



Institut Charles Gerhardt Montpellier

CHEMISTRY: MOLECULES TO MATERIALS



Advances and Perspectives in Quantum Computing for Quantum Chemistry and Material Science

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Table of contents

Quantum Chemistry: the electronic structure problem

Quantum Computation

Ground-state Chemistry on Quantum Computers

Excited-state Chemistry on Quantum Computers

Density Functional Theory on Quantum Computers

Current Works and Perspectives ; Discussion on Quantum Advantage



Table of contents

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Electronic Structure Problem

1 / 18

Hamiltonian operator for the total electronic energy of the system, $\hat{H} = \hat{T} + \hat{V}_{ne} + \hat{W}_{ee}$:

$$\hat{H} = -\sum_i \frac{\nabla_i^2}{2} - \sum_{i,I} \frac{Z_I}{|\mathbf{r}_i - \mathbf{R}_I|} + \frac{1}{2} \sum_{i \neq j} \frac{\mathbf{1}}{|\mathbf{r}_i - \mathbf{r}_j|} \quad \hat{H} |\Psi_n\rangle = E_n |\Psi_n\rangle, \text{ To difficult to solve !}$$



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1 / 18

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Electronic Structure Problem

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Projected onto a basis of N spin-orbitals $\{\phi_p^\alpha(\mathbf{r}), \phi_p^\beta(\mathbf{r})\}$

$|\Phi_0\rangle$

ϕ_s —————
 ϕ_r —————
 ϕ_q —————↑↓
 ϕ_p —————↓↑



Non-interacting problem

$$|\Psi_0\rangle \rightarrow |\Phi_0\rangle, E_0 \rightarrow \sum_{i=1}^{\text{occ}} \varepsilon_i$$



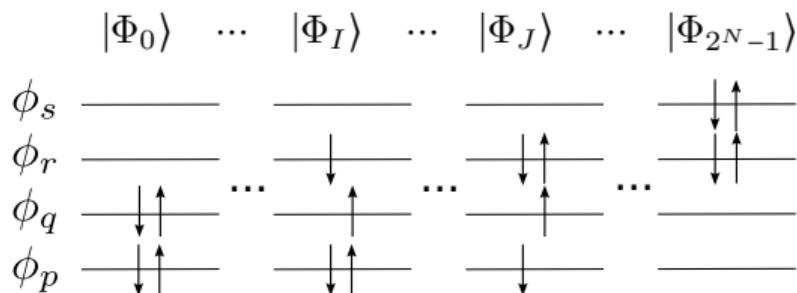
Electronic Structure Problem

1 / 18

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Non-interacting problem

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Exponential Wall problem

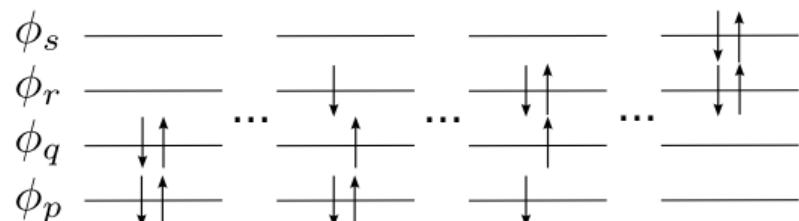
$$|\Psi_0\rangle = \sum_I^{\text{Exponential}} c_I |\Phi_I\rangle$$



Many-body basis

Occupation vector representation of the many-body basis (electronic configuration):

$$|\Phi_0\rangle \quad \dots \quad |\Phi_I\rangle \quad \dots \quad |\Phi_J\rangle \quad \dots \quad |\Phi_{2^N-1}\rangle$$



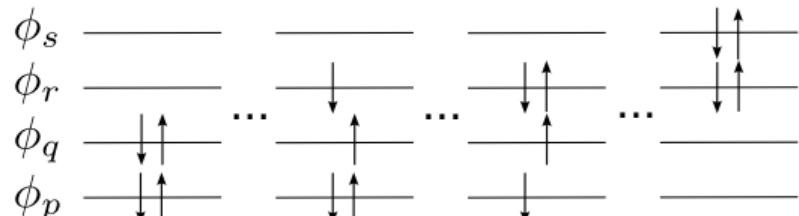
$$\left| \phi_{N/2}^\beta, \dots, \phi_1^\beta, \phi_{N/2}^\alpha, \dots, \phi_1^\alpha \right\rangle, \quad \phi_p = \begin{cases} 0 & \text{if empty} \\ 1 & \text{if occupied} \end{cases}$$



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$|00110011\rangle, |01010011\rangle, |01010110\rangle, |11001100\rangle$

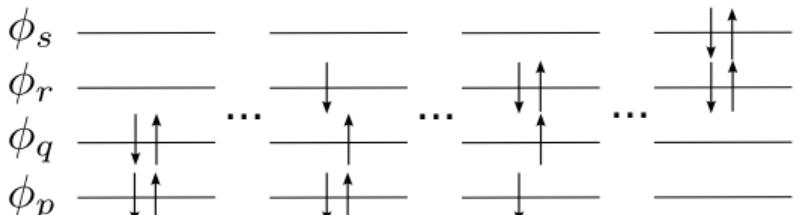


Many-body basis

2 / 18

Occupation vector representation of the many-body basis (electronic configuration):

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$$|00110011\rangle, |01010011\rangle, |01010110\rangle, |11001100\rangle$$

Build and diagonalize the Hamiltonian matrix:

$$\begin{bmatrix} \langle \Phi_0 | \hat{H} | \Phi_0 \rangle & \dots & \langle \Phi_0 | \hat{H} | \Phi_{2^N-1} \rangle \\ \vdots & \ddots & \vdots \\ \langle \Phi_{2^N-1} | \hat{H} | \Phi_0 \rangle & \dots & \langle \Phi_{2^N-1} | \hat{H} | \Phi_{2^N-1} \rangle \end{bmatrix} \xrightarrow{\text{Diagonalization}} \begin{bmatrix} E_0 & & \mathbf{0} \\ & \ddots & \\ \mathbf{0} & & E_{2^N-1} \end{bmatrix}, |\Psi_0\rangle = \sum_I c_I |\Phi_I\rangle$$



Table of contents

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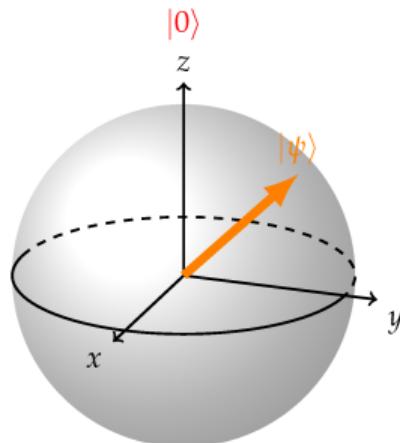
Superposition and Entanglement: Quantum bits

3 / 18

Classical bit to Quantum bit:

Qubit: a (two-)level system

Superposition



$|\psi\rangle$

$$|\psi\rangle = \alpha|0\rangle + \beta|1\rangle, \quad |\alpha|^2 + |\beta|^2 = 1$$



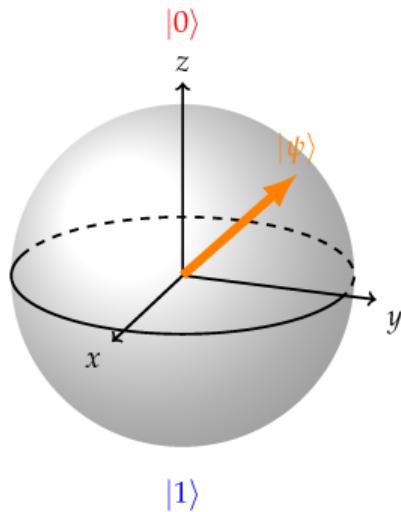
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Qubit register:
Superposition and Entanglement

$$|\Psi\rangle = \sum_{q=0}^{2^N-1} c_q |q\rangle, \quad \sum_q |c_q|^2 = 1$$

where $q = \{0, \dots, 2^N - 1\}$ are all possible bit-strings from N qubits

Encoding?

