Modeling and Specification in OTS/CafeOBJ

CafeOBJ Team of JAIST

Topics

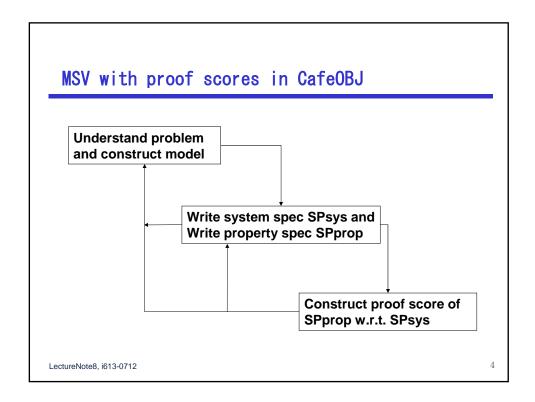
- What is QLOCK?
- Modeling and Description of QLOCK in OTS
- Formal specification of QLOCK in CafeOBJ
- Formal specification of mutual exclusion

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Modeling, Specifying, and Verifying (MSV) in CafeOBJ

- By understanding a problem to be modeled/specified, determine several sorts of <u>objects</u> (entities, data, agents, states) and <u>operations</u> (functions, actions, events) over them for describing the problem
- 2. Define the meanings/functions of the operations by declaring <u>equations</u> over expressions/terms composed of the operations
- 3. Write <u>proof scores</u> for properties to be verified

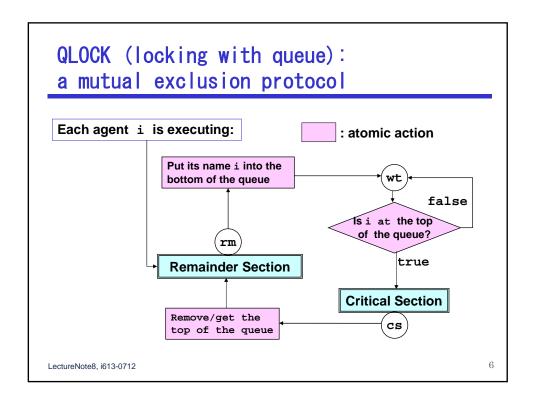
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An example: mutual exclusion protocol

Assume that many agents (or processes) are competing for a common equipment, but at any moment of time only one agent can use the equipment. That is, the agents are mutually excluded in using the equipment. A protocol (mechanism or algorithm) which can achieve the mutual exclusion is called "mutual exclusion protocol".

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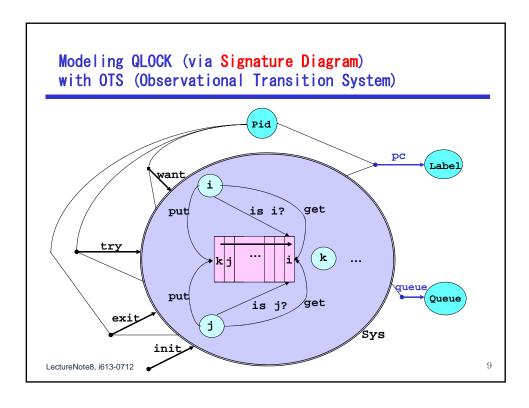
QLOCK: basic assumptions/characteristics

- There is only one queue and all agents/processes share the queue.
- Any basic action on the queue is inseparable (or atomic). That is, when any action is executed on the queue, no other action can be executed until the current action is finished.
- There may be unbounded number of agents.
- In the initial state, every agents are in the remainder section (or at the label rm), and the queue is empty.

The property to be shown is that at most one agent is in the critical section (or at the label cs) at any moment.

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Signature for QLOCKwithOTS

- Sys is the sort for representing the state space of the system.
- Pid is the sort for the set of agent/process names.
- Label is the sort for the set of labels; i.e. {rm, wt, cs}.
- Queue is the sort for the queues of Pid
- pc (program counter) is an observer returning a label where each agent resides.
- queue is an observer returning the current value of the waiting queue of Pid.
- want is an action for agent i of putting its name/id into the queue.
- try is an action for agent i of checking whether its name/id
 is at the top of the queue.
- exit is an action for agent i of removing/getting its name/id from the top of the queue.

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CafeOBJ signature for QLOCKwithOTS

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```
-- state space of the system

*[Sys]*

Hiden sort declaration

-- visible sorts for observation

[Queue Pid Label]

visible sort declaration

-- observations

bop pc : Sys Pid -> Label

bop queue : Sys -> Queue

-- actions

bop want : Sys Pid -> Sys

bop try : Sys Pid -> Sys

bop exit : Sys Pid -> Sys

bop exit : Sys Pid -> Sys
```

Module LABEL specifying (via tight denotation/semantics) "labels" qlock.mod

```
mod! LABEL {
  [Label]
  ops rm wt cs : -> Label
  pred (_=_) : Label Label {comm}
  var L : Label
  eq (L = L) = true .
  eq (rm = wt) = false .
  eq (rm = cs) = false .
  eq (wt = cs) = false .
}
```

Predicate $(_ = _)$ defines identity relation among rm, wt, and cs.

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Module PID specifying (via loose denotation) wagent/process names/identifiers"

qlock.mod

