

On the Aerodynamics of an Electric Vertical Take-off and Landing Aircraft Using Lattice Boltzmann Method

Reng Mo (莫礪),¹ Quan Zhou (周銓),¹ Qing Jia (賈青),¹ Chao Xia (夏超),¹ Huanxia Wei (韦欢夏)*,^{2,1} and Zhigang Yang (杨志刚)^{1,3}

¹⁾School of Automotive Studies, Tongji University, Shanghai, 201804, China

²⁾Department of Mechanical and Aerospace Engineering, University of Manchester, Manchester, M13 9PL, UK

³⁾Beijing Aeronautical Science and Technology Research Institute, Beijing, 102211, China

(*Electronic mail: huanxia.wei@postgrad.manchester.ac.uk)

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This study investigates the static stability and flow field of a cruising Electric Vertical Take-off and Landing (eVTOL) aircraft with compound-wing configuration using Lattice Boltzmann Method (LBM). Numerical accuracy of Finite Volume Method (FVM) and LBM is validated and comparatively analysed based on isolated rotor simulations. The LBM-based simulations are 8~9 times faster than those based on FVM for weakly compressible flows, which exhibits significant advantages in computational efficiency and cost. The maximum error of thrust is $\sim 11\%$ for LBM-based simulations, and that of torque is $\sim 7\%$, which is similar to that of FVM. Unsteady simulations based on LBM are conducted for the whole eVTOL aircraft, and flow field structures and static stability are further analysed. The results reveal that four varieties of vortical structures dominate the flow field, including wingtip and root vortices, vortices generated by static lift rotors, and vortices originating from the counter-rotating tail propeller pair, varying with angle of attack and angle of sideslip. Developing mechanisms and mutual interactions are examined in detail. The aircraft is unstable in terms of longitudinal and directional static stabilities, while it is stable in lateral enhanced by wingtip vortices. Besides, tail-mounted propulsion places higher demands on thrust propellers. Moreover, vortex generating at leading upper lift rotor edges delays separation on the wing upper surface, but imposes negative effects on both longitudinal and lateral stability. The high computational efficiency, accurate flow and realizable aerodynamic forces demonstrated by LBM provide engineering insights for future aerodynamic performance analysis and development of eVTOL aircraft.

Keywords. eVTOL aircraft, Lattice Boltzmann Method, Computational fluid dynamics, Static stability, Vortical structures

¹ I. INTRODUCTION

The Electric Vertical Take-off and Landing (eVTOL) aircraft plays an important role in the future three-dimensional urban transportation system¹. Compared to traditional helicopters, most types of eVTOL aircraft adopt compound-wing (also known as lift + cruise configuration) or multi-rotor designs, and have lower ceiling and airspeed, resulting in different aerodynamic performance.

Among all aerodynamic performance parameters, flight stability is the most critical aspect and receives much attention, as it is directly related to aviation safety. In conventional studies, mathematical models are developed and employed to predict the flight stability of aircraft. Based on the blade element theory, Pitt-Peters dynamic inflow theory and blade flapping motion model, He et al.² studied the flight stability of a compound-wing high-speed helicopter by establishing a comprehensive flight dynamics model. Wang³ investigated the flight characteristics of an inter-meshing rotor helicopter by constructing a mathematical model in a similar way and evaluated its control capability. Luan⁴ built a flight dynamics model of a compound-wing helicopter with two propellers, studied its stability, and then analysed the control performance by calculating dynamic and frequency responses. Wang et al.⁵ established a non-linear flight dynamics model for a tilt-rotor aircraft, and

examined how variations in nacelle tilt angle affect eigenvalues and eigenvectors of motion modes as well as its stability derivatives. With the advancement of computational technique, it is also a common way to gain insights into flight stability through Computational Fluid Dynamics (CFD) simulations, and the modelling and simulation in the early stage of development can contribute to a better design process⁶. Various methods can be used in CFD simulations to capture the aerodynamic characteristics of propellers or rotors as well as the aircraft driven by them. Seaver et al.⁷ compared the results of a flight test on lateral-directional stability with CFD simulations. The simulations were based on the Finite Volume Method (FVM), while zero-thickness disks with a specific pressure jump were used to simplify and substitute the actual physics of propellers. Kim et al.⁸ found it efficient to apply actuator methods when simulating the propellers and analysing the longitudinal and directional flight stability of two distributed propulsion aircraft. Kim et al.⁹ conducted Lattice Boltzmann Method (LBM) to quantify rotor-airframe aerodynamic interaction in hover by varying the airframe geometry (cylinder, cone) and the rotor-airframe separation distance. The computations captured tip vortex breakdown, transition to a turbulent wake, and proximity-induced modifications of the underbody fountain flow driven by rotor downwash circulation. Apart from these mid-fidelity methods, researchers have also adopted high-fidelity methods such as the sliding mesh approach¹⁰ to represent the full blade accurately in numerical simulations, while novel grid setups such as a Cartesian off-body grid¹¹ have proven effective in representing blade rotation and elastic blade deformation. Gao et al.¹² employed unsteady Reynolds-averaged Navier-Stokes (uRANS) to resolve the dynamic stall vortex and trailing edge vortex evolution on a single rotor airfoil, validating the aerodynamic predictions against experimental data and relating vortex-driven unsteady pressure loading to the stall process. Moreover, CFD simulations facilitate the analysis of flow structures around the aircraft. Roh et al.¹³ investigated the wake interaction around the tail propellers of a helicopter, thereby revealing the key factors in its directional stability. Similar technique was also demonstrated for helicopters with leading-edge slatted tailplane¹⁴ and biplane tailplane¹⁵. Qi et al.¹⁶ used detached-eddy simulation (DES) with overset mesh to quantify how a hovering coaxial rotor aerodynamically interacts with the ground and a nearby cubical obstacle at multiple relative positions. Su et al.¹⁷ performed Reynolds-averaged Navier-Stokes (RANS) simulations with overset mesh to resolve the unsteady aerodynamic interactions among the upper and lower rotors, the ship flight deck, and the hangar door during vertical descent and landing. Green et al.¹⁸ measured the flow field around an isolated rotor in axial descent, and Chae et al.¹⁹ expanded this scenario to a pair of twin rotors, revealing the flow structures and thrust characteristics.

Nevertheless, as eVTOL aircraft represent a relatively recent concept, research into their aerodynamics remains in its early stages, with limited studies addressing the flight stability. Lee et al.²⁰ conducted a hover performance analysis of an eVTOL aircraft using a rotorcraft comprehensive analysis code, and identified effective control methods to enhance performance. Stokkermans et al.²¹ conducted wind tunnel experiments on two propellers in side-by-side and one-after-another arrangements to quantify how axial and lateral spacing alters aerodynamic interaction penalties in thrust, power, in-plane forces, and out of plane moments, supported by total pressure and planar PIV measurements of the slipstream. Simmons et al.²² developed a high-fidelity integrated aero propulsive model for the LA-8 tandem tilt-wing distributed electric propulsion (DEP) eVTOL using wind tunnel data obtained with design of experiments (DoE) methods, targeting coupled propeller wing interaction effects and high incidence propeller aerodynamics across the flight envelope. Based on the Vortex Particle Method (VPM), Zanotti et al.²³ performed mid-fidelity simulations to investigate the flow interactions between front and rear propellers. The thrust loss effect of the rear propeller was observed as the overlap between tandem propellers increased. Gao et al.²⁴ introduced a reformulated VPM approach to examine the aerodynamic performance of side-by-side propellers across varying advance ratios and angles of sideslip, and provided insights into the surrounding flow fields of the eVTOL aircraft. Araghizadeh et al.²⁵ employed a mid-fidelity framework with a stochastic turbulence inflow generator to assess how atmospheric turbulence modifies the rotor wake and aerodynamic loading of tandem eVTOL aircraft in cruise. It is concluded that incoming turbulence progressively disrupts and degrades wake coherence, enhances load instability, and promotes blade-vortex interactions. Later, they simulated a full configuration XV-15 tilt-rotor eVTOL during transition flight using VPM to resolve unsteady aerodynamic loads and wake development over varying nacelle tilt angles²⁶. Liu et al.²⁷ did similar investigation on tilt-wing eVTOLs but

71 with high-resolution quasi-steady simulations, to characterize aerodynamic interference and wake
 72 evolution of multirotor tilt-wing eVTOL configurations during configuration conversion, comparing
 73 a single tilt-wing and a tandem tilt-wing layout. Deng et al.²⁸ conducted wind tunnel tests to
 74 characterize tilt-rotor eVTOL aerodynamics under coupled variations of propeller slipstream, angle
 75 of attack (AoA), aileron deflection, and flap deflection, deriving forces, moments, and aerodynamic
 76 coefficients. Luan et al.²⁹ combined test bench measurements with computational fluid dynamics
 77 to quantify how rotor dihedral angle and AoA under horizontal inflow reshape propeller upwash
 78 and downwash, thrust sharing among adjacent rotors, and overall force and moment responses.
 79 Bucherelli et al.³⁰ applied a mid-fidelity numerical framework with a staged buildup from an iso-
 80 lated rotor to a full aircraft configuration, to quantify inter-rotor and airframe interaction effects on
 81 rotor performance in hover and cruise. The simulations indicated limited interaction penalties in
 82 hover, whereas cruise exhibited stronger interactions. Sun et al.³¹ performed numerical simulations
 83 to map how true airspeed, rotational speed, and tip clearance govern ducted fan aerodynamic per-
 84 formance for large-scale electric propulsion, establishing robust parametric correlations for thrust
 85 variation. Another line of related research falls onto the development of eVTOL aircraft with
 86 unique layouts or among diverse configurations. Chang et al.³² proposed a tandem-channel wing
 87 layout for eVTOL aircraft. The longitudinal stability was analysed through CFD simulations based
 88 on FVM and the multiple reference frame method. Kim et al.³³ evaluated a specific eVTOL con-
 89 figuration using vortex lattice method, a low-fidelity analysis tool, and calculated the static margin
 90 under various conditions. However, directional and lateral stability analyses were not yet conducted.

