



02

collaborative approaches

and

Content based approaches

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<https://towardsdatascience.com/introduction-to-recommender-systems-6c66cf15ada>

Recommender systems

Content based methods

Define a model for user-item interactions where users and/or items representations are given (explicit features).

Collaborative filtering methods

Model based

Define a model for user-item interactions where users and items representations have to be learned from interactions matrix.

Memory based

Define no model for user-item interactions and rely on similarities between users or items in terms of observed interactions.

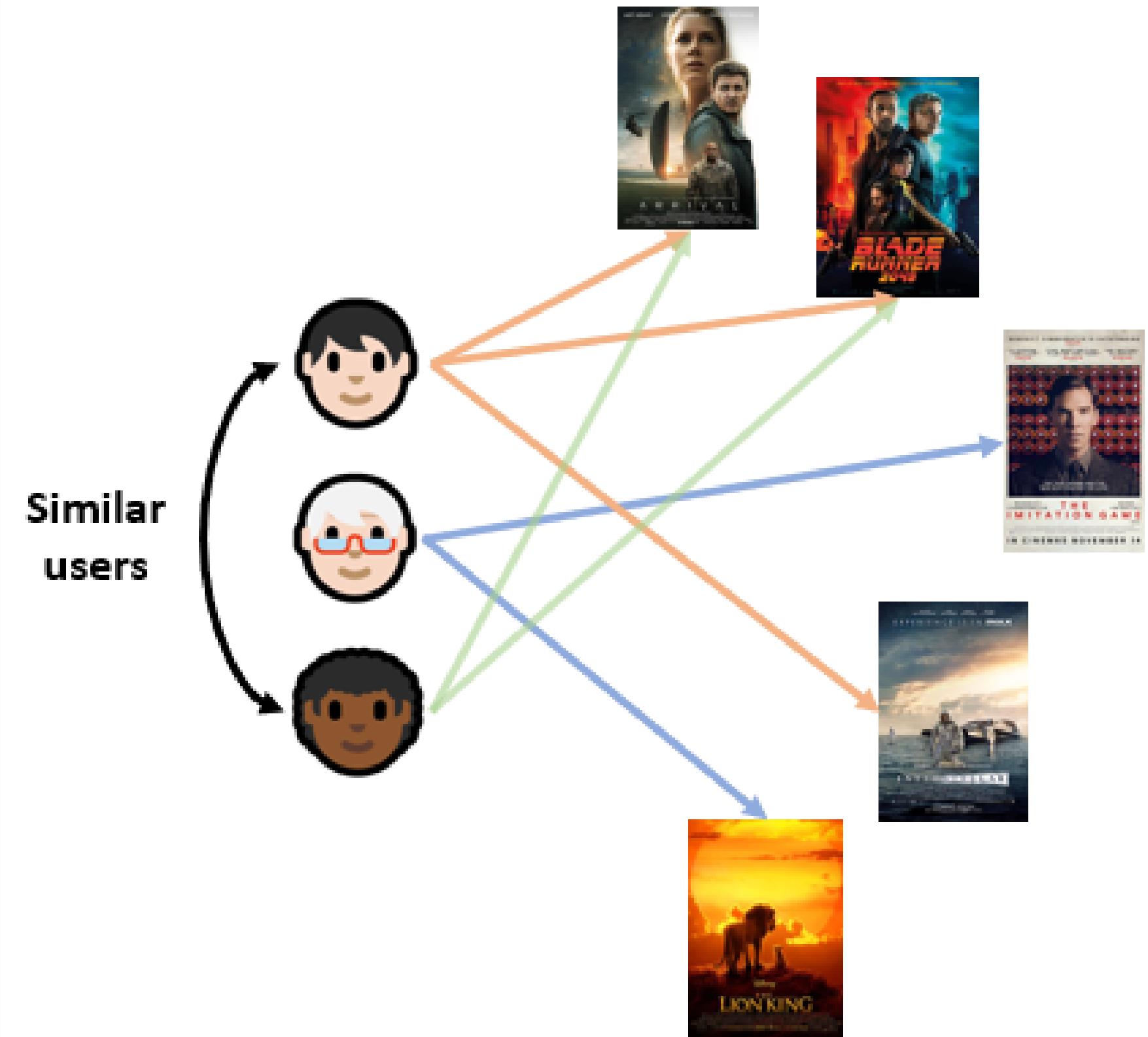
Hybrid methods

Mix content based and collaborative filtering approaches.

