

# Bayesian Parameter Inference of Markov Population Model.

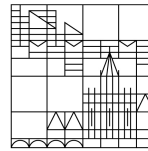
Master Thesis

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**Modeling of Complex, Self-organising Systems**

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## **Abstract**

# Chapter 1

## Introduction

- Brief introduction to Markov Chain
- Brief introduction to parameterization or Markov Chains
- Applications of parameter synthesis problem.
- Description of thesis structure.

We study the parameter synthesis problem of parametric Discrete-Time Markov Chain. Markov Chain is a probabilistic model to formalize stochastic processes.

This thesis is structured as follow.

- **Chapter 1** states the parameter synthesis problem and its applications.
- **Chapter 2** describes the most important definitions and theoretical background. In this chapter, we defines Discrete-Time Markov Chain formally. A brief introduction to Bayesian Inference is also included.
- **Chapter 3** reviews the state-of-the-art works of other researchers on the problem of parameter synthesis.

# Chapter 2

## Preliminaries

- transition system
- markov property
- discrete-time markov chain and parametric dtmc
- continuous-time markov chain
- bayesian inference
- metropolis-hastings algorithm

## **2.1 Discrete-Time Markov Chain**

## **2.2 Probabilistic Model Checking**

## **2.3 Bayesian Inference**

### **2.3.1 Bayesian formula**

### **2.3.2 Posterior conjugation**

## **2.4 Metropolis-Hastings algorithm**

## **2.5 Selection of prior distribution**

The selection of prior distribution has strong effect on the result [what result specifically?] of a Bayesian inference.

# Chapter 3

## Literature review

- Probabilistic model checking: basic building blocks from Katoen and his fellas.
- Parameter synthesis: important papers and concepts
- Bayesian model checking 2 papers
- Tools: mention PRISM and STORM

### 3.1 Probabilistic model checking

### 3.2 Parameter synthesis

### 3.3 Bayesian model checking

### 3.4 Tool