

Learning Deep Discriminative Embedding for Software Defect Prediction

Abstract— The problem of software defect prediction, which involves identifying likely erroneous files in a computer program or system, has recently gained much attention in software engineering community. The ability to identify defects would help developers better focus their efforts on assuring software quality. Traditional approaches for defect prediction generally begin by a feature construction step to encode the characteristics of programs, followed by a defect modeling stage that involves training a classification algorithm. However, the feature construction stage in these approaches is carried out without considering known defect labels, potentially leading to suboptimal learned features. In light of this deficiency, we propose in this paper a new deep learning approach called *deep discriminative autoencoder* (DDA), which performs end-to-end training to jointly learn discriminative (latent) features, and an accurate classification model for effective defect identification. Preliminary experimental results on four popular software projects show that our DDA approach significantly outperforms traditional methods on both within-project (WP) and cross-project (CP) defect prediction. In particular, our approach improves on average by 19.63% in terms of F1 score for the WP problems. For the CP problems, DDA outperforms other methods by 18.95% in terms of F1 score.

I. INTRODUCTION

Software defect prediction techniques [5], [9] have been developed to automatically detect defects among program elements, which in turn help developers reduce their testing efforts and minimize software development costs. In a defect prediction task, one typically constructs defect prediction models from software history data, and uses these models to predict whether new instances of code elements (e.g., files, changes, and methods) contain defects. Traditionally, research efforts to construct accurate defective prediction models fall into two directions: the first direction focuses on manually designing a set of discriminative features that can represent defects more effectively; the second direction aims to apply a new machine learning algorithm [3] that improves the conventional prediction models.

In the first direction, most researchers manually designed features to filter buggy source files from non-buggy files. Typically, features are constructed based on changes in source code (i.e., the number of lines of code added, removed, etc.), complexity of code, or understanding of source code [9], [4]. A common drawback of these approaches is that the features constructed cannot adequately capture the contextual semantic meanings of different programs [24]. For example, two Java programs may have identical `if` and `for` statements, except that the `if` statement is outside the `for` loop in the first program whereas the second program has the `if` statement inside the `for` loop. Although the two program files have different semantics,

the features generated by the traditional approaches may be identical, failing to distinguish the semantics of the two programs. As such, the defect prediction models constructed based on these features are often suboptimal.

In view of this limitation, Wang et al. [24] applied a deep belief network (DBN) model [7] to automatically learn embedding features (referred to as semantic information) that are a compressed representation of token vectors extracted from a program's Abstract Syntax Tree (AST) [6]. The learned features are then utilized as training input to build a defect classification model. However, in this approach, the embedding features and defect prediction model are built separately. That is, the embedding features are learned from source files in an unsupervised manner, without considering the true label of the program element. Moreover, token values are mapped to unique integer identifiers without reflecting the importance of that token in the program element. Hence, the embedding features may be suboptimal for defect prediction purposes.

To address this shortcoming, we propose a new deep learning approach named *deep discriminative autoencoder* (DDA), which provides an end-to-end learning scheme to construct discriminative embedding features and accurate defect classification model in one go. DDA extends a deep autoencoder model [22], which is an unsupervised learning model. Our DDA adds a discriminative power to the deep autoencoder model, making it a supervised learning model. We summarize the key contributions of this paper below:

- We develop a new deep learning approach for defect prediction, which is trained end-to-end using a joint loss function that simultaneously takes into account the defect prediction quality and reconstruction quality of the embedding features.
- We conduct experiments on four popular Java software projects. The results show that our approach significantly improve traditional defect prediction methods by 16.63% and 18.95% in terms of F1 score, for within-project and cross project defect prediction tasks respectively.

The remainder of this paper is organized as follows. Section II elaborates our proposed DDA approach. Section III presents our experimental results, followed by discussion on threats to validity in Section III-E. Finally, Section IV concludes this paper.

II. PROPOSED APPROACH

In this section, we explain how the input features are generated for DDA model and briefly present our proposed approach.

