# University of Science

# Sorting Algorithms - An Overview

# Data Structures and Algorithms

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#### Abstract

Sorting is nothing but alphabetizing, categorizing, arranging, or putting items in an ordered sequence. It is a key fundamental operation in the field of computer science. It is of extreme importance because it adds usefulness to data. In this report, I have compared eleven common sorting algorithms (Selection Sort, Insertion Sort, Bubble Sort, Shaker Sort, Shell Sort, Heap Sort, Merge Sort, Quick Sort, Counting Sort, Radix Sort, and Flash Sort). I have developed a program in C++, Python and experimented with several input sizes 10,000, 30,000, 50,000, 100,000, 300,000, and 500,000 elements. The performance and efficiency of these algorithms in terms of CPU time consumption as well as the number of comparisons that have been recorded and presented in tabular and graphical form.

#### 1. Introduction

Sorting is not a leap but it has emerged in parallel with the development of the human mind. In computer science, alphabetizing, arranging, categorizing, or putting data items in an ordered sequence on the basis of similar properties is called sorting. Sorting is of key importance because it optimizes the usefulness of data. We can observe plenty of sorting examples in our daily life, e.g. we can easily find required items in a shopping mall or utility store because the items are kept categorically.

The items to be sorted may be in various forms i.e. random as a whole, already sorted, very small or extremely large in numer, sorted in reverse order etc. There is no algorithm that is best for sorting all types of data. We must be familiar with sorting algorithms in terms of their suitability in a particular situation.

In this paper, I am going to compare eleven common sorting algorithms (Selection Sort, Insertion Sort, Bubble Sort, Shaker Sort, Shell Sort, Heap Sort, Merge Sort, Quick Sort, Counting Sort, Radix Sort, and Flash Sort) for their CPU time consumption and number of compared operations on four different data arrangements (Sorted data (in ascending order), Nearly sorted data, Revherse sorted data, and Randomized data).

# 2. Algorithm presentation

#### 2.1. Selection Sort

#### Idea

The Selection Sort is based on the idea of finding the minimum element in an unsorted array and then putting it in its correct position in a sorted array.

#### Pseudo code

```
Algorithm 2.1: Selection Sort
  Input: a_1, a_2, ..., a_N
  Output: a_1, a_2, ..., a_N (in sorted)
1 for i \leftarrow 1 to N do
      minIndex \leftarrow i
       for j \leftarrow i + 1 to N do
3
           if a_{minIndex} > a_j then
4
               minIndex \leftarrow j
5
           end
6
7
      end
8
      \operatorname{swap}(a_{minIndex}, a_i)
9 end
```

## Complexity

Best case time complexity:  $O(N^2)$ Worst case time complexity:  $O(N^2)$ Worst case space complexity: O(1)

#### 2.2. Insertion Sort

#### Idea

The main idea of insertion sort is that array is divided in two parts which left part is already sorted, and right part is unsorted. Values from the unsorted part are picked and placed at the correct position in the sorted part. So, at every iteration sorted part grows by one element which is called key. During an iteration, if compared element is greater than key then compared element has to shift to right to open a position for key.

### Algorithm 2.2: Insertion Sort

```
Input: a_1, a_2, ..., a_N
   Output: a_1, a_2, ..., a_N (in sorted)
1 for i \leftarrow 2 to N do
       k \leftarrow i - 1
       key \leftarrow a_i
3
        while a_k > key and k \ge 0 do
4
            a_{k+1} \leftarrow a_k
5
             k \leftarrow k - 1
6
7
        \mathbf{end}
8
       a_{k+1} \leftarrow key
9 end
```

#### Complexity

Best case time complexity: O(N)Average case time complexity:  $O(N^2)$ Worst case time complexity:  $O(N^2)$ Worst case space complexity: O(1)

#### 2.3. Bubble Sort

#### Idea

Bubble sort is based on the idea of repeatedly comparing pairs of adjacent elements and then swapping their positions if they exist in the wrong order.