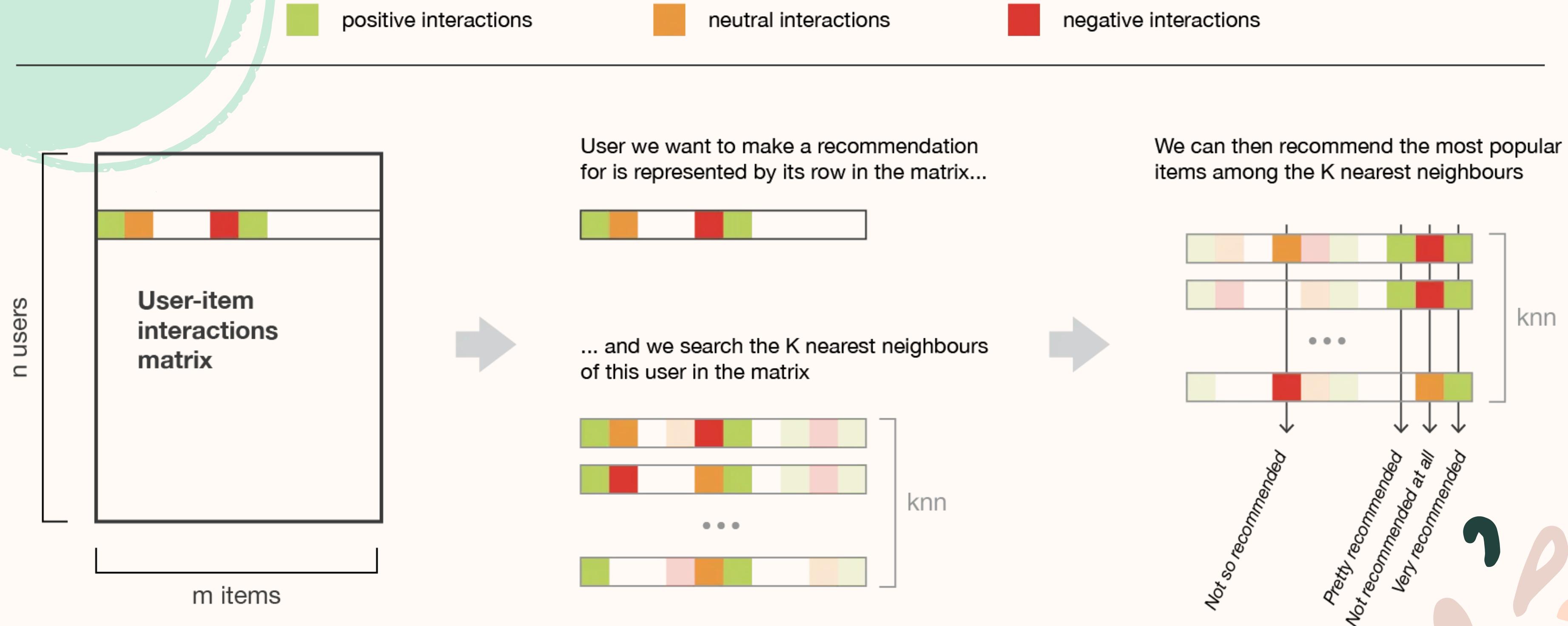
Memory based collaborative approaches



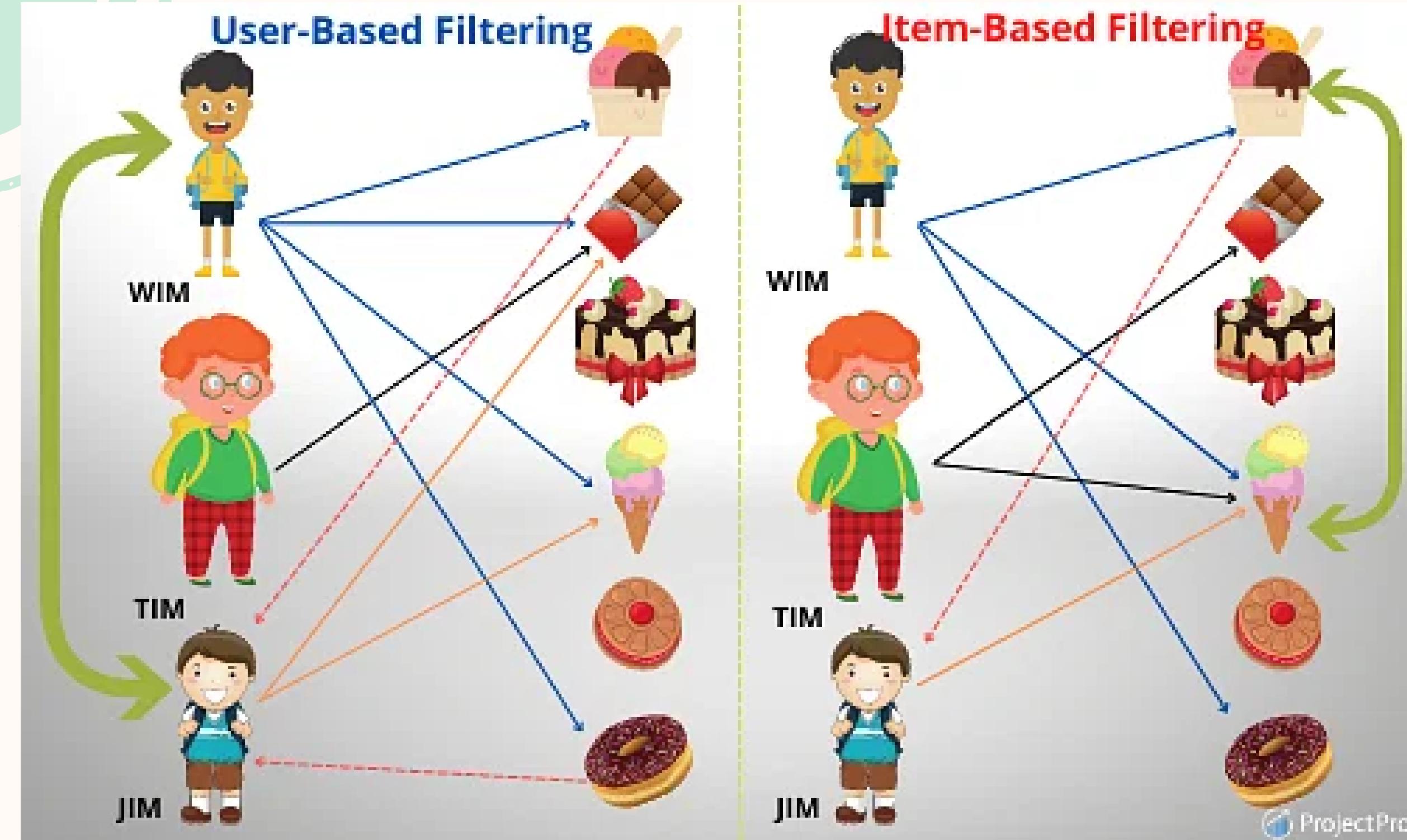
User-user



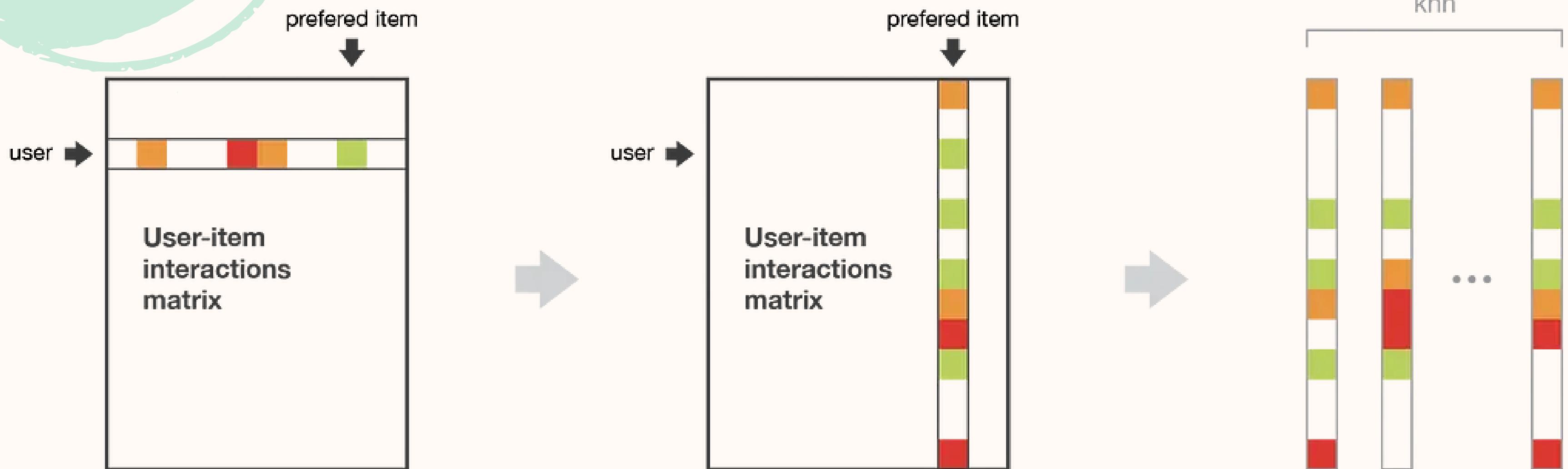
User-user



Item-item



Item-item



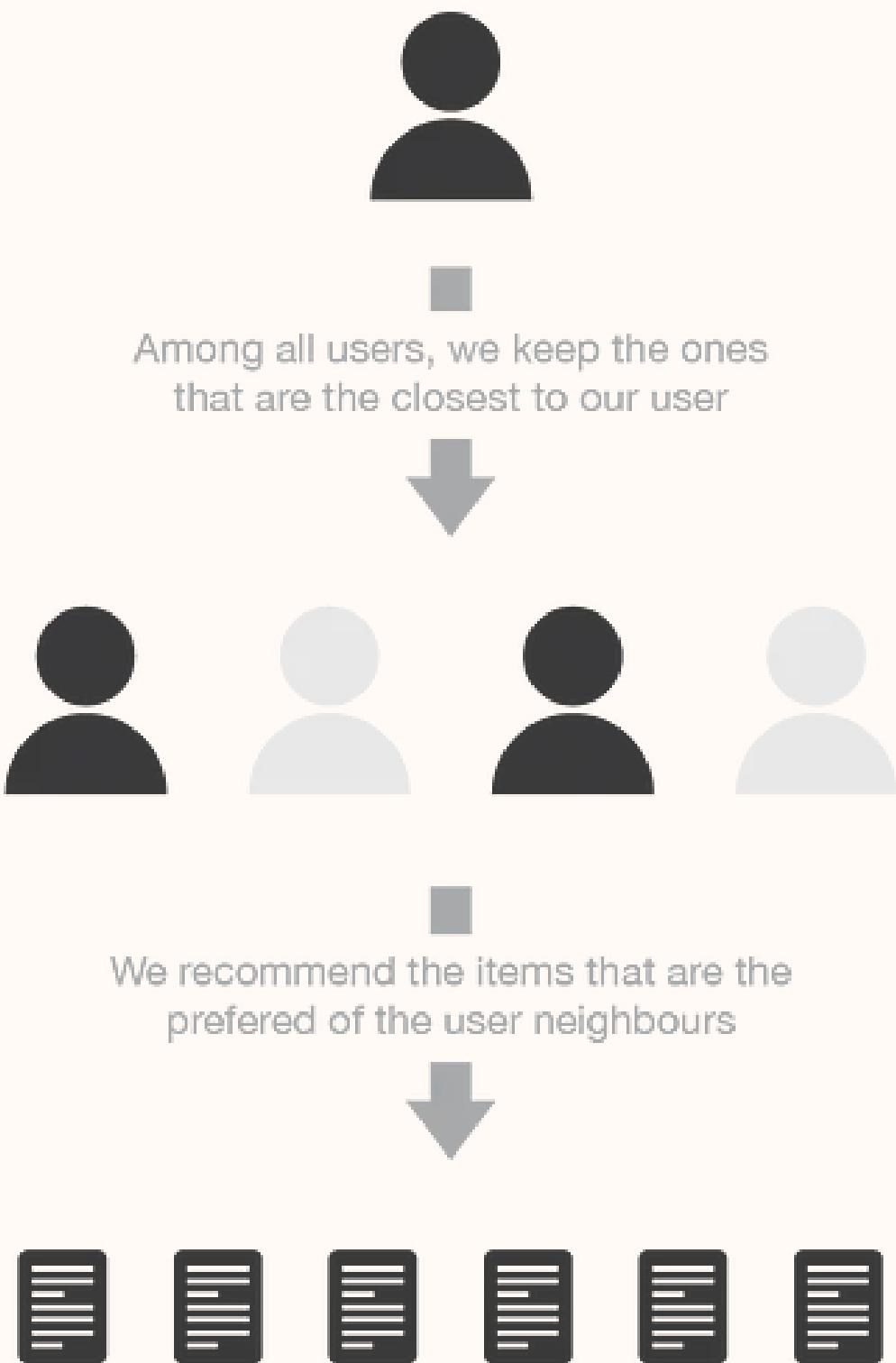
