**WBC dataset:** Features are computed from a digitized image of a fine needle aspirate (FNA) of a breast mass. They describe characteristics of the cell nuclei present in the image.

Data Set Characteristics:	Multivariate	Number of Instances:	1080	Area:	Life
Attribute Characteristics:	Real	Number of Attributes:	30	Date Donated	1995-11-01
Associated Tasks:	Classification	Anomaly ratio	0.02	Number of Web Hits:	1408511

#### **Attribute Information:**

1-30)

Ten real-valued features are computed for each cell nucleus:

- a) radius (mean of distances from center to points on the perimeter)
- b) texture (standard deviation of gray-scale values)
- c) perimeter
- d) area
- e) smoothness (local variation in radius lengths)
- f) compactness (perimeter^2 / area 1.0)
- g) concavity (severity of concave portions of the contour)

- h) concave points (number of concave portions of the contour)
- i) symmetry
- j) fractal dimension ("coastline approximation" 1)

# Sample rule explanation:

# **Anomaly Data:**

Example: perimeter = 20.6, radius\_01 = 29.33, radius\_02 = 140.1, radius\_03 = 1265, radius\_04 = 0.1178, texture\_01 = 0.277, texture\_02 = 0.3514, texture\_03 = 0.152, texture\_04 = 0.2397, permeter = 0.07016, area\_01 = 0.726, area\_02 = 1.595, area\_03 = 5.772, smoothness\_01 = 86.22, smoothness\_02 = 0.006522, compactness\_01 = 0.06158, compactness\_02 = 0.07117, compactness\_03 = 0.01664, compactness\_04 = 0.02324, compactness\_05 = 0.006185, compactness\_06 = 25.74, concavity\_01 = 39.42, concavity\_02 = 184.6, concavity\_03 = 1821, concave\_points = 0.165, symmetry\_01 = 0.8681, symmetry\_02 = 0.9387, symmetry\_03 = 0.265, fractal dimension 01 = 0.4087, fractal dimension 02 = 0.124

constraint rule 1 : perimeter = 20.6, radius\_01 = 29.33, radius\_02 = 140.1, radius\_04 = 0.1178, texture\_01 = 0.277, texture\_02 = 0.3514, texture\_03 = 0.152, texture\_04 = 0.2397, permeter = 0.07016, area\_01 = 0.726, area\_02 = 1.595, area\_03 = 5.772, smoothness\_01 = 86.22, smoothness\_02 = 0.006522, compactness\_01 = 0.06158, compactness\_02 = 0.07117, compactness\_03 = 0.01664, compactness\_04 = 0.02324, compactness\_05 = 0.006185, compactness\_06 = 25.74, concavity\_01 = 39.42, concavity\_02 = 184.6, concave\_points = 0.165, symmetry\_01 = 0.06158, compactness\_06 = 25.74, concavity\_01 = 39.42, concavity\_02 = 184.6, concave\_points = 0.165, symmetry\_01 = 0.06158, compactness\_06 = 0.006185, compactne

0.8681, symmetry\_02 = 0.9387, symmetry\_03 = 0.265, fractal\_dimension\_01 = 0.4087, fractal\_dimension\_02 = 0.124  $\implies$  radius\_03 / perimeter = [24.27, 48.54] concavity\_03 = 0

This means that when (perimeter = 20.6, radius\_01 = 29.33, radius\_02 = 140.1, radius\_04 = 0.1178, texture\_01 = 0.277, texture\_02 = 0.3514, texture\_03 = 0.152, texture\_04 = 0.2397, permeter = 0.07016, area\_01 = 0.726, area\_02 = 1.595, area\_03 = 5.772, smoothness\_01 = 86.22, smoothness\_02 = 0.006522, compactness\_01 = 0.06158, compactness\_02 = 0.07117, compactness\_03 = 0.01664, compactness\_04 = 0.02324, compactness\_05 = 0.006185, compactness\_06 = 25.74, concavity\_01 = 39.42, concavity\_02 = 184.6, concave\_points = 0.165, symmetry\_01 = 0.8681, symmetry\_02 = 0.9387, symmetry\_03 = 0.265, fractal\_dimension\_01 = 0.4087, fractal\_dimension\_02 = 0.124), attribute **concavity\_03** = 0 and attribute **radius\_03** divided by attribute **perimeter** should be between **24.27** and **48.54**, while attribute **concavity\_03** is 1821 and attribute **radius\_03** divided by attribute **perimeter** is **61.4** which is not within the normal value range, so the data is abnormal.

