# **Database Management Systems (COP 5725)**

(Fall 2019)

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## Homework 5

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Pledge (Must be signed according to UF Honor Code)

On my honor, I have neither given nor received unauthorized aid in doing this assignment.

	Weibin Sun	
Signature		

## For scoring use only:

	Maximum	Received
Exercise 1	20	
Exercise 2	25	
Exercise 3	25	
Exercise 4	15	
Exercise 5	15	
Total	100	

### **Exercise 1 - Normalization [20 points]**

Consider the following table which is used to store students and courses records.

UFID	Course_ID	Grade	Student_Name	Department	Tuition Fee	Instructor
4114123	COP01, COP02, COP03	А, А, В	John Smith	CISE	250	James, Andrew, Peter
3124234	BU01, BU02	В, В	Roger Hicks	Business	300	Alan, Alan

Please note that *Tuition Fee* depends on the department.

1. Normalize the table to the 1<sup>st</sup> Normal Form and explain your answer. [5 points]

A relation schema is in first normal form (1NF) if, and only if, the domains of all its attributes only contain atomic (or indivisible) values .

So, we need to change the intersection of each row and each column contains one and only one atomic value. The result is as follows:

<u>UFID</u>	Course_ID	Grade	Student_Name	Department	Tuition Fee	Instructor
4114123	COP01	A	John Smith	CISE	250	James
4114123	COP02	A	John Smith	CISE	250	Andrew
4114123	COP03	В	John Smith	CISE	250	Peter
3124234	BU01	В	Roger Hicks	Business	300	Alan
3124234	BU02	В	Roger Hicks	Business	300	Alan

2. Explain the criteria for 2<sup>nd</sup> Normal Form and normalize the table you obtained from the previous part to meet them. Then explain which anomalies can occur with your answer. [5 points]

A relation schema R is in the second normal form (2NF) with respect to a set F of FDs if, and only if, it is in 1NF and every nonprime attribute A in R is fully functionally dependent on every candidate key of R. In other words, it is in 1NF and for every candidate key K of R and for every nonprime attribute A in R the FD  $K \rightarrow A$  is left-reduced.

In the table of previous part, the primary keys are UFID and Course ID.

But for the FDs: UFID → Student\_Name, UFID → Department, UFID → Tuition Fee and Course\_ID → Instructor hold. So it's a violation of the 2NF.

students				
<u>UFID</u>	Student_Name	Department	Tuition Fee	
4114123	John Smith	CISE	250	
3124234	Roger Hicks	Business	300	

courses			
Course_ID	Instructor		
COP01	James		
COP02	Andrew		
COP03	Peter		
BU01	Alan		
BU02	Alan		

take_courses				
<u>UFID</u>	Course_ID	Grade		
4114123	COP01	A		
4114123	COP02	A		
4114123	COP03	В		
3124234	BU01	В		
3124234	BU02	В		

The 2NF still allows transitive dependencies.

#### Anomalies:

Insertion anomaly: Insert a new department should require a student information.

Update anomaly: If there are one more studnets in a department, a change of the department requires a change for each student in it.

Delete anomaly: If you delete a student's information, you should also delete the department's information.

3. Explain the criteria for 3<sup>rd</sup> Normal Form and normalize the table you obtained for the previous question to meet them. [5 points]

A relation schema R is in the third normal form (3NF) with respect to a set F of FDs if, and only if, it is in 2NF and no nonprime attribute A in R is transitively dependent on any candidate key of R. In other word, for each FD  $X \rightarrow Y$  in F+ with  $X \subseteq R$  and  $Y \subseteq R$  at least one of the following conditions holds:

- $X \rightarrow Y$  is a trivial FD (i.e.,  $Y \subseteq X$  holds), or
- X is a superkey of R, or
- Every element of Y X is a prime attribute (i.e., contained in some candidate key) of R

Relation schema  $student(\underline{UFID}, Student\_Name, Department, Tuition Fee)$  with the additional FD  $\{Department\} \rightarrow \{Tuition Fee\}$ ; both Department and Tuition Fee are nonprime attributes. Thus, we splitting of the schema student into the two 3NF schemas  $student(\underline{UFID}, Student\_Name, Department)$  and  $department\_fee(\underline{Department}, Tuition Fee)$  as follows.