91 It can be seen that the existing literature offers limited investigations on the flight stability of
 92 eVTOL aircraft, despite the critical importance of flight stability, especially in the early stages
 93 of aircraft development. Moreover, the majority of numerical simulations to date have relied on
 94 FVM, while few studies to date have employed the LBM method in this context. With the rapid
 95 development of GPU technology in recent years, the multi-core architecture of GPUs has signifi-
 96 cantly improved the efficiency in parallel floating-point operations, providing a novel computational
 97 paradigm distinct from conventional CPU-based huge clusters. In this regard, LBM stands out for
 98 its algorithmic simplicity, computational accuracy, and suitability for data distribution of parallel
 99 computing, making it especially effective for CFD computations on GPUs³⁴. Additionally, LBM
 100 inherently incorporates discrete time terms, granting it a natural capability for unsteady simulations,
 101 which is essential for high-fidelity CFD simulations of rotating mechanisms such as rotors and pro-
 102 pellers. LBM framework utilizes a Cartesian grid integrated with the immersed boundary method
 103 (IBM), and the numerical algorithm itself is inherently suitable for unsteady simulations with ro-
 104 tating machinery. A critical advantage of this approach is the elimination of interpolation-induced
 105 errors at the interfaces of rotating sub-domains, which are inherent in FVM for rotor simulations
 106 using sliding or overset mesh. Consequently, LBM could represent a highly efficient and promising
 107 approach for CFD simulations in eVTOL research. Nonetheless, also due to numerical methods,
 108 particularly boundary treatments, the numerical accuracy of LBM have prompted discussion by
 109 peers. A systematic study and analysis are urgently needed to quantitatively assess the reliability of
 110 LBM in industrial applications involving rotating machinery such as eVTOL aircraft by comparing
 111 against experiments.

112 We employ the LBM as a high-fidelity framework to resolve the unsteady fluid-dynamic mech-
 113 anisms underlying eVTOL static stability. Dynamic stability such as phugoid and plunging modes
 114 remains outside the current scope, and will be further investigated in our future work. The numerical
 115 approach is validated against experimental study on an eVTOL lift rotor. A comparative evaluation
 116 between LBM and conventional FVM is performed in terms of numerical accuracy, computational
 117 power consumption and fidelity of rotor flow field representations. Accordingly, we demonstrate
 118 the multifaceted advantages of the LBM for eVTOL aerodynamic engineering and research as a
 119 GPU-accelerated, high-efficiency, high-fidelity numerical method, particularly well suited to rotor-
 120 craft applications. Subsequently, unsteady CFD simulations of the complete eVTOL configuration
 121 are conducted using the same LBM approach to capture time-resolved surrounding flow and wake
 122 features, enabling systematic analysis of longitudinal, directional, and lateral stability. The static
 123 stability characteristics are quantified by examining the variation of pitch moment with AoA, yaw
 124 moment with angle of sideslip, and roll moment with angle of sideslip, respectively, which are di-
 125 rectly linked to asymmetric wake loading and unsteady pressure and shear-stress distributions. The

126 contributions of individual components to the overall static stability of the eVTOL aircraft are evaluated.
 127 Furthermore, the surrounding flow field of the eVTOL aircraft is visualized and analysed
 128 via pressure and velocity fields, vortical structures, and wake topology, thereby providing a com-
 129 prehensive flow-based understanding of the stability behaviour of this eVTOL configuration and its
 130 governing factors.

131 The remainder of this paper begins with the description of LBM in Section II A and the validation
 132 of this numerical method in Section II B, followed by eVTOL modelling and computational setup
 133 in Section II C. The time-averaged and instantaneous flow fields of the eVTOL aircraft are shown in
 134 Section III A. The static stability characteristics are presented and discussed in Section III B. Finally,
 135 the conclusion is outlined in Section IV.

136 II. NUMERICAL SIMULATION

137 In this section, the theoretical basis of LBM is briefly introduced. The geometry of eVTOL used
 138 in this study and the numerical configurations are presented. The numerical accuracy of both LBM
 139 and FVM methods are validated by comparing with experimental data of the eVTOL rotor.

140 A. Lattice Boltzmann Method (LBM)

141 LBM is derived from the Boltzmann transport equation

$$142 \frac{\partial f}{\partial t} + \boldsymbol{\xi} \cdot \nabla f + \boldsymbol{a} \cdot \frac{\partial f}{\partial \boldsymbol{\xi}} = \Omega(f), \quad (1)$$

143 where f is the particle velocity distribution function, \boldsymbol{a} denotes the particle acceleration, $\Omega(f)$ is
 144 the collision operator, and then gives

$$145 \begin{aligned} \boldsymbol{\xi} \cdot \nabla f &= \left(\frac{dx}{dt} \mathbf{i} + \frac{dy}{dt} \mathbf{j} + \frac{dz}{dt} \mathbf{k} \right) \cdot \left(\frac{\partial f}{\partial x} \mathbf{i} + \frac{\partial f}{\partial y} \mathbf{j} + \frac{\partial f}{\partial z} \mathbf{k} \right) \\ &= u \frac{\partial f}{\partial x} + v \frac{\partial f}{\partial y} + w \frac{\partial f}{\partial z}, \end{aligned} \quad (2)$$

$$146 \begin{aligned} \boldsymbol{a} \cdot \frac{\partial f}{\partial \boldsymbol{\xi}} &= \left(\frac{du}{dt} \mathbf{i} + \frac{dv}{dt} \mathbf{j} + \frac{dw}{dt} \mathbf{k} \right) \cdot \left(\frac{\partial f}{\partial u} \mathbf{i} + \frac{\partial f}{\partial v} \mathbf{j} + \frac{\partial f}{\partial w} \mathbf{k} \right) \\ &= \frac{du}{dt} \frac{\partial f}{\partial u} + \frac{dv}{dt} \frac{\partial f}{\partial v} + \frac{dw}{dt} \frac{\partial f}{\partial w}, \end{aligned} \quad (3)$$

148 where \mathbf{i} , \mathbf{j} and \mathbf{k} are the unit vectors in x , y and z coordinate directions respectively, u , v and w
 149 are the velocity components of the particle in these directions. Eq. 2 represents the change in the
 150 distribution function in physical space due to velocity, while Eq. 3 represents the change in the
 151 distribution function in velocity space due to acceleration.

152 LBM further discretises the Boltzmann equation along characteristic directions using probability
 153 distribution functions, thus obtaining the Lattice Boltzmann Equation (LBE)

$$154 f_i(\mathbf{x} + \mathbf{e}_i \Delta t, t + \Delta t) - f_i(\mathbf{x}, t) = \Omega_i(\mathbf{x}, t), \quad (4)$$

155 where i represents the characteristic direction, for which three-dimensional twenty-seven (D3Q27)
 156 lattice structure is employed in this study, \mathbf{x} represents the physical space, \mathbf{e}_i is the discrete velocity
 157 vector, Δt is the discrete time step, t denotes the current time; $f_i(\mathbf{x}, t)$ denotes the particle distri-
 158 bution function at position \mathbf{x} , time t and along the direction of discrete velocity vector \mathbf{e}_i , $\Omega_i(\mathbf{x}, t)$
 159 represents the effect of particle collisions on the distribution function at position \mathbf{x} , time t along
 160 \mathbf{e}_i . Since it examines not the state of individual particles, but rather the state of all particles (i.e.
 161 the particle collective) within a sufficiently small control volume centred at the endpoint of the po-
 162 sition vector, LBM describes fluid flow at the mesoscopic scale³⁵. Through specific techniques,

163 the Navier-Stokes equations can be recovered from LBE³⁶, thereby demonstrating the macroscopic
164 similarity between LBE and the original Navier-Stokes equations.

165 The core steps in the LBM iterative process are collision and streaming, and the specific procedure
166 includes the following steps.