$\mathcal{O}(2^N)$
Classical

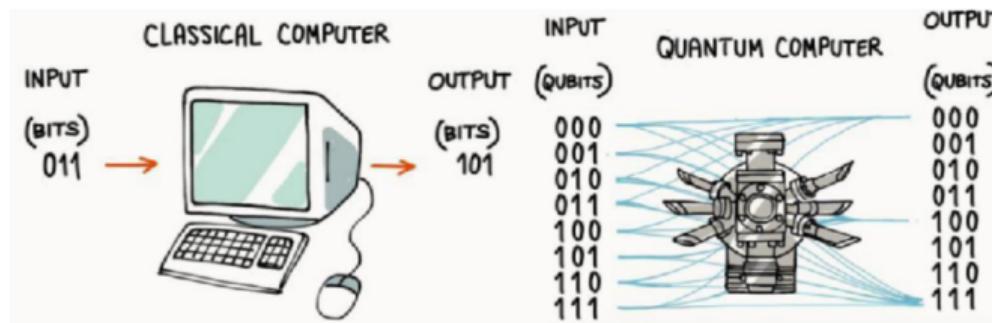
$\mathcal{O}(N)$
Quantum



Quantum circuit: model of quantum computation

4 / 18

$$|\Psi\rangle = \frac{1}{\sqrt{8}} (|000\rangle + |001\rangle + |010\rangle + |011\rangle + |100\rangle + |101\rangle + |110\rangle + |111\rangle)$$



$|0\rangle$ _____

$|0\rangle$ _____

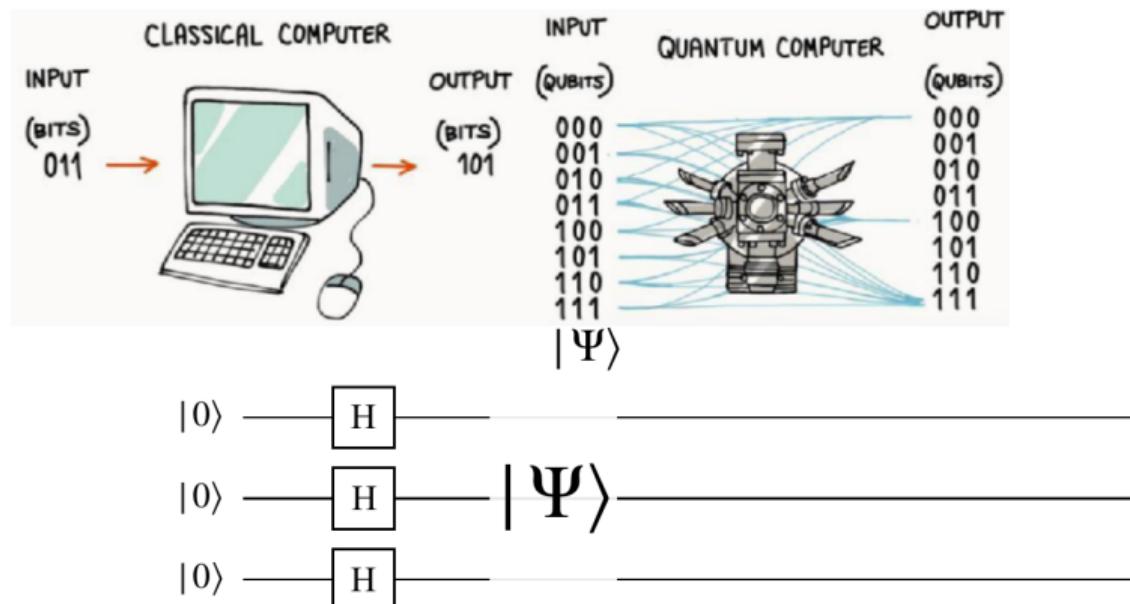
$|0\rangle$ _____



Quantum circuit: model of quantum computation

4 / 18

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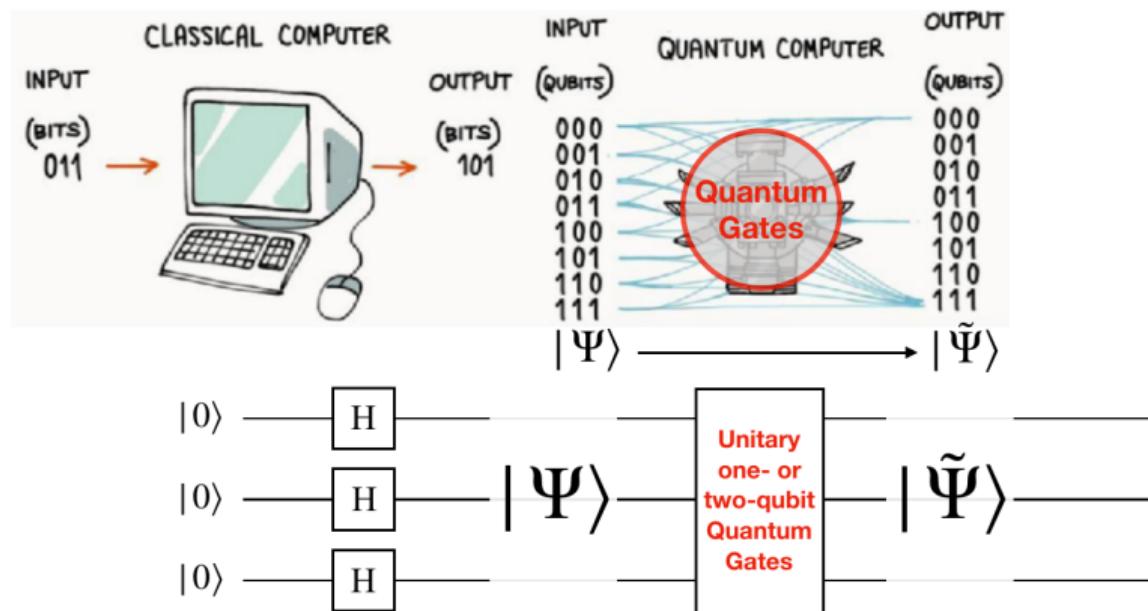




Quantum circuit: model of quantum computation

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Quantum circuit: model of quantum computation

