## Astro2020 Science White Paper

# Messengers from the Early Universe: Cosmic Neutrinos and Other Light Relics

Thematic Area: Cosmology and Fundamental Physics

**Principal Author:**Name: Daniel Green

Institution: University of California San Diego

Email: drgreen@physics.ucsd.edu

Abstract: The hot dense environment of the early universe is known to have produced large numbers of baryons, photons, and neutrinos. These extreme conditions may have also produced other long-lived species, including new light particles (such as axions or sterile neutrinos) or gravitational waves. The gravitational effects of any such light relics can be observed through their unique imprint in the cosmic microwave background (CMB), the large-scale structure, and the primordial light element abundances, and are important in determining the initial conditions of the universe. We argue that future cosmological observations, in particular improved maps of the CMB on small angular scales, can be orders of magnitude more sensitive for probing the thermal history of the early universe than current experiments. These observations offer a unique and broad discovery space for new physics in the dark sector and beyond, even when its effects would not be visible in terrestrial experiments or in astrophysical environments. A detection of an excess light relic abundance would be a clear indication of new physics and would provide the first direct information about the universe between the times of reheating and neutrino decoupling one second later.

Co-authors\*: Mustafa A. Amin<sup>1</sup>, Joel Meyers<sup>2</sup>, Benjamin Wallisch<sup>3,4</sup>, Kevork N. Abazajian<sup>5</sup>, Muntazir Abidi<sup>6</sup>, Peter Adshead<sup>7</sup>, Zeeshan Ahmed<sup>8</sup>, Behzad Ansarinejad<sup>9</sup>, Robert Armstrong<sup>10</sup>, Carlo Baccigalupi<sup>11,12,13</sup>, Kevin Bandura<sup>14,15</sup>, Darcy Barron<sup>16</sup>, Nicholas Battaglia<sup>17</sup>, Daniel Baumann<sup>18,19</sup>, Keith Bechtol<sup>20</sup>, Charles Bennett<sup>21</sup>, Bradford Benson<sup>22,23</sup>, Florian Beutler<sup>24</sup>, Colin Bischoff<sup>25</sup>, Lindsey Bleem<sup>26,23</sup>, J. Richard Bond<sup>27</sup>, Julian Borrill<sup>28</sup>, Elizabeth Buckley-Geer<sup>22</sup>, Cliff Burgess<sup>29</sup>, John E. Carlstrom<sup>30,23,26</sup>, Emanuele Castorina<sup>31</sup>, Anthony Challinor<sup>32,6,33</sup>, Xingang Chen<sup>34</sup>, Asantha Cooray<sup>5</sup>, William Coulton<sup>32,33</sup>, Nathaniel Craig<sup>35</sup>, Thomas Crawford<sup>30,23</sup>, Francis-Yan Cyr-Racine<sup>36,16</sup>, Guido D'Amico<sup>37</sup>, Marcel Demarteau<sup>26</sup>, Olivier Doré<sup>38</sup>, Duan Yutong<sup>39</sup>, Joanna Dunkley<sup>40</sup>, Cora Dvorkin<sup>36</sup>, John Ellison<sup>41</sup>, Alexander van Engelen<sup>27</sup>, Stephanie Escoffier<sup>42</sup>, Tom Essinger-Hileman<sup>43</sup>, Giulio Fabbian<sup>44</sup>, Jeffrey Filippini<sup>7</sup>, Raphael Flauger<sup>4</sup>, Simon Foreman<sup>27</sup>, George Fuller<sup>4</sup>, Marcos A. G. Garcia<sup>1</sup>, Juan García-Bellido<sup>45</sup>, Martina Gerbino<sup>26</sup>, Vera Gluscevic<sup>46</sup>, Satya Gontcho A Gontcho<sup>47</sup>, Krzysztof M. Górski<sup>38</sup>, Daniel Grin<sup>48</sup>, Evan Grohs<sup>31</sup>, Jon E. Gudmundsson<sup>49</sup>, Shaul Hanany<sup>50</sup>, Will Handley<sup>33,51</sup>, J. Colin Hill<sup>3,52</sup>, Christopher M. Hirata<sup>53</sup>, Renée Hložek<sup>54,55</sup>, Gilbert Holder<sup>7</sup>, Shunsaku Horiuchi<sup>56</sup>, Dragan Huterer<sup>57</sup>, Kenji Kadota<sup>58</sup>, Marc Kamionkowski<sup>21</sup>, Ryan E. Keeley<sup>59</sup>, Rishi Khatri<sup>60</sup>, Theodore Kisner<sup>28</sup>, Jean-Paul Kneib<sup>61</sup>, Lloyd Knox<sup>62</sup>, Savvas M. Koushiappas<sup>63</sup>, Ely D. Kovetz<sup>64</sup>, Benjamin L'Huillier<sup>59</sup>, Ofer Lahav<sup>65</sup>, Massimiliano Lattanzi<sup>66</sup>, Hayden Lee<sup>36</sup>, Michele Liguori<sup>67</sup>, Tongyan Lin<sup>4</sup>, Marilena Loverde<sup>68</sup>, Mathew Madhavacheril<sup>40</sup>, Kiyoshi Masui<sup>69</sup>, Jeff McMahon<sup>57</sup>, Matthew McQuinn<sup>70</sup>, P. Daniel Meerburg<sup>33,6,71</sup>, Mehrdad Mirbabayi<sup>72</sup>, Pavel Motloch<sup>27</sup>, Suvodip Mukherjee<sup>73</sup>, Julian B. Munõz<sup>36</sup>, Johanna Nagy<sup>54</sup>, Laura Newburgh<sup>74</sup>, Michael D. Niemack<sup>17</sup>, Andrei Nomerotski<sup>75</sup>, Lyman Page<sup>40</sup>, Francesco Piacentni<sup>76,77</sup>, Elena Pierpaoli<sup>78</sup>, Levon Pogosian<sup>79</sup>, Clement Pryke<sup>50</sup>, Giuseppe Puglisi<sup>37,80</sup>, Radek Stompor<sup>81</sup>, Marco Raveri<sup>23,30</sup>, Christian L. Reichardt<sup>82</sup>, Benjamin Rose<sup>83</sup>, Graziano Rossi<sup>84</sup>, John Ruhl<sup>85</sup>, Emmanuel Schaan<sup>28,31</sup>, Michael Schubnell<sup>57</sup>, Katelin Schutz<sup>86</sup>, Neelima Sehgal<sup>68</sup>, Leonardo Senatore<sup>80</sup>, Hee-Jong Seo<sup>87</sup>, Blake D. Sherwin<sup>6,33</sup>, Sara Simon<sup>57</sup>, Anže Slosar<sup>75</sup>, Suzanne Staggs<sup>40</sup>, Albert Stebbins<sup>22</sup>, Aritoki Suzuki<sup>28</sup>, Eric R. Switzer<sup>43</sup>, Peter Timbie<sup>20</sup>, Matthieu Tristram<sup>88</sup>, Mark Trodden<sup>89</sup>, Yu-Dai Tsai<sup>22</sup>, Caterina Umiltà<sup>25</sup>, Eleonora Di Valentino<sup>90</sup>, M. Vargas-Magaña<sup>91</sup>, Abigail Vieregg<sup>30</sup>, Scott Watson<sup>92</sup>, Thomas Weiler<sup>93</sup>, Nathan Whitehorn<sup>94</sup>, W. L. K. Wu<sup>23</sup>, Weishuang Xu<sup>36</sup>, Zhilei Xu<sup>89</sup>, Siavash Yasini<sup>78</sup>, Matias Zaldarriaga<sup>3</sup>, Gong-Bo Zhao<sup>95,24</sup>, Ningfeng Zhu<sup>89</sup>, Joe Zuntz<sup>96</sup>

<sup>\*</sup>The list of affiliations can be found in the Appendix.

