

Numpy

Numpy is the core library for scientific computing in Python. It provides a high-performance multidimensional array object, and tools for working with these arrays.

Arrays

1. A numpy array is a grid of values, all of the same type, and is indexed by a tuple of nonnegative integers.
2. The number of dimensions is the rank of the array;
3. the shape of an array is a tuple of integers giving the size of the array along each dimension.
4. We can initialize numpy arrays from nested Python lists, and access elements using square brackets:

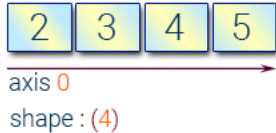
NumPy Basics

Operator	Description
<code>np.array([1,2,3])</code>	1d array
<code>np.array([(1,2,3),(4,5,6)])</code>	2d array
<code>np.arange(start,stop,step)</code>	range array

1D Array

```
>>> import numpy as np
>>> x = np.arange(2, 6).reshape(4)
>>> x
array([ 2, 3, 4, 5])
```

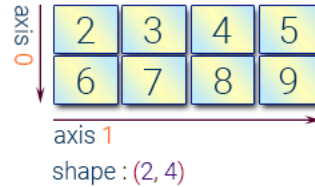
```
>>>
```



2D Array

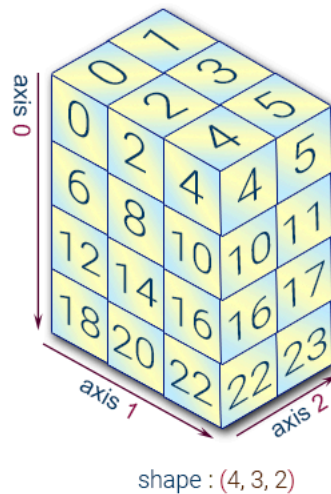
```
>>> import numpy as np
>>> x = np.arange(2, 10).reshape(2, 4)
>>> x
array([[ 2, 3, 4, 5],
       [ 6, 7, 8, 9]])
```

```
>>>
```



3D Array

```
>>> import numpy as np
>>> x = np.arange(24).reshape(4, 3, 2)
>>> x
array([[[ 0, 1],  [ 6, 7],  [12, 13],  [18, 19]],
       [[ 2, 3],  [ 8, 9],  [14, 15],  [20, 21]],
       [[ 4, 5],  [10, 11], [16, 17],  [22, 23]]])
>>>
```



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Placeholders

Operator	Description
<code>np.linspace(0,2,9)</code>	Add evenly spaced values btw interval to array of length
<code>np.zeros((1,2))</code>	Create an array filled with zeros
<code>np.ones((1,2))</code>	Creates an array filled with ones
<code>np.random.random((5,5))</code>	Creates random array
<code>np.empty((2,2))</code>	Creates an empty array

Array

Syntax	Description
<code>array.shape</code>	Dimensions (Rows,Columns)
<code>len(array)</code>	Length of Array
<code>array.ndim</code>	Number of Array Dimensions

Syntax	Description
array.dtype	Data Type
array.astype(type)	Converts to Data Type
type(array)	Type of Array

Copying/Sorting

Operators	Description
np.copy(array)	Creates copy of array
other = array.copy()	Creates deep copy of array
array.sort()	Sorts an array
array.sort(axis=0)	Sorts axis of array

Array Manipulation

Adding or Removing Elements

Operator	Description
np.append(a,b)	Append items to array
np.insert(array, 1, 2, axis)	Insert items into array at axis 0 or 1
np.resize((2,4))	Resize array to shape(2,4)
np.delete(array,1,axis)	Deletes items from array

Combining Arrays

Operator	Description
np.concatenate((a,b),axis=0)	Concatenates 2 arrays, adds to end
np.vstack((a,b))	Stack array row-wise
np.hstack((a,b))	Stack array column wise

Splitting Arrays

Operator	Description
numpy.split()	Split an array into multiple sub-arrays.
np.array_split(array, 3)	Split an array in sub-arrays of (nearly) identical size
numpy.hsplit(array, 3)	Split the array horizontally at 3rd index

More

Operator	Description
other = ndarray.flatten()	Flattens a 2d array to 1d
array = np.transpose(other)	
array.T	Transpose array
inverse = np.linalg.inv(matrix)	Inverse of a given matrix
Mathematics	

