$$\lim_{u\to 1}\overline{\chi}=c>0$$