#### 1 Introduction

Cosmology unites the study of the fundamental laws of particle physics, the history of the universe, the origin of its structure, and its subsequent dynamics. The abundances of baryons, photons, neutrinos, and (possibly) dark matter were determined during the hot thermal phase that dominated the early universe. It is the abundances of these particles and the forces between them that determine the conditions of the cosmos that we see today.

There is strong motivation to determine if other forms of radiation (i.e. relativistic species), including gravitational waves, were produced during the hot big bang. Changes to the radiation density make a measurable impact on cosmological observables, including the amplitude of clustering, the scale of the baryon acoustic oscillations (BAOs), and primordial light element abundances. An accurate measurement of the total radiation density is therefore also crucial in order to calibrate late-time observables, such as the BAO scale or the lensing amplitude.

New sources of (dark) radiation are well motivated by both particle physics and cosmology (cf. e.g. [1–3]). New light particles are predicted in many extensions of the Standard Model (SM), including axions and sterile neutrinos, or can arise as a consequence of solving the hierarchy problem (see e.g. [1–22]). For large regions of unexplored parameter space, these light particles are thermalized in the early universe and lead to additional radiation at later times. Light species are ubiquitous in models of the late universe as well: they may form the dark matter (e.g. axions), be an essential ingredient of a more complicated dark sector as the force carrier between dark matter and the Standard Model (or itself), or provide a source of dark radiation for a dark thermal history. Furthermore, these new particles could also play a role in explaining discrepancies in the measurements of the Hubble constant  $H_0$  [23–27], the amplitude of large-scale matter fluctuations  $\sigma_8$  [28–31], and the properties of clustering on small scales [32,33]. Measuring the total radiation density is a broad window into all these possibilities as well as additional scenarios that we have yet to consider.

Remarkably, cosmological observations provide an increasingly sharp view of the radiation content of the universe. The cosmic neutrino background itself is a compelling example: while it has not been possible to see cosmic neutrinos in the lab, their presence has been observed at high significance in the cosmic microwave background (CMB) and through observations of light element abundances [33, 34]. These indirect measurements of the cosmic neutrino background therefore provide a window back to a few seconds after the big bang, the era of neutrino decoupling. A new thermalized light particle adds at least a percent-level correction to the radiation density that is determined by its decoupling temperature (time). Measurements in the coming decade will be sensitive to decoupling temperatures that are orders of magnitude higher than current experiments, and able to reveal new physics that will be inaccessible in any other setting.

### 2 Light Relics of the Big Bang

#### Cosmic Neutrino Background

The cosmic neutrino background is one of the remarkable predictions of the hot big bang. In the very early universe, neutrinos were kept in thermal equilibrium with the Standard Model plasma. As the universe cooled, neutrinos decoupled from the plasma. A short time later, the relative number density and temperature in photons increased, due primarily to the transfer of entropy from electron-positron pairs to photons. The background of cosmic neutrinos persists today, with a temperature and number density similar to that of the CMB. Their energy density  $\rho_{\nu}$  is most

commonly expressed in terms of the effective number of neutrino species,

$$N_{\rm eff} = \frac{8}{7} \left(\frac{11}{4}\right)^{4/3} \frac{\rho_{\nu}}{\rho_{\gamma}},\tag{1}$$

where  $\rho_{\gamma}$  is the energy density in photons. This definition is chosen so that  $N_{\rm eff}=3$  in the SM if neutrinos had decoupled instantaneously prior to electron-positron annihilation. The neutrino density  $\rho_{\nu}$  receives a number of corrections from this simple picture of decoupling, and the best available calculations give  $N_{\rm eff}^{\rm SM}=3.045$  in the SM [35–37].

Cosmology is sensitive to the gravitational effects of neutrinos, both through their mean energy density [38–41] and their fluctuations, which propagate at the speed of light in the early universe due to the free-streaming nature of neutrinos [41–43]. A radiation fluid whose fluctuations do not exceed the sound speed of the plasma [44,45] could arise from large neutrino self-interactions [46,47], neutrino-dark sector interactions, or dark radiation self-coupling. Such a radiation fluid can be observationally distinguished from free-streaming radiation, and can serve as both a foil for the cosmic neutrino background and a test of new physics in the neutrino and dark sectors [42,48,49].

Neutrinos are messengers from a few seconds after the big bang and provide a new window into our cosmological history. While these relics have been detected in cosmological data, higher precision measurements would advance the use of neutrinos as a cosmological probe. Furthermore, the robust measurement of the neutrino abundance from the CMB is crucial for inferring cosmic parameters, including the expansion history using BAOs [50], the neutrino masses [51], and  $H_0$  [27].

#### **Beyond the Standard Model**

A measurement of the value of  $N_{\text{eff}}$  provides vastly more information than just the energy density in cosmic neutrinos. The parameter  $N_{\text{eff}}$  is a probe of any particles that have the same gravitational influence as relativistic neutrinos, which is true of any (free-streaming) radiation. Furthermore, this radiation could have been created at much earlier times when the energy densities were even higher than in the cores of stars or supernovae, shedding light on the physics at new extremes of temperatures as well as densities, and our early cosmic history.

New light particles that were thermally produced in the early universe contribute to the neutrino density  $\rho_V$  and increase  $N_{\rm eff}$  above the amount from neutrinos alone. The presence of any additional species can therefore be characterized by  $\Delta N_{\rm eff} \equiv N_{\rm eff} - N_{\rm eff}^{\rm SM}$ . Since all such thermalized particles behave in the same way from a cosmological point of view, this parametrization captures a vast range of new physics: axions, sterile neutrinos, dark sectors, and beyond [13, 18, 52, 53].

Constraints on  $N_{\rm eff}$  are broadly useful and, most importantly, allow the exploration of new and interesting territory in a variety of well-motivated models. This can be seen with a simple example: dark matter-baryon scattering. For low-mass (sub-GeV) dark matter, current data allows for relatively large scattering cross sections [54]. If they scatter through a Yukawa potential, which is a force mediated by a scalar particle, this force is consistent with fifth-force experiments and stellar cooling if the mediator has a mass around 200 keV. However, the particle which mediates the force necessarily  $^{\dagger}$  contributes  $\Delta N_{\rm eff} \geq 0.09$  when it comes into thermal equilibrium with the Standard Model [55]. Excluding this value would require that the strength of the interactions is small enough to prevent the particle from reaching equilibrium at any point in the history of the universe, which, consequently, limits the scattering cross section, as shown in the left panel of Fig. 1.

<sup>&</sup>lt;sup>†</sup>The mediator with a mass of 200 keV is too heavy to contribute to  $N_{\rm eff}$ , but it must decay to sub-eV mass particles, which will increase  $N_{\rm eff}$ , in order to avoid more stringent constraints.