167 The fluid density $\rho(\mathbf{x}, 0)$, the velocity vector $\mathbf{u}(\mathbf{x}, 0)$ and the particle distribution function $f_i(\mathbf{x}, 0)$
168 are firstly initialised, then the equilibrium particle distribution function $f_i^{\text{eq}}(\mathbf{x}, t)$ are calculated.
169 Next, the collision operator $\Omega_i(\mathbf{x}, t)$ is to be computed. The Bhatnagar – Gross – Krook (BGK)
170 model³⁷ is commonly used to simplify the collision operator:

$$171 \quad \Omega_i(\mathbf{x}, t) = \frac{1}{\tau} [f_i^{\text{eq}}(\mathbf{x}, t) - f_i(\mathbf{x}, t)]. \quad (5)$$

172 The computation of post-collision distribution function $f_i^*(\mathbf{x}, t)$ is then given by

$$173 \quad f_i^*(\mathbf{x}, t) = f_i(\mathbf{x}, t) + \Omega_i(\mathbf{x}, t), \quad (6)$$

174 and particle streaming is performed based on

$$175 \quad f_i(\mathbf{x} + \mathbf{e}_i \Delta t, t + \Delta t) = f_i^*(\mathbf{x}, t). \quad (7)$$

176 Afterwards, specific boundary conditions are applied, followed by the calculation of macroscopic
177 quantities at time $t + \Delta t$ which includes fluid density ρ and velocity \mathbf{u} :

$$178 \quad \rho = \sum f_i \quad \text{and} \quad \mathbf{u} = \frac{1}{\rho} \sum \mathbf{e}_i f_i. \quad (8)$$

179 Finally, repeat the iterative process above until the convergence criteria are met. The complete
180 iteration is expressed as Fig. 1.

182 The pressure is calculated explicitly in the iteration using ideal gas equation:

$$183 \quad p = \rho R T \quad (9)$$

184 where R is the specific gas constant, and T is the reference temperature.

185 LBM offers advantages such as solving linear equations instead of partial differential equations
186 (PDE), which facilitates explicit computation and enables highly parallelised processing on
187 GPUs, even for real-time simulation³⁸. Furthermore, compared to conventional FVM solvers, LBM
188 demonstrates superior performance and resolution in simulating complex geometries involving flow
189 separation, moving boundaries, and fluid-solid interaction³⁹. However, LBM has inherent limita-
190 tions. In its basic form without corrective measures, it is restricted to low Mach number range and is
191 facing challenges in accurately simulating high-speed and compressible flow⁴⁰. Additionally, fluid
192 velocity can erroneously propagate through solid boundaries of thin structures caused by the use of
193 coarse Cartesian grids, resulting in non-physics fluid leakage⁴¹.

194 In this study, LBM simulations are performed using a novel LBM platform, Aerocae (AEROCAE
195 Digital, version 2025), based on the corrected LBM approach and Large Eddy Simulation (LES).

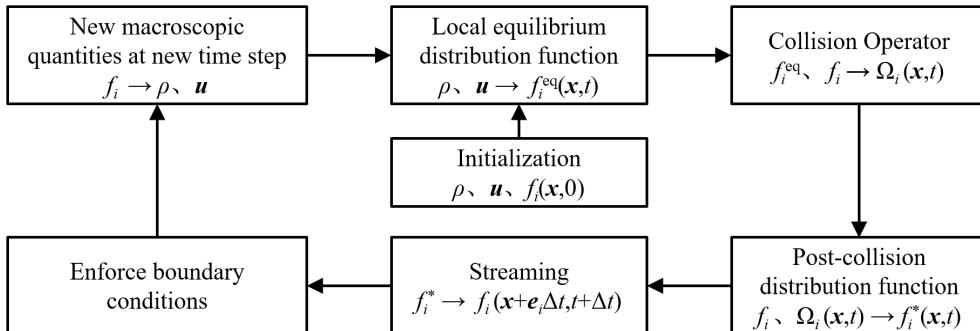


FIG. 1. LBM iterative flowchart.

The D3Q27 lattice structure is employed in the platform. While BGK collision model is a simplistic collision operator, there are significant truncation errors for simulations of high Reynolds number flows based on it since a single relaxation rate is used for all physical quantities. Therefore, a cumulant-based, multiple relaxation time collision model with an optimised higher-order relaxation rates developed by Lyu et al.⁴² is adopted in the solver. To solve the turbulent boundary layer in an unsteady flow more accurately and efficiently and prevent numerical artifacts, a novel hybrid near-wall model by Liu et al.⁴³ is implemented, in which a macroscopic model and a mesoscopic model are combined, predicting a filtered wall velocity and reconstructing non-equilibrium distribution functions normal to the wall. For turbulence modelling, the Wall-Adapting Local Eddy-viscosity (WALE) sub-grid-scale (SGS) model⁴⁴ is used towards LES.

B. Validation

The eVTOL rotor in a hovering state is considered for validation of numerical results. Our eVTOL rotor, T-Motor 62" × 24", has two blades and a diameter of 62 inch (approx. 1.575 m) and made by carbon fibre. The geometry model (Fig. 2) is supplied by the manufacturer T-Motor as their precise model for manufacture. The experimental study is conducted using Series 1780 thrust & torque testing stand (Tyto Robotics, 2019) under varying rotational speed, and the operation of the rotor is powered by U15XXL Kv29 (T-Motor, 2019) and under the control of FLAME 280A HV (T-Motor, 2019) as the electronic speed controller of power system.

CFD simulations are conducted across a range of rotational speed from 1000 rpm to 2200 rpm based on both LBM-LES and FVM-LES numerical methods. As the comparative reference, the FVM-LES simulations are performed using Star-CCM+ (Siemens, version 2506). Low y^+ wall treatment with compressible implicit unsteady solver is selected. The computational domain is spatially discretized with hybrid polyhedral mesh to capture the tip vortices. The surface y^+ is ensured to be below 0.5 with the help of 20 prismatic layers under growth rate of 1.40. The final mesh cell count is 42.0 million. For the mesh strategy of LBM-LES, a six-level multi-resolution Cartesian grid is employed, with the minimum grid size of 3 mm and the outer size of 96 mm, as shown in Fig. 3.

During the validation stage, the FVM-LES simulation is conducted based on a workstation with a single Intel Xeon Platinum 8160T processor with 144 cores, while the LBM-LES simulation is performed on a consumer desktop PC with customised NVIDIA GeForce RTX 2080 Ti graphics card with 22 GB of GPU memory. The actual computational time of both numerical methods increases approximately linearly with the physical time in the simulations, showing no thermal



FIG. 2. CAD model of eVTOL rotor.

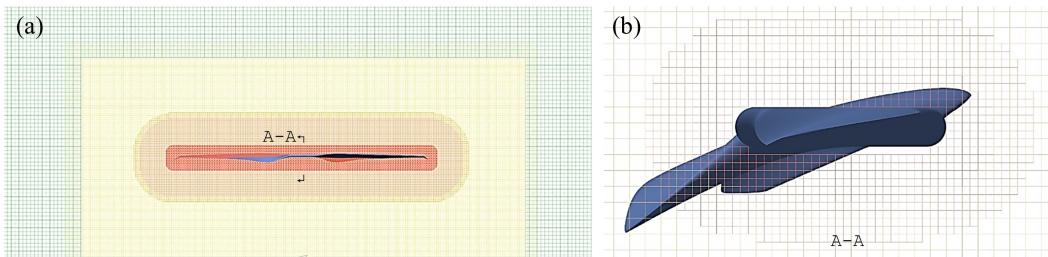


FIG. 3. Mesh sectional view of LBM-LES simulation on the eVTOL rotor. (a) mid-section, (b) a zoomed view.

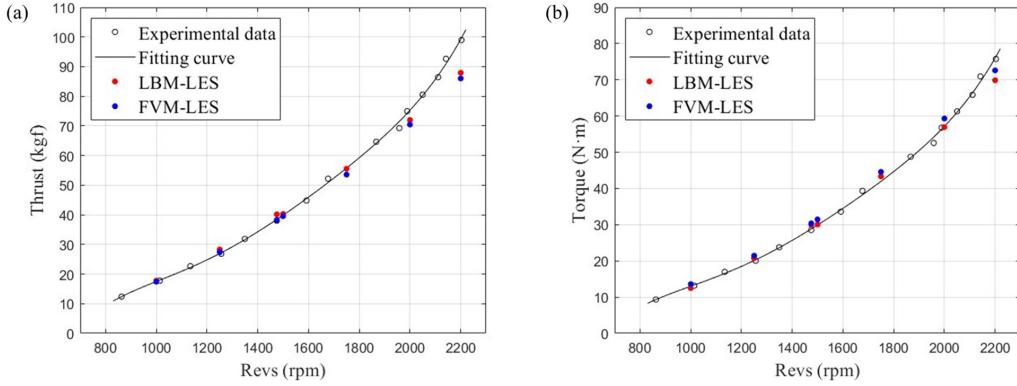


FIG. 4. Thrust and torque by the rotor versus rotational speed based on experimental results with fitting curve, LBM-LES and FVM-LES. (a) Thrust and (b) Torque.

228 performance degradation. For the same physical time, the LBM-LES simulation on the GPU is
 229 approximately 8~9 times faster than FVM-LES on the CPU, substantially reducing the simulation
 230 time for each case and offering considerable effectiveness. Considering the variation in leasing costs
 231 of GPUs and CPUs, the financial advantage is more pronounced than the time savings.