#### Pseudo code

```
Algorithm 2.3: Bubble Sort
```

```
Input: a_1, a_2, ..., a_N
    Output: a_1, a_2, ..., a_N (in sorted)
 1 for i \leftarrow N to 1 do
        isSwap \leftarrow False
 \mathbf{2}
        for j \leftarrow 1 to i - 1 do
 3
             if a_i > a_{i+1} then
 4
                  isSwap \leftarrow True
 \mathbf{5}
                 \operatorname{swap}(a_j, a_{j+1})
 6
             end
 7
        end
 8
        if isSwap = False then
 9
            stop algorithm
10
        end
11
12 end
```

In this paper, I implemented bubble sort with a flag isSwap to stop the algorithm early when the array is sorted.

#### Complexity

Best case time complexity: O(N)Average case time complexity:  $O(N^2)$  Worst case time complexity:  $O(N^2)$ Worst case space complexity: O(1)

#### 2.4. Shaker Sort

#### Idea

Shaker sort is a bidirectional version of bubble sort. The Bubble sort algorithm always traverses elements from left and moves the largest element to its correct position in first iteration and second largest in second iteration and so on. Shaker sort orders the array in both directions. Hence every iteration of the algorithm consists of two phases. In the first one, the lightest bubble ascends to the end of the array, in the second phase the heaviest bubble descends to the beginning of the array.

#### Pseudo code

### Algorithm 2.4: Shaker Sort

```
Input: a_1, a_2, ..., a_N
    Output: a_1, a_2, ..., a_N (in sorted)
 1 left \leftarrow 0
 \mathbf{2} \ right \leftarrow N-1
 \mathbf{s} \ k \leftarrow 0
 4 for i \leftarrow left to right do
         // phase 1
         isSwap \leftarrow False
 5
         for j \leftarrow left \ to \ right - 1 \ do
 6
             if a_j > a_{j+1} then
 7
                  isSwap \leftarrow True
 9
                  \operatorname{swap}(a_i, a_{i+1})
                  k \leftarrow j
10
             end
11
         end
12
         if isSwap = False then
13
             stop algorithm
14
         end
15
         right \leftarrow k
16
         // phase 2
17
         isSwap \leftarrow False
         for j \leftarrow right \ to \ left + 1 \ do
18
             if a_i < a_{i-1} then
19
                  isSwap \leftarrow True
20
                  \operatorname{swap}(a_j, a_{j-1})
21
                  k \leftarrow j
22
             end
23
         end
\mathbf{24}
         if isSwap = False then
25
26
             stop algorithm
27
         end
         left \leftarrow k
28
29 end
```

Best case time complexity: O(N)Average case time complexity:  $O(N^2)$ Worst case time complexity:  $O(N^2)$ Worst case space complexity: O(1)

#### 2.5. Shell Sort

#### Idea

Shell sort is a generalized version of the insertion sort algorithm. It first sorts elements that are far apart from each other and successively reduces the interval between the elements to be sorted.

The interval between the elements is reduced based on the sequence used. Some of the optimal sequences that can be used in the shell sort algorithm are:

- Shell's original sequence
- Knuth's increments
- Sedgewick's increments
- Hibbard's increments
- ..

In this paper, I only implemented the algorithm with optimal sequence based on Shell's original sequence.

#### Pseudo code

```
Algorithm 2.5: Shell Sort
    Input: a_1, a_2, ..., a_N
    Output: a_1, a_2, ..., a_N (in sorted)
 1 interval \leftarrow \frac{N}{2}
 2 while interval > 0 do
 3
         for i \leftarrow interval \ to \ N \ do
             temp \leftarrow a_i
 4
 \mathbf{5}
             while interval \leq j and a_{j-interval} > temp do
 6
 7
                  a_j \leftarrow a_{j-interval}
                  j \leftarrow j - interval
 8
             end
 9
10
         end
         a_i \leftarrow temp
11
        interval \leftarrow \frac{interval}{2}
12
13 end
```

### Complexity

Best case time complexity: O(N)Average case time complexity:  $O(N \log N)$ Worst case time complexity:  $O(N^2)$ Worst case space complexity: O(1)

## 2.6. Heap Sort

#### Idea

Heap sort is a comparison-based sorting algorithm. Heap sort can be thought of as an improved selection sort: like selection sort, heap sort divides its input into a sorted and an unsorted region, and it iteratively shrinks the unsorted region by extracting the largest element from it and inserting it into the sorted region.