student				
<u>UFID</u>	Student_Name	Department		
4114123	John Smith	CISE		
3124234	Roger Hicks	Business		

department_fee			
<u>Department</u>	Tuition Fee		
CISE	250		
Business	300		

courses			
Course_ID	Instructor		
COP01	James		
COP02	Andrew		
COP03	Peter		
BU01	Alan		
BU02	Alan		

take courses				
<u>UFID</u>	Course_ID	Grade		
4114123	COP01	A		
4114123	COP02	A		
4114123	COP03	В		
3124234	BU01	В		
3124234	BU02	В		

4. Explain if the tables you obtained for the previous question is in BCNF and, if not, normalize it to BCNF. [5 points]

Yes. Because for each left-reduced FD  $X \to Y$  in F+ with  $X \subseteq R$  and  $Y \subseteq R$ ,  $X \to Y$  is a trivial FD (i.e.,  $Y \subseteq X$  holds), or X is a candidate key of R, which satisfies the two conditions for the BCNF.

## Exercise 2 – Normal Forms [25 points]

Consider the relation schema R = (A, B, C, D, E) for the following questions.

- 1. Assume we have the following functional dependencies:
  - $AB \rightarrow C$
  - $C \rightarrow D$
  - $B \rightarrow E$

Briefly explain if the relation R is in 2NF. If not, what modifications can be made to normalize it into 2NF? [5 points]

No. Check the attributes that are not in the right-hand sides of F: AB.  $AB^+$  =ABCDE, which is candidate key. So the FDs  $\underline{AB} \rightarrow C$  holds. But the FDs: B  $\rightarrow$  E also hold, we know that attribute E is partially functionally dependent on AB. Therefore, R is not in 2NF.

In order to normalize it, we can divide R into two schema:

$$R1(A, B, C, D)$$
 with FDs:  $AB \rightarrow C, C \rightarrow D$ 

$$R2(\underline{B}, E)$$
 with FD:  $B \rightarrow E$ .

Both schemas satisfy the 2NF.

- 2. Is R in 2NF with the following functional dependencies? If not, normalize it. [5 points]
  - $A \rightarrow BC$
  - $AD \rightarrow E$
  - $B \rightarrow C$

No. Check the attributes that are not in the right-hand sides of F: AD. AD+ =ABCDE, so candidate key is AD. In particular the FDs AD  $\rightarrow$  E hold. But the FDs: A  $\rightarrow$  BC also hold, so BC is partially functionally dependent on any candidate key of R, which violates the 2NF.

In order to normalize, we can split R into two schema:

$$R1(A, B, C)$$
 with FDs:  $A \rightarrow BC, B \rightarrow C$ 

$$R2(A, D, E)$$
 with FD:  $AD \rightarrow E$ 

Both schemas satisfy the 2NF.

3. Are the relations from the answer of question 2 in 3NF? If not, normalize it. [5 points]

No. Relation schema R1( $\underline{A}$ , B, C) with the FDs: A  $\rightarrow$  BC and B  $\rightarrow$ C hold, but B and C are nonprime attributes. Thus it not satisfies 3NF.

In order to normalize it, we can split R1(A, B, C) into two schema:

$$R11(\underline{A}, B)$$
 with FD:  $A \rightarrow B$ 

$$R12(\underline{B}, C)$$
 with FD:  $B \rightarrow C$ 

$$R2(A, D, E)$$
 with FD:  $AD \rightarrow E$ 

Therefore, (ADE), (AB), (BC) form 3NF.

- 4. Briefly explain if the relation R is in 2NF. [2 points].
  - $A \rightarrow BCDE$
  - $BC \rightarrow ADE$
  - $D \rightarrow E$

Further, is R in 3NF? If not, what modifications can be made to normalize it into 3NF? [3 points]

Answer:

It is 2NF. By using the Armstrong's Axioms, we can get **A**+=ABCDE, B+=B, C+=C, D+=DE, E+=E, **BC**+=ABCDE, BD+=BDE, BE+=BE, CD+=CDE, CE+=CE, DE+=DE. So, the candidate keys are A and BC.

A is a key of single attribute, so it satisfies the 2NF. For BC, since we can compute that  $B^+ = B$  and  $C^+ = C$ , we cannot find a partial functional dependency. Therefore, R is in 2NF.

It is not 3NF. Because the FD:  $D \rightarrow E$  hold, we can compute that  $D^+ = DE$ , and D is not a candidate key. Thus, it violates 3NF.