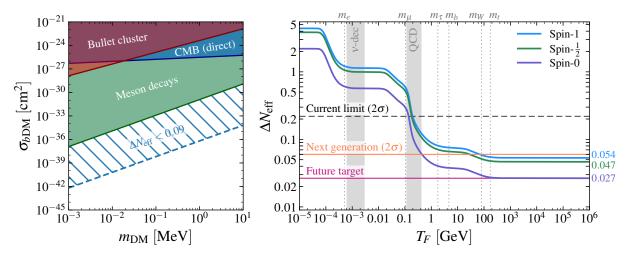


Figure 1: Left: Limits on the dark matter-baryon cross section  $\sigma_{b\mathrm{DM}}$  for a Yukawa potential. Future cosmological constraints will restrict  $\Delta N_{\mathrm{eff}} < 0.09$  and, therefore, exclude cross sections large enough to thermalize the (200 keV-mass) particle mediating the force [55]. This limit is compared to the direct bound on baryon-dark matter scattering from the CMB [57] and to the constraints on dark forces from the Bullet Cluster [58]. The strongest current constraint is from the absence of meson decays to the mediator [59]. Right: Contributions of a single massless particle, which decoupled at the temperature  $T_F$  from the Standard Model, to the effective number of relativistic species,  $N_{\mathrm{eff}} = N_{\mathrm{eff}}^{\mathrm{SM}} + \Delta N_{\mathrm{eff}}$ , with the Standard Model expectation  $N_{\mathrm{eff}}^{\mathrm{SM}} = 3.045$  from neutrinos. The limit at 95% c.l. from a combination of current CMB, BAO and BBN observations [33], and the anticipated sensitivity of next-generation CMB experiments (cf. e.g. [53, 60, 61]) illustrate the current and future power of cosmological surveys to constrain light thermal relics. The displayed values on the right are the observational thresholds for particles with different spins and arbitrarily large decoupling temperature.

This measurement is sensitive to 10–15 orders of magnitude in cross section that are not probed by direct constraints from cosmology and astrophysics, and five orders of magnitude stronger than meson decay searches. We see that cosmological measurements of  $\Delta N_{\rm eff}$  are an extremely sensitive probe of dark sector physics that are complementary to more direct tests, both in the laboratory and with astrophysical observations [55, 56].

More generally, the contribution to  $N_{\rm eff}$  from any thermalized new particle is easy to predict because its energy density in equilibrium is fixed by the temperature and the number of internal states (e.g. spin configurations). Under mild assumptions (see e.g. [62] for a detailed discussion), the contribution to  $\Delta N_{\rm eff}$  is determined by two numbers, the last temperature at which it was in equilibrium,  $T_F$ , and the effective number of spin degrees of freedom,  $g_s$ , according to

$$\Delta N_{\text{eff}} = g_s \left(\frac{43/4}{g_{\star}(T_F)}\right)^{4/3}.$$
 (2)

The function  $g_{\star}(T_F)$  is the number of effective degrees of freedom (defined as the number of independent states with an additional factor of 7/8 for fermions) of the SM particle content at the temperature  $T_F$ . This function appears in the formula for  $\Delta N_{\rm eff}$  because it determines how much the photons are heated relative to a new light particle due to the annihilation of the heavy SM particles as the universe cooled (see the right panel of Fig. 1). The next generation of (proposed) CMB observations are expected to reach a precision of  $\sigma(N_{\rm eff}) = 0.03$ , which would extend our reach in  $T_F$  by several orders of magnitude for a particle with spin s > 0 and be the first measurement sensitive to a real scalar (s = 0) that decouples prior to the QCD phase transition.

To understand the impact of such a measurement, recall that equilibrium at temperature T arises

when the production rate  $\Gamma$  is much larger than the expansion rate H(T). At high temperatures, production is usually fixed by dimensional analysis,  $\Gamma \propto \lambda^2 T^{2n+1}$ , where  $\lambda$  is the coupling to the Standard Model with units of  $[\text{Energy}]^{-n}$ . The particle is therefore in equilibrium if  $\lambda^2 \gg M_{\rm P}^{-1} T^{-2n+1}$ . There are two important features of this formula: (i) the appearance of the Planck scale  $M_{\rm P}$  implies we are sensitive to very weak couplings ( $M_{\rm P}^{-2} = 8\pi G_N$ ), and (ii) for  $n \ge 1$  it scales like an inverse power of T. As a result, sensitivity to increasingly large  $T_F$  implies that we are probing increasingly weak couplings (lower production rates) in proportion to the improvement in  $T_F$  (not  $\Delta N_{\rm eff}$ ). These two features explain why future measurements of  $\Delta N_{\rm eff}$  can be orders of magnitude more sensitive than terrestrial and astrophysical probes of the same physics [18,53].

The impact of the coming generation of observations is illustrated in Fig. 1. Anticipated improvement in measurements of  $N_{\rm eff}$  translate into orders of magnitude in sensitivity to the temperature  $T_F$ . This temperature sets the reach in probing fundamental physics. Even in the absence of a detection, future cosmological probes would place constraints that can be orders of magnitude stronger than current probes of the same physics, including for axion-like particles [18] and dark sectors [21, 22, 55, 63]. It is also worth noting that these contributions to  $N_{\rm eff}$  asymptote to specific values of  $\Delta N_{\rm eff} = 0.027, 0.047, 0.054$  for a massless (real) spin-0 scalar, spin-1/2 (Weyl) fermion and spin-1 vector boson, respectively (see Fig. 1). A cosmological probe with sensitivity to  $\Delta N_{\rm eff}$  at these levels would *probe physics back to the time of reheating for even a single additional species*.

Even without new light particles,  $N_{\text{eff}}$  is a probe of new physics that changes our thermal history, including processes that result in a stochastic background of gravitational waves [64–66]. Violent phase transitions and other nonlinear dynamics in the primordial universe could produce such a background, peaked at frequencies much larger than those accessible to B-mode polarization measurements of the CMB or, in many cases, direct detection experiments such as LIGO and LISA [67–71]. For particularly violent sources, the energy density in gravitational waves can be large enough to make a measurable contribution to  $N_{\text{eff}}$  [71–73].

In addition to precise constraints on  $N_{\rm eff}$ , cosmological probes will provide an *independent high-precision measurement of the primordial helium abundance*  $Y_{\rm p}$  due to the impact of helium on the free electron density prior to recombination. This is particularly useful since  $Y_{\rm p}$  is sensitive to  $N_{\rm eff}$  a few minutes after the big bang, while the CMB and matter power spectra are affected by  $N_{\rm eff}$  prior to recombination, about 370 000 years later. Measuring the radiation content at these well-separated times provides a window onto any nontrivial evolution in the energy density of radiation in the early universe [74–77]. Furthermore,  $N_{\rm eff}$  and  $Y_{\rm p}$  are sensitive to neutrinos and physics beyond the Standard Model in related, but different ways, which allows for even finer probes of new physics, especially in the neutrino and dark sectors.