Operations

Operator	Description
np.add(x,y)	
x + y	Addition
np.subtract(x,y)	
x - y	Subtraction
np.divide(x,y)	
x / y	Division
np.multiply(x,y)	
x @ y	Multiplication
np.sqrt(x)	Square Root
np.sin(x)	Element-wise sine
np.cos(x)	Element-wise cosine
np.log(x)	Element-wise natural log

Operator	Description
<code>np.dot(x,y)</code>	Dot product
<code>np.roots([1,0,-4])</code>	Roots of a given polynomial coefficients

Comparison

Operator	Description
<code>==</code>	Equal
<code>!=</code>	Not equal
<code><</code>	Smaller than
<code>></code>	Greater than
<code><=</code>	Smaller than or equal
<code>>=</code>	Greater than or equal
<code>np.array_equal(x,y)</code>	Array-wise comparison

Basic Statistics

Operator	Description
<code>np.mean(array)</code>	Mean
<code>np.median(array)</code>	Median
<code>array.corrcoef()</code>	Correlation Coefficient
<code>np.std(array)</code>	Standard Deviation

More

Operator	Description
<code>array.sum()</code>	Array-wise sum
<code>array.min()</code>	Array-wise minimum value
<code>array.max(axis=0)</code>	Maximum value of specified axis
<code>array.cumsum(axis=0)</code>	Cumulative sum of specified axis

Slicing and Subsetting

Operator	Description
<code>array[i]</code>	1d array at index i
<code>array[i,j]</code>	2d array at index[i][j]
<code>array[i<4]</code>	Boolean Indexing, see Tricks
<code>array[0:3]</code>	Select items of index 0, 1 and 2
<code>array[0:2,1]</code>	Select items of rows 0 and 1 at column 1
<code>array[:1]</code>	Select items of row 0 (equals <code>array[0:1, :]</code>)
<code>array[1:2, :]</code>	Select items of row 1
<code>[comment]:<></code>	(<code>array[1,...]</code>)
<code>array[: : -1]</code>	Reverses array

✓ 1. Installation

`pip install numpy`

✓ 2. Motivation

Numpy provides extension package to python for multi dimensional arrays.
Also known as array oriented computing.

✓ creating array in numpy

```
import numpy as np

a = np.arange(10) #using arange function
print(a)

b = np.array([1,2,3,4,5]) #creating array from list
print(b)

[0 1 2 3 4 5 6 7 8 9]
[1 2 3 4 5]
```

▼ why to use numpy ?

```
L = range(1000)
%timeit [i**2 for i in L]

299 µs ± 4.36 µs per loop (mean ± std. dev. of 7 runs, 1000 loops each)

A = np.arange(1000)
%timeit A**2

1.54 µs ± 367 ns per loop (mean ± std. dev. of 7 runs, 1000000 loops each)

print("Numpy implementation is {0} times faster than lists implementation".format(272/1.25))

Numpy implementation is 217.6 times faster than lists implementation
```

▼ 3. Creating arrays

▼ 3.1. Manual construction of the arrays

```
#create 1 - D array #vector
a = np.array([1,2,3,4,5])

a

array([1, 2, 3, 4, 5])

#print dimensions
a.ndim

2

#print shape
a.shape

(5,)

len(a)

4

#create 2-D array #matrix
b = np.array([[1,2,3],[4,5,6]]) #list of lists

b

array([[1, 2, 3],
       [4, 5, 6]])

b.ndim

2

b.shape
```

```
(2, 3)
```

```
len(b) #size of first dimension or number of rows
```

```
2
```

```
#create 3 - D array #tensors
```

```
c = np.array([[[0,1],[2,3]],[[4,5],[6,7]]])
```

```
c
```

```
array([[[0, 1],
        [2, 3]],
       [[4, 5],
        [6, 7]]])
```

```
c.ndim
```

```
3
```

```
c.shape
```

```
(2, 2, 2)
```

```
len(c)
```

```
2
```