Unlike selection sort, heapsort does not waste time with a linear-time scan of the unsorted region; rather, heap sort maintains the unsorted region in a **heap data structure** to more quickly find the largest element in each step.

#### Pseudo code

```
Algorithm 2.6: Heap Sort
   Input: a_1, a_2, ..., a_N
    Output: a_1, a_2, ..., a_N (in sorted)
 1 Function HeapRebuild(a, pos, N):
 2
        while 2 \cdot pos + 1 \le N do
            j = 2 \cdot pos + 1
 3
 4
            if j < N then
                if a_j < a_{j+1} then
 5
                    j \leftarrow j + 1
 6
                \quad \mathbf{end} \quad
 7
            end
 8
            if a_{pos} \geq a_i then
 9
               return
10
            end
11
            \operatorname{swap}(a_{pos}, a_j)
12
13
            pos \leftarrow j
14
        end
15 Function HeapConstruct(a, N):
        for i \leftarrow N/2 to 0 do
16
            HEAPREBUILD(a, i, n)
17
18
        end
19 Function HeapSort(a, N):
        HEAPCONSTRUCT(a, N)
20
        r \leftarrow N
\mathbf{21}
        while r > 0 do
22
            \operatorname{swap}(a_1, a_N)
23
            HEAPREBUILD(a, 1, r)
\mathbf{24}
            r \leftarrow r - 1
25
26
        end
```

# Complexity

Best case time complexity:  $O(N \log N)$ Average case time complexity:  $O(N \log N)$ Worst case time complexity:  $O(N \log N)$ Worst case space complexity: O(1)

# 2.7. Merge Sort

#### Idea

Merge sort is a recursive sorting algorithm based on a "divide and conquer" approach. It divides the input array into two halves, calls itself for the two halves, and then merges the two sorted halves.

```
Algorithm 2.7: Merge Sort
    Input: a_1, a_2, ..., a_N
    Output: a_1, a_2, ..., a_N (in sorted)
 1 Function Merge(a, first, mid, last):
        n_1 \leftarrow mid - first + 1
 \mathbf{2}
        n_2 \leftarrow last-mid
 3
 4
         L \leftarrow a_{first}, a_{first+1}, ..., a_{mid}
         R \leftarrow a_{mid+1}, a_{mid+2}, ..., a_{last}
         // merge
        i \leftarrow 0
 6
        j \leftarrow 0
 7
 8
        k \leftarrow first
         while i < n_1 and j < n_2 do
 9
             if L_i < R_j then
10
                  a_k \leftarrow L_i
11
                  i \leftarrow i+1
12
             else
13
                  a_k \leftarrow R_i
14
                 j \leftarrow j + 1
15
             \mathbf{end}
16
             k \leftarrow k + 1
17
        \quad \mathbf{end} \quad
18
         while j < n_2 do
19
             a_k \leftarrow R_j
20
             k \leftarrow k+1
\mathbf{21}
             j \leftarrow j + 1
22
         end
23
         while i < n_1 do
\mathbf{24}
             a_k \leftarrow L_i
25
             k \leftarrow k+1
26
             i \leftarrow i+1
27
        end
28
    Function MergeSort(a, first, last):
29
        if first < last then
30
             mid \leftarrow first + (last - first)/2
31
             MergeSort(a, first, mid)
32
33
             MergeSort(a, mid + 1, last)
             Merge(a, first, mid, last)
34
35
         end
```

Best case time complexity:  $O(N \log N)$ Average case time complexity:  $O(N \log N)$ Worst case time complexity:  $O(N \log N)$ Worst case space complexity: O(N)

#### 2.8. Quick Sort

#### Idea

Like Merge Sort, Quick Sort is a Divide and Conquer algorithm. It picks an element as a pivot and partitions the given array around the picked pivot. There are many different versions of quickSort that pick pivot in different ways.

- Pick first element as pivot.
- Pick last element as pivot
- Pick a random element as pivot.
- Pick median as pivot.