We identify the preferred item of user we want to make recommendation for.

The preferred item is represented by its column in the matrix.

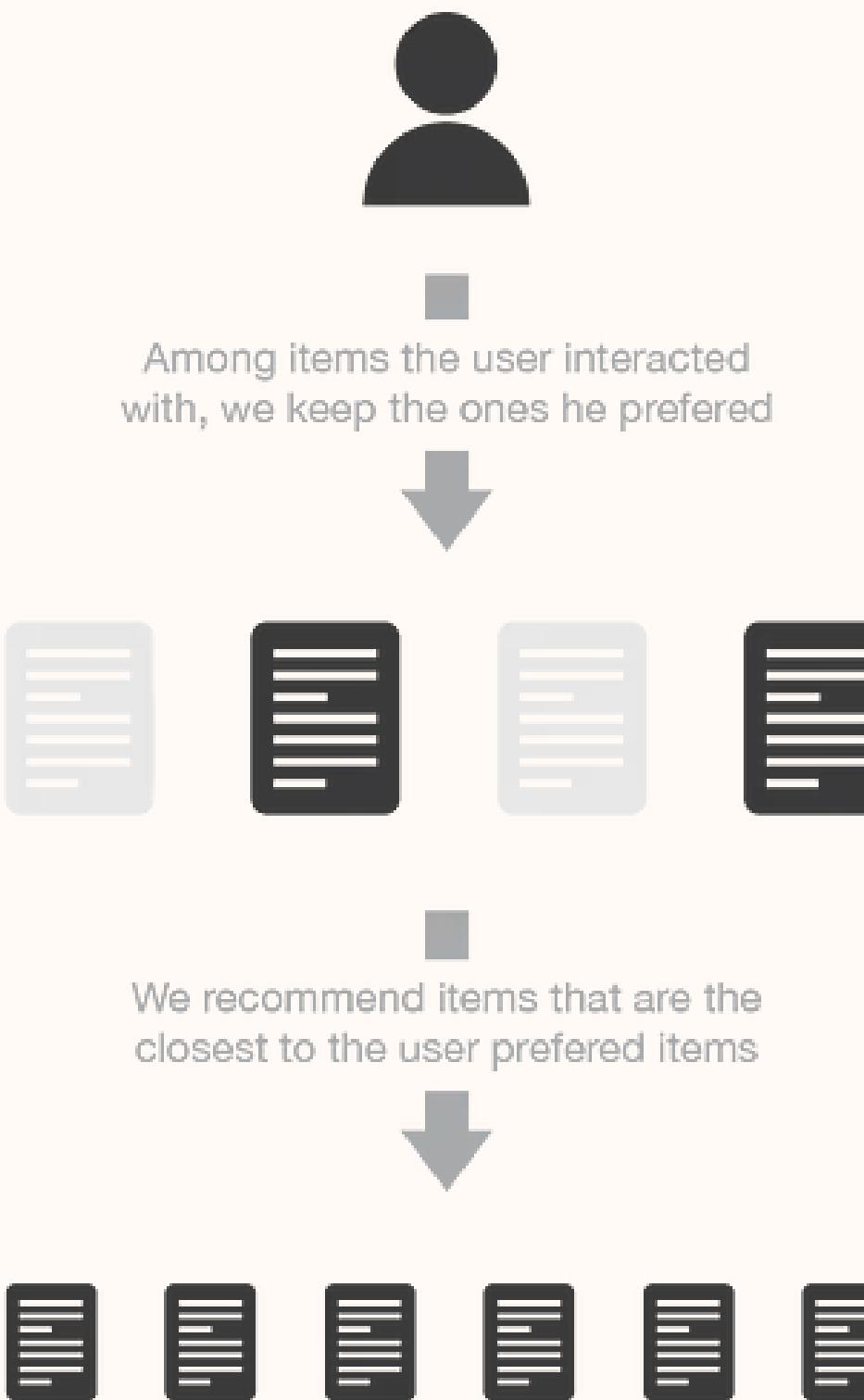
We can search and recommend the K nearest items to this "preferred item"

