

디지털회로개론 HW1

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5. Compute the sub of the following pairs of 6-bit unsigned integers. If the answer is to be stored in a 6-bit location, indicate which of the sums produce overflow. Also, show the decimal equivalent of both operands and the result.

(c): 011100 + 011010

(c)
$$\begin{array}{r} 11 \\ 011100 \\ + 011010 \\ \hline 110110 \end{array} \Rightarrow \begin{array}{r} \text{decimal} \\ 28 \\ 26 \\ \hline 54 \end{array}$$

$\hookrightarrow \underline{0}/110110. \hookrightarrow \text{less than } 6^3.$

$\therefore \text{not overflow.}$

(f)
$$\begin{array}{r} 111 \\ 000101 \\ + 000111 \\ \hline 001100 \end{array} \Rightarrow \begin{array}{r} \text{decimal} \\ 5 \\ 1 \\ \hline 12 \end{array}$$

$\hookrightarrow \underline{0}/001100 \hookrightarrow \text{less than } 6^3$

$\therefore \text{not overflow.}$

9. Each of the following pairs of signed (two's complement) integers are stored in computer words (6 bits). Compute the sum as it is stored in a 6-bit computer word. Show the decimal equivalents of each operand and the sum. Indicate if there is overflow.

(b): 111010
000111

(e): 011010
001100

$$\begin{array}{r}
 \text{(b)} \quad \begin{array}{cccccc} & 1 & 1 & 1 & 1 & 1 \\ & 1 & 1 & 1 & 0 & 1 & 0 \\ + & 0 & 0 & 0 & 1 & 1 & 1 \\ \hline 1 & 0 & 0 & 0 & 0 & 0 & 1 \\ \sim & & & & & & \\ \text{carry} & & & & & & \\ \text{(ignored)} & & & & & & \end{array}
 \end{array}$$

$$\begin{array}{r}
 \Rightarrow \begin{array}{r} 111010 \subseteq \text{decimal 30 변환} \\ 111001 \Rightarrow \text{complement} \\ \Rightarrow 000110 \\ \therefore -6. \end{array}
 \end{array}$$

$$\begin{array}{r}
 \therefore + \begin{array}{r} -6. \\ 7 \\ \hline 1. \end{array} \quad \underline{\text{not overflow}}
 \end{array}$$

$$\begin{array}{r}
 \text{(c)} \quad \begin{array}{r} \begin{array}{cccccc} & 1 & 1 & & & \\ & 0 & 1 & 1 & 0 & 1 & 0 \\ + & 0 & 0 & 1 & 1 & 0 & 0 \\ \hline 0 & 1 & 0 & 0 & 1 & 1 & 0 \end{array} \\ \Rightarrow \begin{array}{r} 26 \\ 12 \\ \hline 38 \end{array} \end{array}
 \end{array}$$

two's complement 0122 152 넘어서면
산출 \therefore overflow

15. We have the following numbers stored in a computer. What is the decimal value represented if number is stored as;

i. BCD 8421

ii. BCD 5421

iii. BCD 2421

iv. BCD excess 3

v. binary unsigned

vi. Binary signed

(e): 1110 1101

(e) i) BCD 8421

$$1110 \Rightarrow 8+4+2 = 14 \Rightarrow \text{unused.}$$

$$1101 \Rightarrow 8+4+1 = 13 \Rightarrow \text{unused}$$

ii) BCD 5421

$$1110 \Rightarrow 5+4+2 = 11 \Rightarrow \text{unused}$$

$$1101 \Rightarrow 5+4+1 = 10 \Rightarrow \text{unused}$$

iii) BCD 2421

$$1110 \Rightarrow 2+4+2 = 8$$

$$1101 \Rightarrow 2+4+1 = 7$$

$\therefore 87.$

iv) BCD excess 3,

$$1110 \Rightarrow \text{unused}$$

$$1101 \Rightarrow \text{unused}$$

v) binary unsigned.

$$11101101$$

$$\Rightarrow 128 + 64 + 32 + 8 + 4 + 1 = 237$$

vi) binary signed.

$$\begin{array}{r} 1101101 \\ - 1101100 \\ \hline \end{array} \quad \begin{array}{l} \text{complement} \\ \rightarrow 0010011 \\ \therefore -19 \end{array}$$

5. Subtract the two pairs of numbers. Show the operands and the results in decimal and binary

a. assuming they are unsigned

b. assuming they are signed

1101 - 1100 1010 - 0110

Indicate if there is overflow.

(a)

$$\begin{array}{r} 1101 \\ - 1100 \\ \hline 0001 \end{array} \Rightarrow \begin{array}{r} 13 \\ - 12 \\ \hline 1 \end{array} \quad \left. \begin{array}{r} \\ \\ \end{array} \right\} \Rightarrow \text{not overflow}$$

$$\begin{array}{r} 1010 \\ - 0110 \\ \hline 0100 \end{array} \Rightarrow \begin{array}{r} 10 \\ - 6 \\ \hline 4 \end{array}$$

(b)

$$\begin{array}{r} 1101 \\ - 1100 \\ \hline \end{array} \Rightarrow \begin{array}{r} 1111 \\ 1101 \\ + 0011 \\ \hline 1) 0000 \end{array} \Rightarrow \begin{array}{r} \text{decimal} \\ -3 \\ 3 \\ \hline 0 \end{array} \quad \therefore \text{not overflow}$$

$$\begin{array}{r} 1010 \\ - 0110 \\ \hline \end{array} \Rightarrow \begin{array}{r} 1010 \\ 1001 \\ + 0011 \\ \hline 1) 0011 \end{array} \Rightarrow \begin{array}{r} -6 \\ -1 \\ \hline -13 \end{array} \quad \therefore \text{overflow}$$

look like positive.