### **Constraint rules for discovery:**

constraint rule 1 : perimeter = 20.6, radius\_01 = 29.33, radius\_02 = 140.1, radius\_03 = 1265.0, radius\_04 = 0.1178, texture\_01 = 0.277, texture\_02 = 0.3514, texture\_03 = 0.152, texture\_04 = 0.2397, permeter = 0.07016, area\_01 = 0.726, area\_02 = 1.595, area\_03 = 5.772, smoothness\_01 = 86.22, smoothness\_02 = 0.006522, compactness\_01 = 0.06158, compactness\_02 = 0.07117, compactness\_03 = 0.01664, compactness\_04 = 0.02324, compactness\_05 = 0.006185, compactness\_06 = 25.74, concavity\_01 = 39.42, concavity\_02 = 184.6,

concave\_points = 0.165, symmetry\_01 = 0.8681, symmetry\_02 = 0.9387, symmetry\_03 = 0.265, fractal\_dimension\_01 = 0.4087, fractal\_dimension\_02 = 0.124,  $\Rightarrow$  concavity 03 / compactness 06 = [16.51, 49.57]

constraint rule 3 : perimeter = 13.08, radius\_01 = 15.71, radius\_02 = 85.63, radius\_04 = 0.1075, texture\_01 = 0.127, texture\_02 = 0.04568, texture\_03 = 0.0311, texture\_04 = 0.1967, permeter = 0.06811, area\_01 = 0.1852, area\_02 = 0.7477, area\_03 = 1.383, smoothness\_01 = 14.67, smoothness\_02 = 0.004097, compactness\_01 = 0.01898, compactness\_02 = 0.01698, compactness\_03 = 0.00649, compactness\_04 = 0.01678, compactness\_05 = 0.002425, compactness\_06 = 14.5, concavity\_01 = 20.49, concavity\_02 = 96.09, concave\_points = 0.1312, symmetry\_01 = 0.2776, symmetry\_02 = 0.189, symmetry\_03 = 0.07283, fractal\_dimension\_01 = 0.3184, fractal\_dimension\_02 = 0.08183,  $\Rightarrow$  radius\_03 = 0.07283, fractal\_dimension\_03 / compactness\_06 = 1.00276, symmetry\_03 / compactness\_06 = 1.00276, symmetry\_08 / compactness\_08 = 1.00276, symmetry\_09 / compactness\_09 = 1.0027

constraint rule 4 : perimeter = 9.504, radius\_01 = 12.44, radius\_02 = 60.34, radius\_04 = 0.1024, texture\_01 = 0.06492, texture\_02 = 0.02956, texture\_03 = 0.02076, texture\_04 = 0.1815, permeter = 0.06905, area\_01 = 0.2773, area\_02 = 0.9768, area\_03 = 1.909, smoothness\_01 = 15.7, smoothness\_02 = 0.009606, compactness\_01 = 0.01432, compactness\_02 = 0.01985, compactness\_03 = 0.01421, compactness\_04 = 0.01432, compactness\_04 = 0.01432, compactness\_05 = 0.01421, compactness\_05 = 0.01421, compactness\_06 = 0.01421, compactness\_07 = 0.01432, compactness\_07 = 0.01432,

0.02027, compactness\_05 = 0.002968, compactness\_06 = 10.23, concavity\_01 = 15.66, concavity\_02 = 65.13, concave\_points = 0.1324, symmetry\_01 = 0.1148, symmetry\_02 = 0.08867, symmetry\_03 = 0.06227, fractal\_dimension\_01 = 0.245, fractal\_dimension\_02 = 0.07773, 

