

Key Literature

Luke Heyfron

1 Key Literature

The focus of the literature review will be on the following articles, roughly in order of importance.

1.1 Progress key

‘*’ means ‘have read’

‘@’ means ‘have understood’

‘!’ means ‘have taken notes’

‘#’ means ‘read next’.

‘-’ means ‘reading’

‘.’ means ‘understanding’

‘?’ means ‘taking notes’

1.2 Multi-Qubit Gate Synthesis

[1]*@?

[2]*.?

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1.3 Single Qubit Gate Synthesis

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1.4 Other

[15]*.?

[16]

2 Discussion points

For each synthesis scheme consider the following (and compare schemes to one another):

- Resource cost
 - Number of elementary gates used
 - Number of expensive/T gates (resource states) used
- Applicability
 - Is the scheme universal or for unitaries generated by a non-universal gate set?
 - Does the scheme yield optimal circuits or circuits that use fewer resources than a certain function of the number of qubits?
 - Is it exact or approximate? If approximate how is the precision characterized i.e. as a function of number of gates used?
 - Is the scheme applicable to multi-qubit circuits or only single qubit circuits?
- Efficiency
 - Is the algorithm for generating the circuit efficient in time and/or space requirements?
 - How fast does the algorithm execute asymptotically?

3 Additional Literature

[17]*! [18]*! [19]- [20]- [21] [22] [23] [24] [25]

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