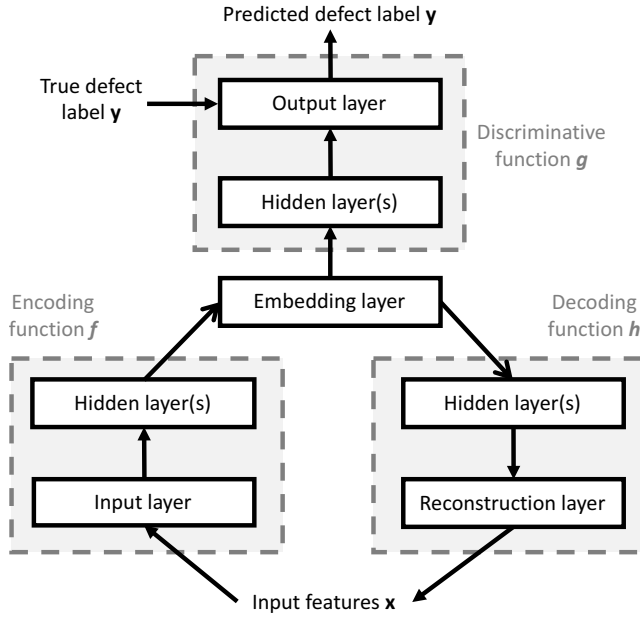


Fig. 1. Our proposed DDA model architecture

A. Parsing Source Code and Generating Input Features

Following Wang et al.'s approach [24], we extract a sequence of AST node tokens from source code files. There are three different types of AST nodes are collected as tokens: 1) nodes of method invocations and class instance creations, 2) method declarations, type declarations, and enum declarations, 3) control-flow nodes like **for**, **if**, etc.

However, in contrast to Wang et al.'s approach which weights the extracted AST tokens as equally, we assign weights to the tokens using a term frequency-inverse document frequency (TF-IDF) scheme [14]. TF refers to the number of times a token appears in a source code file. IDF refers to the reciprocal of the number of source code files in the entire source code files that contain the token. TF-IDF of a token is a multiplication of its TF and IDF. The resultant sequence of AST tokens are weighted by their TF-IDF values.

Our proposed approach (DDA) takes the sequence of AST tokens, which are assigned TF-IDF values, as input vector, and the lengths of the sequence for each source file must be the same. Since our input vectors may have different lengths, we append 0 to the input vectors to make all the length consistent and equal to the length of the longest vector. Through this generating process, the sequence of AST tokens are represented as input vector. Moreover, we also preserve the program structure information of source code since the order of tokens remains unchanged.

B. Deep Discriminative Autoencoder

In this section, we describe our DDA approach to defect prediction, which aims to detect source code files that may potentially contain a bug. Firstly, let $\mathcal{X} = \{x_1, \dots, x_i, \dots, x_n\}$ denotes the set of source code files in a software project and $\mathcal{Y} = \{y_1, \dots, y_i, \dots, y_n\}$ represents the set of labels for the

source code files, where n is the number of source code files in the project. A source code file is labelled as $y_i = 1$ if it contains a bug; otherwise, it is labelled as $y_i = 0$.

Unlike traditional approaches [25], [24], which learn embedding features and defect prediction model separately, our DDA approach performs an end-to-end learning to accomplish the two tasks in one shot. Specifically, DDA simultaneously learns three (non-linear) functions: 1) an *encoding function* f that maps input features to an embedding representation, 2) a *discriminative function* g that maps the embedding representation to defect class labels, and 3) a *decoding function* h that reconstructs the input features from the embedding representation. While an autoencoder model [22] only contains *encoding function* and *decoding function*, we add a *discriminative function* that maps embedding layer to output layer. Fig. 1 presents the architecture of our DDA model that realizes the three functions. Each function is represented using one or more hidden (fully-connected) layers. The embedding layer is shared by the three functions, while the input, output, and reconstruction layer is used by function f , g , and h .

To learn f , g and h simultaneously, we devise the following loss minimization problem:

$$\min \sum_{i=1}^n [\mathcal{L}_{discr}(g(f(x_i)), y_i) + \beta \mathcal{L}_{recon}(h(f(x_i)), x_i)] + \lambda \Omega(\theta) \quad (1)$$

where $\mathcal{L}_{discr}(g(f(x_i)), y_i)$ measures classification loss with respect to defect label y_i , $\mathcal{L}_{recon}(h(f(x_i)), x_i)$ is the reconstruction loss with respect to input feature x_i , and $\Omega(\theta)$ is the regularization terms for the set θ of all weight parameters within the DDA architecture. The parameters $\beta > 0$ and $\lambda > 0$ are user-defined, and serve to control the tradeoff between the different loss/regularization terms.