⇒ radius\_03 / perimeter = [52.61, 105.22] concavity\_03 = 0

constraint rule 5 : perimeter = 10.96, radius\_01 = 17.62, radius\_02 = 70.79, radius\_04 = 0.09687, texture\_01 = 0.09752, texture\_02 = 0.05263, texture\_03 = 0.02788, texture\_04 = 0.1619, permeter = 0.06408, area\_01 = 0.1507, area\_02 = 1.583, area\_03 = 1.165, smoothness\_01 = 10.09, smoothness\_02 = 0.009501, compactness\_01 = 0.03378, compactness\_02 = 0.04401, compactness\_03 = 0.01346, compactness\_04 = 0.01322, compactness\_05 = 0.003534, compactness\_06 = 11.62, concavity\_01 = 26.51, concavity\_02 = 76.43, concave\_points = 0.1428, symmetry\_01 = 0.251, symmetry\_02 = 0.2123, symmetry\_03 = 0.09861, fractal\_dimension\_01 = 0.2289, fractal\_dimension\_02 = 0.08278, area\_03 = 1.165, smoothness\_04 = 0.01322, compactness\_05 = 0.003534, compactness\_06 = 11.62, concavity\_01 = 26.51, concavity\_02 = 76.43, concave\_points = 0.1428, symmetry\_01 = 0.251, symmetry\_02 = 0.2123, symmetry\_03 = 0.09861, fractal\_dimension\_01 = 0.2289, fractal\_dimension\_02 = 0.08278, area\_03 = 0.008278, symmetry\_03 = 0.008278, symmetry\_03 = 0.09861, fractal\_dimension\_01 = 0.2289, fractal\_dimension\_02 = 0.08278, symmetry\_03 = 0.008278, symmet

constraint rule 7 : perimeter = 12.19, radius\_01 = 13.29, radius\_02 = 79.08, radius\_04 = 0.1066, texture\_01 = 0.09509, texture\_02 = 0.02855, texture\_03 = 0.02882, texture\_04 = 0.188, permeter = 0.06471, area\_01 = 0.2005, area\_02 = 0.8163, area\_03 = 1.973, smoothness\_01

= 15.24, smoothness\_02 = 0.006773, compactness\_01 = 0.02456, compactness\_02 = 0.01018, compactness\_03 = 0.008094, compactness\_04 = 0.02662, compactness\_05 = 0.004143, compactness\_06 = 13.34, concavity\_01 = 17.81, concavity\_02 = 91.38, concavity\_03 = 545.2, concave\_points = 0.1427, symmetry\_01 = 0.2585, symmetry\_02 = 0.09915, symmetry\_03 = 0.08187, fractal\_dimension\_01 = 0.3469, fractal\_dimension\_02 = 0.09241,  $\Rightarrow$  radius\_03 / perimeter = [41.02, 82.03]

constraint rule 8 : perimeter = 15.71, radius\_01 = 13.93, radius\_02 = 102.0, radius\_03 = 761.7, radius\_04 = 0.09462, texture\_01 = 0.09462, texture\_02 = 0.07135, texture\_03 = 0.05933, texture\_04 = 0.1816, permeter = 0.05723, area\_01 = 0.3117, area\_02 = 0.8155, area\_03 = 1.972, smoothness\_01 = 27.94, smoothness\_02 = 0.005217, compactness\_01 = 0.01515, compactness\_02 = 0.01678, compactness\_03 = 0.01268, compactness\_04 = 0.01669, compactness\_05 = 0.00233, compactness\_06 = 17.5, concavity\_01 = 19.25, concavity\_02 = 114.3, concave\_points = 0.1223, symmetry\_01 = 0.1949, symmetry\_02 = 0.1709, symmetry\_03 = 0.1374, fractal\_dimension\_01 = 0.2723, fractal\_dimension\_02 = 0.07071, 
\$\Rightarrow\$ concavity\_03 / compactness\_06 = [24.29, 72.91]

constraint rule 9 : perimeter = 15.1, radius\_01 = 16.39, radius\_02 = 99.58, radius\_04 = 0.115, texture\_01 = 0.1807, texture\_02 = 0.1138, texture\_03 = 0.08534, texture\_04 = 0.2001, permeter = 0.06467, area\_01 = 0.4309, area\_02 = 1.068, area\_03 = 2.796, smoothness\_01 = 39.84, smoothness\_02 = 0.009006, compactness\_01 = 0.04185, compactness\_02 = 0.03204, compactness\_03 = 0.02258, compactness\_04 = 0.02353, compactness\_05 = 0.004984, compactness\_06 = 16.11, concavity\_01 = 18.33, concavity\_02 = 105.9, concavity\_03 = 762.6, concave\_points = 0.1386, symmetry\_01 = 0.2883, symmetry\_02 = 0.196, symmetry\_03 = 0.1423, fractal\_dimension\_01 = 0.259, fractal\_dimension\_02 = 0.07779, 

⇒ radius\_03 / perimeter = [33.11, 66.23]

constraint rule 10 : perimeter = 11.41, radius\_01 = 10.82, radius\_02 = 73.34, radius\_04 = 0.09373, texture\_01 = 0.06685, texture\_02 =