So sánh user-user và item-item

user-user



item-item



Độ phức tạp và tác dụng phụ

Collaborative filtering techniques	Memory-based filtering	Model-based filtering	Hybrid filtering
Advantages	Easy implementation	Better sparsity and scalability, Improve recommendation performance, Not require so much memory and cpu time	Improve sparsity
Disadvantages	Performance decrease when data are sparse, require lots of memory and cpu time	Loose useful information for dimensionality reduction technique, Expensive	Increased complexity, expensive in implementation

Model based collaborative approaches



	10	-1	8	10	9	4
	8	9	10	-1	-1	8
	10	5	4	9	-1	-1
	9	10	-1	-1	-1	3
	6	-1	-1	-1	8	10

**User-item Interaction Matrix
(R)**

$$\approx \begin{matrix} & & \\ & & \\ \text{User Matrix} & \times & \text{Item Matrix} \\ (\mathbf{Q}) & & (\mathbf{P}) \end{matrix}$$

The diagram illustrates the decomposition of the User-item Interaction Matrix (R) into two matrices: the User Matrix (Q) and the Item Matrix (P). The User Matrix (Q) is a 5x3 matrix where the first column is green, the second is orange, and the third is blue. The Item Matrix (P) is a 6x3 matrix where the first column is green, the second is orange, and the third is blue. The approximate symbol (\approx) indicates that the product of Q and P approximates R.