In this work, we define \mathcal{L}_{discr} and \mathcal{L}_{recon} respectively as:

$$\mathcal{L}_{discr}(g(f(x_i)), y_i) = -[y_i \ln(\sigma(g(f(x_i)))) + (1 - y_i) \ln(1 - \sigma(g(f(x_i))))] \quad (2)$$

$$\mathcal{L}_{recon}(h(f(x_i)), x_i) = \frac{1}{2} \|h(f(x_i)) - x_i\|^2 \quad (3)$$

while the regularization term Ω is given by:

$$\Omega(\theta) = \frac{1}{2} \sum_{w \in \theta} w^2 \quad (4)$$

where $\sigma(x) = \frac{1}{1 + \exp(-x)}$ is the logistic/sigmoid function, and $w \in \theta$ is a particular weight parameter in the DDA network. It is worth noting that equation (2) corresponds the so-called cross-entropy loss commonly used for classification in deep learning [18], while equation (3) is the least square loss used to measure reconstruction quality in an autoencoder [22]. Finally, equation (4) corresponds to the ridge regularization term, which enforces the weight parameters w to be small so as to reduce the risk of data overfitting [3].

To minimize the joint loss function in (1), we employ in this work an adaptive gradient-based algorithm called Adam [12]. More specifically, Adam is an efficient algorithm for stochastic

optimization that computes individual adaptive learning rates for different parameters from estimates of first and second moments of the gradients. This method is straightforward to implement, is computationally efficient, and has little memory requirements [12], making it well-suited to optimize such deep architecture as our DDA model.

C. Handling Imbalanced Class Distribution

In defect prediction tasks, oftentimes there are only a handful of program files that contain bugs, while the other program files are clean (i.e., bug-free) [11]. As such, we can expect to see a highly-skewed (imbalanced) distribution of class labels (i.e., buggy vs clean). This imposes difficulties for gradient-based learning approaches, making them more biased towards the majority class (i.e., the class with more data instances). As such, class imbalance learning mechanisms would be helpful to tackle defect prediction problems [23].

In a similar vein, we develop a simple alternating (random) sampling strategy [13] when training DDA. In a nutshell, we divide the training data into two sets, i.e., buggy set and clean sets. Then, we perform an Adam update step by presenting a randomly-selected buggy sample and a randomly-selected clean sample in an alternating manner. That is, in update step i , we present a buggy sample to DDA, and a clean sample in update step $i + 1$, and so on. Effectively, this renders a balanced (bootstrapped) training data for DDA, which would help mitigate the bias from the majority (i.e., clean) class.

D. Parameter Setting for DDA Training

In this work, we use a DDA architecture with one hidden layer for each function f , g , and h . We configure the DDA model is as follows: The number of neurons (nodes) in the hidden layer of f and h is set to 1000 [21], while that of g is 50. Also, the number of neurons in the embedding layer is set to 100 which is similar to [24]. Meanwhile, the regularization parameter λ is set to 0.01, and the reconstruction parameter β is chosen via cross validation on the training data. Finally, we use early stopping [26] to reduce the training time of DDA model.

III. EXPERIMENTAL RESULTS

We conduct extensive experiments to study the performance of the proposed approach and compare it with existing defect prediction approaches. We also discuss threats to the validity of our approach.

A. Evaluation Metrics

To measure defect prediction performance, we employ three different evaluation metrics: *Precision*, *Recall* and *F1* score. These metrics are widely used to evaluate the performance of defect prediction [15], [16]. Below is the equation for each of these metrics:

$$Precision = \frac{TP}{TP + FP} \quad (5)$$

$$Recall = \frac{TP}{TP + FN} \quad (6)$$

$$F1 = \frac{2 * Precision * Recall}{Precision + Recall} \quad (7)$$

where TP , FP , and FN are considered as true positive, false positive, and false negative, respectively. A higher precision makes the manual inspection on a certain amount of predicted defective files find more defects, while an increase in recall reveals more defects in a project. F1 score considers both precision and recall.

B. Datasets

We perform several steps to create our benchmark dataset. We do not use PROMISE defect dataset¹ since the projects are old (i.e., average age is around 10 years). Firstly, we fetch the latest top open-source Java projects from GitHub (sorted by the number of their stars and forks). We ignore projects with less than 150 source files as these projects are too small to employ deep neural network. We also filter out projects which have less than 100 tested files. For our preliminary experiment, we pick 4 projects. For each project, we extract two versions: training version (i.e., version as of January 1st, 2015), and testing version (i.e., version as of July 1st, 2015).

For labeling training version, we extract commits between January 1st, 2015 to July 1st 2015. We then identify bug fixing commits by checking whether the commit message contains a bug fixing pattern. We follow the pattern used by Antoniol et al. [2] as follows.

`\bfix\bbug\bproblem\bdefect\bpatch`

We consider changed files in bug fixing commits as buggy files and label their corresponding files (i.e., files of the same path) in training version as buggy. For labeling testing version, we extract commits between July 1st, 2015 to January 1st 2016 and perform the same labeling process that was done for the training version.

