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1  /*
2      | Monotone Chain |
3      Finding Convex Hull in  $O(n \log(n))$ 
4      Source: USACO Guide
5      State: Idk its from USACO Guide
6  */
7
8  #include <bits/stdc++.h>
9  using namespace std;
10
11  using pii = pair<int, int>;
12
13  vector<pii> points;
14  vector<pii> hull;
15
16  // cross product, the signed area of these there points
17  int area(pii O, pii P, pii Q) {
18      return (P.first - O.first) * (Q.second - O.second) -
19             (P.second - O.second) * (Q.first - O.first);
20  }
21
22  void monotone_chain() {
23      // sort with respect to the x and y coordinates
24      sort(points.begin(), points.end());
25      // distinct the points
26      points.erase(unique(points.begin(), points.end()), points.end());
27      int n = points.size();
28
29      // 1 or 2 points are always in the convex hull
30      if (n < 3) {
31          hull = points;
32          return;
33      }
34
35      // lower hull
36      for (int i = 0; i < n; i++) {
37          // if with the new point points[i], a right turn will be formed,
38          // then we remove the last point in the hull and test further
39          while (hull.size() > 1 &&
40                 area(hull[hull.size() - 2], hull.back(), points[i]) ≤ 0)
41
42              hull.pop_back();
43          // otherwise, add the point to the hull
44          hull.push_back(points[i]);
45      }
46
47      // upper hull, following the same logic as the lower hull
48      auto lower_hull_length = hull.size();
49      for (int i = n - 2; i ≥ 0; i--) {

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50         // we can only remove a point if there are still points left in
    the
51         // upper hull
52         while (hull.size() > lower_hull_length &&
53             area(hull[hull.size() - 2], hull.back(), points[i]) ≤ 0)
54             hull.pop_back();
55         hull.push_back(points[i]);
56     }
57     // delete point[0] that has been added twice
58     hull.pop_back();
59 }
60
61 int main() {
62     cin.tie(0)→sync_with_stdio(false);
63
64     int n;
65     cin >> n;
66     while (n ≠ 0) {
67         points.assign(n, {});
68         hull = {};
69         for (auto &p : points) cin >> p.first >> p.second;
70         monotone_chain();
71
72         cout << hull.size() << "\n";
73         for (auto &p : hull) cout << p.first << " " << p.second << "\n";
74
75         cin >> n;
76     }
77
78     return 0;
79 }
```