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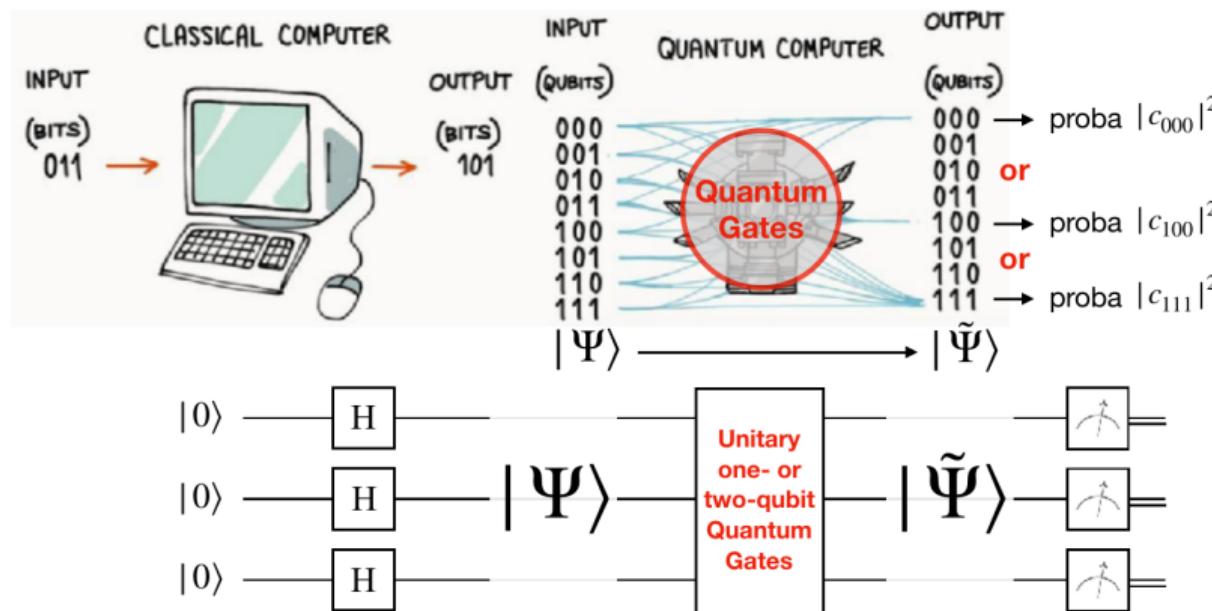




Table of contents

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 $\hat{H} |\Psi_n\rangle = E_n |\Psi_n\rangle$ on quantum computers

5 / 18

$$\begin{bmatrix} \langle \Phi_0 | \hat{H} | \Phi_0 \rangle & \cdots & \langle \Phi_0 | \hat{H} | \Phi_{2^N-1} \rangle \\ \vdots & \ddots & \vdots \\ \langle \Phi_{2^N-1} | \hat{H} | \Phi_0 \rangle & \cdots & \langle \Phi_{2^N-1} | \hat{H} | \Phi_{2^N-1} \rangle \end{bmatrix} \xrightarrow{\text{Diagonalization}} \begin{bmatrix} E_0 & & \mathbf{0} \\ & \ddots & \\ \mathbf{0} & & E_{2^N-1} \end{bmatrix}, |\Psi_0\rangle = \sum_I c_I |\Phi_I\rangle$$



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We don't want to:

- ▶ Build the Hamiltonian matrix (**exponentially costly to build**)
- ▶ Store the wavefunction (**exponentially costly to store**)



$\hat{H} |\Psi_n\rangle = E_n |\Psi_n\rangle$ on quantum computers

5 / 18

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- ▶ Extract the energies and molecular properties at **polynomial cost**



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5 / 18

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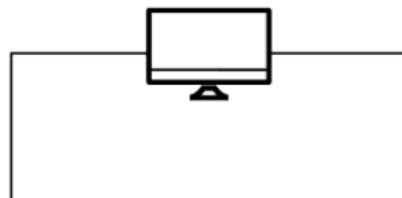
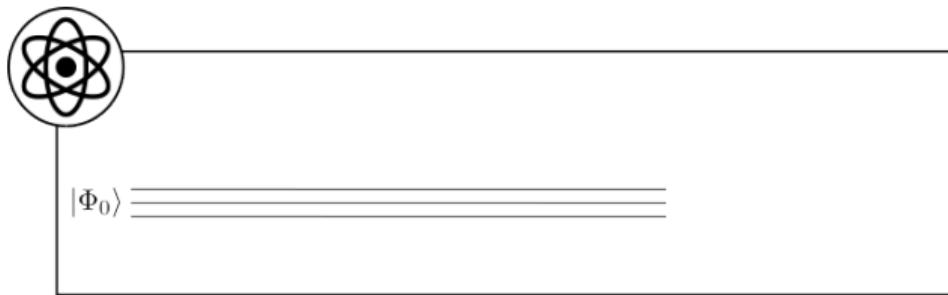
- ▶ Extract the energies and molecular properties at **polynomial cost**

We can:

- ▶ Generate **exponentially many** electronic configurations with only **N qubits** through **superposition and entanglement**



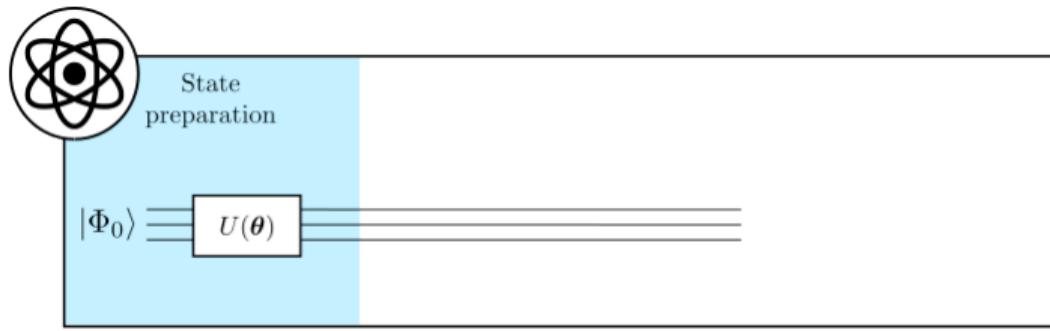
Variational Quantum Eigensolver



Start with
a very
simple state

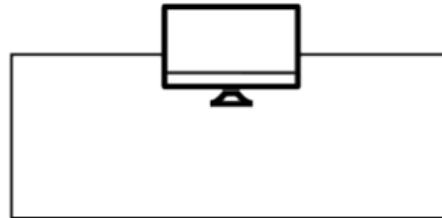


Variational Quantum Eigensolver



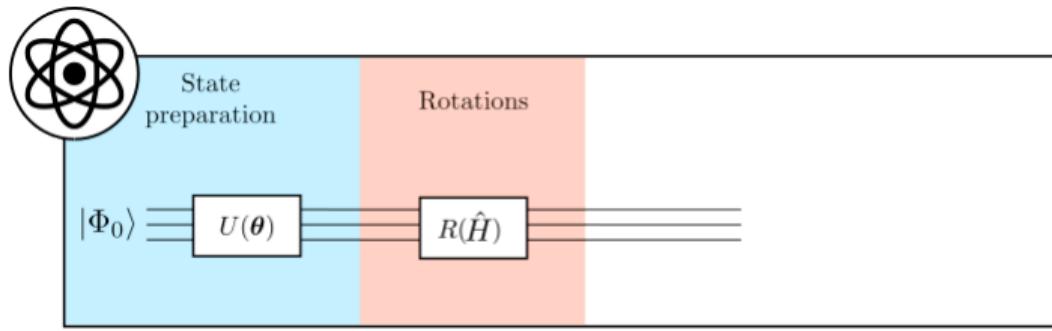
State preparation:

$$|\Psi(\theta)\rangle = U(\theta) |\Phi_0\rangle$$

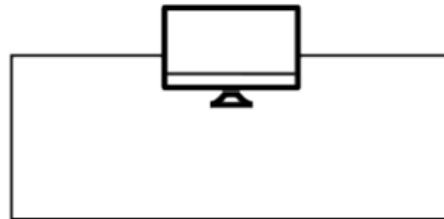




Variational Quantum Eigensolver

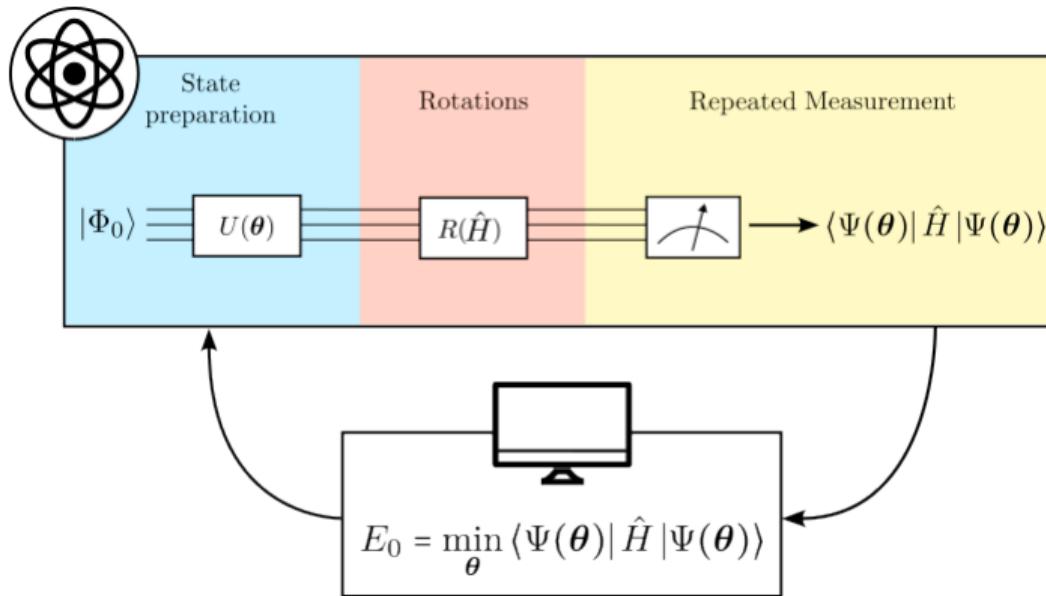


Rotations to the
computational basis





Variational Quantum Eigensolver



Measurements:
Reconstruction of the energy

Classical optimization following the
variational principle:
find new θ parameters



Table of contents

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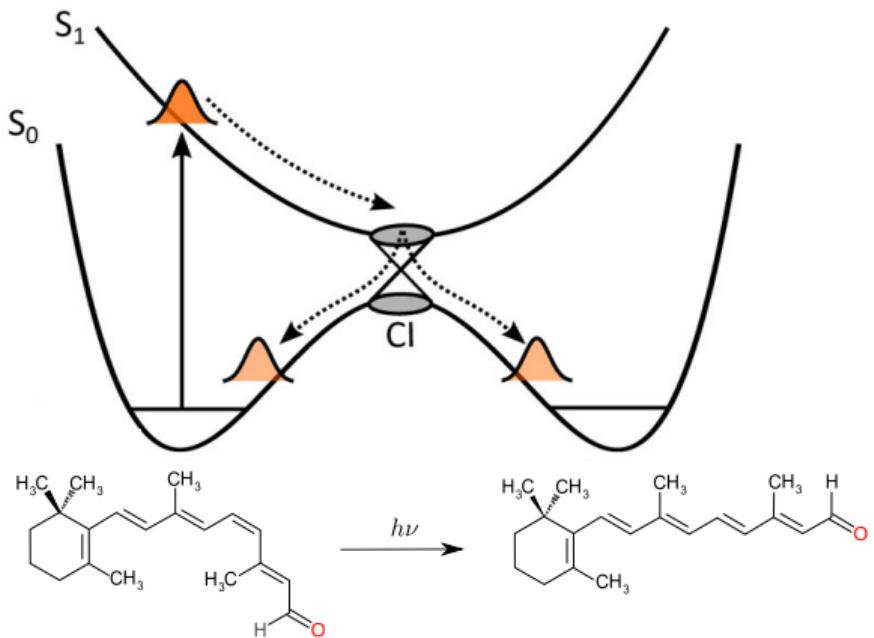
Current Works and Perspectives ; Discussion on Quantum Advantage