In this paper, I implemented the algorithm with pivot is a median of array.

```
Algorithm 2.8: Quick Sort
   Input: a_1, a_2, ..., a_N
    Output: a_1, a_2, ..., a_N (in sorted)
 1 Function Partition(a, l, r):
 \mathbf{2}
        pivot \leftarrow a_{(l+r)/2}
 3
        while l \leq r do
             while a_l < pivot do
 4
               l \leftarrow l + 1
 \mathbf{5}
            end
 6
            while a_r > pivot do
 7
             r \leftarrow r - 1
 8
            end
            if l \leq r then
10
                \operatorname{swap}(a_l, a_r)
11
                 l \leftarrow l + 1
12
                r \leftarrow r - 1
13
            end
14
15
        end
        return l
16
   Function QuickSort (a, l, r):
17
        if l < r then
18
            mid \leftarrow \text{Partition}(a, l, r)
19
             QuickSort(a, l, mid - 1)
20
            QuickSort(a, mid, r)
\mathbf{21}
22
        end
```

Best case time complexity: O(N)Average case time complexity:  $O(N \log N)$ Worst case time complexity:  $O(N^2)$ Worst case space complexity: O(1)

# 2.9. Counting Sort

### Idea

Counting sort is a sorting algorithm that sorts the elements of an array by counting the number of occurrences of each unique element in the array. The count is stored in an auxiliary array and the sorting is done by mapping the count as an index of the auxiliary array.

#### Pseudo code

```
Algorithm 2.9: Counting Sort
```

```
Input: a_1, a_2, ..., a_N
    Output: a_1, a_2, ..., a_N (in sorted)
 1 maxVal \leftarrow a_0
 2 for i \leftarrow 1 to N do
        if a_i > maxVal then
         maxVal \leftarrow a_i
 4
        \quad \text{end} \quad
 \mathbf{5}
 6 end
 7 count \leftarrow [0] * (maxVal + 1) // initialize 0-value counting array
 s foreach u \in a do
        count_u \leftarrow count_u + 1
 9
10 end
    // restore the elements to array
11 idx \leftarrow 0
12 for i \leftarrow 0 to maxVal do
        while count_i > 0 do
13
            a_{idx} \leftarrow i
14
            idx \leftarrow idx + 1
15
            count_i \leftarrow count_i - 1
16
        end
17
18 end
```

# Complexity

Best case time complexity: O(MaxValue)Average case time complexity: O(MaxValue)Worst case time complexity: O(MaxValue)Worst case space complexity: O(MaxValue)where MaxValue is the maximum value of input array.

#### 2.10. Radix Sort

#### Idea

The idea of Radix Sort is to do digit by digit sort starting from least significant digit to most significant digit. Radix sort uses counting sort as a subroutine to sort.

Pseudo code

```
Algorithm 2.10: Radix Sort
   Input: a_1, a_2, ..., a_N
   Output: a_1, a_2, ..., a_N (in sorted)
 1 \ maxVal \leftarrow a_0
 2 for i \leftarrow 1 to N do
       if a_i > maxVal then
           maxVal \leftarrow a_i
 4
       end
 6 end
 7 \ exp \leftarrow 1
 s while \frac{maxVal}{exp} > 0 do
       digit \leftarrow array  with of N elements
 9
       for i \leftarrow 1 to N do
10
           // get corresponding digit
           digit_i \leftarrow \frac{a_i}{exp} \mod 10
11
       end
12
       // do counting sort of a[] according to the digit represented by exp
       CountingSort(a, n, digit)
13
14
       exp \leftarrow exp \cdot 10
15 end
```

### Complexity

Best case time complexity:  $O(N \cdot d)$ Average case time complexity:  $O(N \cdot d)$ Worst case time complexity:  $O(N \cdot d)$ Worst case space complexity: O(N)where d is the maximum number of digits

#### 2.11. Flash Sort

#### Idea

The main idea of Flash Sort is to assign each of the n input elements to one of m partitions, efficiently rearranges the input to place the partitions in the correct order, then sorts each partition.