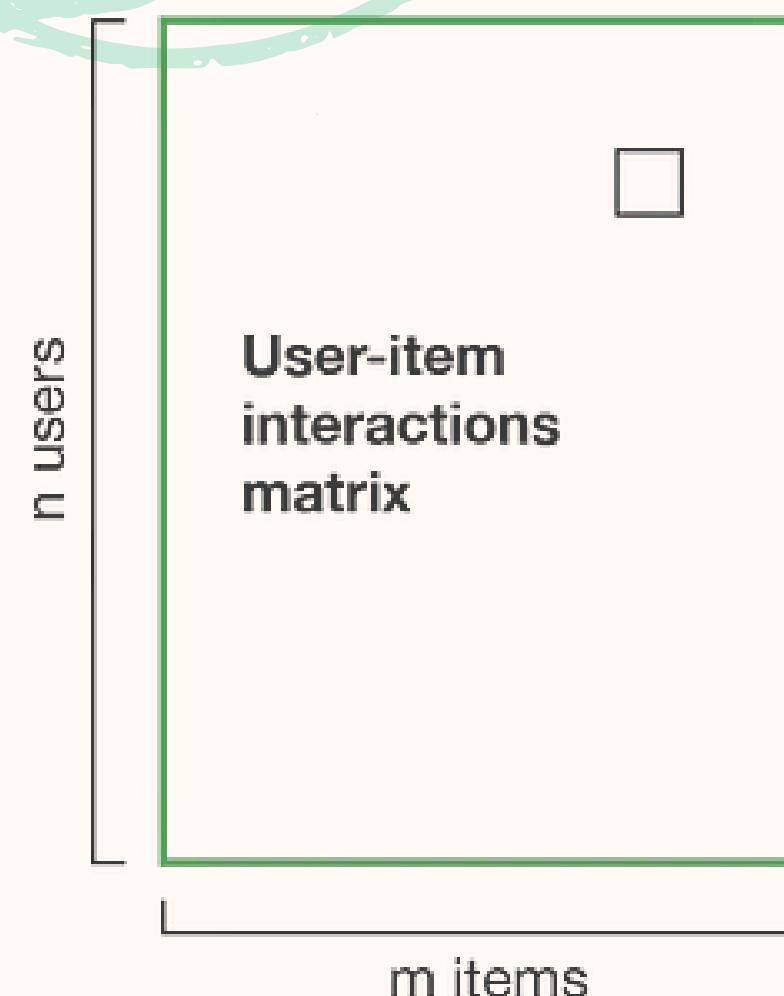
**User Matrix
(Q)**

**Item Matrix
(P)**

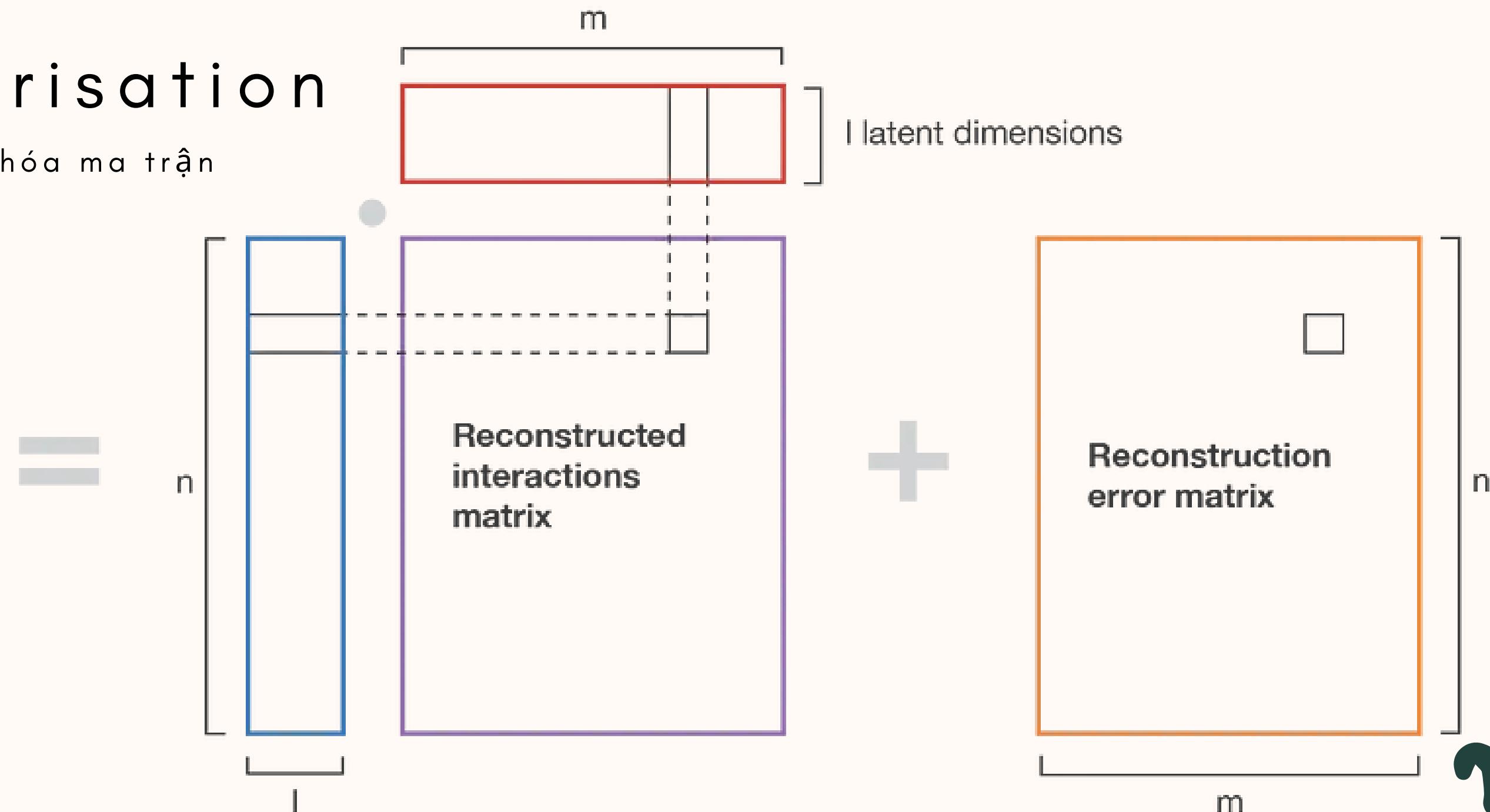
Model based collaborative approaches

Matrix factorisation

Phương pháp thừa số hóa ma trận



The **user-item interactions matrix** is assumed to be equal to...



... the **dot product** of a **user matrix** and a **transposed item matrix**...

... plus some **reconstruction error**

Model based collaborative approaches

Mathematics of matrix factorisation

$$M \approx X \cdot Y^T$$

interaction matrix M ($n \times m$)

X is the “user matrix” ($n \times l$)

Y is the “item matrix” ($m \times l$)

$$\text{user}_i \equiv X_i \quad \forall i \in \{1, \dots, n\}$$

$$\text{item}_j \equiv Y_j \quad \forall j \in \{1, \dots, m\}$$

Model based collaborative approaches

$$(X, Y) = \operatorname{argmin}_{X, Y} \sum_{(i, j) \in E} [(X_i)(Y_j)^T - M_{ij}]^2$$

E the ensemble of pairs (i, j) such that M_{ij} is set (not None),

we want to find X and Y that minimise the
“rating reconstruction error”

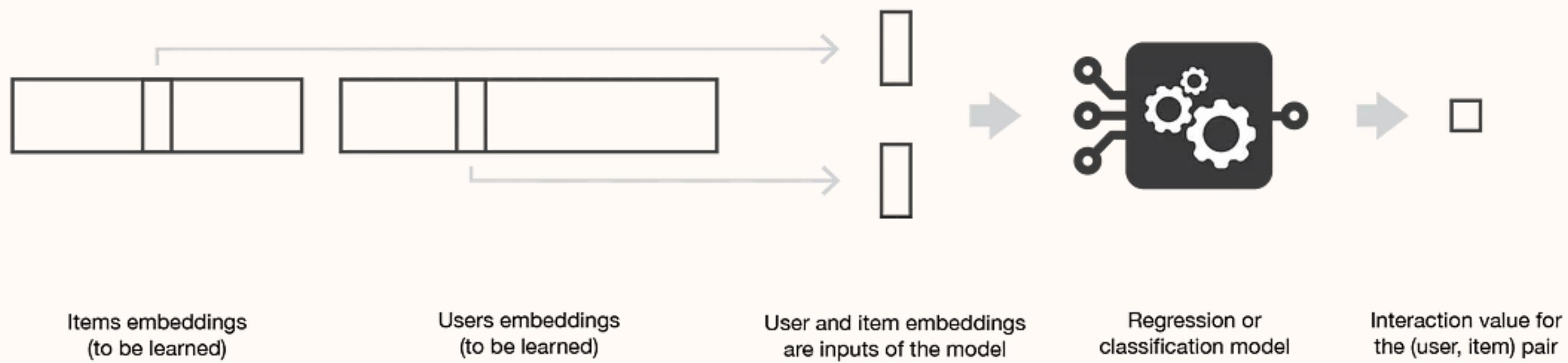
$$(X, Y) = \operatorname{argmin}_{X, Y} \frac{1}{2} \sum_{(i, j) \in E} [(X_i)(Y_j)^T - M_{ij}]^2 + \frac{\lambda}{2} \left(\sum_{i, k} (X_{ik})^2 + \sum_{j, k} (Y_{jk})^2 \right)$$