232 The thrust and torque of the motor from both numerical and experimental studies are plotted
 233 in Fig. 4. It can be shown that the maximum error of the FVM-LES simulation is approximately
 234 13% for thrust, while that of the LBM-LES simulation is about 11%. For torque, the maximum
 235 errors of both numerical methods are around 7%. It is also worth noting that, the thrust obtained by
 236 both methods begin to deviate evidently from the experimental values when the rotor speed reaches
 237 2000 rpm. For torque data, the errors from both methods are smaller until the rotor speed reaches the
 238 highest 2200 rpm, although they still underestimate the torque. Overall, for both numerical methods,
 239 the errors in thrust and torque increase with rotor speeds, and their accuracy is comparable with
 240 each other. When the rotor speed reaches 2000 rpm, the tip Mach number is approximately 0.46,
 241 at which point the relative airflow near the rotor tip reaches a weakly compressible state. Given
 242 that the error margin is acceptable for most engineering applications and surpasses that of most
 243 existing studies, it can be concluded that the LBM-LES numerical method demonstrates acceptable
 244 accuracy for weakly compressible airflow and can be considered a viable numerical approach for
 245 the following unsteady simulations of eVTOL aircraft. Currently, the validation is limited to thrust
 246 and torque of a single isolated rotor at various rotational speeds, limited by accessible experimental
 247 and measurement techniques.

248 C. Geometric model and computational setup

249 1. eVTOL design and configuration

250 A compound-wing configuration of the eVTOL aircraft is designed with reference to various
 251 commercial eVTOL models. The model measures 4.975 m in length (L) and 1.603 m in height (H).
 252 The fixed-wing uses a rectangular wing with a NACA 2412 aerofoil, a chord length of 1.2 m and
 253 a wingspan (W) of 8 m, resulting in a reference wing area of 9.6 m^2 . There are no aerodynamic
 254 control surfaces (e.g. ailerons, flaps, rudder or elevator) on the simplified eVTOL model, because
 255 this study focuses on the inherent stability of the aircraft, and all the control surfaces should be in
 256 the neutral position. Each wing has a pylon mounted beneath its mid-span, each equipped with two
 257 coaxial counter-rotating lift rotors at the front and rear. A rear-mounted propeller group with two
 258 coaxial counter-rotating propellers is installed at the aft end of the fuselage. Both tail propellers
 259 have a three-blade configuration with a diameter of 1.72 m and a twist angle of 12° . For simplicity,
 260 the material is considered to be of uniform density, thereby the geometric centre is regarded as

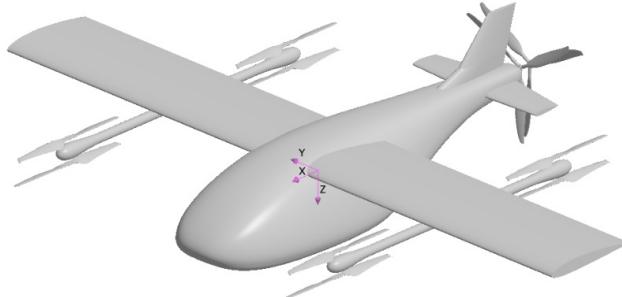


FIG. 5. The eVTOL CAD model with its local coordinate system.

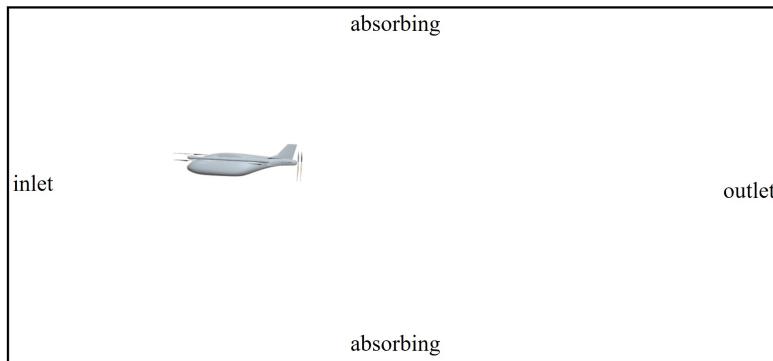


FIG. 6. Computational domain and boundary conditions of the eVTOL aircraft simulation.

the centre of gravity (CoG) of the aircraft. Thus, the origin of both the body axis system and the air-path axis system is located at the geometric centre. The geometric model and its body axis system are shown in Fig. 5, with the coordinate origin at CoG. In the following sections, $W/2$ is adopted as the characteristic length for non-dimensionalisation, with the superscript asterisks denoting dimensionless quantities.

2. Computational domain and boundary conditions

The computational domain measures 35 m in length, 20 m in width and 16 m in height, yielding a cross-sectional area of 320 m^2 . The blockage ratio is 0.7875%, calculated by $A_{\text{eVTOL},x}/A_{\text{section},x}$, which is regarded as sufficiently small. On the surface of the aircraft, the near-wall model proposed by Liu et al.⁴³ is applied within the bounce-back scheme as the boundary condition. The node-refilling method⁴⁵ is employed to update new fluid nodes generated within the computational domain due to the rotation of the tail propellers. The boundaries of the rectangular fluid domain except the inlet and outlet are treated with an absorbing boundary condition, which allows fluid to exit freely without reflecting pressure waves. A free-stream velocity of 60 m/s is imposed at the inlet boundary, which is regarded as reference velocity for non-dimensionalisation. Therefore, the Reynolds number based on the wing chord and cruise speed is $Re_c = 4.6 \times 10^6$. The tail propeller speed is set to 2000 rpm, in which case the tip Mach number can be estimated as $Ma_{\text{tip}} = 0.55$ using the rotational speed, propeller disk diameter, free-stream velocity and acoustic velocity, and it is in the weakly-compressible regime (i.e. $0.3 < Ma_{\text{tip}} < 0.7$). The advance ratio is $J = 1.05$. The simulation condition parameters are summarized in Tab. I. The computational domain and boundary conditions are shown in Fig. 6.

The physical continuum is ideal gas with a reference density of 1.18415 kg/m^3 , a reference pressure of $1.01325 \times 10^5 \text{ Pa}$ and a reference temperature of 300 K. The WALE SGS model⁴⁴ is em-

ployed in the simulation. A test case with an AoA of 3° and an angle of sideslip of 0° is adopted. The forces acting on the fuselage are observed to have stabilised under these conditions. Therefore, a physical time of 0.5 s satisfies the convergence requirement and is used for all the following simulations.

For studies on longitudinal stability, simulations are typically conducted at a fixed angle of sideslip while varying AoA to investigate the variation of pitch moment coefficient with AoA^{6,8}. For studies on lateral and directional stability, AoA is set to the cruise condition, and simulations are performed at various angles of sideslip to analyse the changes in yaw moment coefficient and roll moment coefficient with respect to the angle of sideslip^{6,8,10}. The simulation conditions of AoA and angle of sideslip selected for different static stability analyses in this study are listed in Table II. To simplify the expression and improve readability, AoA and angle of sideslip are denoted by the symbols α and β , respectively.

3. LBM mesh strategy

Since the collision and streaming processes in LBM rely on local interactions among discrete lattice nodes and their immediate neighbours, and the regular structure of Cartesian grids, which facilitates the streaming step of the distribution functions, naturally aligns with the discrete velocity directions of the LBM, a structured Cartesian grid strategy is employed. However, due to limited computational resources, achieving close conformity with curved solid boundaries through extreme grid refinement is often impractical. Therefore, the immersed boundary method⁴⁶ is adopted. This method discretises both the fluid domain and the solid interior with computational nodes. By comparing the positions of these nodes with the closed solid boundary, each node is classified as belonging to either the fluid domain or the solid structure.

The details of grid setup for the LBM-based eVTOL simulation in this study are configured as follows. The minimum grid resolution is 3 mm, with a total of 7 multi-resolution levels, similar to which of the single rotor simulation. Four layers of overlap grids are incorporated to facilitate numerical transition. A wake refinement zone is configured behind and below the fuselage of aircraft, extending 1 m in both directions, which is specifically targeted at the near-wake region where the most significant turbulence and interactions occur. The total count of grid cells is approximately 167 million. A mesh convergence study is conducted to eliminate the influence of cell counts on the simulation results, performed on a single NVIDIA A800 80GB GPU. By adjusting the minimum lattice size, five distinct sets of grids with varying refinement levels are generated. The mesh quality is assessed by the convergence of the lift coefficient C_L and drag coefficient C_D , given by

$$\begin{aligned} C_L &= \frac{L}{\frac{1}{2}\rho U_\infty^2 A_x}, \\ C_D &= \frac{D}{\frac{1}{2}\rho U_\infty^2 A_x}, \end{aligned} \quad (10)$$

where F_x and F_z are the total drag and lift force, respectively. Additionally, ρ is the density of the air, U_∞ is the free stream velocity, and A_x is the projected area in the free stream direction. The convergence rate is defined by

$$\text{Cov}_{C_i} = \frac{C_i^{\text{current}}}{C_i^{\text{finest}}}, \quad (11)$$

| Non-dimensional parameter | Value |
|-----------------------------------|-------------------|
| Cruise speed (m/s) | 60 |
| Reynolds number Re_c | 4.6×10^6 |
| Tip Mach number Ma_{tip} | 0.55 |
| Advance ratio J | 1.05 |

TABLE I. Governing parameters of conditions.

| Static stability | AoA (°) | angle of sideslip (°) |
|------------------------|------------------------|------------------------|
| Longitudinal stability | -9, -6, -3, 0, 3, 6, 9 | 0 |
| Directional stability | 3 | -9, -6, -3, 0, 3, 6, 9 |
| Lateral stability | 3 | -9, -6, -3, 0, 3, 6, 9 |

TABLE II. Overview of simulation conditions for static stability analysis.