## 3 Cosmological and Astrophysical Observables

Cosmic Microwave Background The effect of the radiation density on the damping tail of the anisotropy power spectrum drives the constraint on  $N_{\rm eff}$  from the CMB. The largest effect comes from the change to the expansion rate, which impacts the amount of photon diffusion, which in turn causes an exponential suppression of short wavelength modes [78]. This effect on the damping tail is dominant when holding fixed the scale of matter-radiation equality and the location of the first acoustic peak [40], both of which are precisely measured. At the noise level and resolution of upcoming observations [53,61,79–81], this effect is predominately measured through the TE power spectrum on small scales. *Planck* has provided a strong constraint of  $N_{\rm eff} = 2.92^{+0.18}_{-0.19}$  using

temperature and polarization data [33]. Future high-resolution maps of the CMB could realistically achieve  $\sigma(N_{\rm eff}) = 0.03$  in the coming decade [53,61].

In addition to the effect on the expansion rate, perturbations in neutrinos (and other free-streaming light relics) affect the photon-baryon fluid through their gravitational influence. The contributions from neutrino fluctuations are well described by a correction to the amplitude and the phase of the acoustic peaks in both temperature and polarization [41]. The phase shift is a particularly compelling signature since it is not degenerate with other cosmological parameters (unlike the damping tail) [41,42] and has a direct connection to the underlying particle properties [42]. Recently, the phase shift from neutrinos has also been established directly in the *Planck* temperature data [82], which provides the most direct evidence for free-streaming radiation consistent with the cosmic neutrino background. If  $\Delta N_{\text{eff}} \neq 0$  is detected, this phase could provide a powerful confirmation.

**Big Bang Nucleosynthesis (BBN)** The production of light elements in the early universe is affected by the density of light relics through their impact on the expansion rate during the first few minutes after reheating. Cosmic neutrinos play a special role during BBN since they also participate in the weak interactions that interconvert protons and neutrons. Measurements of the primordial abundances of light elements can therefore be used to infer the relic density of neutrinos and other light species, with deuterium [83] and helium-4 [84,85] currently providing the tightest constraints. Future improvements will be driven by 30 m-class telescopes, but are limited by the analysis of the most pristine astrophysical systems rather than statistics. When abundance measurements are combined with *Planck* CMB data, the density of light relics is found to be  $N_{\text{eff}} = 3.04 \pm 0.11$  [33].

**Large-Scale Structure (LSS)** Maps of the large-scale structure of the universe from galaxy and weak lensing surveys can provide complementary measurements of the radiation content. The main observable is the shape of the matter power spectrum, which can be decomposed into a smooth (broadband) component and the spectrum of baryon acoustic oscillations. Additional radiation alters the sound horizon, which is routinely captured in current BAO analyses. While this is highly degenerate with other parameters, combining BAO and CMB observations slightly improves the sensitivity to  $N_{\rm eff}$  over the CMB alone,  $N_{\rm eff} = 2.99 \pm 0.17$  [33]. The BAO spectrum also exhibits the same phase shift observed in the CMB spectra. A nonzero phase shift was recently extracted from the distribution of galaxies observed by the Baryon Oscillation Spectroscopic Survey (BOSS) [60, 86] and upcoming galaxy surveys will significantly improve on this measurement.

The two main consequences of a different radiation density on the broadband shape of the power spectrum are a change of the power on small scales and in the location of the turn-over of the spectrum. Although these effects are clearly visible in the linear matter power spectrum, they are limited by uncertainties related to gravitational nonlinearities and biasing. The combination of planned spectroscopic LSS surveys with *Planck* data could reach  $\sigma(N_{\rm eff}) = 0.08$  [60]. However, these surveys would not contribute a meaningful improvement when combined with a CMB experiment achieving  $\sigma(N_{\rm eff}) \approx 0.03$ . If nonlinear effects can be controlled, very large-volume and high-resolution LSS maps can reach comparable sensitivity to the CMB [60, 87] and would significantly add to the scientific impact of the CMB alone. Furthermore, LSS observations are also sensitive to effects induced by neutrinos and other light relics beyond  $N_{\rm eff}$ , for example in the Lyman- $\alpha$  forest and the biasing of galaxies (see e.g. [88–92]).

**Summary** Sub-percent-level measurements of the radiation density would transform our understanding of the early universe, the neutrino and dark sectors, and more. To reach clear observational targets, future CMB observations offer the most promising and concrete path in the next decade.

#### **Affiliations**

- <sup>1</sup> Department of Physics & Astronomy, Rice University, Houston, TX 77005, USA
- <sup>2</sup> Southern Methodist University, Dallas, TX 75275, USA
- <sup>3</sup> Institute for Advanced Study, Princeton, NJ 08540, USA
- <sup>4</sup> University of California San Diego, La Jolla, CA 92093, USA
- <sup>5</sup> University of California Irvine, Irvine, CA 92697, USA
- <sup>6</sup> DAMTP, University of Cambridge, Cambridge CB3 0WA, UK
- <sup>7</sup> Department of Physics, University of Illinois at Urbana-Champaign, Urbana, IL 61801, USA
- <sup>8</sup> SLAC National Accelerator Laboratory, Menlo Park, CA 94025, USA
- <sup>9</sup> Department of Physics, Durham University, Durham DH1 3LE, UK
- $^{\rm 10}$  Lawrence Livermore National Laboratory, Livermore, CA 94550, USA
- <sup>11</sup> International School for Advanced Studies (SISSA), 34136 Trieste, Italy
- <sup>12</sup> Institute for Fundamental Physics of the Universe (IFPU), 34014 Trieste, Italy
- <sup>13</sup> National Institute for Nuclear Physics (INFN), 34127 Trieste, Italy
- <sup>14</sup> CSEE, West Virginia University, Morgantown, WV 26505, USA
- <sup>15</sup> Center for Gravitational Waves and Cosmology, West Virginia University, Morgantown, WV 26505, USA
- <sup>16</sup> University of New Mexico, Albuquerque, NM 87131, USA
- <sup>17</sup> Cornell University, Ithaca, NY 14853, USA
- 18 GRAPPA, University of Amsterdam,
- 1098 XH Amsterdam, The Netherlands
- <sup>19</sup> Institute for Theoretical Physics, University of Amsterdam, 1098 XH Amsterdam, The Netherlands
- <sup>20</sup> Department of Physics, University of
- Wisconsin-Madison, Madison, WI 53706, USA
- <sup>21</sup> Johns Hopkins University, Baltimore, MD 21218, USA
- <sup>22</sup> Fermi National Accelerator Laboratory, Batavia, IL 60510, USA
- <sup>23</sup> Kavli Institute for Cosmological Physics, Chicago, IL 60637, USA
- <sup>24</sup> Institute of Cosmology & Gravitation, University of Portsmouth, Portsmouth PO1 3FX, UK
- <sup>25</sup> University of Cincinnati, Cincinnati, OH 45221, USA
- <sup>26</sup> HEP Division, Argonne National Laboratory, Lemont, IL 60439, USA
- <sup>27</sup> Canadian Institute for Theoretical Astrophysics, University of Toronto, Toronto, ON M5S 3H8, Canada
- <sup>28</sup> Lawrence Berkeley National Laboratory, Berkeley,

