Buổi thực hành 5: Phân cụm dữ liệu (K-Means)

Câu 1: Cho tập dữ liệu gồm các mẫu có hai thuộc tính như sau:

S1[5.9, 3.2], S2[4.6, 2.9], S3[6.2, 2.8], S4[4.7, 3.2], S5[5.5, 4.2], S6[5.0, 3.0], S7[4.9 3.1], S8[6.7, 3.1], S9[5.1, 3.8], S10[6.0 3.0].

Phân cụm K-means với K = 3 và độ đo khoảng cách giữa các điểm là khoảng cách Euclid. Các tâm cụm khởi tạo ban đầu C1(6.2,3.2); C2(6.6,3.7); C3(6.5,3.0).

Thực hiện các thao tác tính toán thủ công và trình bày kết quả tâm cụm sau mỗi lần lặp.

Trả lời:

Gọi
$$C = \{C1, C2, C3\}$$

- Ta có cetroid:
- +C1(6.2, 3.2)
- + C2(6.6, 3.7)
- + C3(6.5, 3.0)

- Lần lặp 1:

$$+ S1[5.9, 3.2]$$

dist(S1, C1) =
$$\sqrt{(6.2 - 5.9)^2 + (3.2 - 3.2)^2} = 0.3$$

dist(S1, C2) =
$$\sqrt{(6.6 - 5.9)^2 + (3.7 - 3.2)^2} = 0.86$$

dist(S1, C3) =
$$\sqrt{(6.5 - 5.9)^2 + (3.0 - 3.2)^2} = 0.632$$

$$+ S2[4.6, 2.9]$$

dist(S2, C1) =
$$\sqrt{(6.2 - 4.6)^2 + (3.2 - 2.9)^2}$$
 = 1.627

dist(S2, C2) =
$$\sqrt{(6.6 - 4.6)^2 + (3.7 - 2.9)^2}$$
 = 2.154

dist(S2, C3) =
$$\sqrt{(6.5 - 4.6)^2 + (3.0 - 2.9)^2} = 1.902$$

$$+ S3[6.2, 2.8]$$

dist(S3, C1) =
$$\sqrt{(6.2 - 6.2)^2 + (3.2 - 2.8)^2} = 0.4$$

dist(S3, C2) =
$$\sqrt{(6.6 - 6.2)^2 + (3.7 - 2.8)^2} = 0.984$$

dist(S3, C3) =
$$\sqrt{(6.5 - 6.2)^2 + (3.0 - 2.8)^2} = 0.36$$

$$\Rightarrow$$
 S3 \in C3

$$+ S4[4.7, 3.2]$$

dist(S4, C1) =
$$\sqrt{(6.2 - 4.7)^2 + (3.2 - 3.2)^2} = 1.5$$

dist(S4, C2) =
$$\sqrt{(6.6 - 4.7)^2 + (3.7 - 3.2)^2} = 1.96$$

dist(S4, C3) =
$$\sqrt{(6.5 - 4.7)^2 + (3.0 - 3.2)^2} = 1.81$$

$$\Rightarrow$$
 S4 \in C1

$$+ S5[5.5, 4.2]$$

dist(S5, C1) =
$$\sqrt{(6.2 - 5.5)^2 + (3.2 - 4.2)^2}$$
 = 1.22

dist(S5, C2) =
$$\sqrt{(6.6 - 5.5)^2 + (3.7 - 4.2)^2} = 1.208$$

dist(S5, C3) =
$$\sqrt{(6.5 - 5.5)^2 + (3.0 - 4.2)^2} = 1.562$$

 $\Rightarrow S5 \in C2$

$$+ S6[5.0, 3.0]$$

dist(S6, C1) =
$$\sqrt{(6.2 - 5.0)^2 + (3.2 - 3.0)^2} = 1.216$$

dist(S6, C2) =
$$\sqrt{(6.6 - 5.0)^2 + (3.7 - 3.0)^2} = 1.746$$

dist(S6, C3) =
$$\sqrt{(6.5 - 5.0)^2 + (3.0 - 3.0)^2} = 1.5$$

 $\Rightarrow S6 \in C1$

$$+ S7[4.9, 3.1]$$

dist(S7, C1) =
$$\sqrt{(6.2 - 4.9)^2 + (3.2 - 3.1)^2} = 1.303$$

dist(S7, C2) =
$$\sqrt{(6.6 - 4.9)^2 + (3.7 - 3.1)^2} = 1.802$$

dist(S7, C3) =
$$\sqrt{(6.5 - 4.9)^2 + (3.0 - 3.1)^2} = 1.603$$

 \Rightarrow S7 \in C1

$$+$$
 S8[6.7, 3.1]