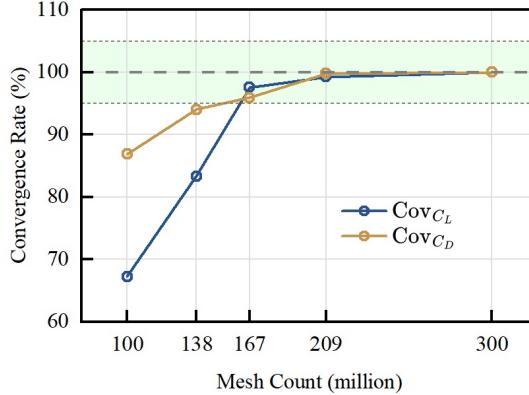


FIG. 7. Mesh convergence study for eVTOL simulations.

and is shown in Fig. 7. It can be seen that C_D and C_L remain unchanged with further reduction in the minimum lattice size once it reaches 3.0 mm. Considering the balance between simulation accuracy and computational efficiency, this size is selected for all subsequent eVTOL simulations in this study.

To further validate the mesh strategy towards a satisfactory LES configuration, two approaches are applied. First, the mesh resolution is also evaluated using two-point correlation in a series of continuously-distributed probes behind the tip of propeller, referring to Davidson⁴⁷. The normalized two-point correlation is given by

$$C_{U_i}^{\text{norm}}(\vec{x}_0, \vec{x}) = \frac{\overline{U'_i(\vec{x}_0) U'_i(\vec{x})}}{\overline{U'_{i\text{RMS}}(\vec{x}_0) U'_{i\text{RMS}}(\vec{x})}}, \quad U'_{i\text{RMS}}(\vec{x}_i) = \overline{(U'_i(\vec{x}_i))^2}^{1/2}, \quad (12)$$

where \vec{x}_0 and \vec{x} are the spatial coordinates of the reference point and the current point, respectively, and U_i is the local velocity in the i^{th} direction. In our study, the reference point is located at (-7.05, 0, -0.86) m, following with other 19 continuous points spacing in single mesh size (Figure 8(a)). It is recommended that the largest eddies should be resolved by at least eight cells, corresponding to a positive correlation for a minimum of 8 cells. The correlation versus stride number of cells is presented in Figure 8(b). It is shown that, the correlation with the reference point remains high for the first 15 cells, demonstrating a reasonable resolution of the mesh in our study. Furthermore, the spectral kinetic energy density at the wavenumber vector \mathbf{k} is defined as

$$e(\mathbf{k}) = \frac{1}{2} \left(|\hat{u}(\mathbf{k})|^2 + |\hat{v}(\mathbf{k})|^2 + |\hat{w}(\mathbf{k})|^2 \right), \quad (13)$$

where $\hat{\mathbf{u}}(\mathbf{k}) = \mathcal{F}\{\mathbf{u}'(\mathbf{x})\}$ denotes the Fourier transform of the velocity-fluctuation field \mathbf{u}' , with $\mathbf{u}' = \mathbf{u} - \langle \mathbf{u} \rangle$. The corresponding three-dimensional isotropic (one-dimensional) energy spectrum is obtained by averaging over all wavevectors with identical magnitude $k = \|\mathbf{k}\|$, such that the total kinetic energy satisfies $\int_0^\infty E(k) dk = \int_{\mathbb{R}^3} e(\mathbf{k}) d\mathbf{k}$, equivalently,

$$E(k) = \int_{\|\mathbf{k}\|=k} e(\mathbf{k}) dS_{\mathbf{k}} = k^2 \int_{4\pi} e(k, \Omega) d\Omega, \quad (14)$$

as shown in Figure 8(c). To assess consistency with the Kolmogorov $-5/3$ inertial-range scaling, we additionally compute the compensated spectrum $k^{5/3}E(k)$. The Nyquist wavenumber k_N and the

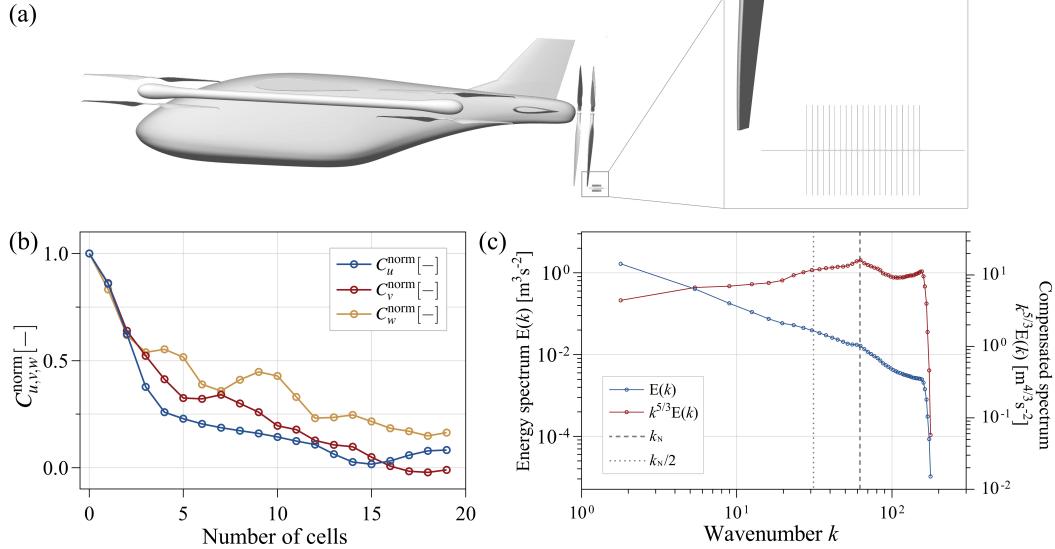


FIG. 8. Turbulence statistics verification. (a) Reference and computed points for correlation convergence study, (b) Convergence of two-point correlation $C_{u,v,w}^{\text{norm}}$ versus stride number of cells, and (c) energy spectrum $E(k)$ and compensated spectrum $k^{5/3}E(k)$.

reference limit $k_N/2$ are marked. From the figure, the energy spectrum remains strictly positive and varies smoothly over the entire set of resolved wavenumber range, with no spurious oscillations and discontinuities. For wavenumbers below $k_N/2$, $E(k)$ exhibits an approximately power-law decay and the compensated spectrum forms a broad, near-horizontal plateau, consistent with Kolmogorov inertial-range -5/3 scaling. This behavior indicates that the LES resolves a physically meaningful inertial cascade over a substantial portion of the spectrum. At high wavenumber end, there is no anomalous upturn, demonstrating no spectral pile-up (spectral blocking) or aliasing-driven energy accumulation. Overall, the spectral shape supports that the resolved range is physically consistent and that no grid-scale instabilities are present.

III. RESULTS

In this section, the dominant flow structures of this eVTOL aircraft are first analysed, followed by an evaluation of its static stability in longitudinal, directional and lateral directions.

A. Flow structures

The presentation of results on flow fields starts from the Euler vortices indicated by dimensionless Q-criterion (Fig. 9) during its cruise flight at $\alpha = 3^\circ$ and $\beta = 0^\circ$, in this context, the lift rotors stay inactive, aligning with the streamwise direction. Because the variations in AoA and sideslip angle are relatively small, the fundamental characteristics of the vortex system structure remain largely unchanged, with only minor differences in details and relative proportions. Therefore, only the flow structures under this condition are analysed in detail. Considering the need to balance the post-processing computational cost of hundred-million-cell grids with vortex identification performance, we employ the Q-criterion to capture three-dimensional vortical structures, which is defined using the velocity gradient tensor:

$$\nabla \mathbf{u} = \mathbf{S} + \boldsymbol{\Omega}, \quad \text{where} \quad \mathbf{S} = \frac{1}{2}(\nabla \mathbf{u} + (\nabla \mathbf{u})^T) \quad \text{and} \quad \boldsymbol{\Omega} = \frac{1}{2}(\nabla \mathbf{u} - (\nabla \mathbf{u})^T). \quad (15)$$

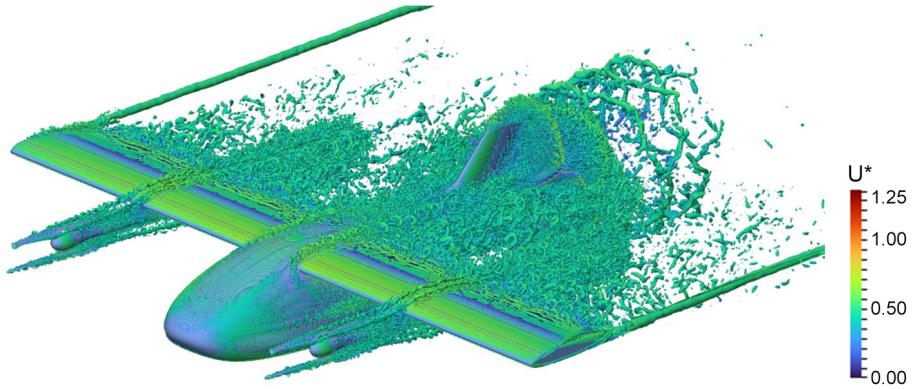


FIG. 9. Q-criterion isosurface ($Q^* = 10^4$ and 10^5) of eVTOL aircraft under $\alpha = 3^\circ$ and $\beta = 0^\circ$, coloured by velocity magnitude.