3.2. Functions for creating arrays

```
#using arange function
```

```
a = np.arange(10)
```

```
a
```

```
array([0, 1, 2, 3, 4, 5, 6, 7, 8, 9])
```

```
b = np.arange(1,10,2) #start, end, step
```

```
b
```

```
array([1, 3, 5, 7, 9])
```

```
#using linspace #linearspace
```

```
c = np.linspace(5, 10, 5) #start, end, number of points
```

```
c
```

```
array([ 5. ,  6.25,  7.5 ,  8.75, 10.  ])
```

```
#common arrays
```

```
d = np.ones((3,3))
```

```
d
```

```
array([[1., 1., 1.],
       [1., 1., 1.],
       [1., 1., 1.]])
```

```
x = np.zeros((3,3))
```

```
x
```

```
array([[0., 0., 0.],
       [0., 0., 0.],
       [0., 0., 0.]])
```

```
[0., 0., 0.]])
```

```
y = np.eye(3) #creates a matrix with 1 as the diagonals and 0 as non-diagonal elements
```

```
y
```

```
array([[1., 0., 0.],
       [0., 1., 0.],
       [0., 0., 1.]])
```

```
z = np.eye(3,2)
```

```
z
```

```
array([[1., 0.],
       [0., 1.],
       [0., 0.]])
```

```
a = np.diag([1,2,3,4]) #construct a diagonal array
```

```
print(a)
```

```
[[1 0 0 0]
 [0 2 0 0]
 [0 0 3 0]
 [0 0 0 4]]
```

```
np.diag(a) #extracts the diagonal elements of matrix a
```

```
array([1, 2, 3, 4])
```

```
#creates a array using random
```

```
a = np.random.rand(4)
```

```
print(a)
```

```
[0.65322898 0.73547486 0.74396941 0.39548332]
```

✓ 4. Datatypes

```
#we can explicitly specify the required data type
```

```
a = np.arange(10, dtype='float')
```

```
print(a)
```

```
[0. 1. 2. 3. 4. 5. 6. 7. 8. 9.]
```

```
b = np.array([1+2j, 5+1j])
```

```
print(b.dtype)
```

```
complex128
```

```
c = np.array([True, False, True])
```

```
print(c.dtype)
```

```
bool
```

✓ 5. Indexing and slicing

✓ 5.1. Indexing

```

a = np.arange(10)

print(a)
print(a[5])
print(a[-1])

[0 1 2 3 4 5 6 7 8 9]
5
9

b = np.diag([1,2,3])

print(b)
print(b[2,2])

[[1 0 0]
 [0 2 0]
 [0 0 3]]
3

b[2,1] = 10 #assigning value to a index

print(b)

[[ 1  0  0]
 [ 0  2  0]
 [ 0 10  3]]

```

✓ 5.2. Slicing

```

a = np.arange(10)

print(a[1:10:2]) #[start_value: end_value(exclusive): step]

[1 3 5 7 9]

b = np.arange(10)

b[5:] = 10 #assign 10 from index 5 to end

print(b)

[ 0  1  2  3  4 10 10 10 10 10]

c = np.arange(5)

b[5:] = c[::-1] #assign in reverse order

print(b)

[0 1 2 3 4 4 3 2 1 0]

```

✓ 6. Copies and views

Slicing operation creates a view on the original array which is just a way of accessing the data. Thus, the original array is not copied in the memory. You can use **np.may_share_memory()** to check whether two arrays share the same memory block.

```

a = np.arange(10)

b = a[:2]

np.shares_memory(a,b)

True

```



```

b[0] = 10

print(b)
print(a) #a is also updated, since it shares the same location in memory

[[10  2  4  6  8]
 [10  1  2  3  4  5  6  7  8  9]]

c = a[:,2].copy() #force the copy

np.shares_memory(a,c)

False

c[0] = 5

print(c)
print(a)

[[5  2  4  6  8]
 [10  1  2  3  4  5  6  7  8  9]]

```

7. Fancy Indexing

7.1 Using Boolean mask

```

a = np.random.randint(0,20,15)

print(a)

[ 3  7  3 16  6  0  7  8  4 12  6 11 12 16  1]

mask = (a % 2 == 0)
print(mask)

[False False False False False False False False False False False
 False False False]

even_numbers = a[mask]

print(even_numbers)

[]

a[mask]=-1 #it can be very useful to assign a new value to sub array

print(a)

[ 3  7  3 -1 -1 -1  7 -1 -1 -1 -1 11 -1 -1  1]