0.03512, texture\_03 = 0.02623, texture\_04 = 0.1667, permeter = 0.06113, area\_01 = 0.1408, area\_02 = 0.4607, area\_03 = 1.103, smoothness\_01 = 10.5, smoothness\_02 = 0.00604, compactness\_01 = 0.01529, compactness\_02 = 0.01514, compactness\_03 = 0.00646, compactness\_04 = 0.01344, compactness\_05 = 0.002206, compactness\_06 = 12.82, concavity\_01 = 15.97, concavity\_02 = 83.74, concave\_points = 0.1548, symmetry\_01 = 0.239, symmetry\_02 = 0.2102, symmetry\_03 = 0.08958, fractal\_dimension\_01 = 0.3016, fractal\_dimension\_02 = 0.08523, ⇒ radius\_03 / perimeter = [43.82, 87.64] concavity\_03 = 0.08958, fractal\_dimension\_01 = 0.3016, fractal\_dimension\_02 = 0.08523, ⇒ radius\_03 / perimeter = [43.82, 87.64] concavity\_03 = 0.08958, fractal\_dimension\_01 = 0.3016, fractal\_dimension\_02 = 0.08523, ⇒ radius\_03 / perimeter = [43.82, 87.64] concavity\_03 = 0.08958, fractal\_dimension\_01 = 0.3016, fractal\_dimension\_02 = 0.08523, ⇒ radius\_03 / perimeter = [43.82, 87.64] concavity\_03 = 0.08958, fractal\_dimension\_01 = 0.3016, fractal\_dimension\_02 = 0.08523, ⇒ radius\_03 / perimeter = [43.82, 87.64] concavity\_03 = 0.08958, fractal\_dimension\_01 = 0.3016, fractal\_dimension\_02 = 0.08523, ⇒ radius\_03 / perimeter = [43.82, 87.64] concavity\_03 = 0.08958, fractal\_dimension\_01 = 0.3016, fractal\_dimension\_02 = 0.08523, ⇒ radius\_03 / perimeter = [43.82, 87.64] concavity\_03 = 0.08958, fractal\_dimension\_01 = 0.3016, fractal\_dimension\_02 = 0.08523, ⇒ radius\_03 / perimeter = [43.82, 87.64] concavity\_03 = 0.08958, fractal\_dimension\_01 = 0.3016, fractal\_dimension\_02 = 0.08958, fractal\_dimension\_01 = 0.3016, fractal\_dimension\_02 = 0.08958, fractal\_dimension\_01 = 0.3016, fractal\_dimension\_02 = 0.08958, fractal\_dimension\_0

constraint rule 11 : perimeter = 11.64, radius\_01 = 18.33, radius\_02 = 75.17, radius\_03 = 412.5, radius\_04 = 0.1142, texture\_01 = 0.1017, texture\_02 = 0.0707, texture\_03 = 0.03485, texture\_04 = 0.1801, permeter = 0.0652, area\_01 = 0.306, area\_02 = 1.657, area\_03 = 2.155, smoothness\_01 = 20.62, smoothness\_02 = 0.00854, compactness\_01 = 0.0231, compactness\_02 = 0.02945, compactness\_03 = 0.01398, compactness\_04 = 0.01565, compactness\_05 = 0.00384, compactness\_06 = 13.14, concavity\_01 = 29.26, concavity\_02 = 85.51, concave\_points = 0.1688, symmetry\_01 = 0.266, symmetry\_02 = 0.2873, symmetry\_03 = 0.1218, fractal\_dimension\_01 = 0.2806, fractal\_dimension\_02 = 0.09097, 
\$\Rightarrow\$ concavity\_03 / compactness\_06 = [32.34, 97.11]

constraint rule 13 : perimeter = 12.18, radius\_01 = 17.84, radius\_02 = 77.79, radius\_04 = 0.1045, texture\_01 = 0.07057, texture\_02 = 0.0249, texture\_03 = 0.02941, texture\_04 = 0.19, permeter = 0.06635, area\_01 = 0.3661, area\_02 = 1.511, area\_03 = 2.41, smoothness\_01 = 24.44, smoothness\_02 = 0.005433, compactness\_01 = 0.01179, compactness\_02 = 0.01131, compactness\_03 = 0.01519, compactness\_04 = 0.0222, compactness\_05 = 0.003408, compactness\_06 = 12.83, concavity\_01 = 20.92, concavity\_02 = 82.14, concave\_points = 0.114, symmetry\_01 = 0.09358, symmetry\_02 = 0.0498, symmetry\_03 = 0.05882, fractal\_dimension\_01 = 0.2227, fractal\_dimension\_02 = 0.07376, area\_03 = 0.001319, compactness\_06 = [33.13, 99.45]

