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1  /*
2   | Monotone Chain |
3   Finding Convex Hull in  $O(n \log n)$ 
4   Source: USACO Guide
5   State: Idk its from USACO Guide
6 */
7
8 #include <bits/stdc++.h>
9 using namespace std;
10
11 using pii = pair<int, int>;
12
13 vector<pii> points;
14 vector<pii> hull;
15
16 // cross product, the signed area of these three points
17 int area(pii O, pii P, pii Q) {
18     return (P.first - O.first) * (Q.second - O.second) -
19             (P.second - O.second) * (Q.first - O.first);
20 }
21
22 void monotone_chain() {
23     // sort with respect to the x and y coordinates
24     sort(points.begin(), points.end());
25     // distinct the points
26     points.erase(unique(points.begin(), points.end()), points.end());
27     int n = points.size();
28
29     // 1 or 2 points are always in the convex hull
30     if (n < 3) {
31         hull = points;
32         return;
33     }
34
35     // lower hull
36     for (int i = 0; i < n; i++) {
37         // if with the new point points[i], a right turn will be formed,
38         // then we remove the last point in the hull and test further
39         while (hull.size() > 1 &&
40                 area(hull[hull.size() - 2], hull.back(), points[i]) <= 0)
41
42             hull.pop_back();
43         // otherwise, add the point to the hull
44         hull.push_back(points[i]);
45     }
46
47     // upper hull, following the same logic as the lower hull
48     auto lower_hull_length = hull.size();
49     for (int i = n - 2; i >= 0; i--) {

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50          // we can only remove a point if there are still points left in
51          // the
52          // upper hull
53          while (hull.size() > lower_hull_length &&
54                  area(hull[hull.size() - 2], hull.back(), points[i]) ≤ 0)
55                  hull.pop_back();
56          hull.push_back(points[i]);
57      }
58      // delete point[0] that has been added twice
59      hull.pop_back();
60  }
61
62  int main() {
63      cin.tie(0)→sync_with_stdio(false);
64
65      int n;
66      cin >> n;
67      while (n ≠ 0) {
68          points.assign(n, {});
69          hull = {};
70          for (auto &p : points) cin >> p.first >> p.second;
71          monotone_chain();
72
73          cout << hull.size() << "\n";
74          for (auto &p : hull) cout << p.first << " " << p.second << "\n";
75
76          cin >> n;
77      }
78
79  return 0;
}
```