Problematic: avoided-crossings, conical intersections

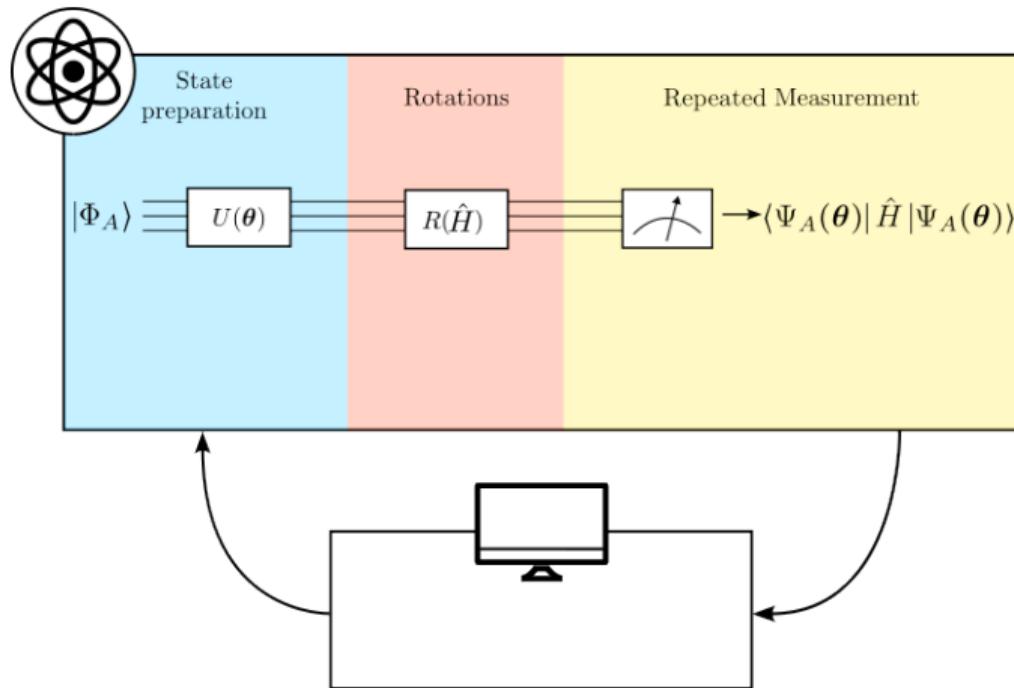
7 / 18

Photoisomerisation of the retinal molecule



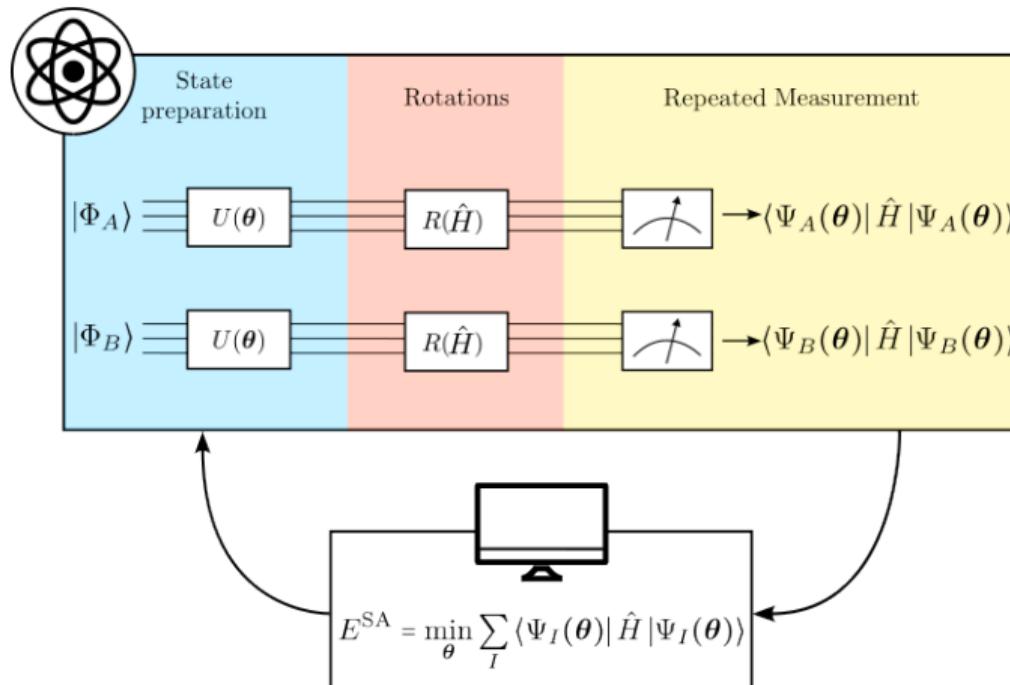
Conical intersection → Point of degeneracy between the states

Requires a
DEMOCRATIC description
of the states

Ensemble VQE¹



Ensemble VQE¹



But to a **ensemble** of states

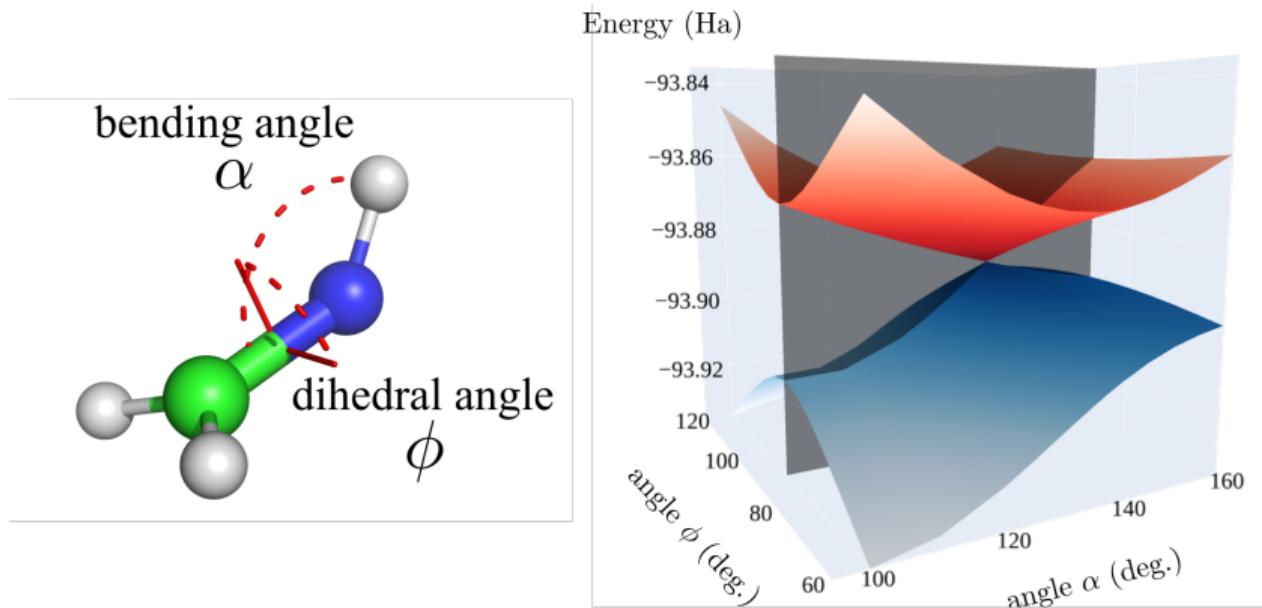
Generalized variational principle



Example on a minimal Schiff base: formaldimine

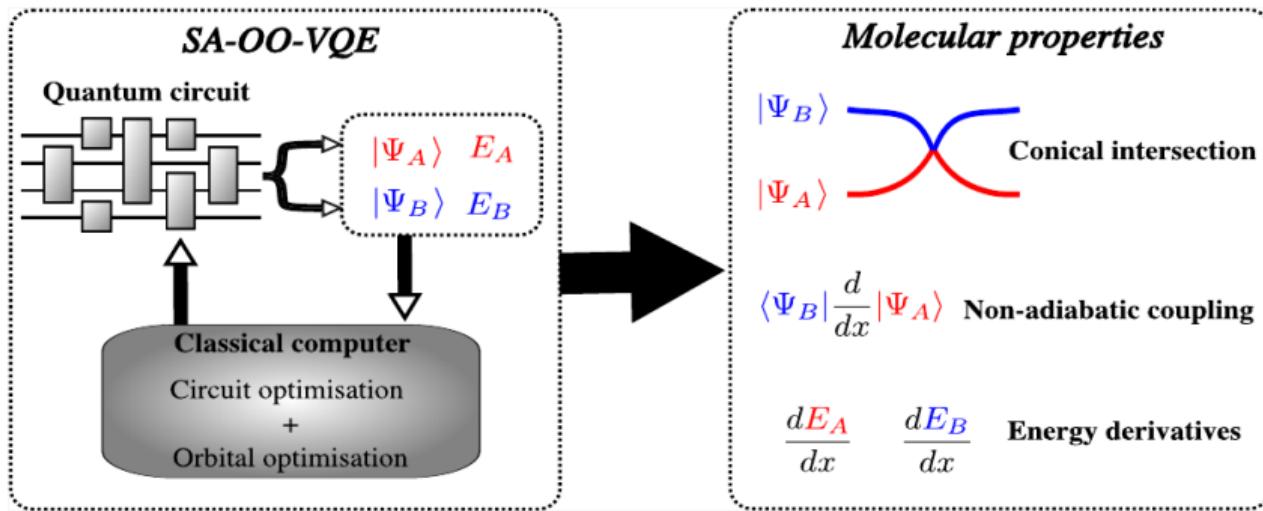
9 / 18

2D PES obtained by ensemble VQE





Towards excited-state quantum dynamics^{3,4}



- We are currently showing the ensemble VQE can lead to **quasi-diabatic states**²

