

$$\textcircled{b} \quad \text{Var}[Y] = E[(Y - E[Y])^2] \\ = E[Y^2] - (E[Y])^2$$

$$E[Y] = a'(n)$$

$$\frac{\partial}{\partial n} E[Y] = a''(n)$$

$$\Rightarrow \frac{\partial}{\partial n} \int_{-\infty}^{\infty} y b(y) e^{(ny - a(n))} dy$$

$$= \int_{-\infty}^{\infty} (y - a'(n)) y b(y) e^{(ny - a(n))} dy$$

$$= \int_{-\infty}^{\infty} y^2 b(y) e^{(ny - a(n))} dy - a'(n) \int_{-\infty}^{\infty} y b(y) e^{(ny - a(n))} dy$$

$$\Rightarrow E[Y^2] - (E[Y])^2 = a''(\eta)$$

$$\Rightarrow E[(Y - E[Y])^2] = a''(\eta)$$

$$\Rightarrow \boxed{\text{Var}(Y) = a''(\eta)}$$