NT=32: 0.000422 Average GPU time for N=2048, NB=16, NT=2: 0.000408 Average GPU time for N=2048, NB=16, NT=4: 0.000408 Average GPU time for N=2048, NB=16, NT=8: 0.000409 Average GPU time for N=2048, NB=16, NT=16: 0.000408 Average GPU time for N=2048, NB=16, NT=2: 0.000417 Average GPU time for N=2048, NB=32, NT=2: 0.000417 Average GPU time for N=2048, NB=32, NT=1: 0.000399 Average GPU time for N=2048, NB=32, NT=8: 0.000399 Average GPU time for N=2048, NB=32, NT=6: 0.000399 Average GPU time for N=2048, NB=32, NT=16: 0.000399	Average	GPU	time	for	N=2048,	NB=8,	NT=8:	0.000417
Average GPU time for N=2048, NB=16, NT=2: 0.000408 Average GPU time for N=2048, NB=16, NT=4: 0.000425 Average GPU time for N=2048, NB=16, NT=8: 0.000409 Average GPU time for N=2048, NB=16, NT=16: 0.000409 Average GPU time for N=2048, NB=16, NT=32: 0.000417 Average GPU time for N=2048, NB=32, NT=2: 0.000361 Average GPU time for N=2048, NB=32, NT=4: 0.000399 Average GPU time for N=2048, NB=32, NT=8: 0.000392 Average GPU time for N=2048, NB=32, NT=16: 0.000420	Average	GPU	time	for	N=2048,	NB=8,	NT=16:	0.000409
Average GPU time for N=2048, NB=16, NT=4: 0.000425 Average GPU time for N=2048, NB=16, NT=8: 0.000409 Average GPU time for N=2048, NB=16, NT=6: 0.000428 Average GPU time for N=2048, NB=16, NT=32: 0.000417 Average GPU time for N=2048, NB=32, NT=2: 0.000361 Average GPU time for N=2048, NB=32, NT=4: 0.000399 Average GPU time for N=2048, NB=32, NT=8: 0.000392 Average GPU time for N=2048, NB=32, NT=16: 0.0003420	Average	GPU	time	for	N=2048,	NB=8,	NT=32:	0.000422
Average GPU time for N=2048, NB=16, NT=8: 0.000409 Average GPU time for N=2048, NB=16, NT=8: 0.000428 Average GPU time for N=2048, NB=16, NT=32: 0.000417 Average GPU time for N=2048, NB=32, NT=2: 0.000437 Average GPU time for N=2048, NB=32, NT=4: 0.000399 Average GPU time for N=2048, NB=32, NT=8: 0.000399 Average GPU time for N=2048, NB=32, NT=16: 0.0003420	Average	GPU	time	for	N=2048,	NB=16,	NT=2:	0.000408
Average GPU time for N=2048, NB=16, NT=16: 0.000428 Average GPU time for N=2048, NB=16, NT=32: 0.000417 Average GPU time for N=2048, NB=32, NT=2: 0.000361 Average GPU time for N=2048, NB=32, NT=4: 0.000399 Average GPU time for N=2048, NB=32, NT=8: 0.000392 Average GPU time for N=2048, NB=32, NT=16: 0.000420	Average	GPU	time	for	N=2048,	NB=16,	NT=4:	0.000425
Average GPU time for N=2048, NB=16, NT=32: 0.000417 Average GPU time for N=2048, NB=32, NT=2: 0.000361 Average GPU time for N=2048, NB=32, NT=4: 0.000399 Average GPU time for N=2048, NB=32, NT=8: 0.000392 Average GPU time for N=2048, NB=32, NT=16: 0.000420	Average	GPU	time	for	N=2048,	NB=16,	NT=8:	0.000409
Average GPU time for N=2048, NB=32, NT=2: 0.000361 Average GPU time for N=2048, NB=32, NT=4: 0.000399 Average GPU time for N=2048, NB=32, NT=8: 0.000392 Average GPU time for N=2048, NB=32, NT=16: 0.000420	Average	GPU	time	for	N=2048,	NB=16,	NT=16	5: 0.000428
Average GPU time for N=2048, NB=32, NT=4: 0.000399 Average GPU time for N=2048, NB=32, NT=8: 0.000392 Average GPU time for N=2048, NB=32, NT=16: 0.000420	Average	GPU	time	for	N=2048,	NB=16,	NT=32	2: 0.000417
Average GPU time for N=2048, NB=32, NT=8: 0.000392 Average GPU time for N=2048, NB=32, NT=16: 0.000420	Average	GPU	time	for	N=2048,	NB=32,	NT=2:	0.000361
Average GPU time for N=2048, NB=32, NT=16: 0.000420	Average	GPU	time	for	N=2048,	NB=32,	NT=4:	0.000399
	Average	GPU	time	for	N=2048,	NB=32,	NT=8:	0.000392
Average GPU time for N=2048, NB=32, NT=32: 0.000411	Average	GPU	time	for	N=2048,	NB=32,	NT=16	5: 0.000420
	Average	GPU	time	for	N=2048,	NB=32,	NT=32	2: 0.000411

Figure 8 & 9: NB/NT Benchmark (10 Runs per Value)

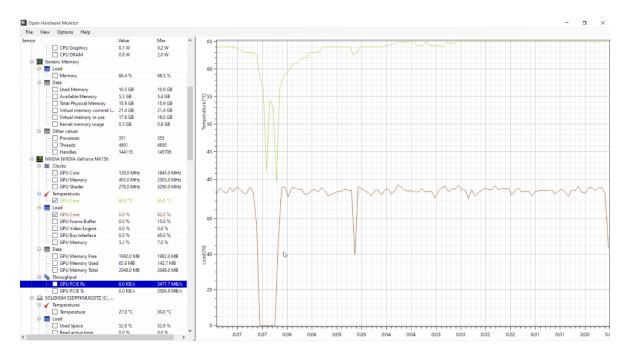


Figure 10: Throttling behavior and thermal characteristics (1000 Runs per Value, throttling engages within first set of values)

With this in mind it's difficult to draw conclusively which values of NB and NT are best from the raw data, but it would make sense for higher values to perform better up to a limit. There are hard

limitation that are encountered based on GPU capabilities, but within a reasonable range of 2-32, NB = 32 and NT = 32 should have given the best results, if not maybe 16.

# Compilation and Testing

As all code was written and tested on my own local device (Nvidia MX150, Ubuntu 22 via WSL), compilation was as simple as *nvcc -o mm\_\* mm\_\*.cu*. The submitted code is left in the ideal state for performance benchmarks, but a few lines can be uncommented to display RMSE for all runs and decrease to a limited number of runs.