```
mod* PID {
   [Pid < PidErr]
   op none : -> PidErr
   pred (_=_) : PidErr PidErr {comm}
   var I : Pid .
   eq (I = I) = true .
   eq (none = I) = false .
   -- (none = none) is not defined intentionally
}
```

- The constant none of the sort PidErr is intended to indicate the result of getting top of the empty queue.
- Any element in the sort Pid is defined not equal to none, that is, return false for predicate (_ = _).
- Notice that (none = none) does not reduced to true or false.

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Module QUEUE specifying "queue" (1)

- an parameterized module

qlock.mod

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Module QUEUE specifying "queue" (2)

-- an parameterized module

qlock.mod

```
-- CafeOBJ variables
  var Q : Queue
  vars X Y : Elt.D
-- equations
  eq put(X,empty) = empty,X .
  eq put(X,(Q,Y)) = put(X,Q),Y .
  -- get(empty) is not defined intentionally
  eq get((Q,X)) = Q .
  eq top(empty) = (none):EltErr.D .
  eq top((Q,X)) = X .
  eq empty?(empty) = true .
  eq empty?((Q,X)) = false .
}
```

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```
Module QLOCK specifying "QLOCK" (1-1)
                                                              qlock.mod
           view TRIVerr2PID from TRIVerr to PID {
             sort Elt -> Pid,
             sort EltErr -> PidErr,
             op (none):EltErr -> (none):PidErr }
                  mod* QLOCK {
                   pr(LABEL)
                   pr(QUEUE(D <= TRIVerr2PID))</pre>
                   *[Sys]*
                  -- any initial state
                   op init : -> Sys
                  -- observations
                           : Sys Pid -> Label
                   bop pc
                   bop queue : Sys -> Queue
                  -- actions
                   bop want : Sys Pid -> Sys
                   bop try : Sys Pid -> Sys
                   bop exit : Sys Pid -> Sys
                  -- for any initial state
                   eq pc(init,I:Pid) = rm .
                   eq queue(init) = empty .
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```

Module QLOCK specifying "QLOCK" (1-2)

qlock.mod

```
mod* QLOCK {
 pr(LABEL)
  pr(QUEUE(PID{sort Elt -> Pid,
               sort EltErr -> PidErr,
               op (none):EltErr -> none):PidErr}))
 *[Sys]*
-- any initial state
 op init : -> Sys
-- observations
           : Sys Pid -> Label
 bop pc
 bop queue : Sys -> Queue
-- actions
 bop want : Sys Pid -> Sys
 bop try : Sys Pid -> Sys
bop exit : Sys Pid -> Sys
-- for any initial state
  eq pc(init,I:Pid) = rm .
  eq queue(init) = empty .
```

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Module QLOCK specifying "QLOCK" (2)

qlock.mod

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Module QLOCK specifying "QLOCK" (3)

qlock.mod

```
op c-try : Sys Pid -> Bool {strat: (0 1 2)}
 eq c-try(S,I) = (pc(S,I) = wt and top(queue(S)) = I).
 ceq pc(try(S,I),J)
    = (if I = J then cs else pc(S,J) fi) if c-try(S,I) .
 eq queue(try(S,I)) = queue(S) .
 ceq try(S,I)
                     = S
                                          if not c-try(S,I) .
-- for exit
 op c-exit : Sys Pid -> Bool {strat: (0 1 2)}
 eq c-exit(S,I) = (pc(S,I) = cs).
 ceq pc(exit(S,I),J)
    = (if I = J then rm else pc(S,J) fi) if c-exit(S,I) .
 ceq queue(exit(S,I)) = get(queue(S))
                                         if c-exit(S,I) .
 ceq exit(S,I)
                      = S
                                          if not c-exit(S,I) .
```

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(_ =*= _) is congruent for OTS

The binary relation (S1:Sys =*= S2:Sys) is defined to be true iff S1 and S2 have the same observation values.

OTS style of defining the possible changes of the values of obervations is characterized by the equations of the form: $o(a(s,d),d') = \ldots o_1(s,d_1)\ldots o_2(s,d_2)\ldots o_n(s,d_n)\ldots$ for appropriate data values of d,d',d_1,d_2,\ldots,d_n .

It can be shown that OTS style guarantees that (_ =*= _) is congruent with respect to all actions.

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R_{QLOCK} (set of reachable states) of $\text{OTS}_{\text{QLOCK}}$ (OTS defined by the module QLOCK)

Signature determining R_{QLOCK}

```
-- any initial state
op init: -> Sys
-- actions
bop want: Sys Pid -> Sys
bop try: Sys Pid -> Sys
bop exit: Sys Pid -> Sys
```

Recursive definition of R_{QLOCK}

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Mutual exclusion property as an invariant

invariants-0.mod

Formulation of proof goal for mutual exclusion property

```
INV1 |= \forall s \in R_{OLOCK} \forall i, j \in Pid.inv1(s, i, j)
```

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Induction scheme induced by the structure of R_{QLOCK}

```
mx(s) = def = \forall i, j \in Pid.inv1(s, i, j)
```

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