

$$2, \quad 1 \text{ として } x'_i = x_i - \bar{x}, \quad y'_i = y_i - \bar{y} \quad \text{と置く.}$$

$$\bar{x}' = 0, \quad \bar{y}' = 0.$$

$$\overline{x'^2} = \frac{1}{N} \sum_{i=1}^N (x_i - \bar{x})^2 = \overline{x^2} - \bar{x}^2$$

$$\overline{x'y'} = \frac{1}{N} \sum_{i=1}^N (x_i - \bar{x})(y_i - \bar{y}) = \overline{xy} - \bar{x}\bar{y}.$$

$$1 \text{ の 結果より } \hat{\beta}_1 = \frac{\overline{x'y'}}{\overline{x'^2}} = \frac{\overline{x^2} - \bar{x}^2}{\overline{xy} - \bar{x}\bar{y}}.$$

$$\text{また, } \bar{y} = \hat{\beta}_0 + \hat{\beta}_1 \bar{x} \quad \text{より,}$$

$$\hat{\beta}_0 = \bar{y} - \hat{\beta}_1 \bar{x}.$$