constraint rule 14 : perimeter = 9.787, radius\_01 = 19.94, radius\_02 = 62.11, radius\_04 = 0.1024, texture\_01 = 0.05301, texture\_02 = 0.006829, texture\_03 = 0.007937, texture\_04 = 0.135, permeter = 0.0689, area\_01 = 0.335, area\_02 = 2.043, area\_03 = 2.132, smoothness\_01 = 20.05, smoothness\_02 = 0.01113, compactness\_01 = 0.01463, compactness\_02 = 0.005308, compactness\_03 = 0.00525, compactness\_04 = 0.01801, compactness\_05 = 0.005667, compactness\_06 = 10.92, concavity\_01 = 26.29, concavity\_02 = 68.81, concavity\_03 = 366.1, concave\_points = 0.1316, symmetry\_01 = 0.09473, symmetry\_02 = 0.02049, symmetry\_03 = 0.02381, fractal\_dimension\_01 = 0.1934, fractal\_dimension\_02 = 0.08988, 
\Rightarrow radius\_03 / perimeter = [51.09, 102.18]

constraint rule 15 : perimeter = 11.6, radius\_01 = 12.84, radius\_02 = 74.34, radius\_03 = 412.6, radius\_04 = 0.08983, texture\_01 = 0.07525, texture\_02 = 0.04196, texture\_03 = 0.0335, texture\_04 = 0.162, permeter = 0.06582, area\_01 = 0.2315, area\_02 = 0.5391, area\_03 = 1.475, smoothness\_01 = 15.75, smoothness\_02 = 0.006153, compactness\_01 = 0.0133, compactness\_02 = 0.01693, compactness\_03 = 0.006884, compactness\_04 = 0.01651, compactness\_05 = 0.002551, compactness\_06 = 13.06, concavity\_01 = 17.16, concavity\_02 = 82.96, concave\_points = 0.1431, symmetry\_01 = 0.1851, symmetry\_02 = 0.1922, symmetry\_03 = 0.08449, fractal\_dimension\_01 = 0.2772,

fractal dimension 02 = 0.08756,  $\Rightarrow$  concavity 03 / compactness 06 = [32.54, 97.7]

constraint rule 16 : perimeter = 13.27, radius\_01 = 14.76, radius\_02 = 84.74, radius\_04 = 0.07355, texture\_01 = 0.05055, texture\_02 = 0.03261, texture\_03 = 0.02648, texture\_04 = 0.1386, permeter = 0.05318, area\_01 = 0.4057, area\_02 = 1.153, area\_03 = 2.701, smoothness\_01 = 36.35, smoothness\_02 = 0.004481, compactness\_01 = 0.01038, compactness\_02 = 0.01358, compactness\_03 = 0.01082, compactness\_04 = 0.01069, compactness\_05 = 0.001435, compactness\_06 = 16.36, concavity\_01 = 22.35, concavity\_02 = 104.5, concavity\_03 = 830.6, concave\_points = 0.1006, symmetry\_01 = 0.1238, symmetry\_02 = 0.135, symmetry\_03 = 0.1001, fractal\_dimension\_01 = 0.2027, fractal\_dimension\_02 = 0.06206, ⇒ radius\_03 / perimeter = [37.68, 75.36]

constraint rule 17 : perimeter = 13.45, radius\_01 = 18.3, radius\_02 = 86.6, radius\_04 = 0.1022, texture\_01 = 0.08165, texture\_02 = 0.03974, texture\_03 = 0.0278, texture\_04 = 0.1638, permeter = 0.0571, area\_01 = 0.295, area\_02 = 1.373, area\_03 = 2.099, smoothness\_01 = 25.22, smoothness\_02 = 0.005884, compactness\_01 = 0.01491, compactness\_02 = 0.01872, compactness\_03 = 0.009366, compactness\_04 = 0.01884, compactness\_05 = 0.001817, compactness\_06 = 15.1, concavity\_01 = 25.94, concavity\_02 = 97.59, concave\_points = 0.1339, symmetry\_01 = 0.1751, symmetry\_02 = 0.1381, symmetry\_03 = 0.07911, fractal\_dimension\_01 = 0.2678, fractal\_dimension\_02 = 0.06603,  $\Rightarrow$  radius\_03 = 0.00cavity\_03 / compactness\_06 = [28.15, 84.5]