Model based collaborative approaches

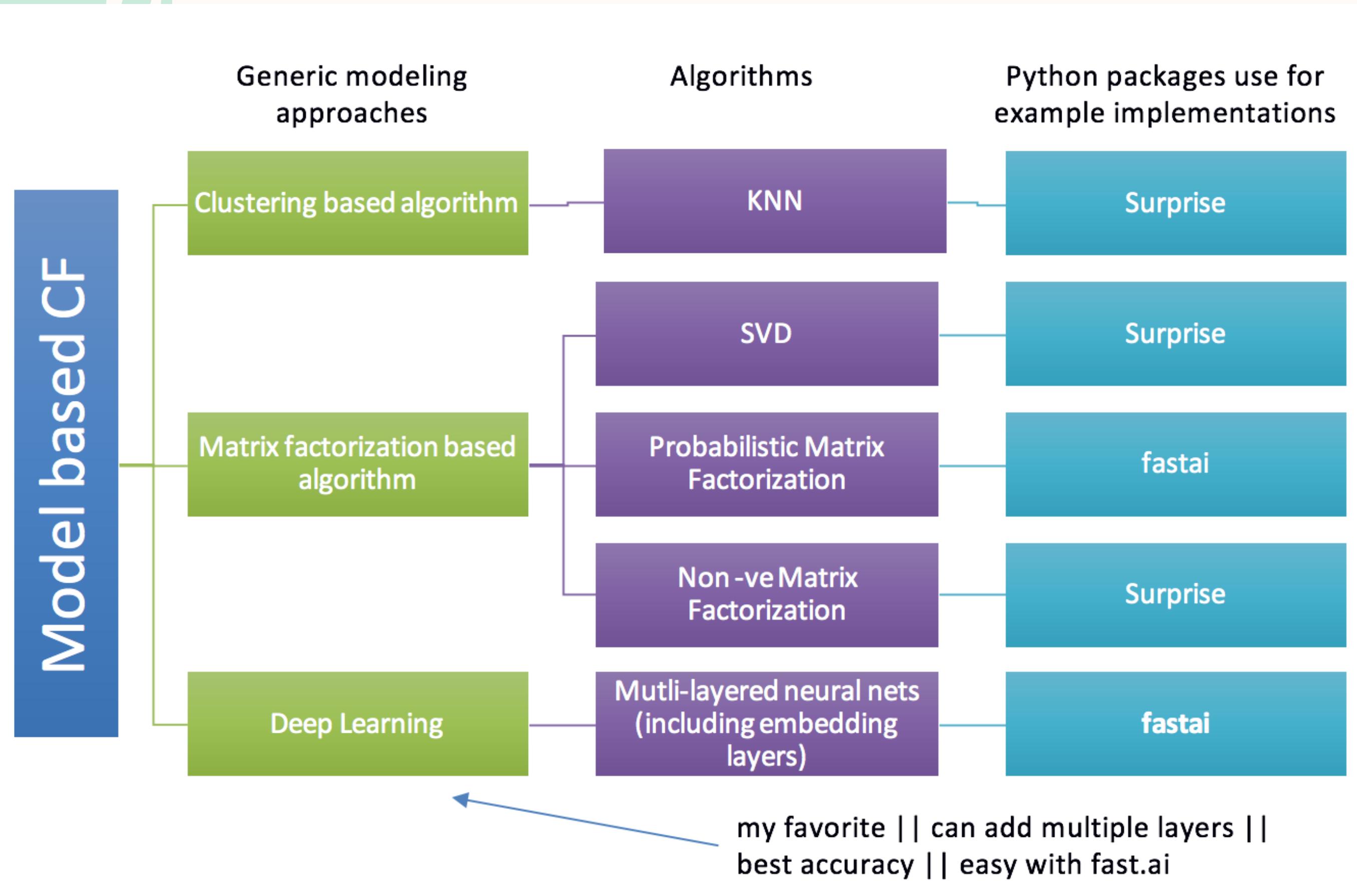
Extensions of matrix factorisation

$$(X, Y) = \underset{X, Y}{\operatorname{argmin}} \frac{1}{2} \sum_{(i,j) \in E} [f((X_i)(Y_j)^T) - M_{ij}]^2 + \frac{\lambda}{2} (\sum_{i,k} (X_{ik})^2 + \sum_{j,k} (Y_{jk})^2)$$