370 Here, \mathbf{S} is the symmetric strain-rate tensor and $\boldsymbol{\Omega}$ is the asymmetric rotation-rate (spin) tensor. The
371 Q-criterion is then the second invariant of $\nabla \mathbf{u}$, often written as:

$$372 \quad Q = \frac{1}{2} (\|\boldsymbol{\Omega}\|^2 - \|\mathbf{S}\|^2). \quad (16)$$

373 A region in which $Q^* > 0$ is often identified as a vortex, on the premise that local rotation $\|\boldsymbol{\Omega}\|$
374 dominates over strain $\|\mathbf{S}\|$. Four kinds of vortical structures dominate the surrounding and wake
375 flow of the aircraft. Multiple Q-criterion thresholds are tested, and the flow structures are shown to
376 be insensitive to the values. Accordingly, $Q^* = 10^4$ and 10^5 are used to facilitate clear visualization.

377 First, the eight lift rotors are aligned parallel to the directional axis of the aircraft, each producing
378 a pair of counter-rotating vortices at their edges. Among these, the tip vortices generated by the
379 two upper-front rotors are influenced by the fixed-wing and advect along its upper surface, whereas
380 those originating from the two lower-front rotors remain farther from the wing due to the package
381 alignment of the eVTOL aircraft. In addition, a pair of counter-rotating vortices develops at the
382 wing-fuselage junction, which gradually merges downstream with smaller vortices shed from the
383 rear fuselage.

384 Another distinct vortical structure forms at the wingtips, exhibiting high core vorticity and thus
385 a broader region of influence, with larger Q-criterion isosurface diameters than other stable vortex
386 structures. Fig. 10 shows a single dominant wingtip vortex that rolls up immediately aft of the
387 tip and remains attached to the trailing edge in the near field. The constant thickness tip and the
388 absence of winglets allow strong lateral pressure relief, thereby the crossflow wraps around the tip
389 early and close to the surface. The vortex is fed by three visible streams that converge at the trailing
390 edge. One stream curls from the forward segment of the tip onto the suction side. A second stream
391 issues from the region aft of maximum thickness along the suction side where the boundary layer
392 is locally thick and is swept outward to the tip. A third stream originates on the pressure side, turns
393 around the tip, and enters the roll up, supplying most of the circulation. The blunt, constant thick-
394 ness tip yields relatively thick initial shear layers, therefore the nascent vortex exhibits a larger core
395 radius and rapid early radial growth. In addition, intermittent small fragments convected with the
396 main tip vortex, arising where the tip shear layers meet and peel into the spiral sheet. Therefore, the
397 wingtip vortex lasts for a long distance with high stability. Finally, the tail propellers generate two
398 intertwined double-helical vortices at the blade tips, which are known as the tip vortex of propellers.
399 Due to the aft-mounted propulsion configuration, the stability of the thrust propeller's tip vortices is
400 relatively poor, evidently influenced by the upstream vortex structures. Examination of the isosur-
401 faces based on the Q-criterion reveals that the vortex tubes are discontinuous and dissipate almost
402 completely within merely three to four vortex helix pitches.

403 The velocity magnitude on the symmetry plane and the C_p on both the symmetry plane and the
404 fuselage surface are shown in Fig. 11a-b, respectively. The oncoming stream decelerates against the
405 rounded nose and terminates in a distinct stagnation region, visible as the near-zero velocity spot,

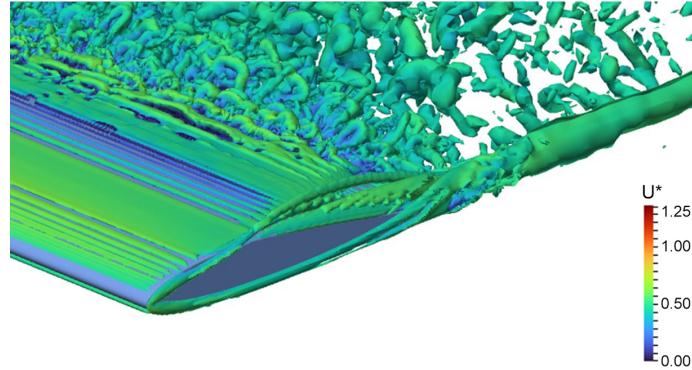


FIG. 10. Q-criterion isosurface ($Q^* = 10^4$ and 10^5) at the wingtip under $\alpha = 3^\circ$ and $\beta = 0^\circ$, coloured by velocity magnitude.

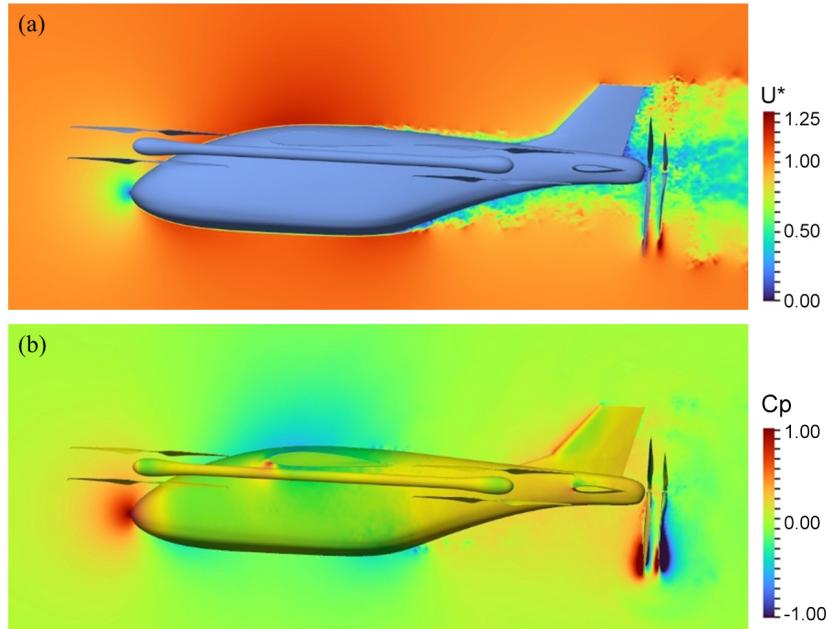


FIG. 11. Velocity and C_p of the eVTOL aircraft under $\alpha = 3^\circ$ and $\beta = 0^\circ$. (a) U^* and (b) C_p .

which sets the stagnation streamline that divides the upper and lower surface flows. Downstream of the nose the flow accelerates over the crown of the fuselage, producing a low- C_p band on the upper surface, while the lower surface maintains relatively higher C_p . This top to bottom pressure imbalance yields a modest positive normal force on the fuselage at the analysed incidence. Forebody to afterbody, the pressure recovers. The recovery on the lower afterbody imposes an adverse pressure gradient, and the velocity map shows a thickening low-speed layer with a local deficit immediately upstream of the empennage, consistent with boundary-layer separation on the lower aft fuselage and the onset of a momentum-deficit wake. The combination of high static pressure at the forebody and reduced static pressure over the afterbody identifies the fore to aft pressure differential as the dominant contributor to fuselage form drag under this condition.

Furthermore, Fig. 12 presents the Q-criterion isosurface of the eVTOL aircraft in a top view during cruising, focusing on the thrust propellers operating within the wake region of the fuselage, where its flow velocity is reduced due to the fuselage blockage. Therefore, the propeller blades experience a larger local effective AoA compared to front-mounted propulsion configuration, resulting in relatively higher blade efficiency, which is also known as the boundary layer ingestion

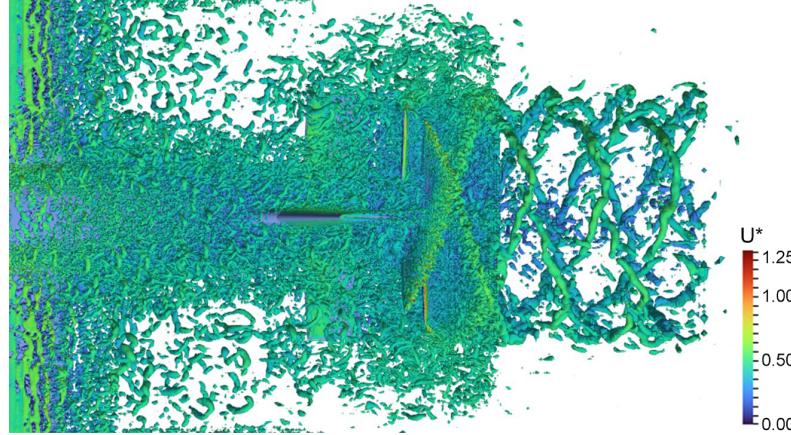


FIG. 12. Q-criterion isosurface ($Q^* = 10^4$ and $Q^* = 10^5$) of the eVTOL aircraft in a top view under $\alpha = 3^\circ$ and $\beta = 0^\circ$.