2. Show truth tables for each of the following.

(c). The system has four inputs. The first two, a and b, represent a number in the range 1 to 3 (0 is not used). The other two, c and d, represent a second number in the same range. The output, y, is to be 1 if and only if the first number is greater than the second or the second is 2 greater than the first.

| A | B | C | D | First | Second | Y |
|---|---|---|---|-------|--------|---|
| 0 | 0 | 0 | 0 | 0 | 0 | X |
| 0 | 0 | 0 | 1 | 0 | 1 | X |
| 0 | 0 | 1 | 0 | 0 | 2 | X |
| 0 | 1 | 0 | 0 | 1 | 0 | X |
| 1 | 0 | 0 | 0 | 2 | 0 | X |
| 0 | 0 | 1 | 1 | 0 | 3 | X |
| 0 | 1 | 0 | 0 | 1 | 0 | X |
| 1 | 0 | 0 | 0 | 2 | 0 | X |
| 0 | 1 | 1 | 0 | 1 | 2 | 0 |
| 1 | 0 | 1 | 0 | 2 | 2 | 0 |
| 1 | 1 | 0 | 0 | 3 | 0 | X |
| 0 | 1 | 1 | 1 | 1 | 3 | 1 |
| 1 | 0 | 1 | 1 | 2 | 3 | 0 |
| 1 | 1 | 0 | 1 | 3 | 1 | 1 |
| 1 | 1 | 1 | 0 | 3 | 2 | 1 |
| 1 | 1 | 1 | 1 | 3 | 3 | 0 |

8. Using properties 1 to 10, reduce the following expressions to a minimum SOP form. Show each step (number of terms and number of literals in minimum shown in parentheses).

(h): $a'b'c' + a'bc' + a'bc + ab'c + abc' + abc$ (3 terms, 5 literals)

$$(h) : \underbrace{a'b'c' + a'bc'}_{i)} + \underbrace{a'bc + ab'c + abc' + abc}_{ii)}$$

$$\begin{aligned} i) \quad a'b'c' + a'bc' &= a'c'(b' + b) \\ &= a'c' \quad \therefore \text{Adjacency.} \end{aligned}$$

$$abc = abc + abc + abc \quad \therefore \text{Idempotency.}$$

$$\begin{aligned} ii) \quad (abc + a'bc) + (abc + ab'c) + (abc + abc') \\ = bc + ac + ab \quad \therefore \text{Adjacency} \end{aligned}$$

$$\therefore a'c' + b(a+c) + ac \quad \therefore \text{Distributive}$$

$$= a'c' + b + ac \quad \therefore \text{simplification}$$

9. Using properties 1 to 10, reduce the following expressions to a minimum POS form.

The number of terms and number of literals are shown in parentheses.

(a): $(a + b + c)(a + b' + c)(a + b' + c')(a' + b' + c')$ (2 terms, 4 literals)

$$(a+b+c)(a+b'+c)$$

$$= a+c \quad \therefore \text{Adjacency.}$$

$$(a+b'+c')(a'+b'+c')$$

$$= b'+c' \quad \therefore \text{Adjacency.}$$

$$\therefore (a+c)(b'+c')$$

13. For each of the following functions:

$$f(x, y, z) = \sum m(1, 3, 6), \quad g(x, y, z) = \sum m(0, 2, 4, 6)$$

(c): Show a minimum SOP expression (a: 2 terms, 5 literals; b: 1 term, 1 literal)

(f): Show a minimum POS expression (f: 2 solutions, 3 terms, 6 literals; g: 1 term, 1 literal)

$$f : x'y'z + x'yz + xyz'$$

$$g : x'y'z' + x'yz' + xy'z' + xyz'$$

(c) i) f .

$$x'y'z + x'yz = x'z \quad \therefore \text{Adjacency}$$

$$\therefore x'z + xyz'$$

ii) g .

$$x'y'z' + x'yz' = x'z' \quad \therefore \text{Adjacency}$$

$$xy'z' + xyz' = xz' \quad \therefore \text{Adjacency}$$

$$x'z' + xz' = z' \quad \therefore \text{Adjacency}$$

$$\therefore z'$$

(f)

$$\textcircled{1} \quad f': x'y'z' + x'y z' + xy'z' + xy'z + xyz$$

$$f: \underbrace{(x+y+z)(x+y'+z)}_{i)} \underbrace{(x'+y+z)(x'+y+z')}(ii) (x'+y'+z')$$

$$i) (x+y+z)(x+y'+z) = x+z$$

$$ii) (x'+y+z)(x'+y+z') = x'+y \quad \left. \vphantom{ii)} \right\} \therefore \text{Adjacency}$$

$$\therefore (x+z)(x'+y)(x'+y'+z')$$

$$\textcircled{2} \quad f': x'y'z + x'y z + xy'z + xyz$$

$$f: \underbrace{(x+y+z')(x+y'+z')}_i \underbrace{(x'+y+z')(x'+y'+z')}_ii$$

$$i) (x+y+z')(x+y'+z') = x+z'$$

$$ii) (x'+y+z')(x'+y'+z') = x'+z' \quad \left. \vphantom{ii)} \right\} \therefore \text{Adjacency}$$

$$\therefore (x+z')(x'+z') = z' \quad \therefore \text{Adjacency.}$$