```

7.2. Using Integer Array

```

import numpy as np
a = np.arange(0,100,10)

print(a)

[ 0 10 20 30 40 50 60 70 80 90]

b = a[[2,3,5,2,4]]

print(b)

[20 30 50 20 40]

```

```
a[[9,7]] = -200

print(a)
print(b)

[  0  10  20  30  40  50  60 -200  80 -200]
[20 30 50 20 40]
```

✓ 8. Numerical Operations on numpy

✓ 8.1. Element wise operations

```
a = np.arange(10)

print(a+1)

[ 1  2  3  4  5  6  7  8  9 10]

print(a ** 2)

[ 0  1  4  9 16 25 36 49 64 81]

b = np.ones(10) + 1
print("b = ", b)

print("a - b = ",a-b)

b = [2. 2. 2. 2. 2. 2. 2. 2. 2. 2.]
a - b = [-2. -1.  0.  1.  2.  3.  4.  5.  6.  7.]

print(a*b)

[ 0.  2.  4.  6.  8. 10. 12. 14. 16. 18.]
```

#Matrix Multiplication

```
c = np.diag([1,2,3,4])

print(c)
print(""*100)
print(c*c)
print(""*100)
print(c.dot(c))

[[1 0 0 0]
 [0 2 0 0]
 [0 0 3 0]
 [0 0 0 4]]
*****
[[ 1  0  0  0]
 [ 0  4  0  0]
 [ 0  0  9  0]
 [ 0  0  0 16]]
*****
[[ 1  0  0  0]
 [ 0  4  0  0]
 [ 0  0  9  0]
 [ 0  0  0 16]]
```

element comparisions

```
a = np.array([1,2,5,4])
b = np.array([6,2,9,4])

print(a==b)

[False  True False  True]

print(a>b)

[False False False False]
```

```
print(a<b)

[ True False  True False]

print(a<=b)

[ True  True  True  True]

#array wise comparision

print(np.array_equal(a,b))

False
```

```
c = np.array([1,2,5,4])

print(np.array_equal(a,c))

True
```

✓ Logical Operations

```
a = np.array([1,0,0,1],dtype='bool')
b = np.array([0,1,0,1],dtype='bool')

print(np.logical_or(a,b))

[ True  True False  True]

print(np.logical_and(a,b))

[False False False  True]

print(np.logical_not(a))

[False  True  True False]
```

✓ Transcendental Functions:

```
a = np.arange(5)+1

print(np.sin(a))

[ 0.84147098  0.90929743  0.14112001 -0.7568025  -0.95892427]

print(np.log(a))

[0.          0.69314718  1.09861229  1.38629436  1.60943791]

print(np.exp(a))

[ 2.71828183  7.3890561  20.08553692  54.59815003 148.4131591 ]
```

✓ Shape Mismatch:

```
a = np.array([1,2,3,4])

b = np.array([5, 10,8,9])

print(a+b)

[ 6 12 11 13]
```

✓ 8.2. Basic Reductions

```

x = np.array([1,2,3,4])

print(np.sum(x))

10

y = np.array([[1,2],[3,4]])

print(y)
print(""*100)
print(y.T)

[[1 2]
 [3 4]]
*****
[[1 3]
 [2 4]]

print(y.sum(axis=0)) #column wise sum

[4 6]

print(y.sum(axis=1)) #row wise sum

[3 7]

```

▼ other reductions

```

print(y.min())

1

print(y.max())

4

print(y.argmin()) #index of minimum element

0

print(y.argmax()) #index of maximum element

3

```

▼ Logical reductions

```

print(np.all([True, False, False])) #logical and

False

print(np.any([True, False, False])) #logical or

True

a = np.zeros((50,50))

print(np.any(a!=0)) #checks whether any element in a is not equal to zero

False

```

▼ Statistics

```

x = np.arange(1,10)

print(np.mean(x))