The algorithm can be represented as four stages:

- 1. The number of partitions is calculated.
- 2. Set clear boundaries in our original array for every partitions.
- 3. Rearrange the elements in the original array so that each of them was in its place, in its partition.
- 4. Do Insertion Sort for sorting locally.

46 end

### Algorithm 2.11: Flash Sort

```
Input: a_1, a_2, ..., a_N
    Output: a_1, a_2, ..., a_N (in sorted)
    // stage 1
    // d should be in range [0.4, 0.6]
 1 \ m \leftarrow d \cdot n
    // stage 2
 2 minVal \leftarrow a_1
 \mathbf{3} \ maxIndex \leftarrow 1
 4 for i \leftarrow 1 to N do
        if a_i < minVal then
           minVal \leftarrow a_i
 6
        end
 7
        if a_{maxIndex} < a_i then
 8
         | maxIndex \leftarrow i
 9
        end
10
11 end
12 if a_{maxIndex} == minVal then
stop algorithm
14 end
    // classify elements into corresponding partition
         a_{maxIndex} - minVal
16 for i \leftarrow 1 to N do
        cls \leftarrow c \cdot (a_i - minVal)
18
        L_{cls} \leftarrow L_{cls} + 1
19 end
20 for i \leftarrow 1 to m do
21 	 L_i \leftarrow L_i + L_{i-1}
22 end
    // stage 3
23 swap(a_{maxIndex}, a_1) nmove \leftarrow 0
24 j \leftarrow 0
25 k \leftarrow m - 1
26 t \leftarrow 0
27 while nmove < N do
        while j > L_k - 1 do
            j \leftarrow j + 1
29
            k \leftarrow c \cdot (a_j - minVal)
30
31
        \mathbf{end}
        flash \leftarrow a_j
32
        if k \neq 0 then
33
         break
34
35
        end
        while j \neq L_k do
36
            k \leftarrow c \cdot (flash - minVal)
37
             L_k \leftarrow L_k - 1
38
            t \leftarrow L_k
39
             hold \leftarrow a_t
40
            a_t \leftarrow flash
41
             flash \leftarrow hold
\mathbf{42}
            nmove \leftarrow nmove + 1
\mathbf{43}
        end
44
        // stage 4
        InsertionSort(a, n)
\mathbf{45}
```

The time complexity of Flash Sort base on choosing value m. For example, if m is chosen proportional to  $\sqrt{n}$ , the time complexity is  $O(n^{3/2})$ . In this paper, I chose 0.45 for m. Space complexity: O(1)

# 3. Experimental results

All the eleven sorting algorithms were implemented in C++ programming language and tested on six input of length 10000, 30000, 50000, 100000, 300000, and 500000 of four data orders (Sorted data, Nearly sorted data, Reverse sorted data and Randomized data). All experiments were executed on machine Operating System having Intel(R) Core(TM) i5-10210U CPU @ 1.60Ghz (8 CPUs) and installed memory (RAM) 8GB. The results were calculated after tabulation and their graphical represention was developed using Python programming language.

		Data	a Order: Sorted	data		
Data size	10,000		30,000		50,000	
Result	Time (ms)	Comparision	Time (ms)	Comparision	Time (ms)	Comparision
Selection	112.733	50005001	993.92	450015001	2661.613	1250025001
Insertion	0.052	19999	0.119	59999	0.177	99999
Bubble	0.029	20001	0.067	60001	0.114	100001
Shaker	0.026	20001	0.073	60001	0.129	100001
Shell	0.558	240024	1.762000	780029	3.423000	1400028
Heap	2.333	518705	5.418	1739633	9.129000	3056481
Merge	1.694	406234	3.632	1332186	6.21	2320874
Quick	0.598	193611	1.327	627227	2.218	1084459
Counting	0.162	60003	0.369	180003	0.572	300003
Radix	1.489	170106	3.738	630132	7.198	1050132
Flash	0.597	103496	1.118	310496	2.359	517496
Data size	100,000		300,000		500,000	
Result	Time (ms)	Comparision	Time (ms)	Comparision	Time (ms)	Comparision
Selection	11578.892	5000050001	101293.857	45000150001	281740.886	125000250001
Insertion	0.411	199999	1.044	599999	1.829	999999
Bubble	0.282	200001	0.765	600001	1.303	1000001
Shaker	0.245	200001	0.778	600001	1.272	1000001
Shell	7.336	3000029	25.944	10200035	41.04	17000033
Heap	19.542	6519813	60.3	21431637	102.634	37116275
Merge	1.694	406234	3.632	1332186	6.21	2320874
Quick	13.286	4891754	43.119	15848682	71.659	27234634
Counting	1.267	600003	3.35	1800003	5.708	3000003
Radix	13	2100132	44.787	7500158	76.2	12500158
Flash	4.02	1034996	11.634	3104996	19.422	5174996