- CA 94720, USA
- <sup>29</sup> Perimeter Institute, Waterloo, ON N2L 2Y5, Canada
- <sup>30</sup> University of Chicago, Chicago, IL 60637, USA
- <sup>31</sup> Department of Physics, University of California Berkeley, Berkeley, CA 94720, USA
- <sup>32</sup> Institute of Astronomy, University of Cambridge, Cambridge CB3 0HA, UK
- <sup>33</sup> Kavli Institute for Cosmology, Cambridge CB3 0HA, UK
- <sup>34</sup> Harvard-Smithsonian Center for Astrophysics, Cambridge, MA 02138, USA
- <sup>35</sup> University of California Santa Barbara, Santa Barbara, CA 93106, USA
- <sup>36</sup> Department of Physics, Harvard University, Cambridge, MA 02138, USA
- <sup>37</sup> Stanford University, Stanford, CA 94305, USA
- <sup>38</sup> Jet Propulsion Laboratory, California Institute of Technology, Pasadena, CA 91109, USA
- <sup>39</sup> Boston University, Boston, MA 02215, USA
- <sup>40</sup> Princeton University, Princeton, NJ 08544, USA
- <sup>41</sup> University of California Riverside, Riverside, CA 92521, USA
- <sup>42</sup> CPPM, Aix-Marseille Université, CNRS/IN2P3, 13007 Marseille, France
- <sup>43</sup> Goddard Space Flight Center, Greenbelt, MD 20771, USA
- <sup>44</sup> Astronomy Centre, School of Mathematical and Physical Sciences, University of Sussex, Brighton BN1 9QH, UK
- <sup>45</sup> Universidad Autónoma de Madrid, 28049 Madrid, Spain
- <sup>46</sup> University of Florida, Gainesville, FL 32611, USA
- <sup>47</sup> Department of Physics and Astronomy, University of Rochester, Rochester, NY 14627, USA
- <sup>48</sup> Haverford College, Haverford, PA 19041, USA
- <sup>49</sup> Oskar Klein Centre for Cosmoparticle Physics, Stockholm University, AlbaNova, 106 91 Stockholm, Sweden
- <sup>50</sup> University of Minnesota, Minneapolis, MN 55455, USA
- <sup>51</sup> Astrophysics Group, Cavendish Laboratory, University of Cambridge, Cambridge CB3 0HE, UK
- <sup>52</sup> Center for Computational Astrophysics, Flatiron Institute, New York, NY 10010, USA
- <sup>53</sup> The Ohio State University, Columbus, OH 43212, USA
- <sup>54</sup> Dunlap Institute for Astronomy and Astrophysics, University of Toronto, ON M5S 3H4, Canada
- <sup>55</sup> Department of Astronomy and Astrophysics, University of Toronto, ON M5S 3H4, Canada
- <sup>56</sup> Virginia Tech, Blacksburg, VA 24061, USA

- <sup>57</sup> University of Michigan, Ann Arbor, MI 48109, USA
- <sup>58</sup> Institute for Basic Science (IBS), Daejeon 34051, Korea
- <sup>59</sup> Korea Astronomy and Space Science Institute, Daejeon 34055, Korea
- <sup>60</sup> Tata Institute of Fundamental Research, Mumbai 400005, India
- <sup>61</sup> Institute of Physics, Laboratory of Astrophysics, École Polytechnique Fédérale de Lausanne (EPFL),
- Observatoire de Sauverny, 1290 Versoix, Switzerland
- 62 University of California Davis, Davis, CA 95616, USA
- <sup>63</sup> Brown University, Providence, RI 02912, USA
- <sup>64</sup> Department of Physics, Ben-Gurion University, Be'er Sheva 84105, Israel
- 65 University College London, London WC1E 6BT, UK
- <sup>66</sup> Istituto Nazionale di Fisica Nucleare, Sezione di Ferrara, 40122 Ferrara, Italy
- <sup>67</sup> Dipartimento di Fisica e Astronomia "G. Galilei",
  Università degli Studi di Padova, 35131 Padova, Italy
  <sup>68</sup> Stony Brook University, Stony Brook, NY 11794,
  USA
- <sup>69</sup> Massachusetts Institute of Technology, Cambridge, MA 02139, USA
- <sup>70</sup> University of Washington, Seattle, WA 98195, USA
- Van Swinderen Institute for Particle Physics and Gravity, University of Groningen, 9747 AG Groningen, The Netherlands
- <sup>72</sup> International Centre for Theoretical Physics (ICTP),34151 Trieste, Italy
- <sup>73</sup> Institut d'Astrophysique de Paris (IAP), CNRS & Sorbonne University, 75014 Paris, France
- <sup>74</sup> Department of Physics, Yale University, New Haven, CT 06520, USA
- <sup>75</sup> Brookhaven National Laboratory, Upton, NY 11973, USA
- <sup>76</sup> Dipartimento di Fisica, Università La Sapienza, 00185 Roma, Italy
- <sup>77</sup> Istituto Nazionale di Fisica Nucleare, Sezione di Roma, 00185 Roma, Italy

- <sup>78</sup> University of Southern California, Los Angeles, CA 90089, USA
- <sup>79</sup> Department of Physics, Simon Fraser University, Burnaby, BC V5A 1S6, Canada
- <sup>80</sup> Kavli Institute for Particle Astrophysics and Cosmology, Stanford, CA 94305, USA
- <sup>81</sup> Laboratoire Astroparticule et Cosmologie (APC), CNRS/IN2P3, Université Paris Diderot, 75205 Paris, France
- 82 School of Physics, The University of Melbourne, Parkville, VIC 3010, Australia
- <sup>83</sup> Space Telescope Science Institute, Baltimore, MD 21218, USA
- <sup>84</sup> Department of Physics and Astronomy, Sejong University, Seoul 143-747, Korea
- <sup>85</sup> Case Western Reserve University, Cleveland, OH 44106, USA
- <sup>86</sup> Department of Astronomy, University of California Berkeley, Berkeley, CA 94720, USA
- <sup>87</sup> Department of Physics and Astronomy, Ohio University, Athens, OH 45701, USA
- <sup>88</sup> LAL, Université Paris-Sud, 91898 Orsay Cedex, France & CNRS/IN2P3, 91405 Orsay, France
- <sup>89</sup> Department of Physics and Astronomy, University of Pennsylvania, Philadelphia, PA 19104, USA
- <sup>90</sup> Jodrell Bank Center for Astrophysics, School of Physics and Astronomy, University of Manchester, Manchester M13 9PL, UK
- <sup>91</sup> Instituto de Física (IFUNAM), Universidad Nacional Autónoma de México, 04510 Ciudad de México, Mexico
- 92 Syracuse University, Syracuse, NY 13244, USA
- <sup>93</sup> Physics & Astronomy Department, Vanderbilt University, Nashville, TN 37235, USA
- <sup>94</sup> University of California Los Angeles, Los Angeles, CA 90095, USA
- 95 National Astronomical Observatories, Chinese Academy of Sciences, Beijing, China
- <sup>96</sup> University of Edinburgh, Edinburgh EH8 9YL, UK