dist(S8, C1) =
$$\sqrt{(6.2 - 6.7)^2 + (3.2 - 3.1)^2} = 0.51$$

dist(S8, C2) =
$$\sqrt{(6.6 - 6.7)^2 + (3.7 - 3.1)^2} = 0.61$$

dist(S8, C3) =
$$\sqrt{(6.5 - 6.7)^2 + (3.0 - 3.1)^2} = 0.223$$

 \Rightarrow S8 \in C3

dist(S9, C1) =
$$\sqrt{(6.2 - 5.1)^2 + (3.2 - 3.8)^2} = 1.252$$

dist(S9, C2) =
$$\sqrt{(6.6 - 5.1)^2 + (3.7 - 3.8)^2} = 1.503$$

dist(S9, C3) =
$$\sqrt{(6.5 - 5.1)^2 + (3.0 - 3.8)^2} = 1.612$$

 \Rightarrow S9 \in C1

dist(S10, C1) =
$$\sqrt{(6.2 - 6.0)^2 + (3.2 - 3.0)^2} = 0.282$$

dist(S10, C2) =
$$\sqrt{(6.6 - 6.0)^2 + (3.7 - 3.0)^2} = 0.922$$

dist(S10, C3) =
$$\sqrt{(6.5 - 6.0)^2 + (3.0 - 3.0)^2} = 0.5$$

Vậy: Ta thu được 3 cụm:

$$+ C1 = \{S1, S2, S4, S6, S7, S9, S10\}$$

$$+ C2 = {S5}$$

$$+ C3 = \{S3, S8\}$$

Cập nhật lại trọng tâm cụm:

$$C1 = (\frac{5.9 + 4.6 + 4.7 + 5.0 + 4.9 + 5.1 + 6.0}{7}, \frac{3.2 + 2.9 + 3.2 + 3.0 + 3.1 + 3.8 + 3.0}{7}) = (5.17, 3.17)$$

$$C2 = (5.5, 4.2)$$

C3 =
$$(\frac{6.2+6.7}{2}, \frac{2.8+3.1}{2})$$
 = $(6.45, 2.95)$

- Lần lặp 2:

$$+ S1[5.9, 3.2]$$

dist(S1, C1) =
$$\sqrt{(5.17 - 5.9)^2 + (3.17 - 3.2)^2} = 0.730$$

dist(S1, C2) =
$$\sqrt{(5.5 - 5.9)^2 + (4.2 - 3.2)^2} = 1.077$$

dist(S1, C3) =
$$\sqrt{(6.45 - 5.9)^2 + (2.95 - 3.2)^2} = 0.604$$

$$+ S2[4.6, 2.9]$$

dist(S2, C1) =
$$\sqrt{(5.17 - 4.6)^2 + (3.17 - 2.9)^2} = 0.63$$

dist(S2, C2) =
$$\sqrt{(5.5 - 4.6)^2 + (4.2 - 2.9)^2} = 1.58$$

dist(S2, C3) =
$$\sqrt{(6.45 - 4.6)^2 + (2.95 - 2.9)^2} = 1.85$$

$$+ S3[6.2, 2.8]$$

dist(S3, C1) =
$$\sqrt{(5.17 - 6.2)^2 + (3.17 - 2.8)^2} = 1.09$$

dist(S3, C2) =
$$\sqrt{(5.5 - 6.2)^2 + (4.2 - 2.8)^2} = 1.56$$

dist(S3, C3) =
$$\sqrt{(6.45 - 6.2)^2 + (2.95 - 2.8)^2} = 0.29$$

$$\Rightarrow$$
 S3 \in C3

$$+ S4[4.7, 3.2]$$

dist(S4, C1) =
$$\sqrt{(5.17 - 4.7)^2 + (3.17 - 3.2)^2} = 0.47$$

dist(S4, C2) =
$$\sqrt{(5.5 - 4.7)^2 + (4.2 - 3.2)^2} = 1.28$$

dist(S4, C3) =
$$\sqrt{(6.45 - 4.7)^2 + (2.95 - 3.2)^2} = 1.76$$

$$+ S5[5.5, 4.2]$$

dist(S4, C1) =
$$\sqrt{(5.17 - 5.5)^2 + (3.17 - 4.2)^2} = 1.08$$

dist(S4, C2) =
$$\sqrt{(5.5 - 5.5)^2 + (4.2 - 4.2)^2} = 0$$

dist(S4, C3) =
$$\sqrt{(6.45 - 5.5)^2 + (2.95 - 4.2)^2} = 1.57$$

$$\Rightarrow$$
 S5 \in C2

$$+ S6[5.0, 3.0]$$

dist(S6, C1) =
$$\sqrt{(5.17 - 5.0)^2 + (3.17 - 3.0)^2} = 0.24$$

dist(S6, C2) =
$$\sqrt{(5.5 - 5.0)^2 + (4.2 - 3.0)^2} = 1.3$$

dist(S6, C3) =
$$\sqrt{(6.45 - 5.0)^2 + (2.95 - 3.0)^2} = 1.45$$

$$\Rightarrow$$
 S6 \in C1

$$+$$
 S7[4.9, 3.1]

dist(S7, C1) =
$$\sqrt{(5.17 - 4.9)^2 + (3.17 - 3.1)^2} = 0.27$$

dist(S7, C2) =
$$\sqrt{(5.5 - 4.9)^2 + (4.2 - 3.1)^2} = 1.25$$

dist(S7, C3) =
$$\sqrt{(6.45 - 4.9)^2 + (2.95 - 3.1)^2} = 1.55$$

$$+$$
 S8[6.7, 3.1]

dist(S8, C1) =
$$\sqrt{(5.17 - 6.7)^2 + (3.17 - 3.1)^2} = 1.53$$

dist(S8, C2) =
$$\sqrt{(5.5 - 6.7)^2 + (4.2 - 3.1)^2} = 1.62$$

dist(S8, C3) =
$$\sqrt{(6.45 - 6.7)^2 + (2.95 - 3.1)^2} = 0.29$$

 \Rightarrow S8 \in C3

dist(S9, C1) =
$$\sqrt{(5.17 - 5.1)^2 + (3.17 - 3.8)^2} = 0.63$$

dist(S9, C2) =
$$\sqrt{(5.5 - 5.1)^2 + (4.2 - 3.8)^2} = 0.56$$

dist(S9, C3) =
$$\sqrt{(6.45 - 5.1)^2 + (2.95 - 3.8)^2} = 1.59$$

 $\Rightarrow S9 \in C2$

$$+$$
 S10[6.0, 3.0]

dist(S10, C1) =
$$\sqrt{(5.17 - 6.0)^2 + (3.17 - 3.0)^2} = 0.84$$

dist(S10, C2) =
$$\sqrt{(5.5 - 6.0)^2 + (4.2 - 3.0)^2} = 1.3$$

dist(S10, C3) =
$$\sqrt{(6.45 - 6.0)^2 + (2.95 - 3.0)^2} = 0.45$$

Vậy: Sau bước lặp thứ 2 ta thu được 3 cụm:

$$+ C1 = \{S2, S4, S6, S7\}$$

$$+ C2 = \{S5, S9\}$$

$$+ C3 = \{S1, S3, S8, S10\}$$

Cập nhật lại trọng tâm cụm:

C1 =
$$(\frac{4.6+4.7+5.0+4.9}{4}, \frac{2.9+3.2+3.0+3.1}{4})$$
 = $(4.8, 3.05)$

$$C2 = (\frac{5.5+5.1}{2}, \frac{4.2+3.8}{2}) = (5.3, 4)$$

C3 =
$$(\frac{5.9+6.2+6.7+6.0}{4}, \frac{3.2+2.8+3.1+3.0}{4})$$
 = $(6.2, 3.025)$

- Lần lặp 3:

dist(S1,C1) =
$$\sqrt{(4.8 - 5.9)^2 + (3.05 - 3.2)^2}$$
 = 1.11

$$dist(S1,C2) = \sqrt{(5.3 - 5.9)^2 + (4 - 3.2)^2} = 1$$

dist(S1,C3) =
$$\sqrt{(6.2 - 5.9)^2 + (3.025 - 3.2)^2} = 0.35$$

 $\Rightarrow S1 \in C3$
 $+ S2[4.6, 2.9]$
dist(S2,C1) = $\sqrt{(4.8 - 4.6)^2 + (3.05 - 2.9)^2} = 0.25$
dist(S2,C3) = $\sqrt{(5.3 - 4.6)^2 + (4 - 2.9)^2} = 1.30$
dist(S2,C3) = $\sqrt{(6.2 - 4.6)^2 + (3.025 - 2.9)^2} = 1.61$
 $\Rightarrow S2 \in C1$
 $+ S3[6.2, 2.8]$
dist(S3,C1) = $\sqrt{(4.8 - 6.2)^2 + (3.05 - 2.8)^2} = 1.422$
dist(S3,C3) = $\sqrt{(6.2 - 6.2)^2 + (3.025 - 2.8)^2} = 0.225$
 $\Rightarrow S3 \in C3$
 $+ S4[4.7, 3.2]$
dist(S4,C1) = $\sqrt{(4.8 - 4.7)^2 + (3.05 - 3.2)^2} = 0.18$
dist(S4,C2) = $\sqrt{(5.3 - 4.7)^2 + (4 - 3.2)^2} = 1$
dist(S4,C3) = $\sqrt{(6.2 - 4.7)^2 + (3.025 - 3.2)^2} = 1.51$
 $\Rightarrow S4 \in C1$
 $+ S5[5.5, 4.2]$
dist(S5,C1) = $\sqrt{(4.8 - 5.5)^2 + (3.05 - 4.2)^2} = 1.34$
dist(S5,C2) = $\sqrt{(5.3 - 5.5)^2 + (4 - 4.2)^2} = 0.28$
dist(S5,C3) = $\sqrt{(6.2 - 5.5)^2 + (3.025 - 4.2)^2} = 1.36$
 $\Rightarrow S5 \in C2$
 $+ S6[5.0, 3.0]$
dist(S6,C1) = $\sqrt{(4.8 - 5.0)^2 + (3.025 - 3.0)^2} = 0.21$
dist(S6,C2) = $\sqrt{(5.3 - 5.0)^2 + (4 - 3.0)^2} = 1.044$
dist(S6,C3) = $\sqrt{(6.2 - 5.0)^2 + (4 - 3.0)^2} = 1.044$

⇒ S6 ∈ C1

$$+ S7[4.9 \ 3.1]$$

$$dist(S7,C1) = \sqrt{(4.8 - 4.9)^2 + (3.05 - 3.1)^2} = 0.111$$

dist(S7,C1) =
$$\sqrt{(5.3 - 4.9)^2 + (4 - 3.1)^2} = 0.98$$

dist(S7,C1) =
$$\sqrt{(6.2 - 4.9)^2 + (3.025 - 3.1)^2} = 1.302$$

$$+$$
 S8[6.7, 3.1]

dist(S8,C1) =
$$\sqrt{(4.8 - 6.7)^2 + (3.05 - 3.1)^2} = 1.9$$

$$dist(S8,C2) = \sqrt{(5.3 - 6.7)^2 + (4 - 3.1)^2} = 1.66$$

$$dist(S8,C3) = \sqrt{(6.2 - 6.7)^2 + (3.025 - 3.1)^2} = 0.505$$

$$\Rightarrow$$
 S8 \in C3

$$+ S9[5.1, 3.8]$$

$$dist(S9,C1) = \sqrt{(4.8 - 5.1)^2 + (3.05 - 3.8)^2} = 0.807$$

$$dist(S9,C2) = \sqrt{(5.3 - 5.1)^2 + (4 - 3.8)^2} = 0.28$$

$$dist(S9,C3) = \sqrt{(6.2 - 5.1)^2 + (3.025 - 3.8)^2} = 1.345$$

$$+ S10[6.03.0].$$

dist(S10,C1) =
$$\sqrt{(4.8 - 6.0)^2 + (3.05 - 3.0)^2}$$
 = 1.201

dist(S10,C1) =
$$\sqrt{(5.3 - 6.0)^2 + (4 - 3.0)^2} = 1.22$$

dist(S10,C1) =
$$\sqrt{(6.2 - 6.0)^2 + (3.025 - 3.0)^2} = 0.201$$

Vậy: Sau bước lặp 3 ta thu được 3 cụm:

$$+ C1 = \{S2, S4, S6, S7\}$$

$$+ C2 = \{S5, S9\}$$

$$+ C3 = \{S1, S3, S8, S10\}$$

Nhân xét:

- Kết quả phân cụm giữ nguyên sau 3 lần lặp, giải thuật dừng và cho kết quả phân cụm:

$$\circ$$
 C1 = {S2, S4, S6, S7}

$$\circ$$
 C2 = {S5, S9}

o C3 = {S1, S3, S8, S10}