Table 1: Experimental results on sorted data

		Data Or	der: Nearly Soi	rted data		
Data size	10,000		30,000		50,000	
Result	Time (ms)	Comparision	Time (ms)	Comparision	Time (ms)	Comparision
Selection	114.804	50005001	892.508	450015001	2815.055	1250025001
Insertion	0.272	186007	0.533	421299	1.59	792443
Bubble	138.364	95109345	825.406	773520000	2760.609	2463630480
Shaker	0.538	195793	1.251	470236	2.147	833872
Shell	0.675	288983	2.146	907030	4.659	1684266
Heap	1.407	518491	5.226	1739623	11.406	3056352
Merge	1.052	421044	3.477	1381719	5.788	2407406
Quick	0.422	193651	1.343	627279	2.527	1084495
Counting	0.122	60003	0.364	180003	0.519	300003
Radix	1.026	170106	3.725	630132	6.265	1050132
Flash	0.455	103470	1.063	310464	1.951	517470
Data size	100	,000	300	),000	500	0,000
Data size Result	100 Time (ms)	,000 Comparision	300 Time (ms)	0,000 Comparision	500 Time (ms)	0,000 Comparision
		,		,		·
Result	Time (ms)	Comparision	Time (ms)	Comparision	Time (ms)	Comparision
Result Selection	Time (ms) 10517.345	Comparision 5000050001	Time (ms) 98131.833	Comparision 45000150001	Time (ms) 268308.098	Comparision 125000250001
Result Selection Insertion	Time (ms) 10517.345 2.862	Comparision 5000050001 2143771	Time (ms) 98131.833 3.917	Comparision 45000150001 2784471	Time (ms) 268308.098 9.615	Comparision 125000250001 7687035
Result Selection Insertion Bubble	Time (ms) 10517.345 2.862 10614.255	Comparision 5000050001 2143771 9835488445	Time (ms) 98131.833 3.917 91618.611	Comparision 45000150001 2784471 80529222960	Time (ms) 268308.098 9.615 244003.655	Comparision 125000250001 7687035 214177110017
Result Selection Insertion Bubble Shaker Shell Heap	Time (ms) 10517.345 2.862 10614.255 6.193	Comparision 5000050001 2143771 9835488445 2239517	Time (ms) 98131.833 3.917 91618.611 9.282	Comparision 45000150001 2784471 80529222960 3358098	Time (ms) 268308.098 9.615 244003.655 21.366	Comparision 125000250001 7687035 214177110017 8256564
Result Selection Insertion Bubble Shaker Shell	Time (ms) 10517.345 2.862 10614.255 6.193 9.193	Comparision 5000050001 2143771 9835488445 2239517 3710600	Time (ms) 98131.833 3.917 91618.611 9.282 28.038	Comparision 45000150001 2784471 80529222960 3358098 11204764	Time (ms) 268308.098 9.615 244003.655 21.366 39.989	Comparision 125000250001 7687035 214177110017 8256564 19115054
Result Selection Insertion Bubble Shaker Shell Heap	Time (ms) 10517.345 2.862 10614.255 6.193 9.193 18.311	Comparision 5000050001 2143771 9835488445 2239517 3710600 6519703	Time (ms) 98131.833 3.917 91618.611 9.282 28.038 57.692	Comparision 45000150001 2784471 80529222960 3358098 11204764 21431472	Time (ms) 268308.098 9.615 244003.655 21.366 39.989 90.107	Comparision 125000250001 7687035 214177110017 8256564 19115054 37116054
Result Selection Insertion Bubble Shaker Shell Heap Merge	Time (ms) 10517.345 2.862 10614.255 6.193 9.193 18.311 13.929 4.53 0.962	Comparision 5000050001 2143771 9835488445 2239517 3710600 6519703 5052616	Time (ms) 98131.833 3.917 91618.611 9.282 28.038 57.692 40.513	Comparision 45000150001 2784471 80529222960 3358098 11204764 21431472 16239347	Time (ms) 268308.098 9.615 244003.655 21.366 39.989 90.107 63.774 22.691 4.906	Comparision 125000250001 7687035 214177110017 8256564 19115054 37116054 27981864
Result Selection Insertion Bubble Shaker Shell Heap Merge Quick	Time (ms) 10517.345 2.862 10614.255 6.193 9.193 18.311 13.929 4.53	Comparision 5000050001 2143771 9835488445 2239517 3710600 6519703 5052616 2268955	Time (ms) 98131.833 3.917 91618.611 9.282 28.038 57.692 40.513 15.264	Comparision 45000150001 2784471 80529222960 3358098 11204764 21431472 16239347 7275735	Time (ms) 268308.098 9.615 244003.655 21.366 39.989 90.107 63.774 22.691	Comparision 125000250001 7687035 214177110017 8256564 19115054 37116054 27981864 12475755