²S. Illesova, M. Beseda, S. Yalouz, B. Lasorne, **BS**, to be submitted

³S. Yalouz, **BS** et al., *Quantum Sci. Technol.* 6, 024004 (2021)

⁴S. Yalouz, E. Kordion, **BS** et al. *J. Chem. Theory Comput.*, 18, 776-794 (2022)



Table of contents

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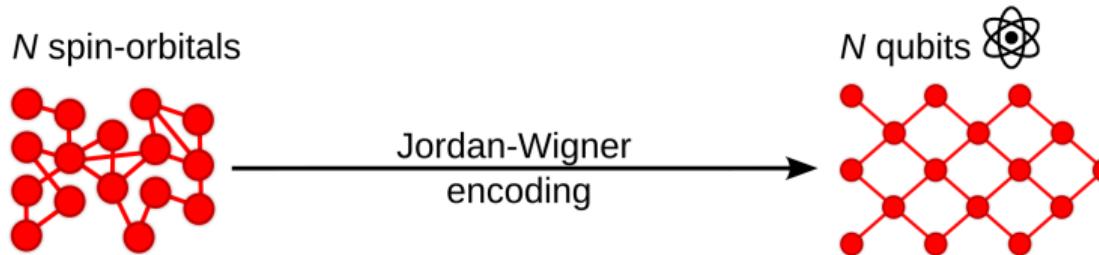
Density Functional Theory on Quantum Computers

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Mappings of the fully interacting problem

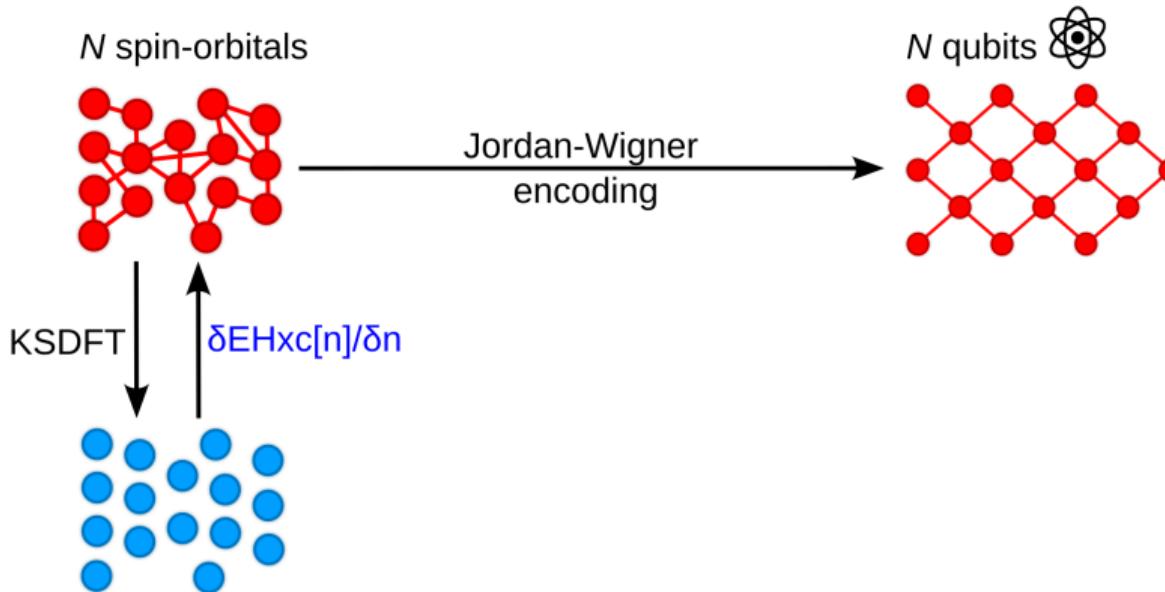
11 / 18





Mappings of the fully interacting problem

11 / 18





Density Functional Theory (DFT)

12 / 18

- ▶ (1964) Hohenberg–Kohn theorem: $n(\mathbf{r}) \longleftrightarrow v(\mathbf{r}) \longleftrightarrow \Psi_0$

$$E_0[v] = \min_n E_v[n], \quad E_v[n] = F[n] + \int d\mathbf{r} v(\mathbf{r})n(\mathbf{r})$$

The minimizing density is the **ground-state density** $n_0(\mathbf{r})$.



Density Functional Theory (DFT)

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The minimizing density is the **ground-state density** $n_0(\mathbf{r})$.

- ▶ **Universal functional:** Levy–Lieb constrained search formalism

$$F[n] = \min_{\Psi \rightarrow n} \{ \langle \Psi | \hat{T} + \hat{\mathbf{W}}_{ee} | \Psi \rangle \}$$

- ▶ The problem seems **even more complicated!**



Density Functional Theory (DFT)

12 / 18

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- ▶ **Universal functional:** Levy–Lieb constrained search formalism

$$F[n] = \min_{\Psi \rightarrow n} \{ \langle \Psi | \hat{T} + \hat{\mathbf{W}}_{ee} | \Psi \rangle \}$$

- ▶ The problem seems **even more complicated!** Decomposition:

$$F[n] = \text{unknown} = \text{known} + (\text{unknown} - \text{known})$$



Kohn-Sham DFT

13 / 18

- ▶ (1965) Kohn–Sham: noninteracting system with $n_s(\mathbf{r}) = n_0(\mathbf{r})$

$$F[n] = T_s[n] + \mathbf{E}_{\text{Hxc}}[\mathbf{n}], \quad T_s[n] = \min_{\Phi \rightarrow n} \{ \langle \Phi | \hat{T} | \Phi \rangle \}$$

- ▶ Kohn–Sham self-consistent equations:

$$\underbrace{\left(-\frac{\nabla^2}{2} + v(\mathbf{r}) + \frac{\delta \mathbf{E}_{\text{Hxc}}[\mathbf{n}_{\Phi_{\text{KS}}}] }{\delta \mathbf{n}(\mathbf{r})} \right)}_{\hat{h}^{\text{KS}}[\mathbf{n}_{\Phi_{\text{KS}}}] } \varphi_{\mathbf{k}}(\mathbf{r}) = \varepsilon_{\mathbf{k}} \varphi_{\mathbf{k}}(\mathbf{r}), \quad \mathbf{n}(\mathbf{r}) = 2 \sum_{k=1}^{N_{\text{occ}}} |\varphi_{\mathbf{k}}(\mathbf{r})|^2$$