To because 3NF, we can split R(A, B, C, D, E) into two schema:

 $R1(\underline{A}, B, C, D)$  with FDs:  $A \rightarrow BCD, BC \rightarrow AD$ 

 $R2(\underline{D}, E)$  with FD:  $D \rightarrow E$ 

- 5. Assume we have the following functional dependencies:
  - $AB \rightarrow D$
  - $C \rightarrow E$
  - $E \rightarrow C$
  - $C \rightarrow A$
  - $A \rightarrow C$

We decompose R into schemas R1(ABC) and R2(ABDE). Show whether it is dependency preserving by using one of the algorithms that covered in the lecture. [5 points]

Using algorithm 2:

For  $AB \rightarrow D$ : Result = AB

Round 1: OldResult = AB

For R1(ABC),  $C = CalculateAttributeClosure(F, AB) \cap R1 = ABC$ 

Result = ABC

For R2(ABDE), C = CalculateAttributeClosure(F, AB)  $\cap$  R2 = ABDE

Result =  $ABCDE \neq OldResult$ 

Round 2: OldResult = ABCDE

For R1(ABC),  $C = CalculateAttributeClosure(F, ABC) \cap R1 = ABC$ 

Result = ABCDE

For R2(ABDE), C = ClaculateAttributeClosure(F, ABDE)  $\cap$  R2 = ABDE

Result = ABCDE = OldResult

 $D \cap Result = D$ 

```
For C \rightarrow E: Result = C
```

Round 1: OldResult = C

For R1(ABC),  $C = CalculateAttributeClosure(F, C) \cap R1 = AC$ 

Result = AC

For R2(ABDE), C = CalculateAttributeClosure(F, A)  $\cap$  R2 = AE

 $Result = ACE \neq OldResult$ 

Round 2: OldResult = ACE

For R1(ABC),  $C = CalculateAttributeClosure(F, AC) \cap R1 = AC$ 

Result = ACE

For R2(ABDE),  $C = CalculateAttributeClosure(F, AE) \cap R2 = AE$ 

Result = ACE = OldResult

 $E \cap Result = E$ 

For  $E \rightarrow C$ : Result = E

Round 1: OldResult = E

For R1(ABC), C = CalculateAttributeClosure(F,  $\emptyset$ )  $\cap$  R1 =  $\emptyset$ 

Result = E

For R2(ABDE),  $C = CalculateAttributeClosure(F, E) \cap R2 = AE$ 

Result =  $AE \neq OldResult$ 

Round 2: OldResult = AE

For R1(ABC),  $C = CalculateAttributeClosure(F, A) \cap R1 = AC$ 

Result = ACE

For R2(ABDE), C = ClaculateAttributeClosure(F, AE)  $\cap$  R2 = AE

Result =  $ACE \neq OldResult$ 

Round 3: OldResult = ACE

For R1(ABC),  $C = CalculateAttributeClosure(F, AC) \cap R1 = AC$ 

Result = ACE

For R2(ABDE), C = ClaculateAttributeClosure(F, AE)  $\cap$  R2 = AE

Result = ACE = OldResult

 $C \cap Result = C$ 

For  $C \rightarrow A$ : Result = C

Round 1: OldResult = C

For R1(ABC),  $C = CalculateAttributeClosure(F, C) \cap R1 = AC$ 

Result = AC

For R2(ABDE),  $C = CalculateAttributeClosure(F, A) \cap R2 = AE$ 

Result =  $ACE \neq OldResult$ 

Round 2: OldResult = ACE

For R1(ABC),  $C = CalculateAttributeClosure(F, AC) \cap R1 = AC$ 

Result = ACE

For R2(ABDE),  $C = ClaculateAttributeClosure(F, AE) \cap R2 = AE$ 

Result = ACE = OldResult

 $A \cap Result = A$ 

For  $A \rightarrow C$ : OldResult = A

Round 1: OldResult = A

For R1(ABC),  $C = CalculateAttributeClosure(F, A) \cap R1 = AC$ 

Result = AC

For R2(ABDE),  $C = CalculateAttributeClosure(F, A) \cap R2 = AE$ 

Result =  $ACE \neq OldResult$ 

Round 2: OldResult = ACE

For R1(ABC),  $C = CalculateAttributeClosure(F, AC) \cap R1 = AC$ 

Result = ACE

For R2(ABDE),  $C = ClaculateAttributeClosure(F, AE) \cap R2 = AE$ 

Result = ACE = OldResult

 $C \cap Result = C$ 

Therefore, it is dependency preserving.