Table I shows statistics on this dataset. In average, our dataset contains around 783.88 source files with bug rate of 17.4%, showing the imbalanced problem in defect prediction [23], [11]. To deal with class imbalance, we use random sampling strategy described in Section II-C during the learning process.

C. Baselines

We compare our approach with the defect prediction models constructed based on two traditional features. The first traditional features are AST features extracted from source code's AST. Specifically, we collect AST nodes from source code and represent the source code as vector of term frequencies of the AST nodes. The second traditional features are embedding features generated following Wang et al. [24]. These two baselines were shown their effectiveness in solving defect prediction problem [24]. The first traditional features are embedding features generated following Wang et al. [24].

We employ three popular machine learning algorithms, which are decision tree, logistic regression, and naïve Bayes, with default parameters² to build defect prediction models for

¹<http://openscience.us/repo/defect/>

²<http://scikit-learn.org/>

TABLE I
DESCRIPTION OF FOUR POPULAR SOFTWARE PROJECTS.

Project	Description	Avg File	Avg Bug (%)
Checkstyle	a program to check whether source code conforms to coding standard	433.5	30.9
NuvolabBase	an add on to create, share, and exchange database in the cloud	1292.5	12.3
OrientDB	a Multi-Model DBMS with document and graphe engine	1194.5	9.17
Traccar	a server for various GPS tracking systems	215	17.3

TABLE II

PRECISION, RECALL AND F1 SCORES OF WITHIN-PROJECT PREDICTION. ALL THE SCORES ARE MEASURED BY PERCENTAGE. THE BEST F1 SCORES ARE HIGHLIGHTED IN BOLD. DEEP DISCRIMINATIVE AUTOENCODER, DECISION TREE, LOGISTIC REGRESSION, AND NAÏVE BAYES ARE DENOTED AS DDA, DT, LR, NB RESPECTIVELY.

Project	DDA			Embedding									AST								
				DT			LR			NB			DT			LR			NB		
	P	R	F1	P	R	F1	P	R	F1	P	R	F1	P	R	F1	P	R	F1	P	R	F1
Checkstyle	74.6	84.7	79.3	78.3	55.3	64.8	83.6	68.8	75.5	72.3	82.9	77.3	82.4	63.5	71.8	79.7	62.4	70.0	82.7	64.7	72.6
Nuvolabbase	33.8	66.0	44.7	32.8	7.51	12.2	36.2	44.7	40.0	31.1	73.5	43.7	50.7	14.2	22.2	59.6	12.2	20.3	20.3	41.1	27.1
OrientDB	32.9	47.9	39.0	25.6	6.94	10.9	27.3	47.2	34.6	20.8	69.4	32.0	40.3	18.8	25.6	44.2	13.2	20.3	12.1	38.2	18.4
Traccar	33.9	75.0	46.7	14.0	80.0	23.9	12.7	75.0	21.7	12.8	95.0	22.0	20.0	20.0	12.2	70.0	20.7	9.47	90.0	17.1	
Average	43.8	68.4	52.4	37.7	37.4	28.0	39.9	58.9	42.9	34.3	80.2	43.8	48.4	29.1	34.9	48.9	39.5	32.8	31.1	58.5	33.8

TABLE III

PRECISION, RECALL AND F1 SCORES OF CROSS-PROJECT DEFECT PREDICTION. ALL THE SCORES ARE MEASURED BY PERCENTAGE. THE BEST F1 SCORES ARE HIGHLIGHTED IN BOLD.

Source	Target	Cross-project						Within-project		
		DDA			Embedding					
		P	R	F1	P	R	F1	P	R	F1
Nuvolabbase	Checkstyle	79.0	57.6	66.7	54.5	38.8	45.3	74.6	84.7	79.3
OrientDB	Checkstyle	94.3	29.4	44.8	54.7	48.2	51.3			
Checkstyle	Nuvolabbase	45.5	36.4	40.4	27.0	52.2	35.6	33.8	66.0	44.7
Traccar	Nuvolabbase	44.2	36.4	40.0	27.1	41.5	32.8			
Nuvolabbase	OrientDB	57.1	16.7	25.8	16.2	31.9	21.5	32.9	47.9	39.0
Traccar	OrientDB	25.4	43.1	31.9	18.5	45.1	26.3			
Nuvolabbase	Traccar	13.9	85.0	23.9	16.7	15.0	15.8	33.9	75.0	46.7
Checkstyle	Traccar	16.0	20.0	17.8	9.8	50.0	16.4			
Average		46.9	40.6	36.4	28.1	40.3	30.6	43.8	68.4	52.4

TABLE IV

TRAINING TIME OF THE PROPOSED DDA APPROACH

Project	Time (s)
Checkstyle	10.2
Nuvolabbase	62.5
OrientDB	59.2
Traccar	5.67
Average	34.4

each traditional features. These algorithms are widely used in software engineering [24], [10]. We also try ensemble methods such as random forest, however the results were inferior compared to the decision tree.