```

```
5.0
```

```
print(np.median(x))
```

```
5.0
```

```
y = np.array([[1,2,3],[4,5,6]])
```

```
print(np.mean(y,axis=0)) #column wise mean
```

```
print(np.mean(y,axis=1)) #row wise mean
```

```
[2.5 3.5 4.5]
[2. 5.]
```

```
print(np.std(x))
```

```
2.581988897471611
```

✓ Example:

```
data = np.loadtxt("dataset/populations.txt")
```

```
-----
FileNotFoundError                                Traceback (most recent call last)
<ipython-input-8-fe63850b1259> in <cell line: 1>()
----> 1 data = np.loadtxt("dataset/populations.txt")
```

```
----- 3 frames -----
/usr/local/lib/python3.10/dist-packages/numpy/lib/_datasource.py in open(self, path, mode, encoding, newline)
    531         encoding=encoding, newline=newline)
    532     else:
--> 533         raise FileNotFoundError(f"{path} not found.")
    534
    535
```

```
FileNotFoundError: dataset/populations.txt not found.
```

```
print(data)
```

```
-----
NameError                                Traceback (most recent call last)
<ipython-input-40-dbd883db58b7> in <cell line: 1>()
----> 1 print(data)
```

```
NameError: name 'data' is not defined
```

```
data.shape
```

```
year, hare, lynx, carrot = data.T
```

```
print(year)
```

```
populations = data[:,1:]
```

```
print(populations)
```

```
populations.std(axis=0)
```

```
populations.mean(axis=0)
```

```
-----
NameError                                Traceback (most recent call last)
<ipython-input-7-f9c90115a8bf> in <cell line: 1>()
----> 1 populations.mean(axis=0)

NameError: name 'populations' is not defined
```

#which species has the highest population each year

```
print(np.argmax(populations, axis=1))
```

```
-----
NameError                                Traceback (most recent call last)
<ipython-input-9-6fb936716219> in <cell line: 3>()
      1 #which species has the highest population each year
      2
----> 3 print(np.argmax(populations, axis=1))

NameError: name 'populations' is not defined
```

9. Broadcasting

```
from IPython.display import Image
```

```
Image("photos/broadcasting.PNG")
```

```
-----
TypeError                                Traceback (most recent call last)
/usr/local/lib/python3.10/dist-packages/IPython/core/display.py in _data_and_metadata(self, always_both)
    1299         try:
-> 1300             b64_data = b2a_base64(self.data).decode('ascii')
    1301         except TypeError:
```

TypeError: a bytes-like object is required, not 'str'

During handling of the above exception, another exception occurred:

```
-----
FileNotFoundError                        Traceback (most recent call last)
----- 2 frames -----
/usr/local/lib/python3.10/dist-packages/IPython/core/display.py in _data_and_metadata(self, always_both)
    1300             b64_data = b2a_base64(self.data).decode('ascii')
    1301         except TypeError:
-> 1302             raise FileNotFoundError(
    1303                 "No such file or directory: '%s'" % (self.data))
    1304         md = {}
```

FileNotFoundError: No such file or directory: 'photos/broadcasting.PNG'

```
-----
TypeError                                Traceback (most recent call last)
/usr/local/lib/python3.10/dist-packages/IPython/core/display.py in _data_and_metadata(self, always_both)
    1299         try:
-> 1300             b64_data = b2a_base64(self.data).decode('ascii')
    1301         except TypeError:
```

TypeError: a bytes-like object is required, not 'str'

During handling of the above exception, another exception occurred:

```
-----
FileNotFoundError                        Traceback (most recent call last)
----- 2 frames -----
/usr/local/lib/python3.10/dist-packages/IPython/core/display.py in _data_and_metadata(self, always_both)
    1300             b64_data = b2a_base64(self.data).decode('ascii')
    1301         except TypeError:
-> 1302             raise FileNotFoundError(
    1303                 "No such file or directory: '%s'" % (self.data))
    1304         md = {}
```