constraint rule 18: perimeter = 8.196, radius\_01 = 16.84, radius\_02 = 51.71, radius\_04 = 0.086, texture\_01 = 0.05943, texture\_02 = 0.01588, texture\_03 = 0.005917, texture\_04 = 0.1769, permeter = 0.06503, area\_01 = 0.1563, area\_02 = 0.9567, area\_03 = 1.094, smoothness\_01 = 8.205, smoothness\_02 = 0.008968, compactness\_01 = 0.01646, compactness\_02 = 0.01588, compactness\_03 = 0.005917, compactness\_04 = 0.02574, compactness\_05 = 0.002582, compactness\_06 = 8.964, concavity\_01 = 21.96, concavity\_02 = 57.26,

concave\_points = 0.1297, symmetry\_01 = 0.1357, symmetry\_02 = 0.0688, symmetry\_03 = 0.02564, fractal\_dimension\_01 = 0.3105, fractal\_dimension\_02 = 0.07409,  $\Rightarrow$  radius 03 / perimeter = [61.01, 122.01] concavity 03 = 0

constraint rule 19 : perimeter = 9.173, radius\_01 = 13.86, radius\_02 = 59.2, radius\_03 = 260.9, radius\_04 = 0.07721, texture\_01 = 0.08751, texture\_02 = 0.05988, texture\_03 = 0.0218, texture\_04 = 0.2341, permeter = 0.06963, area\_01 = 0.4098, area\_02 = 2.265, area\_03 = 2.608, smoothness\_01 = 23.52, smoothness\_02 = 0.008738, compactness\_01 = 0.03938, compactness\_02 = 0.04312, compactness\_03 = 0.0156, compactness\_04 = 0.04192, compactness\_05 = 0.005822, compactness\_06 = 10.01, concavity\_01 = 19.23, concavity\_02 = 65.59, concave\_points = 0.09836, symmetry\_01 = 0.1678, symmetry\_02 = 0.1397, symmetry\_03 = 0.05087, fractal\_dimension\_01 = 0.3282, fractal\_dimension\_02 = 0.0849,  $\Rightarrow$  concavity\_03 / compactness\_06 = [42.46, 127.47]

constraint rule 20 : perimeter = 8.888, radius\_01 = 14.64, radius\_02 = 58.79, radius\_04 = 0.09783, texture\_01 = 0.1531, texture\_02 = 0.08606, texture\_03 = 0.02872, texture\_04 = 0.1902, permeter = 0.0898, area\_01 = 0.5262, area\_02 = 0.8522, area\_03 = 3.168, smoothness\_01 = 25.44, smoothness\_02 = 0.01721, compactness\_01 = 0.09368, compactness\_02 = 0.05671, compactness\_03 = 0.01766, compactness\_04 = 0.02541, compactness\_05 = 0.02193, compactness\_06 = 9.733, concavity\_01 = 15.67, concavity\_02 = 62.56, concave\_points = 0.1207, symmetry\_01 = 0.2436, symmetry\_02 = 0.1434, symmetry\_03 = 0.04786, fractal\_dimension\_01 = 0.2254, fractal\_dimension\_02 = 0.1084, area\_03 / perimeter = [56.26, 112.51] concavity\_03 = 0.04786, fractal\_dimension\_01 = 0.2254, fractal\_dimension\_02 = 0.1084, area\_03 / perimeter = [56.26, 112.51] concavity\_03 = 0.04786, fractal\_dimension\_01 = 0.2254, fractal\_dimension\_02 = 0.1084, area\_03 / perimeter = [56.26, 112.51] concavity\_03 = 0.04786, fractal\_dimension\_01 = 0.2254, fractal\_dimension\_02 = 0.1084, area\_01 = 0.02541, concavity\_03 = 0.04786, fractal\_dimension\_01 = 0.2254, fractal\_dimension\_02 = 0.1084, area\_02 = 0.04786, fractal\_dimension\_01 = 0.2254, fractal\_dimension\_02 = 0.1084, area\_03 / perimeter = [56.26, 112.51] concavity\_03 = 0.04786, fractal\_dimension\_01 = 0.2254, fractal\_dimension\_02 = 0.1084, area\_03 / perimeter = [56.26, 112.51] concavity\_03 = 0.04786, fractal\_dimension\_01 = 0.2254, fractal\_dimension\_02 = 0.1084, area\_03 / perimeter = [56.26, 112.51] concavity\_03 = 0.04786, fractal\_dimension\_01 = 0.2254, fractal\_dimension\_02 = 0.1084, area\_03 / perimeter = [56.26, 112.51] concavity\_03 = 0.04786, fractal\_dimension\_02 = 0.04786, fractal\_dimen