Table 2: Experimental results on nearly sorted data

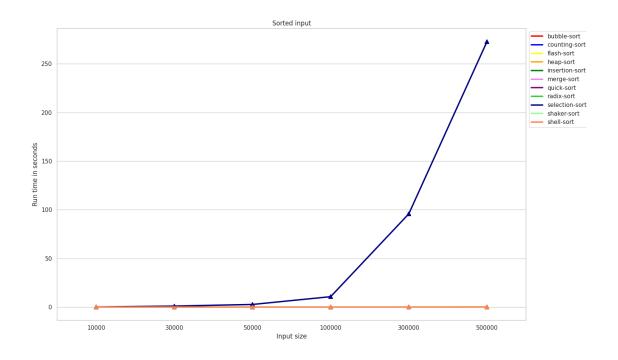


Figure 1: Visualizing the algorithms' running times on sorted data

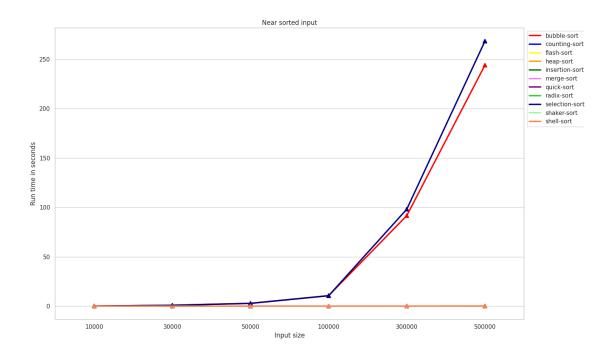


Figure 2: Visualizing the algorithms' running times on nearly sorted data

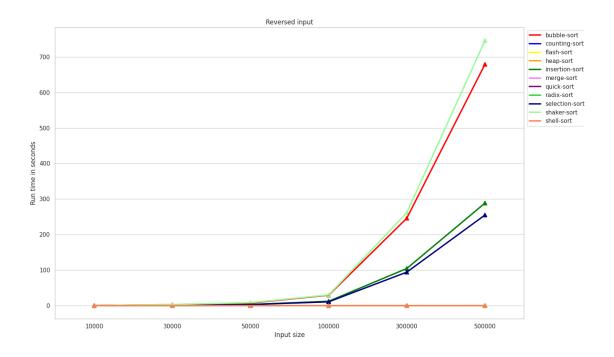


Figure 3: Visualizing the algorithms' running times on reverse sorted data

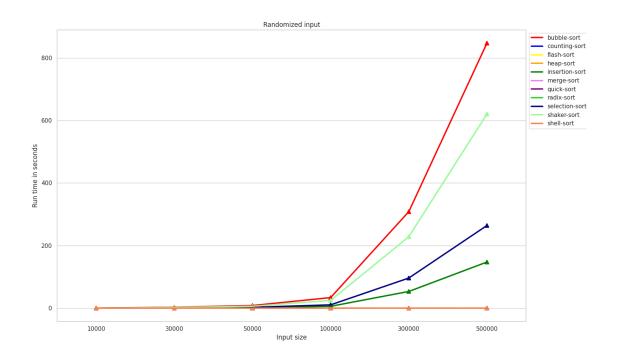


Figure 4: Visualizing the algorithms' running times on randomized data

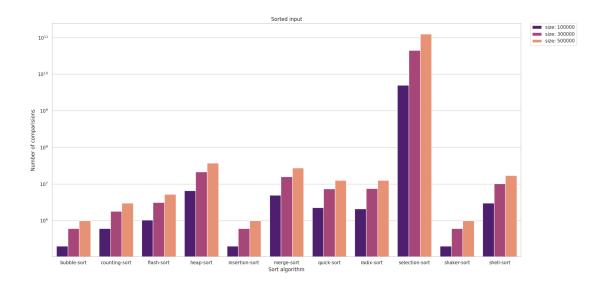


Figure 5: Visualizing the algorithms' numbers of comparisons on sorted data

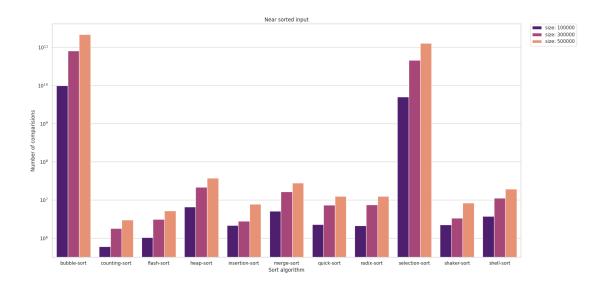


Figure 6: Visualizing the algorithms' numbers of comparisons on nearly sorted data

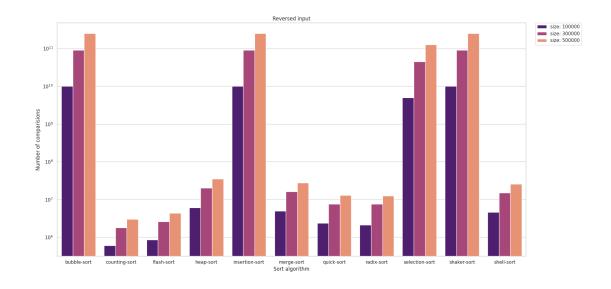


Figure 7: Visualizing the algorithms' numbers of comparisons on reverse sorted data