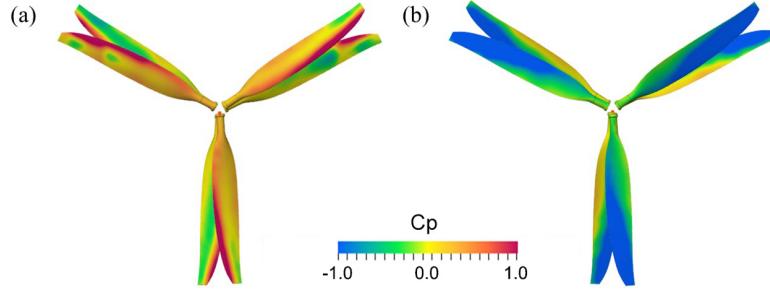


FIG. 13. Surface C_p contour of the tail propellers. (a) Pressure surface, (b) suction surface.

propulsion⁴⁸. Furthermore, for the counter-rotating propellers, the wake formed by their tip vortices exhibits two interwoven double-helical patterns, where the two tip vortices interact with each other and demonstrate stronger instability, and thereby can only persist shortly, see Fig 9. Fig. 13 further illustrates the difference in surface C_p between the windward side and the leeward side of the tail propellers. For the reasons discussed above, the pressure on the windward side of the propellers is higher than that on the leeward side, reducing the thrust by the tail-mounted propulsion system. In addition, because the blade rotational speed is relatively low near the root, the resulting inflow velocity induces local flow separation on the leeward side of the blade, leading to partial pressure recovery in this region. This effect partly reduces the pressure drag behind, and around the propeller hub and thereby mitigates thrust depreciation.

To expose rotor-wing interference mechanisms that are muted at a low AoA, we examine a higher AoA where adverse pressure gradients promote separation and the rotor-induced vortex more clearly delays stall while altering longitudinal stability. Fig. 14 presents the velocity contours on longitudinal sections at $y^* = 0.5$ (through the lift rotors with support structures and fixed-wing) and $y^* = 0.625$ (only going through the fixed-wing) at $\alpha = 9^\circ$ and $\beta = 0^\circ$. By comparing the velocity distribution near the upper wing surface, it is evident that the vortex shed from the upper front lift rotor convects close to the upper wing surface, which delays separation on the upper surface at high AoA while simultaneously generating a stable vortex-induced lift there. Although this vortex-induced lift can postpone wing stall to some extent, it also shifts the wing's centre of pressure forward, which may adversely affect the aircraft's longitudinal stability.

With a further increase in angle of sideslip, Fig. 15 illustrates the development of rotor-tip vortices from the upper-front lift rotors at $\alpha = 3^\circ$ and $\beta = 6^\circ$, where notable flow structures emerge. Two vortical tubes form near the windward blade tip of the upper-front rotors, representing a variant

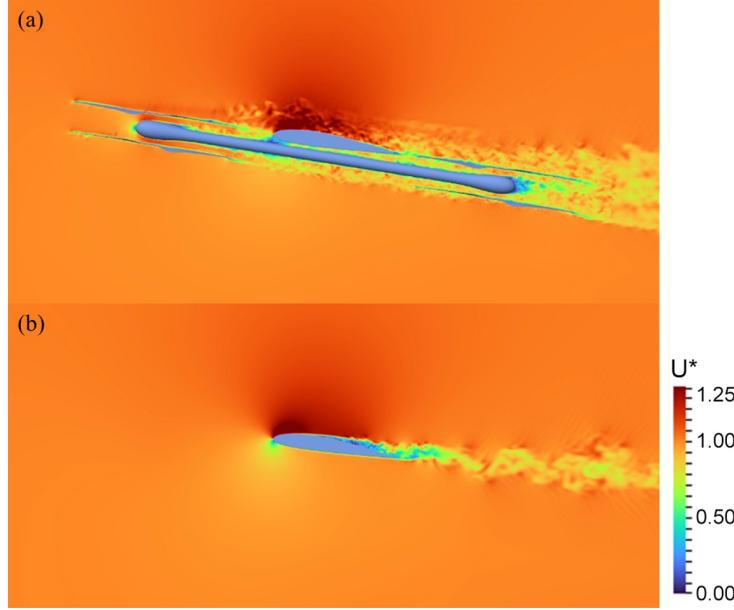


FIG. 14. Velocity contours on longitudinal sections of eVTOL under $\alpha = 9^\circ$ and $\beta = 0^\circ$. (a) $y^* = 0.5$ and (b) $y^* = 0.625$.

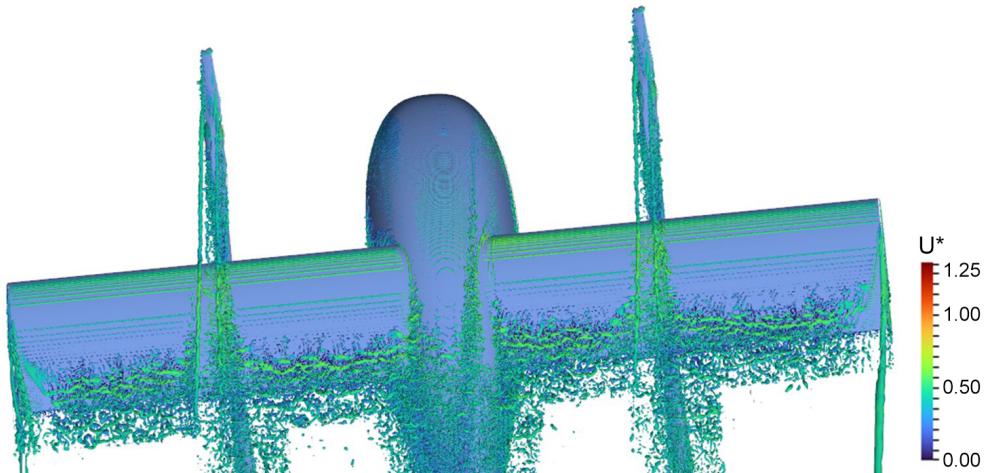


FIG. 15. Q-criterion isosurface ($Q^* = 10^4$ and $Q^* = 10^5$) from top view of eVTOL under $\alpha = 3^\circ$ and $\beta = 6^\circ$.

of the tip-vortex pair discussed above. One tube is the conventional tip vortex shed where bound circulation terminates at the blade tip and, once detached, convects with the free stream. The second tube originates on the windward edge near the tip but remains semi-attached to the rotor. Local acceleration around the windward tip and the curvature of the separating shear layer supply axial core momentum that delays complete roll-up and detachment, yielding an orientation closer to the heading direction. As both tubes convect into the fixed-wing influence region, the spanwise pressure gradient on the upper surface and the pre-existing downwash impose an outward deflection. The resulting strain aligns and thins the vortices, after which they merge with the wingtip and trailing-edge vortex system and undergo rapid breakdown through Kelvin–Helmholtz instability and viscous diffusion.

454 **B. Static stability**

455 **1. Longitudinal stability**

456 Longitudinal stability refers to the ability of an aircraft to return to level flight state within the
 457 symmetric plane⁴⁹. For a longitudinally stable aircraft, an increase in the AoA induces an increase in
 458 the negative pitching moment (nose-down tendency), which will reduce the AoA in turn, expressed
 459 in Eq. 17:

460
$$\frac{dC_m}{d\alpha} < 0, \quad (17)$$

461 where C_m is pitching moment coefficient. The pitching moment coefficient is defined as

462
$$C_m = \frac{M}{\frac{1}{2}\rho v^2 S_{Wc_A}}, \quad (18)$$

463 where M is the pitching moment, ρ is the air density, v is the incident flow velocity, S_W is the wing
 464 reference area which is the product of the span and chord length for a rectangular wing, and c_A is the
 465 mean geometric chord of the wing.