## Exercise 3 – Lossless Join Decomposition [25 points]

1. For the relation schema R = (ABCDEF) and functional dependencies F = {AB → C, AC → B, AD → E, B → D, BC → A, E → F}, determine whether the following decomposition is lossless. Also, determine if it is dependency preserving.

 $P = \{R1(AB), R2(BC), R3(ABDE), R4(EF)\} [10 points]$ 

#### Apply the chase test:

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A	В	С	D	Е	F
a	ь	c1	d1	e1	f1
a2	ь	c	d2	e2	f2
a	ь	c3	d	e	f3
a4	b4	c4	d4	e	f

#### Apply $AB \rightarrow C$ :

A	В	C	D	Е	F
a	ь	c1	d1	e1	f1
a2	ь	c	d2	e2	f2
a	ь	c1	d	e	f3
a4	b4	c4	d4	e	f

#### Apply $AC \rightarrow B$ :

A	В	С	D	E	F
a	ь	c1	d1	e1	f1
a2	ь	c	d2	e2	f2
a	ь	c1	d	e	f3
a4	b4	c4	d4	e	f

# Apply $AD \rightarrow E$ :

A	В	С	D	Е	F
a	ь	c1	d1	e1	f1
a2	ь	c	d2	e2	f2
a	ь	c1	d	e	f3
a4	b4	c4	d4	e	f

#### Apply $B \rightarrow D$ :

A	В	С	D	Е	F
a	ь	c1	d	e1	f1
a2	ь	c	d	e2	f2
a	ь	c1	d	e	f3
a4	b4	c4	d4	e	f

#### Apply BC $\rightarrow$ A:

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A	В	C	D	E	F
a	ь	c1	d	e1	f1
a2	ь	c	d	e2	f2
a	ь	c1	d	e	f3
a4	b4	c4	d4	e	f

Apply  $E \rightarrow F$ :

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A	В	C	D	E	F
a	ь	c1	d	e1	f1
a2	ь	c	d	e2	f2
a	ь	c1	d	e	f
a4	b4	c4	d4	e	f

Apply  $AD \rightarrow E$ :

A	В	С	D	Е	F
a	ь	c1	d	e	f1
a2	b	c	d	e2	f2
a	ь	c1	d	e	f
a4	b4	c4	d4	e	f

We cannot find 1 row with all unsubscripted variables, so it is not a lossless decomposition.

We can check the FD:  $AB \rightarrow C$ ,  $AC \rightarrow B$  and  $BC \rightarrow A$  are not fit into any relations, so it is not dependency preserving.

#### 2. Consider the relation schema R = (ABCDE).

a. For the functional dependencies  $F = \{AB \rightarrow C, C \rightarrow E, B \rightarrow D, E \rightarrow A\}$ , is P  $\{R1 (BCD), R2 (ACE)\}$  a lossless decomposition? Show all the steps. [5 points]

Using the chase test:

A	В	С	D	Е
a1	ь	c	d	e1
a	b2	c	d2	e

Apply  $AB \rightarrow C$ :

A	В	С	D	E
al	ь	c	d	e1
a	b2	c	d2	e

Apply  $C \rightarrow E$ :

A	В	С	D	Е
al	ь	c	d	e
a	b2	С	d2	e

Apply  $B \rightarrow D$ :

A	В	C	D	E
al	ь	c	d	e
a	b2	c	d2	e

Apply  $E \rightarrow A$ :

A	В	С	D	E
a	ь	c	d	e
a	b2	c	d2	e

The first row is fully unsubscripted, so it is a lossless decomposition.

b. For the functional dependencies  $F = \{A \rightarrow CD, B \rightarrow CE, E \rightarrow B\}$ , give a lossless-join decomposition of R into BCNF. [5 points]

Step 1: Decomposition by  $A \rightarrow CD$ . R1 = (A, B, E), R2 = (A, C, D).

Step 2: Decomposition of R1 by  $E \rightarrow B$ . R11 = (A, E), R12 = (B, E).