constraint rule 21 : perimeter = 12.31, radius\_01 = 16.52, radius\_02 = 79.19, radius\_03 = 470.9, radius\_04 = 0.09172, texture\_01 = 0.06829, texture\_02 = 0.03372, texture\_03 = 0.02272, texture\_04 = 0.172, permeter = 0.05914, area\_01 = 0.2505, area\_02 = 1.025, area\_03 = 1.74, smoothness\_01 = 19.68, smoothness\_02 = 0.004854, compactness\_01 = 0.01819, compactness\_02 = 0.01826, compactness\_03 = 0.004854, compactness\_01 = 0.01819, compactness\_02 = 0.01826, compactness\_03 = 0.004854, compactness\_01 = 0.01819, compactness\_02 = 0.01826, compactness\_03 = 0.004854, compactness\_01 = 0.01819, compactness\_02 = 0.01826, compactness\_03 = 0.004854, compactness\_01 = 0.01819, compactness\_02 = 0.01826, compactness\_03 = 0.004854, compactness\_01 = 0.01819, compactness\_02 = 0.01826, compactness\_03 = 0.004854, compactness\_01 = 0.01819, compactness\_02 = 0.01826, compactness\_03 = 0.004854, compactness\_01 = 0.01819, compactness\_02 = 0.01826, compactness\_03 = 0.004854, compactness\_01 = 0.01819, compactness\_02 = 0.01826, compactness\_03 = 0.004854, compactness\_01 = 0.01819, compactness\_02 = 0.01826, compactness\_03 = 0.004854, compactness\_01 = 0.01819, compactness\_01 = 0.018

constraint rule 22 : perimeter = 13.53, radius\_01 = 10.94, radius\_02 = 87.91, radius\_03 = 559.2, radius\_04 = 0.1291, texture\_01 = 0.1047, texture\_02 = 0.06877, texture\_03 = 0.06556, texture\_04 = 0.2403, permeter = 0.06641, area\_01 = 0.4101, area\_02 = 1.014, area\_03 = 2.652, smoothness\_01 = 32.65, smoothness\_02 = 0.0134, compactness\_01 = 0.02839, compactness\_02 = 0.01162, compactness\_03 = 0.008239, compactness\_04 = 0.02572, compactness\_05 = 0.006164, compactness\_06 = 14.08, concavity\_01 = 12.49, concavity\_02 = 91.36, concave\_points = 0.1451, symmetry\_01 = 0.1379, symmetry\_02 = 0.08539, symmetry\_03 = 0.07407, fractal\_dimension\_01 = 0.271, fractal\_dimension\_02 = 0.07191,  $\Rightarrow$  concavity\_03 / compactness\_06 = [30.18, 90.62]

constraint rule 23 : perimeter = 12.0, radius\_01 = 15.65, radius\_02 = 76.95, radius\_04 = 0.09723, texture\_01 = 0.07165, texture\_02 = 0.04151, texture\_03 = 0.01863, texture\_04 = 0.2079, permeter = 0.05968, area\_01 = 0.2271, area\_02 = 1.255, area\_03 = 1.441, smoothness\_01 = 16.16, smoothness\_02 = 0.005969, compactness\_01 = 0.01812, compactness\_02 = 0.02007, compactness\_03 = 0.007027, compactness\_04 = 0.01972, compactness\_05 = 0.002607, compactness\_06 = 13.67, concavity\_01 = 24.9, concavity\_02 = 87.78, concavity\_03 = 567.9, concave\_points = 0.1377, symmetry\_01 = 0.2003, symmetry\_02 = 0.2267, symmetry\_03 = 0.07632, fractal\_dimension\_01 = 0.3379, fractal\_dimension\_02 = 0.07924, \Rightarrow radius\_03 / perimeter = [41.67, 83.33]

**Lymphography dataset:** This is one of three domains provided by the Oncology Institute that has repeatedly appeared in the machine learning literature.