D. Results

This section presents our experimental results. We examine the performance of our proposed DDA approach in both within-project and cross-project defect prediction setting. In the within-project setting, we use the source code of an older version of a project to construct the DDA model and evaluate the model based on the source code of the newer version of the project. In the cross-project setting, we randomly pick one project as a source project to build the DDA model and use the

model to predict defects for a target project that is randomly picked from a set of projects that excludes the source project.

We answer the following research questions:

RQ1: In within-project defect prediction, does our proposed approach outperform the baselines?

Table II shows the precision, recall and F1 score of different defect prediction models. The highest F1 scores are highlighted in bold. For example, the F1 score of our approach is 46.7% for Traccar project, while the best F1 score is only 23.9% for approaches that use embedding features (using decision tree), and the best F1 score is 20.7% for approaches that use AST features (using logistic regression). On average, the best baseline that uses AST features achieves an F1 score of 34.9%, while the best baseline that uses embedding features constructed following Wang et al. [24] approach achieves an F1 score of 43.8%. Our DDA approach beats these two baselines by achieving an F1 score of 52.4%. The results demonstrate that we can improve the F1 score by 19.63% when compared with the best baseline.

RQ2: In cross-project defect prediction, does our proposed approach outperform the baselines?

We evaluate eight pairs of projects. For each pair, we take two different projects for training and testing. Table III presents the precision, recall and F1 scores of our proposed method (DDA) vs. best defect prediction model constructed using embedding features. Note that we employ different machine learning algorithms (i.e., decision tree, logistic regression, naïve Bayes) to build defect prediction model from embedding features. The results show that naïve Bayes achieves the best results in cross-project setting, which is similar to Wang et al. [24]. For this reason, we compare DDA to defect prediction model built using naïve Bayes algorithm. The best F1 scores are highlighted in bold. For example, when the source project is Nuvolabbase (training) and the target project is Checkstyle (testing), our DDA achieves an F1 score of 66.7% whereas the best defect prediction model using embedding features only achieves an F1 score 45.3%. In average, DDA

achieves an F1 score of 36.4%, which improves by 18.95% in term of F1 score compared to the best model that uses embedding features.

RQ3: What is the training time of proposed approach?

We run experiments on a NVIDIA DGX-1 [1] machine to construct the DDA model. We keep track of the training time that our server needs to build the DDA model on the four software projects in the within-project setting. Table IV shows the training time to build the DDA model. In average, the training time for our proposed approach varies from 5.67 seconds (Traccar) to 62.5 seconds (Checkstyle). On average, it takes 34.4 seconds to build the DDA model. It shows that our DDA is applicable in practice.

E. Threats to validity

Threats to validity includes threats to internal, external, and construct validity. To minimize threats to internal validity, we have made sure that our implementations are correct. For baseline, Wang et al. [24] are unable to share their source code since their approach is under US patent application. Thus, we reimplement their approach by following the description in their paper and querying with the first author. We provide the source code of our implementation at <https://goo.gl/QMwPfc>. Regarding threats to external validity, our dataset consists only of four open source Java projects. However, the projects has varying statistics in average buggy rates and number of source code files. Since we consider all files changed in bug fixing commits are buggy, it will lead to a external validity in our dataset. In the future, we will minimize threats to external validity further by experimenting on more projects with more varying statistics and also projects that are closed source and written in different programming languages (i.e., C++, Python, etc.). To minimize threats to construct validity, we use of evaluation metrics that are common in defect prediction [17].

IV. CONCLUSION AND FUTURE WORK

This paper presents a new deep discriminative autoencoder (DDA) approach to achieve an effective software defect prediction. DDA provides an end-to-end learning approach to simultaneously learn embedding features that can well represent token vectors extracted from programs' ASTs, and build an accurate classification model for defect prediction. Empirical studies on four software projects show that our approach significantly outperforms the existing defect prediction approaches. Specifically, our approach improve the F1 score by 19.63% and 18.95% for both within-project and cross-project setting, respectively.

While DDA offers a powerful approach for defect prediction, there remains room for improvement. In the future, we plan to improve the effectiveness of our approach, potentially by either generating better features or enhancing our DDA model. We also plan to experiment on more dataset and evaluate our approach more thoroughly.

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