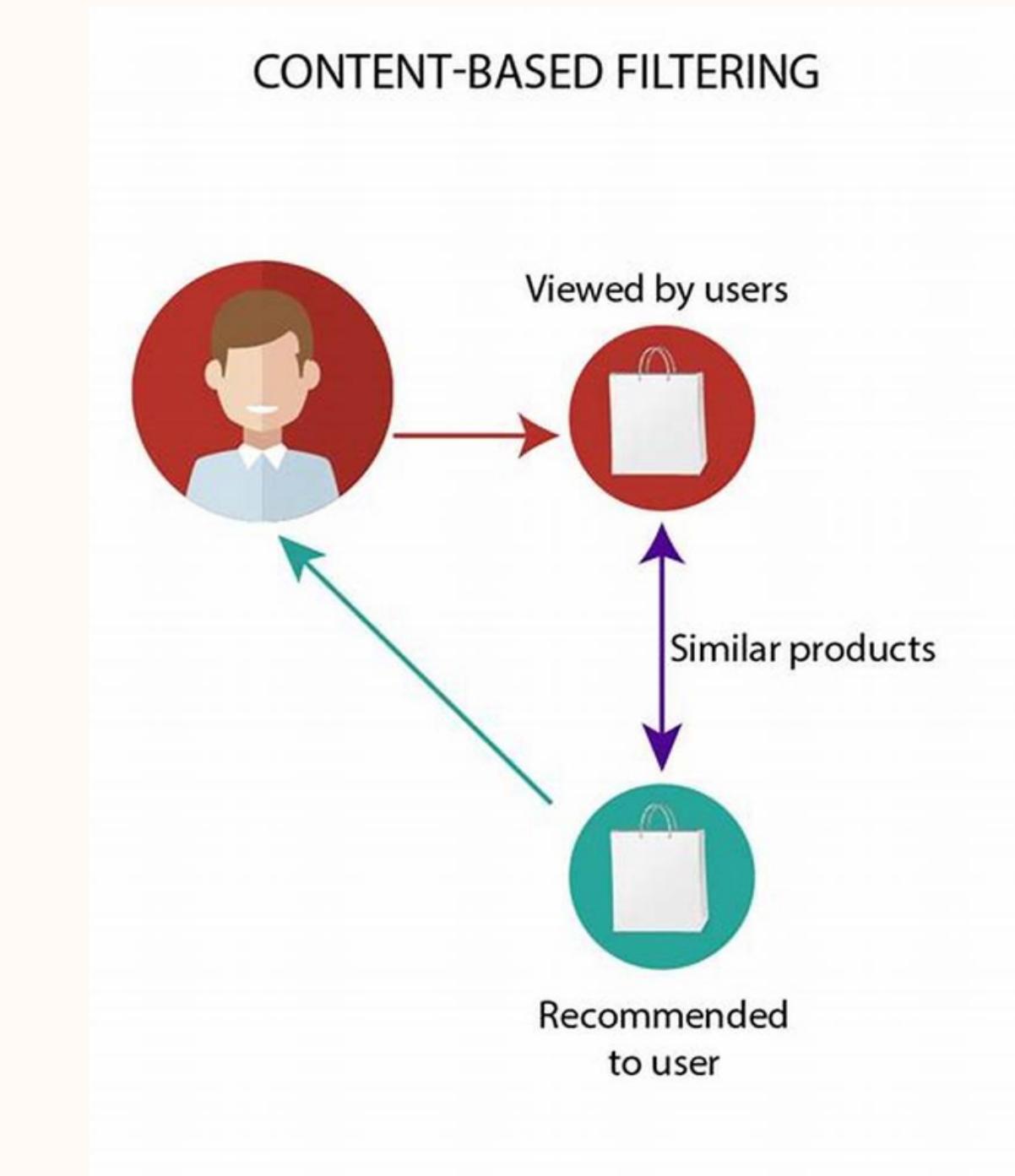
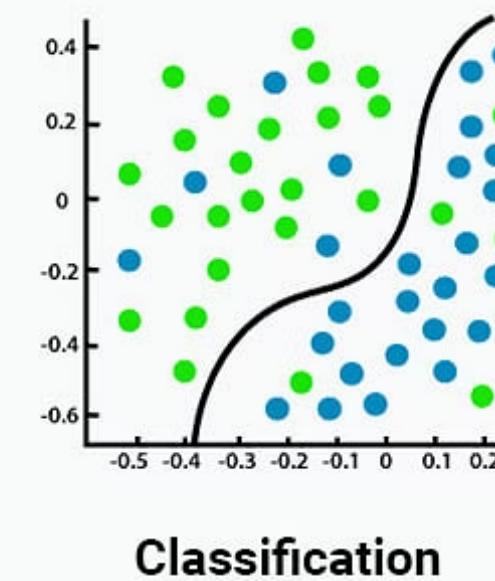
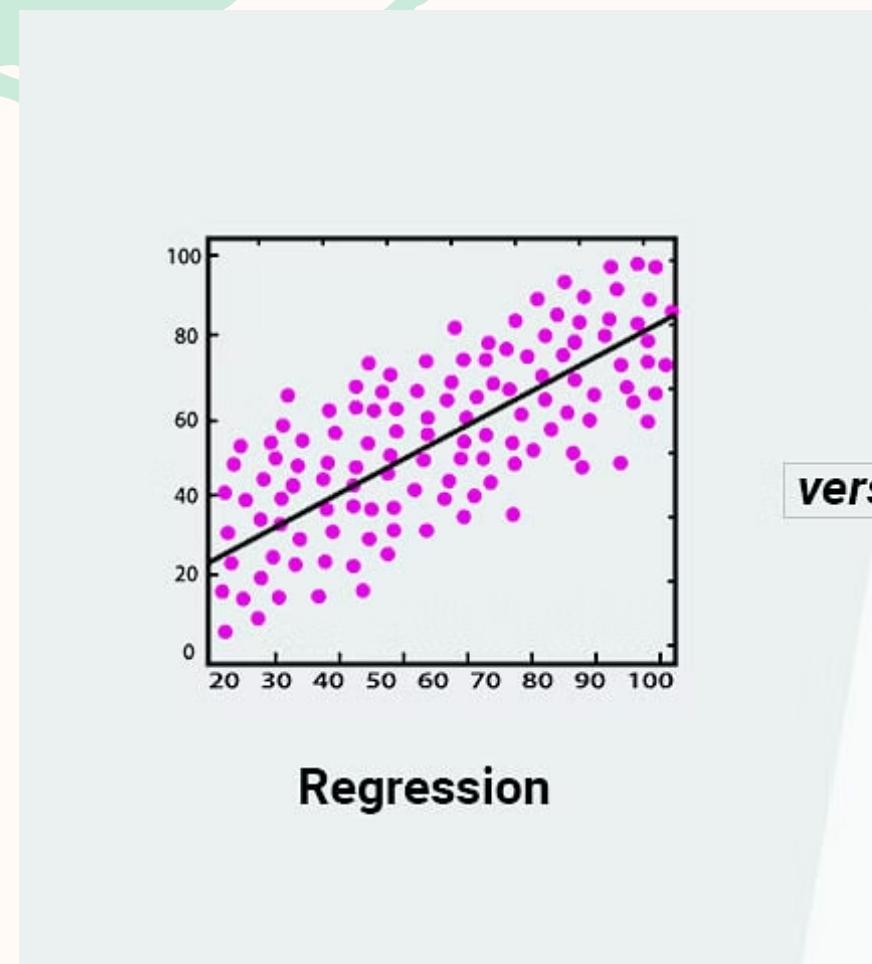
we get a model that takes its value in $[0, 1]$



Model based collaborative approaches



Content based approaches



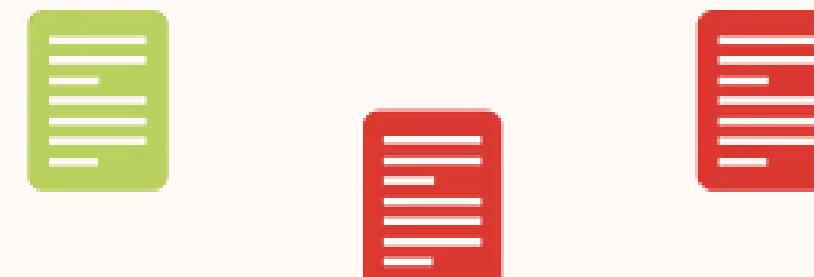
Content based approaches



Model for a given user based on items features



Items that the concerned user has interacted with (dataset)



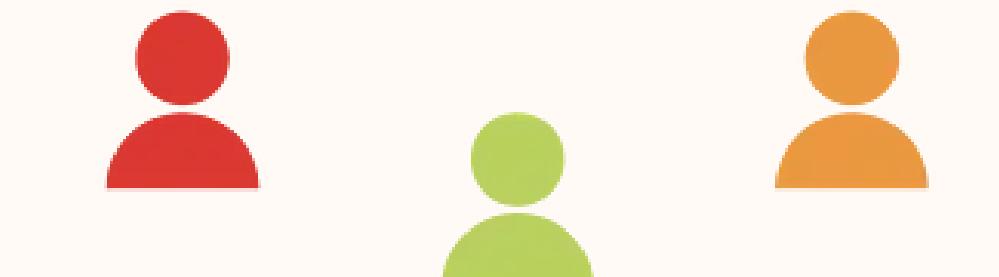
item-centred



Model for a given item based on user features



Users that have interacted with the concerned item (dataset)



user-centred

Content based approaches

Item-centred Bayesian classifier

$$\frac{\mathbb{P}_{item}(like|user_features)}{\mathbb{P}_{item}(dislike|user_features)}$$