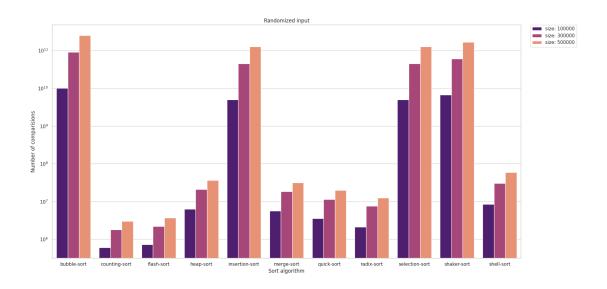


Figure 8: Visualizing the algorithms' numbers of comparisons on randomized data

# 4. Project organization

C++ programming language was used in sorting algorithms' implementation. Python programming language and open libraries (Pandas, Matplotlib, Seaborn) were used in processing data and graphical visualizing.

Source code: https://github.com/huynhtuan17ti/Sorting-Overview

# 5. References

- 1. https://www.geeksforgeeks.org/ (Explanations and source code of several sorting algorithms)
- 2. https://www.wikipedia.org/ (Scientific explanations of all sorting algorithms)
- 3. https://www.researchgate.net/publication/315662067\_Sorting\_Algorithms\_-\_A\_Comparative\_ Study
- 4. https://www.researchgate.net/publication/259911982\_Review\_on\_Sorting\_Algorithms\_A\_Comparative\_Study
- 5. Introduction to Algorithms (Third edition)