Data Set Characteristics:	Multivariate	Number of Instances:	5000	Area:	Life
Attribute Characteristics:	Categorical	Number of Attributes:	18	Date Donated	1988-11-01
Associated Tasks:	Classification	Anomaly ratio	0.0036	Number of Web Hits:	94762

# **Attribute Information:**

1. lymphatics: normal, arched, deformed, displaced

2. block of affere: no, yes

3. bl. of lymph. c: no, yes

4. bl. of lymph. s: no, yes

5. by pass: no, yes

6. extravasates: no, yes

7. regeneration of: no, yes

8. early uptake in: no, yes

9. lym.nodes dimin: 0-3

- 10. lym.nodes enlar: 1-4
- 11. changes in lym.: bean, oval, round
- 12. defect in node: no, lacunar, lac. marginal, lac. central
- 13. changes in node: no, lacunar, lac. margin, lac. central
- 14. changes in stru: no, grainy, drop-like, coarse, diluted, reticular, stripped, faint,
- 15. special forms: no, chalices, vesicles
- 16. dislocation of: no, yes
- 17. exclusion of no: no, yes
- 18. no. of nodes in: 0-9, 10-19, 20-29, 30-39, 40-49, 50-59, 60-69, >=70

### **Constraint rules for discovery:**

```
constraint rule 1: block of affere = 1, bl.of lymph.c = 1, bl.of lymph.s = 1, by_pass = 1, extravasates = 1, regeneration_of = 1, early_uptake_in = 1, lym.nodes_dimin = 1, lym.nodes_enlar = 1, changes_in_lym = 1, defect_in_node = 1, changes_in_node = 1, changes_in_stru = 1, special_forms = 1, dislocation_of = 1, exclusion_of_no = 1, no_of_nodes_in = 1, \implies lymphatics = 0.0 constraint rule 2: block of affere = 1, bl.of lymph.c = 1, bl.of lymph.s = 1, by_pass = 1, extravasates = 2, regeneration_of = 1, early_uptake_in = 2, lym.nodes_dimin = 1, lym.nodes_enlar = 2, changes_in_lym = 2, defect_in_node = 1, changes_in_node = 1,
```

```
changes_in_stru = 2, special_forms = 1, dislocation_of = 1, exclusion_of_no = 1, no_of_nodes_in = 2, \implies \text{ lymphatics} = 0.0

constraint rule 3: lymphatics = 3, block of affere = 2, bl.of lymph.c = 2, bl.of lymph.s = 2, by_pass = 2, extravasates = 2, regeneration_of = 2, early_uptake_in = 2, lym.nodes_dimin = 3, lym.nodes_enlar = 1, changes_in_lym = 1, defect_in_node = 2, changes_in_node = 2,

special_forms = 1, dislocation_of = 2, exclusion_of_no = 2, \implies \text{ changes_in_stru} = 2 \text{ no_of_nodes_in} = 0

constraint rule 4: lymphatics = 3, block of affere = 2, bl.of lymph.c = 2, bl.of lymph.s = 2, by_pass = 2, extravasates = 2, regeneration_of = 2, early_uptake_in = 1, lym.nodes_dimin = 2, lym.nodes_enlar = 2, changes_in_lym = 2, defect_in_node = 4, changes_in_node = 2,

special_forms = 3, dislocation_of = 2, exclusion_of_no = 2, no_of_nodes_in = 7, \implies \text{ changes_in_stru} = 0.0

constraint rule 5: lymphatics = 3, block of affere = 1, bl.of lymph.c = 1, bl.of lymph.s = 1, by_pass = 2, extravasates = 2, regeneration_of = 2, early_uptake_in = 1, lym.nodes_dimin = 3, lym.nodes_enlar = 1, changes_in_lym = 1, defect_in_node = 2, changes_in_node = 1,

special_forms = 3, dislocation_of = 1, exclusion_of_no = 1, \implies \text{ changes_in_lym} = 1, defect_in_node = 2, changes_in_node = 1,

special_forms = 3, dislocation_of = 1, exclusion_of_no = 1, \implies \text{ changes_in_lym} = 1, defect_in_node = 2, changes_in_node = 1,

special_forms = 3, dislocation_of = 1, exclusion_of_no = 1, \implies \text{ changes_in_lym} = 1, defect_in_node = 2, changes_in_node = 1,

special_forms = 3, dislocation_of_no = 1, exclusion_of_no = 1, \implies \text{ changes_in_lym} = 1, defect_in_node = 2, changes_in_node = 1,

special_forms = 3, dislocation_of_no_nodes_in_node = 1,

special_forms = 3, dislocation_of_nodes_in_node = 1,

special_forms_nodes_in_node_in_nodes_in_node = 1,

special_forms_nodes_in_node_in_node_in_node_in_node_in_node_in_node_in_node_in_node_in_node_in_node_in_node_in_node_in_node_in_node
```