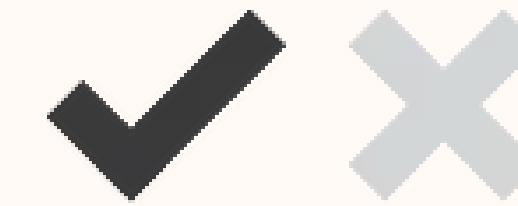
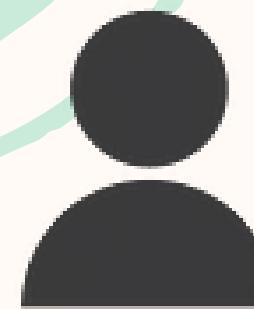
$$\mathbb{P}_{item}(like|user_features) = \frac{\mathbb{P}_{item}(user_features|like) \times \mathbb{P}_{item}(like)}{\mathbb{P}_{item}(user_features)}$$

$$\mathbb{P}_{item}(dislike|user_features) = \frac{\mathbb{P}_{item}(user_features|dislike) \times \mathbb{P}_{item}(dislike)}{\mathbb{P}_{item}(user_features)}$$

$$\frac{\mathbb{P}_{item}(like|user_features)}{\mathbb{P}_{item}(dislike|user_features)} = \frac{\mathbb{P}_{item}(user_features|like) \times \mathbb{P}_{item}(like)}{\mathbb{P}_{item}(user_features|dislike) \times \mathbb{P}_{item}(dislike)}$$

$$\mathbb{P}_{item}(like) \quad \text{and} \quad \mathbb{P}_{item}(dislike)(= 1 - \mathbb{P}_{item}(like))$$

Content based approaches



User described by some features

(features can be of various kind
and define the inputs of the model)

Bayesian classifier for a given item

(parameters of the bayesian classifier
are specific to the item and learned
on past item interactions)

Predicted class ("like" or "dislike")

(output of the bayesian classifier model
when inputs are the features of the user)

Illustration of the item-centred content
based Bayesian classifier.

Content based approaches

User-centred linear regression

$$X_i = \underset{X_i}{\operatorname{argmin}} \frac{1}{2} \sum_{(i,j) \in E} [(X_i)(Y_j)^T - M_{ij}]^2 + \frac{\lambda}{2} (\sum_k (X_{ik})^2)$$

for a given user i



Item described by some features

(features can be of various kind
and define the inputs of the model)



Linear regression for a given user

(parameters of the linear regression
are specific to the user and learned
on past user interactions)



Predicted rating

(output of the linear regression model
when inputs are the features of the item)

Evaluation of a recommender system

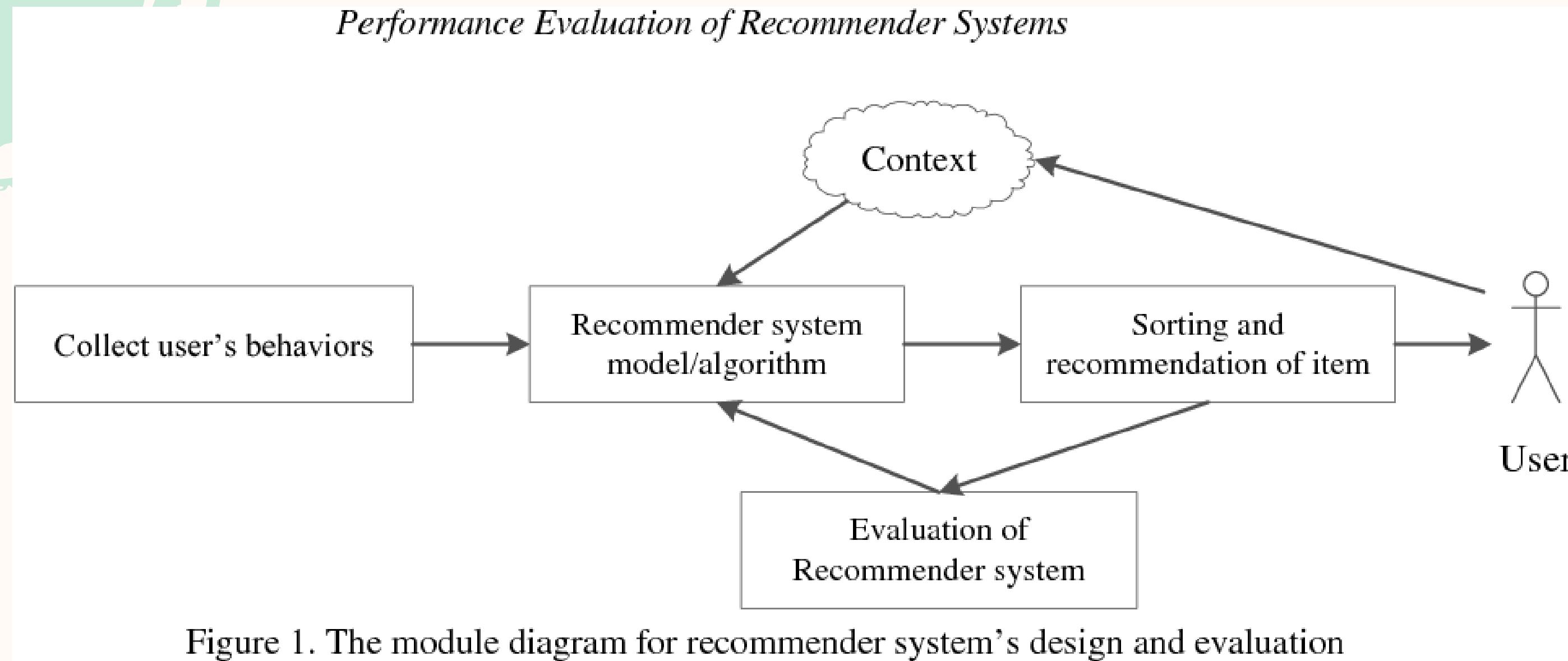


Figure 1. The module diagram for recommender system's design and evaluation

Metrics based evaluation

Human based evaluation



Thank
you