#### References

- [1] R. Essig et al., "Working Group Report: New Light Weakly Coupled Particles," in Community Summer Study 2013: Snowmass on the Mississippi (CSS2013), Minneapolis, MN, USA, July 29-August 6, 2013. 2013. arXiv:1311.0029 [hep-ph].
- [2] D. J. E. Marsh, "Axion Cosmology," *Phys. Rep.* **643** (2016) 1, arXiv:1510.07633 [astro-ph.CO].
- [3] J. Alexander *et al.*, "Dark Sectors 2016 Workshop: Community Report," arXiv:1608.08632 [hep-ph].
- [4] K. Abazajian, G. Fuller, and M. Patel, "Sterile Neutrino Hot, Warm, and Cold Dark Matter," *Phys. Rev. D* **64** (2001) 023501, arXiv:astro-ph/0101524 [astro-ph].
- [5] A. Strumia and F. Vissani, "Neutrino Masses and Mixings and...," arXiv:hep-ph/0606054 [hep-ph].
- [6] L. Ackerman, M. Buckley, S. Carroll, and M. Kamionkowski, "Dark Matter and Dark Radiation," *Phys. Rev. D* **79** (2009) 023519, arXiv:0810.5126 [hep-ph].
- [7] A. Boyarsky, O. Ruchayskiy, and M. Shaposhnikov, "The Role of Sterile Neutrinos in Cosmology and Astrophysics," *Ann. Rev. Nucl. Part. Sci.* **59** (2009) 191, arXiv:0901.0011 [hep-ph].
- [8] A. Arvanitaki, S. Dimopoulos, S. Dubovsky, N. Kaloper, and J. March-Russell, "String Axiverse," *Phys. Rev. D* **81** (2010) 123530, arXiv:0905.4720 [hep-th].
- [9] D. Cadamuro, S. Hannestad, G. Raffelt, and J. Redondo, "Cosmological Bounds on Sub-MeV Mass Axions," *JCAP* **02** (2011) 003, arXiv:1011.3694 [hep-ph].
- [10] D. E. Kaplan, G. Krnjaic, K. Rehermann, and C. Wells, "Dark Atoms: Asymmetry and Direct Detection," *JCAP* **10** (2011) 011, arXiv:1105.2073 [hep-ph].
- [11] K. Abazajian *et al.*, "Light Sterile Neutrinos: A White Paper," arXiv:1204.5379 [hep-ph].
- [12] F.-Y. Cyr-Racine and K. Sigurdson, "Cosmology of Atomic Dark Matter," *Phys. Rev. D* **87** (2013) 103515, arXiv:1209.5752 [astro-ph.CO].
- [13] C. Brust, D. E. Kaplan, and M. Walters, "New Light Species and the CMB," *JHEP* **12** (2013) 058, arXiv:1303.5379 [hep-ph].
- [14] S. Weinberg, "Goldstone Bosons as Fractional Cosmic Neutrinos," *Phys. Rev. Lett.* **110** (2013) 241301, arXiv:1305.1971 [astro-ph.CO].
- [15] A. Salvio, A. Strumia, and W. Xue, "Thermal Axion Production," *JCAP* **01** (2014) 011, arXiv:1310.6982 [hep-ph].

- [16] M. Kawasaki, M. Yamada, and T. Yanagida, "Observable Dark Radiation from a Cosmologically Safe QCD Axion," *Phys. Rev. D* **91** (2015) 125018, arXiv:1504.04126 [hep-ph].
- [17] P. Graham, D. E. Kaplan, and S. Rajendran, "Cosmological Relaxation of the Electroweak Scale," *Phys. Rev. Lett.* **115** (2015) 221801, arXiv:1504.07551 [hep-ph].
- [18] D. Baumann, D. Green, and B. Wallisch, "New Target for Cosmic Axion Searches," *Phys. Rev. Lett.* **117** (2016) 171301, arXiv:1604.08614 [astro-ph.CO].
- [19] N. Arkani-Hamed, T. Cohen, R. D'Agnolo, A. Hook, H. Kim, and D. Pinner, "Solving the Hierarchy Problem at Reheating with a Large Number of Degrees of Freedom," *Phys. Rev. Lett.* **117** (2016) 251801, arXiv:1607.06821 [hep-ph].
- [20] Z. Chacko, N. Craig, P. Fox, and R. Harnik, "Cosmology in Mirror Twin Higgs and Neutrino Masses," *JHEP* **07** (2017) 023, arXiv:1611.07975 [hep-ph].
- [21] N. Craig, S. Koren, and T. Trott, "Cosmological Signals of a Mirror Twin Higgs," *JHEP* **05** (2017) 038, arXiv:1611.07977 [hep-ph].
- [22] Z. Chacko, D. Curtin, M. Geller, and Y. Tsai, "Cosmological Signatures of a Mirror Twin Higgs," *JHEP* **09** (2018) 163, arXiv:1803.03263 [hep-ph].
- [23] M. Archidiacono, E. Giusarma, S. Hannestad, and O. Mena, "Cosmic Dark Radiation and Neutrinos," *Adv. High Energy Phys.* **2013** (2013) 191047, arXiv:1307.0637 [astro-ph.CO].
- [24] J. Bernal, L. Verde, and A. Riess, "The Trouble with  $H_0$ ," JCAP 10 (2016) 019, arXiv:1607.05617 [astro-ph.C0].
- [25] B. Zhang, M. Childress, T. Davis, N. Karpenka, C. Lidman, B. Schmidt, and M. Smith, "A Blinded Determination of  $H_0$  from Low-Redshift Type Ia Supernovae, Calibrated by Cepheid Variables," *Mon. Not. Roy. Astron. Soc.* **471** (2017) 2254, arXiv:1706.07573 [astro-ph.CO].
- [26] G. Addison, D. Watts, C. Bennett, M. Halpern, G. Hinshaw, and J. Weiland, "Elucidating ACDM: Impact of Baryon Acoustic Oscillation Measurements on the Hubble Constant Discrepancy," *Astrophys. J.* **853** (2018) 119, arXiv:1707.06547 [astro-ph.CO].
- [27] K. Aylor, M. Joy, L. Knox, M. Millea, S. Raghunathan, and K. Wu, "Sounds Discordant: Classical Distance Ladder & ACDM-Based Determinations of the Cosmological Sound Horizon," arXiv:1811.00537 [astro-ph.C0].
- [28] N. MacCrann, J. Zuntz, S. Bridle, B. Jain, and M. Becker, "Cosmic Discordance: Are Planck CMB and CFHTLenS Weak Lensing Measurements Out of Tune?," *Mon. Not. Roy. Astron. Soc.* **451** (2015) 2877, arXiv:1408.4742 [astro-ph.C0].
- [29] J. Lesgourgues, G. Marques-Tavares, and M. Schmaltz, "Evidence for Dark Matter Interactions in Cosmological Precision Data?," *JCAP* **02** (2016) 037, arXiv:1507.04351 [astro-ph.CO].