Thus, (A, E), (B, E) and (A, C, D) form a decomposition into BCNF.

c. For the functional dependencies  $F = \{A \rightarrow CD, B \rightarrow CE, E \rightarrow B\}$ , give a lossless-join decomposition of R into 3NF preserving functional dependencies. [5 points]

Step 1: Computation of a minimal cover: The given FDs are already the minimal cover

Step 2: Generation of relation schemas from the FDs

From A  $\rightarrow$  CD, we obtain:  $R_1 = (A, C, D), F_1 = \{A \rightarrow CD\}$ 

From B  $\rightarrow$  CE, we obtain:  $R_2 = (B, C, E), F_2 = \{B \rightarrow CE, E \rightarrow B\}$ 

From  $E \to B$ , we obtain:  $R_3 = (B, E)$ ,  $F_3 = \{E \to B\}$ , but E, B are in R2.

Step 3: Check if a relation schema contains a candidate key

The candidate keys are AB and AE. There is no relation has a candidate key, so we add  $R_4 = (A, B)$ .

Step 4: We can have that  $R_3 \subseteq R_2$ 

Step 5: So we have the decomposition  $R_1 = ACD$ ,  $R_2 = BCE$ ,  $R_3 = AB$ .

Therefore, (A, C, D), (B, C, E), (A, B) can form BCNF.

### **Exercise 4 - Normalization [15 points]**

Suppose we have a relation schema R(A, B, C, D, E, F, G) and a set of functional dependencies  $F = \{BCD \rightarrow A, BC \rightarrow E, A \rightarrow F, F \rightarrow G, C \rightarrow D, A \rightarrow G, A \rightarrow B\}$ . Decompose R into 3NF by using the 3NF synthesis algorithm. Show all steps and argue precisely. Is this decomposition also in BCNF? If so, why? If not, why not? [15 points]

Step 1: Computation of a minimal cover:  $\{BC \rightarrow AE, A \rightarrow BF, F \rightarrow G, C \rightarrow D\}$ 

Step 2: Generation of relation schemas from the FDs

From BC  $\rightarrow$  AE, we obtain: R1 = ABCE, F1 = {BC  $\rightarrow$  AE, A  $\rightarrow$  B}

From A  $\rightarrow$  BF, we obtain: R2 = ABF, F2 = {A  $\rightarrow$  BF}

From  $F \rightarrow G$ , we obtain R3 = FG, F3 =  $\{F \rightarrow G\}$ 

From  $C \rightarrow D$ , we obtain R4 = CD,  $F4 = \{C \rightarrow D\}$ 

Step 3: Check if a relation schema contains a candidate key

The candidate keys are AC and BC, and the R1 contains AC and BC. Therefore, we don't need to add extra schemas.

Step 4: So we have the decomposition R1 = ABCE, R2 = ABF, R3 = FG, R4 = CD.

The decomposition is not in BCNF, since for R1 = ABCE, the FD A  $\rightarrow$  B holds, but A is not a superkey.

## **Exercise 5 – Integrity Constraints [15 points]**

Consider the following tables:

```
CREATE TABLE PRODUCT
(MAKER VARCHAR2 (50),
MODEL VARCHAR2(50),
TYPE VARCHAR2(30));
CREATE TABLE DESKTOP
(MODEL VARCHAR2 (50) NOT NULL,
SPEED NUMBER (8),
RAM VARCHAR2 (30),
HD VARCHAR2 (30),
PRICE NUMBER(8));
CREATE TABLE LAPTOP
(MODEL VARCHAR2 (50) NOT NULL,
SPEED NUMBER(8),
RAM VARCHAR2 (30),
HD VARCHAR2(30),
SCREEN VARCHAR2 (30),
PRICE NUMBER(8));
CREATE PRINTER
(MODEL VARCHAR2 (50) NOT NULL,
COLOR VARCHAR2 (30),
TYPE VARCHAR2 (30),
PRICE NUMBER(8));
```

1. Write a check condition to ensure that no manufacturer of desktops also makes laptops. [3 points]

2. Write a check condition to ensure that a manufacturer of a desktop also makes a laptop with at least the same processor speed. [4 points]

```
Create assertion speed_constraint
check (
Not Exists (
Select x.maker
From (Select product.maker, desktop.speed
From product, desktop
Where product.model = desktop.model) x,
(select product.maker, laptop.speed
From product, laptop
Where product.model = laptop.model) y
Where x.maker = y.maker and x.speed > y.speed));
```

3. Create a trigger that checks that there is no lower priced desktop with the same speed when the price of a desktop is updated. [4points]

4. Create a trigger that checks if the model number exists in the *Product* table when a new printer is inserted. [4 points]