FileNotFoundError: No such file or directory: 'photos/broadcasting.PNG'

```
<IPython.core.display.Image object>
```

```

a = np.tile(np.arange(0, 40, 10),(3,1)) #replicate rows 3 times and columns 1 time # change columns
print(a)
print(""*100)

a = a.T
print(a)

[[ 0 10 20 30]
 [ 0 10 20 30]
 [ 0 10 20 30]]
*****
[[ 0  0  0]
 [10 10 10]
 [20 20 20]
 [30 30 30]]

b = np.array([0,1,2])

print(b)

c = a + b

print(c)

a = np.arange(0,40,10)
print(a.shape)

a = a[:, np.newaxis] #adds a new axis
print(a.shape)

print(a)

print(a+b)

```

✓ 10. Array Manipulation

✓ 10.1. Flattening

```

a = np.array([[1,2,3],[4,5,6]])
print(a)

print(a.ravel())

print(a.T)

print(a.T.ravel())

```

✓ 10.2. Reshaping

```

print(a.shape)

b = a.ravel()
print(b.shape)

b = b.reshape(2,3)
print(b.shape)

```

✓ 10.3. Adding a new dimension

```

z = np.arange(1,10,2)
print(z.shape)

```

```
z = z[:,np.newaxis]
print(z.shape)
```

```
z = z[:,np.newaxis]
print(z.shape)
```

✓ 10.4. Dimension Shuffling

```
a = np.arange(4*3*2)
print(a)
```

```
a = a.reshape(4,3,2) # 4 matrices of 3 rows and 2 columns each
print(a)
```

```
a[3,1,1]
```

✓ 10.5. Resizing

```
a = np.arange(5)
a.resize((10,))
```

✓ 10.6. Sorting

```
a = np.array([[5,4,3],[2,1,9]])
print(a)
```

```
b = np.sort(a, axis=1)
print(b)
```

```
c = np.sort(a, axis=0)
print(c)
```

```
d = a.ravel()
print(d)
```

```
print(np.sort(d))
```

✓ 11. Exercises

(Type you code in the below cell)

1. Write a NumPy program to convert a list of numeric value into a one-dimensional NumPy array.

Expected Output:

Original List: [12.23, 13.32, 100, 36.32]

One-dimensional NumPy array: [12.23 13.32 100. 36.32]

Start coding or [generate](#) with AI.

2. Write a NumPy program to create a 3x3 matrix with values ranging from 2 to 10.

Expected Output:

[[2 3 4] [5 6 7] [8 9 10]]

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3. Write a NumPy program to sort an along the first, last axis of an array.*

Sample array: `[[2,5],[4,4]]`

Expected Output:

Original array: `[[4 6] [2 1]]`

Sort along the first axis: `[[2 1] [4 6]]`

Sort along the last axis: `[[1 2] [4 6]]`

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4. Write a NumPy program to create a contiguous flattened array.

Expected Output:

Original array: `[[10 20 30] [20 40 50]]`

New flattened array: `[10 20 30 20 40 50]`

Start coding or [generate](#) with AI.

5. Write a NumPy program to display all the dates for the month of March, 2017.

Expected Output:

March, 2017

`['2017-03-01' '2017-03-02' '2017-03-03' '2017-03-04' '2017-03-05' '2017-03-06' '2017-03-07' '2017-03-08' '2017-03-09' '2017-03-10' '2017-03-11' '2017-03-12' '2017-03-13' '2017-03-14' '2017-03-15' '2017-03-16' '2017-03-17' '2017-03-18' '2017-03-19' '2017-03-20' '2017-03-21' '2017-03-22' '2017-03-23' '2017-03-24' '2017-03-25' '2017-03-26' '2017-03-27' '2017-03-28' '2017-03-29' '2017-03-30' '2017-03-31']`

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6. Write a NumPy program to generate six random integers between 10 and 30.

Expected Output:

`[20 28 27 17 28 29]`

Start coding or [generate](#) with AI.

7. Write a NumPy program to create a 5x5 array with random values and find the minimum and maximum values.

Expected Output

Original Array:

`[[0.96336355 0.12339131 0.20295196 0.37243578 0.88105252] [0.93228246 0.67470158 0.38103235 0.32242645 0.40610231] [0.3113495 0.31688 0.79189089 0.08676434 0.60829874] [0.30360149 0.94316317 0.98142491 0.77222542 0.51532195] [0.97392305 0.16669609 0.81377917 0.2165645 0.00121611]]`

... ..