- [30] F. Köhlinger *et al.*, "KiDS-450: The Tomographic Weak Lensing Power Spectrum and Constraints on Cosmological Parameters," *Mon. Not. Roy. Astron. Soc.* **471** (2017) 4412, arXiv:1706.02892 [astro-ph.CO].
- [31] S. Joudaki *et al.*, "KiDS-450 + 2dFLenS: Cosmological Parameter Constraints from Weak Gravitational Lensing Tomography and Overlapping Redshift-Space Galaxy Clustering," *Mon. Not. Roy. Astron. Soc.* **474** (2018) 4894, arXiv:1707.06627 [astro-ph.C0].
- [32] D. Weinberg, J. Bullock, F. Governato, R. Kuzio de Naray, and A. Peter, "Cold Dark Matter: Controversies on Small Scales," *Proc. Nat. Acad. Sci.* **112** (2015) 12249, arXiv:1306.0913 [astro-ph.CO].
- [33] N. Aghanim *et al.* (Planck Collaboration), "Planck 2018 Results. VI. Cosmological Parameters," arXiv:1807.06209 [astro-ph.CO].
- [34] R. Cyburt, B. Fields, K. Olive, and T.-H. Yeh, "Big Bang Nucleosynthesis: 2015," *Rev. Mod. Phys.* **88** (2016) 015004, arXiv:1505.01076 [astro-ph.CO].
- [35] G. Mangano, G. Miele, S. Pastor, T. Pinto, O. Pisanti, and P. Serpico, "Relic Neutrino Decoupling Including Flavour Oscillations," *Nucl. Phys. B* **729** (2005) 221, arXiv:hep-ph/0506164 [hep-ph].
- [36] E. Grohs, G. Fuller, C. Kishimoto, M. Paris, and A. Vlasenko, "Neutrino Energy Transport in Weak Decoupling and Big Bang Nucleosynthesis," *Phys. Rev. D* **93** (2016) 083522, arXiv:1512.02205 [astro-ph.CO].
- [37] P. de Salas and S. Pastor, "Relic Neutrino Decoupling with Flavour Oscillations Revisited," *JCAP* **07** (2016) 051, arXiv:1606.06986 [hep-ph].
- [38] P. J. E. Peebles, "Primordial Helium Abundance and the Primordial Fireball. II," *Astrophys. J.* **146** (1966) 542.
- [39] D. Dicus, E. Kolb, Gleeson, Sudarshan, V. Teplitz, and M. Turner, "Primordial Nucleosynthesis Including Radiative, Coulomb, and Finite-Temperature Corrections to Weak Rates," *Phys. Rev. D* **26** (1982) 2694.
- [40] Z. Hou, R. Keisler, L. Knox, M. Millea, and C. Reichardt, "How Massless Neutrinos Affect the Cosmic Microwave Background Damping Tail," *Phys. Rev. D* **87** (2013) 083008, arXiv:1104.2333 [astro-ph.C0].
- [41] S. Bashinsky and U. Seljak, "Neutrino Perturbations in CMB Anisotropy and Matter Clustering," *Phys. Rev. D* **69** (2004) 083002, arXiv:astro-ph/0310198 [astro-ph].
- [42] D. Baumann, D. Green, J. Meyers, and B. Wallisch, "Phases of New Physics in the CMB," *JCAP* **01** (2016) 007, arXiv:1508.06342 [astro-ph.CO].
- [43] D. Baumann, D. Green, and M. Zaldarriaga, "Phases of New Physics in the BAO Spectrum," *JCAP* 11 (2017) 007, arXiv:1703.00894 [astro-ph.CO].

- [44] N. Bell, E. Pierpaoli, and K. Sigurdson, "Cosmological Signatures of Interacting Neutrinos," *Phys. Rev. D* **73** (2006) 063523, arXiv:astro-ph/0511410 [astro-ph].
- [45] A. Friedland, K. Zurek, and S. Bashinsky, "Constraining Models of Neutrino Mass and Neutrino Interactions with the Planck Satellite," arXiv:0704.3271 [astro-ph].
- [46] F.-Y. Cyr-Racine and K. Sigurdson, "Limits on Neutrino-Neutrino Scattering in the Early Universe," *Phys. Rev. D* **90** (2014) 123533, arXiv:1306.1536 [astro-ph.CO].
- [47] L. Lancaster, F.-Y. Cyr-Racine, L. Knox, and Z. Pan, "A Tale of Two Modes: Neutrino Free-Streaming in the Early Universe," *JCAP* **07** (2017) 033, arXiv:1704.06657 [astro-ph.CO].
- [48] C. Brust, Y. Cui, and K. Sigurdson, "Cosmological Constraints on Interacting Light Particles," *JCAP* **08** (2017) 020, arXiv:1703.10732 [astro-ph.CO].
- [49] G. Choi, C.-T. Chiang, and M. LoVerde, "Probing Decoupling in Dark Sectors with the Cosmic Microwave Background," *JCAP* **06** (2018) 044, arXiv:1804.10180 [astro-ph.CO].
- [50] S. Dodelson, K. Heitmann, C. Hirata, K. Honscheid, A. Roodman, U. Seljak, A. Slosar, and M. Trodden, "Cosmic Visions Dark Energy: Science," arXiv:1604.07626 [astro-ph.CO].
- [51] K. Abazajian *et al.*, "Neutrino Physics from the Cosmic Microwave Background and Large-Scale Structure," *Astropart. Phys.* **63** (2015) 66, arXiv:1309.5383 [astro-ph.CO].
- [52] Z. Chacko, Y. Cui, S. Hong, and T. Okui, "Hidden Dark Matter Sector, Dark Radiation and the CMB," *Phys. Rev. D* **92** (2015) 055033, arXiv:1505.04192 [hep-ph].
- [53] K. Abazajian *et al.* (CMB-S4 Collaboration), "CMB-S4 Science Book, First Edition," arXiv:1610.02743 [astro-ph.C0].
- [54] M. Battaglieri *et al.*, "US Cosmic Visions: New Ideas in Dark Matter 2017: Community Report," arXiv:1707.04591 [hep-ph].
- [55] D. Green and S. Rajendran, "The Cosmology of Sub-MeV Dark Matter," *JHEP* **10** (2017) 013, arXiv:1701.08750 [hep-ph].
- [56] S. Knapen, T. Lin, and K. Zurek, "Light Dark Matter: Models and Constraints," *Phys. Rev. D* **96** (2017) 115021, arXiv:1709.07882 [hep-ph].
- [57] V. Gluscevic and K. Boddy, "Constraints on Scattering of keV-TeV Dark Matter with Protons in the Early Universe," *Phys. Rev. Lett.* **121** (2018) 081301, arXiv:1712.07133 [astro-ph.CO].
- [58] M. Markevitch, A. Gonzalez, D. Clowe, A. Vikhlinin, L. David, W. Forman, C. Jones, S. Murray, and W. Tucker, "Direct Constraints on the Dark Matter Self-Interaction Cross-Section from the Merging Galaxy Cluster 1E0657-56," *Astrophys. J.* 606 (2004) 819, arXiv:astro-ph/0309303 [astro-ph].