Kohn-Sham DFT

13 / 18

- ▶ (1965) Kohn–Sham: noninteracting system with $n_s(\mathbf{r}) = n_0(\mathbf{r})$

$$F[n] = T_s[n] + \mathbf{E}_{\text{Hxc}}[\mathbf{n}], \quad T_s[n] = \min_{\Phi \rightarrow n} \{ \langle \Phi | \hat{T} | \Phi \rangle \}$$

- ▶ Kohn–Sham self-consistent equations:

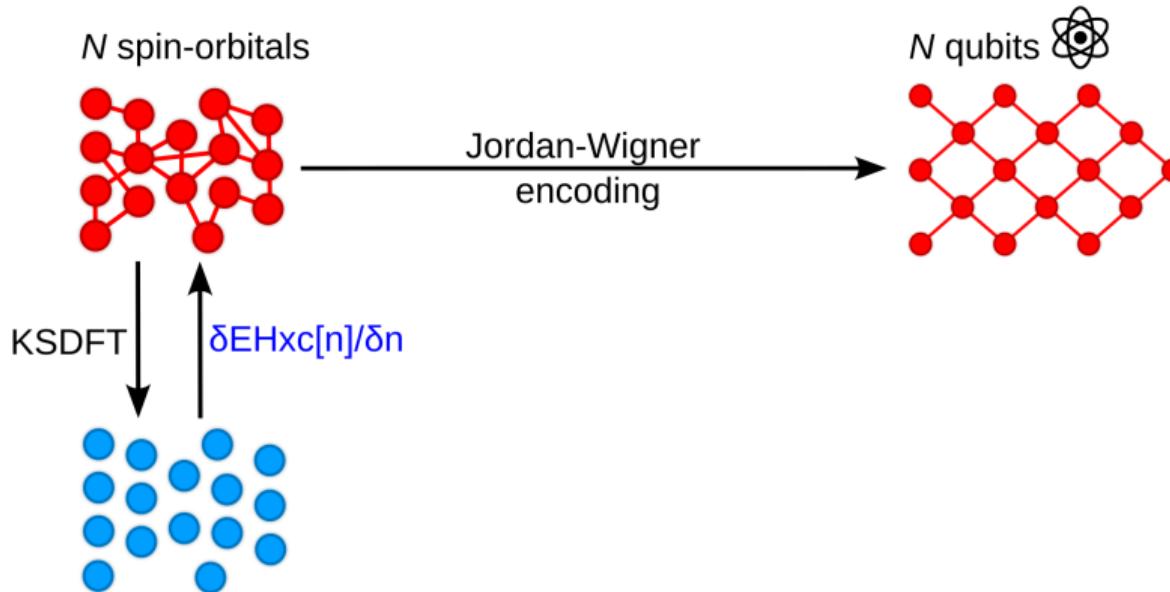
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- ▶ (in-principle-exact) Ground-state energy in $\mathcal{O}(N^3)$:

$$E_0 = 2 \sum_{k=1}^{N_{\text{occ}}} \varepsilon_{\mathbf{k}} + E_{\text{Hxc}}[\mathbf{n}^{\Phi_{\text{KS}}^\text{}}] - \int d\mathbf{r} v_{\text{Hxc}}[n^{\Phi_{\text{KS}}^\text{}}](\mathbf{r}) \mathbf{n}^{\Phi_{\text{KS}}^\text{}}(\mathbf{r})$$

