

1. (1) $O(1)$
 (2) $O(\log n)$
 (3) $O(n)$
 (4) $O(n^2)$
 (5) $O(n^2)$
 (6) 一般 $O(n^3)$
 Strassen算法 $O(n^{\log_2 7})$
2. 8, 1
3. (1) 正确 随着 n 的增大 $2^n > k * n$ 必然成立, 无论常数 k 有多大
 $2^n > 10^{1000} * n$
when $n > N$, N 为一确定常数
 (2) 正确 随着 n 的增大, $\log(n)$ 会越来越高于 1
 $\log 10^{1000} = 1000 \gg 1$
4. $T(n) = T(n-1) + T(n-2)$
 解得 $T(n) = O(\phi^n) \quad \phi = \frac{\sqrt{5}+1}{2}$
 功能 计算斐波拉契数列的第 n 项
5. $\frac{(1-\alpha)N * N + \alpha * N^{\frac{1+2+\dots+N}{N}}}{N} = (1 - \frac{\alpha}{2}) * N + \frac{\alpha}{2}$
6. 修改后的代码:

```

template<typename T>
void Vector<T>::mergeSort(Rank lo, Rank hi)
{
    if (hi - lo < 2) return;

    bool flag = true;
    for (int i = lo; i < hi - 1; i++)
        if (A[i] > A[i+1])
            flag = false, break;
    if (flag) return;

    int mi = (lo + hi)/2;
    mergeSort(lo, mi), mergeSort(mi, hi);
    merge(lo, mi, hi);
}

template <typename T>
void Vector<T>::merge ( Rank lo, Rank mi, Rank hi ) {
    T* A = _elem + lo;
    int lb = mi - lo; T* B = new T[lb];
    for ( Rank i = 0; i < lb; B[i] = A[i++] );
    int lc = hi - mi; T* C = _elem + mi;
    for ( Rank i = 0, j = 0, k = 0; (j < lb) || (k < lc); ) {
        if ( ( j < lb ) && ( ! ( k < lc ) || ( B[j] <= C[k] ) ) ) A[i++] =
B[j++];
        if ( ( k < lc ) && ( ! ( j < lb ) || ( C[k] < B[j] ) ) ) A[i++] =
C[k++];
    }
    delete [] B;
}

```

若子序列已经有序，进入mergeSort后会直接退出，此时复杂度达到线性。