- [59] R. Essig, R. Harnik, J. Kaplan, and N. Toro, "Discovering New Light States at Neutrino Experiments," *Phys. Rev. D* **82** (2010) 113008, arXiv:1008.0636 [hep-ph].
- [60] D. Baumann, D. Green, and B. Wallisch, "Searching for Light Relics with Large-Scale Structure," *JCAP* **08** (2018) 029, arXiv:1712.08067 [astro-ph.CO].
- [61] S. Hanany *et al.* (PICO Collaboration), "PICO: Probe of Inflation and Cosmic Origins," arXiv:1902.10541 [astro-ph.IM].
- [62] B. Wallisch, "Cosmological Probes of Light Relics," arXiv:1810.02800 [astro-ph.C0].
- [63] P. Adshead, Y. Cui, and J. Shelton, "Chilly Dark Sectors and Asymmetric Reheating," *JHEP* **06** (2016) 016, arXiv:1604.02458 [hep-ph].
- [64] L. Boyle and A. Buonanno, "Relating Gravitational Wave Constraints from Primordial Nucleosynthesis, Pulsar Timing, Laser Interferometers, and the CMB: Implications for the Early Universe," *Phys. Rev. D* **78** (2008) 043531, arXiv:0708.2279 [astro-ph].
- [65] A. Stewart and R. Brandenberger, "Observational Constraints on Theories with a Blue Spectrum of Tensor Modes," *JCAP* **08** (2008) 012, arXiv:0711.4602 [astro-ph].
- [66] P. D. Meerburg, R. Hložek, B. Hadzhiyska, and J. Meyers, "Multiwavelength Constraints on the Inflationary Consistency Relation," *Phys. Rev. D* **91** (2015) 103505, arXiv:1502.00302 [astro-ph.CO].
- [67] M. Maggiore, "Gravitational Wave Experiments and Early Universe Cosmology," *Phys. Rept.* **331** (2000) 283, arXiv:gr-qc/9909001 [gr-qc].
- [68] R. Easther and E. Lim, "Stochastic Gravitational Wave Production After Inflation," *JCAP* **04** (2006) 010, arXiv:astro-ph/0601617 [astro-ph].
- [69] J. Dufaux, A. Bergman, G. Felder, L. Kofman, and J.-P. Uzan, "Theory and Numerics of Gravitational Waves from Preheating after Inflation," *Phys. Rev. D* **76** (2007) 123517, arXiv:0707.0875 [astro-ph].
- [70] M. Amin, M. Hertzberg, D. Kaiser, and J. Karouby, "Nonperturbative Dynamics of Reheating After Inflation: A Review," *Int. J. Mod. Phys. D* **24** (2014) 1530003, arXiv:1410.3808 [hep-ph].
- [71] C. Caprini and D. Figueroa, "Cosmological Backgrounds of Gravitational Waves," *Class. Quant. Grav.* **35** (2018) 163001, arXiv:1801.04268 [astro-ph.CO].
- [72] P. Adshead, J. Giblin, and Z. Weiner, "Gravitational Waves from Gauge Preheating," *Phys. Rev. D* **98** (2018) 043525, arXiv:1805.04550 [astro-ph.CO].
- [73] M. Amin, J. Fan, K. Lozanov, and M. Reece, "Cosmological Dynamics of Higgs Potential Fine Tuning," *Phys. Rev. D* **99** (2019) 035008, arXiv:1802.00444 [hep-ph].
- [74] W. Fischler and J. Meyers, "Dark Radiation Emerging After Big Bang Nucleosynthesis?," *Phys. Rev. D* **83** (2011) 063520, arXiv:1011.3501 [astro-ph.C0].

- [75] J. Hasenkamp, "Dark Radiation from the Axino Solution of the Gravitino Problem," *Phys. Lett. B* **707** (2012) 121, arXiv:1107.4319 [hep-ph].
- [76] D. Hooper, F. Queiroz, and N. Gnedin, "Nonthermal Dark Matter Mimicking an Additional Neutrino Species in the Early Universe," *Phys. Rev. D* **85** (2012) 063513, arXiv:1111.6599 [astro-ph.CO].
- [77] J. Hasenkamp and J. Kersten, "Dark Radiation from Particle Decay: Cosmological Constraints and Opportunities," *JCAP* **08** (2013) 024, arXiv:1212.4160 [hep-ph].
- [78] M. Zaldarriaga and D. Harari, "Analytic Approach to the Polarization of the Cosmic Microwave Background in Flat and Open Universes," *Phys. Rev. D* **52** (1995) 3276, arXiv:astro-ph/9504085 [astro-ph].
- [79] B. Benson *et al.* (SPT-3G Collaboration), "SPT-3G: A Next-Generation Cosmic Microwave Background Polarization Experiment on the South Pole Telescope," *Proc. SPIE Int. Soc. Opt. Eng.* **9153** (2014) 91531P, arXiv:1407.2973 [astro-ph.IM].
- [80] S. Henderson *et al.*, "Advanced ACTPol Cryogenic Detector Arrays and Readout," *J. Low. Temp. Phys.* **184** (2016) 772, arXiv:1510.02809 [astro-ph.IM].
- [81] J. Aguirre *et al.* (Simons Observatory Collaboration), "The Simons Observatory: Science Goals and Forecasts," *JCAP* **02** (2019) 056, arXiv:1808.07445 [astro-ph.CO].
- [82] B. Follin, L. Knox, M. Millea, and Z. Pan, "First Detection of the Acoustic Oscillation Phase Shift Expected from the Cosmic Neutrino Background," *Phys. Rev. Lett.* **115** (2015) 091301, arXiv:1503.07863 [astro-ph.CO].
- [83] R. Cooke, M. Pettini, and C. Steidel, "One-Percent Determination of the Primordial Deuterium Abundance," *Astrophys. J.* **855** (2018) 102, arXiv:1710.11129 [astro-ph.CO].
- [84] E. Aver, K. Olive, and E. Skillman, "The Effects of He-I  $\lambda 10830$  on Helium Abundance Determinations," *JCAP* **07** (2015) 011, arXiv:1503.08146 [astro-ph.CO].
- [85] A. Peimbert, M. Peimbert, and V. Luridiana, "The Primordial Helium Abundance and the Number of Neutrino Families," *Rev. Mex. Astron. Astrofis.* **52** (2016) 419, arXiv:1608.02062 [astro-ph.C0].
- [86] D. Baumann, F. Beutler, R. Flauger, D. Green, A. Slosar, M. Vargas-Magaña, B. Wallisch, and C. Yèche, "First Constraint on the Neutrino-Induced Phase Shift in the Spectrum of Baryon Acoustic Oscillations," *Nat. Phys.* (2019), arXiv:1803.10741 [astro-ph.C0].
- [87] R. Ansari *et al.* (Cosmic Visions 21 cm Collaboration), "Inflation and Early Dark Energy with a Stage II Hydrogen Intensity Mapping Experiment," arXiv:1810.09572 [astro-ph.CO].
- [88] A. Boyarsky, J. Lesgourgues, O. Ruchayskiy, and M. Viel, "Lyman-α Constraints on Warm and on Warm-Plus-Cold Dark Matter Models," *JCAP* **05** (2009) 012, arXiv:0812.0010 [astro-ph].

- [89] H.-M. Zhu, U.-L. Pen, X. Chen, and D. Inman, "Probing Neutrino Hierarchy and Chirality via Wakes," *Phys. Rev. Lett.* **116** (2016) 141301, arXiv:1412.1660 [astro-ph.CO].
- [90] M. LoVerde, "Halo Bias in Mixed Dark Matter Cosmologies," *Phys. Rev. D* **90** (2014) 083530, arXiv:1405.4855 [astro-ph.CO].
- [91] J. Muñoz and C. Dvorkin, "Efficient Computation of Galaxy Bias with Neutrinos and Other Relics," *Phys. Rev. D* **98** (2018) 043503, arXiv:1805.11623 [astro-ph.CO].
- [92] C.-T. Chiang, M. LoVerde, and F. Villaescusa-Navarro, "First Detection of Scale-Dependent Linear Halo Bias in *N*-Body Simulations with Massive Neutrinos," *Phys. Rev. Lett.* **122** (2019) 041302, arXiv:1811.12412 [astro-ph.CO].