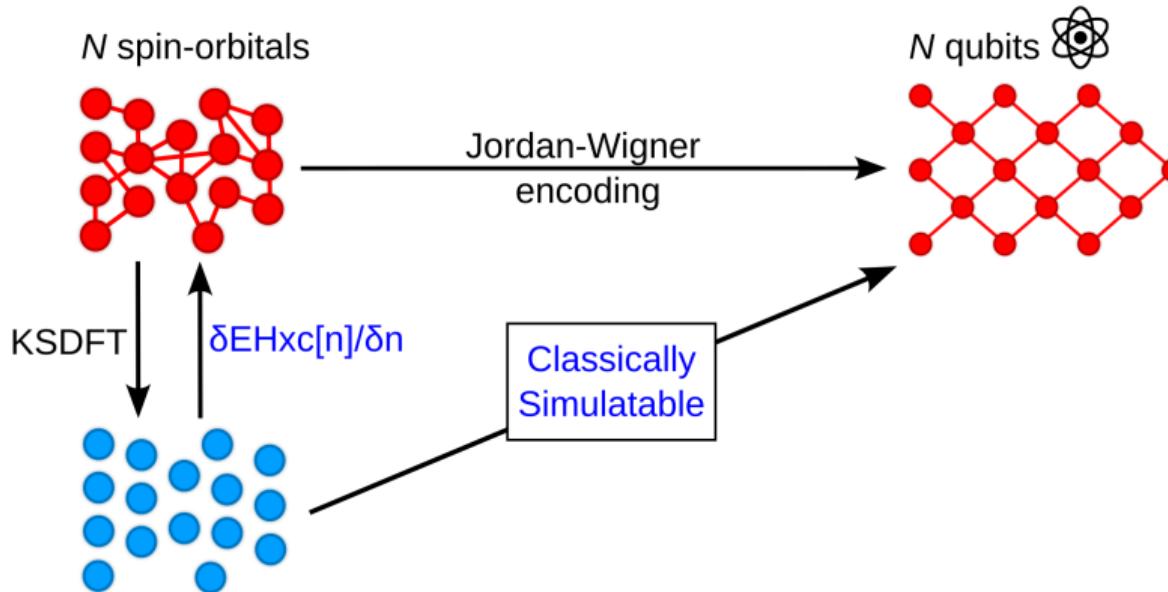


Flowchart



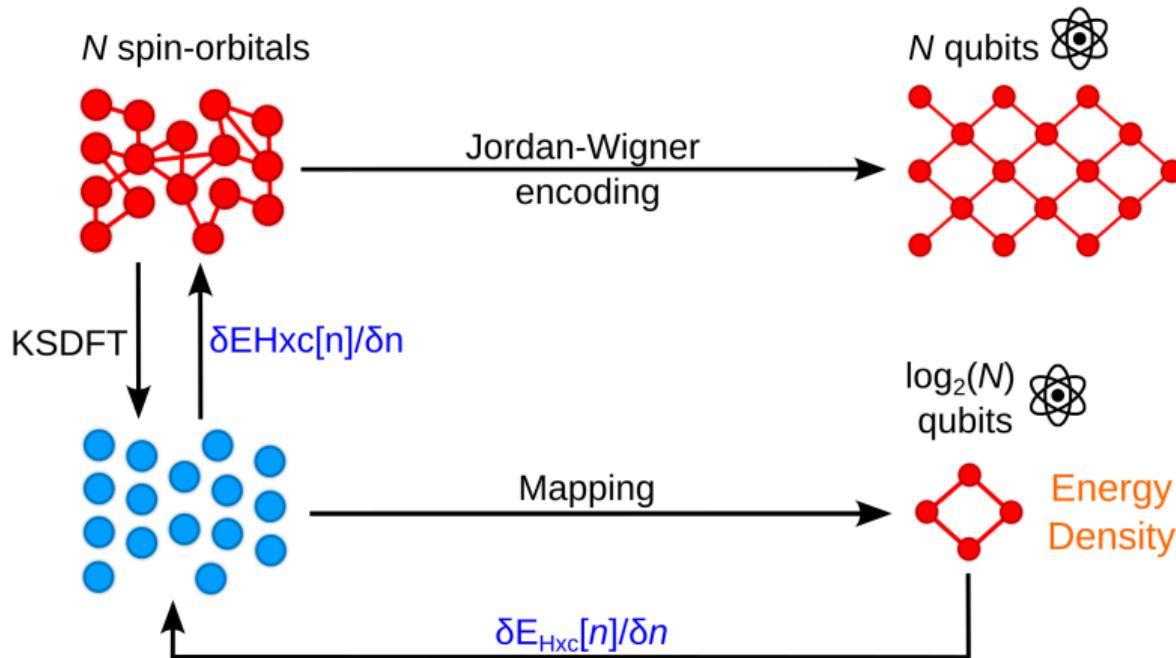


Flowchart





Flowchart





DFT encoding

15 / 18

One-body non-int. Hamiltonian with N spin-orbitals $\{|\chi_i\rangle\} \xrightarrow{\text{map}} N$ **qubits**, classically simulatable

Basis set one-body states	Unary ⁵
$ \chi_0\rangle$	$ 00000001\rangle$
$ \chi_1\rangle$	$ 00000010\rangle$
$ \chi_2\rangle$	$ 00000100\rangle$
$ \chi_3\rangle$	$ 00001000\rangle$
$ \chi_4\rangle$	$ 00010000\rangle$
$ \chi_5\rangle$	$ 00100000\rangle$
$ \chi_6\rangle$	$ 01000000\rangle$
$ \chi_7\rangle$	$ 10000000\rangle$

⁵N.P.D. Sawaya *et al.*, npj Quantum Inf 6, 49 (2020).

⁶BS, S. Yalouz, M. Saubanère, SciPost Phys. 14, 055 (2023) ; Y. Shee et al. PRR 4, 023154 (2022)



DFT encoding

15 / 18

One-body non-int. Hamiltonian with N spin-orbitals $\{|\chi_i\rangle\} \xrightarrow{\text{map}} \log_2(N)$ interacting qubits

Basis set one-body states	Unary ⁵	Standard Binary ⁶
$ \chi_0\rangle$	$ 00000001\rangle$	$ 000\rangle$
$ \chi_1\rangle$	$ 00000010\rangle$	$ 001\rangle$
$ \chi_2\rangle$	$ 00000100\rangle$	$ 010\rangle$
$ \chi_3\rangle$	$ 00001000\rangle$	$ 011\rangle$
$ \chi_4\rangle$	$ 00010000\rangle$	$ 100\rangle$
$ \chi_5\rangle$	$ 00100000\rangle$	$ 101\rangle$
$ \chi_6\rangle$	$ 01000000\rangle$	$ 110\rangle$
$ \chi_7\rangle$	$ 10000000\rangle$	$ 111\rangle$

⁵N.P.D. Sawaya *et al.*, npj Quantum Inf 6, 49 (2020).

⁶BS, S. Yalouz, M. Saubanère, SciPost Phys. 14, 055 (2023) ; Y. Shee *et al.* PRR 4, 023154 (2022)



DFT encoding

15 / 18

One-body non-int. Hamiltonian with N spin-orbitals $\{|\chi_i\rangle\} \xrightarrow{\text{map}} \log_2(N)$ interacting qubits

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$$\hat{\mathbf{h}}^{\text{KS}} |\varphi_{\mathbf{k}}\rangle = \varepsilon_{\mathbf{k}} |\varphi_{\mathbf{k}}\rangle \quad \rightarrow \quad \hat{\mathcal{H}}^{\text{aux}} |\varphi_{\mathbf{k}}\rangle = \varepsilon_{\mathbf{k}} |\varphi_{\mathbf{k}}\rangle, \quad k = 1, \dots, N_{\text{occ}} \quad \rightarrow \text{Ensemble VQE}$$

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Table of contents

Quantum Chemistry: the electronic structure problem

Quantum Computation

Ground-state Chemistry on Quantum Computers

Excited-state Chemistry on Quantum Computers

Density Functional Theory on Quantum Computers

Current Works and Perspectives ; Discussion on Quantum Advantage



Current Works and Perspectives

16 / 18

About ensemble VQE:

- ▶ Non-adiabatic excited-state dynamics

- ▶ On-the-fly calculation of diabatic states



Current Works and Perspectives

16 / 18

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- ▶ Extensions to time-dependent DFT
- ▶ Calculation of gradients to perform geometry optimization



Current Works and Perspectives

16 / 18

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Quantum Embedding methods:

- ▶ Fragmenting the system and merging different methods



Discussions

17 / 18

About the 'Noisy Intermediate Scale Quantum' era:

- ▶ Is there room for VQE (and extensions)? (Z. Holmes ArXiv ; L. Bittel PRL 2021)
- ▶ Revival of old and intractable methods such as UCC in Quantum Chemistry
- ▶ Using qubit noise in quantum algorithms (C. Bertrand and many others for open systems)



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17 / 18

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- ▶ Is it achievable? ($\sim 10^2 - 10^4$ logical qubits, $\sim 10^{10} - 10^{15}$ Toffoli gates)



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17 / 18

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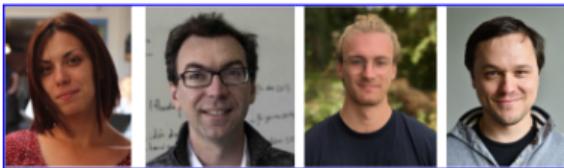
Are we only looking to (asymptotic exponential) quantum advantage?

- ▶ Exponential, polynomial or constant factor advantage (G. Chan, arXiv:2407.11235)
- ▶ No advantage?... QC is a **new path** to explore the electronic structure problem



Acknowledgments and Collaborations on Quantum Computing 18 / 18

Q-DFT on Qudits



Johanna Klein David Guéry-Odelin Eloi Flament Bruno Peaudecerf

Schrieffer-Wolf & Embedding & DFT



Quentin Marécat Matthieu Saubanère Emmanuel Fromager Wafa Makhlof

SA-OO-VQE



Emiel Kordon Thomas O'Brien Lucas Visscher

Extensions of SA-OO-VQE



Martin Beseda Silvie Illesova Benjamin Lasorne Yohann Scribano Joachim Knapik

Vibrational/Vibronic

Open-access codes:

<https://gitlab.com/MartinBeseda/sa-oo-vqe-qiskit>

<https://github.com/bsenjean/QDFT>

Q-DFT in BigDFT



Thierry Deutsch Akilan Rajamani Luigi Genovese

Kind of everything...



Saad Yalouz



Institut Charles Gerhardt Montpellier

Thank you for your attention

CHEMISTRY: MOLECULES TO MATERIALS