466 The variation of the pitching moment coefficient with AoA for this eVTOL aircraft is shown
 467 in Fig. 16. For the overall aircraft, as the AoA increases, the pitching moment coefficient also
 468 increases, resulting in a positive $C_{m\alpha} = \partial C_m / \partial \alpha$, which is the key criterion for instability determi-
 469 nation. At negative AoA, the curve of the overall aircraft remains below zero, which means that
 470 the aircraft generates a nose down pitching moment that has to be balanced by the flight control
 471 system or by suitable trim settings. As the AoA approaches 0° , the pitching moment coefficient of
 472 the complete configuration tends to zero, which confirms that the calculated condition corresponds
 473 to a trimmed state close to level flight. In the range from $\alpha = 0^\circ$ to about $\alpha = 6^\circ$, the increase
 474 of C_m with α is nearly linear, therefore this interval governs the static longitudinal behaviour in
 475 typical low speed climb and conversion flight. The curve corresponding to the fuselage and wing
 476 is very close to the curve of the overall aircraft over the entire AoA range. This confirms that the
 477 aerodynamics of these components is responsible for almost all of the destabilizing gradient. The
 478 curve associated with the propellers stays nearly horizontal and slightly above zero, which indicates
 479 that the propulsive system contributes a small nose up moment but does not vary with AoA in a
 480 significant way. This is because the thrust line is located near the CoG and the inflow variation with
 481 AoA is limited, therefore, the propellers do not provide an AoA dependent stabilizing contribution.
 482 For $\alpha > 6^\circ$, the slope of the overall curve decreases. This behaviour can be related to the onset
 483 of local flow separation or to changes in the effective interference between lifting surfaces, which

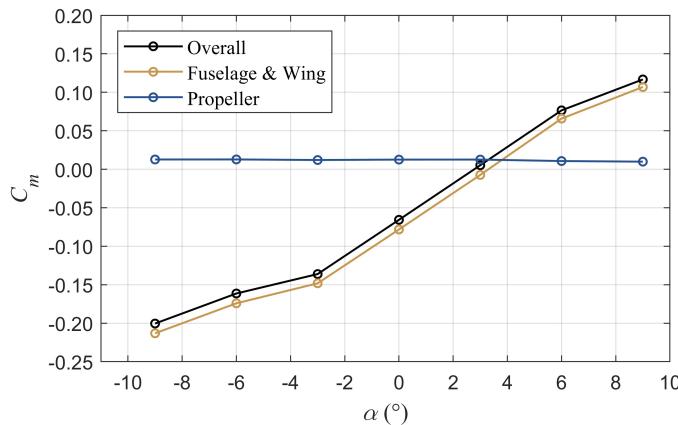


FIG. 16. Variation of pitching moment coefficient with AoA.

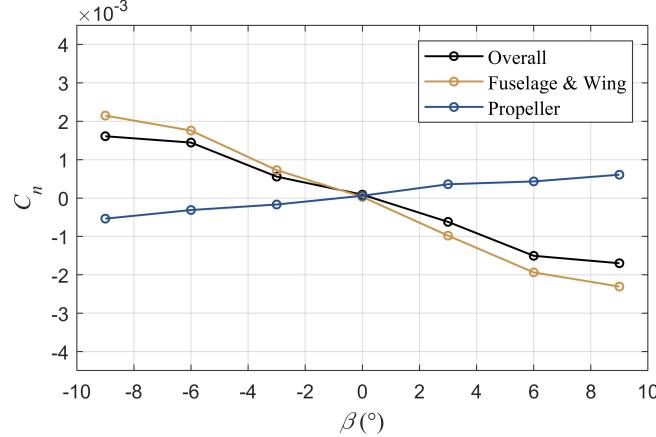


FIG. 17. Variation of yawing moment coefficient with angle of sideslip.

reduce the rate at which the nose up moment grows. The aircraft therefore remains longitudinally unstable, although the instability is moderated at higher AoA. This characteristic is favourable for operation near the maximum lift condition because it prevents an excessive nose up tendency that would require large control surface deflections or very aggressive automatic stabilization.

To enhance the longitudinal stability of the eVTOL configuration, several approaches can be adopted, such as adjusting the mass distribution of the fuselage, relocating the fixed-wing rearwards, and increasing the horizontal tail area, so as to position the CoG in front of the aerodynamic centre. Within a certain range of AoA, lift increases with AoA. This increased lift generates a nose-down moment, thereby providing the aircraft with longitudinal restoring characteristics. In addition, lowering the installation position of the tail propellers can align their thrust line with the aircraft CoG, eliminating the influence of the longitudinal force exerted on propellers on the aircraft's overall longitudinal stability. While there are several potential improvements regarding longitudinal stability worth investigating, a detailed quantitative study is not present in this study, since our focus remains on the advantages of LBM as a numerical method for eVTOL simulations rather than a specific aircraft design.

2. Directional stability

Directional stability refers to the tendency of an aircraft to return to its equilibrium in yaw⁴⁹. For an aircraft that possesses directional stability, a positive increase in angle of sideslip, which means the aircraft is slipping to the right, generates a positive yawing moment that turns the nose to the right. This yawing moment acts to reduce the angle of sideslip, as expressed in Eq. 19:

$$C_{n\beta} = \frac{\partial C_n}{\partial \beta} > 0 \quad (19)$$

where C_n is yawing moment coefficient. The yawing moment coefficient is defined as:

$$C_n = \frac{N}{\frac{1}{2}\rho v^2 S_w b} \quad (20)$$

where N is yawing moment, and b is the wing span of the eVTOL aircraft.

The variation of the yawing moment coefficient with angle of sideslip for this eVTOL aircraft is shown in Fig. 17. For the overall aircraft, as the angle of sideslip increases, the yawing moment coefficient decreases, leading to negative $C_{n\beta}$ which indicates an unstable state in directional direction. Similar to C_m , the fuselage and wing are the primary sources of the overall directional instability among all the components, while the propellers provide a slight positive contribution to directional

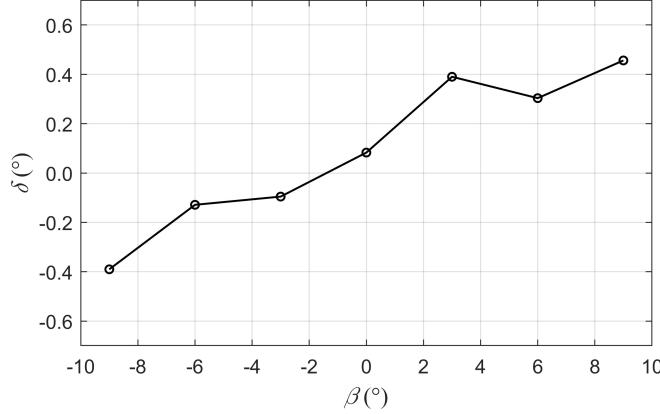


FIG. 18. Variation of the direction of the horizontal component of the tail propeller force and the aircraft angle of sideslip.

514 stability. However, the overall yawing moment coefficients remain relatively small by comparison
 515 with the study of Kim⁸ on distributed-propulsion aircraft, thereby the eVTOL aircraft in this paper
 516 exhibits a mild degree of directional instability.

517 Furthermore, as shown in Fig. 18, when the angle of sideslip increases, the angle between the
 518 horizontal component of the tail propeller force and the aircraft longitudinal axis also increases,
 519 indicating that the aerodynamic force acting on the tail rotor deflects in response to the incident
 520 flow direction. Since the tail propellers are located relatively far aft of the aircraft's CoG, when
 521 the aircraft is facing lateral incident flow, the aerodynamic force on the tail propellers produces a
 522 yawing moment about the centre of gravity that turns the aircraft toward the flow, thus reducing the
 523 angle of sideslip. Therefore, the tail propellers contribute to the directional stability of the aircraft
 524 during the flight. However, the directional stability provided by the tail propellers is obviously
 525 insufficient to counteract the directional instability induced by the fuselage. Moreover, when the
 526 propellers produce sufficient thrust, they may even exhibit a directionally unstable characteristic.

527 Generally, the directional stability of fixed-wing aircraft is guaranteed by the restoring moment
 528 provided by the vertical tail. In this case, Fig. 9 shows that the vertical tail is enveloped by the
 529 burst shed vortices from the fixed wing and the tip vortices from the tail propeller. Consequently,
 530 the airflow in the vicinity of the vertical tail is characterised by low velocity and high turbulence,
 531 leading to a significant loss in total pressure. When the vertical tail operates within this energy-
 532 deficient flow, the lateral force generated on its surface is drastically reduced. As a result, the
 533 restoring moment of the aircraft under sideslip conditions decreases substantially, which is incapable
 534 of providing sufficient directional stability for the eVTOL aircraft.

535 Therefore, to enhance the directional stability of this eVTOL configuration, the vertical tail area
 536 should be increased to strengthen the yawing moment generated by the vertical tail under oblique
 537 free-stream conditions, thereby enabling the aircraft to yaw toward the incoming flow. In-depth
 538 quantitative analysis of the optimisation for directional stability of eVTOL aircraft remains to be
 539 focused in our future study.

540 3. Lateral stability

541 Lateral stability refers to the resistance to instability of an aircraft in the roll direction⁴⁹. For an
 542 aircraft possessing lateral stability, when the angle of sideslip increases positively, a negative rolling
 543 moment is generated, which will reduce the angle of sideslip:

544

$$C_{l\beta} = \frac{\partial C_l}{\partial \beta} < 0, \quad (21)$$

545 where C_l is rolling moment coefficient:

$$546 \quad C_l = \frac{L}{\frac{1}{2}\rho v^2 S_{wb}}, \quad (22)$$

547 where L is rolling moment. The variation of the rolling moment coefficient with angle of sideslip for
 548 the eVTOL aircraft is shown in Fig. 19. For the aircraft as a whole, the rolling moment coefficient
 549 decreases as the angle of sideslip increases, indicating that the aircraft tends to roll about its CoG
 550 in a direction that reduces the angle of sideslip, thereby exhibiting lateral stability. The fuselage
 551 and wing structures constitute the primary sources of this overall lateral stability, whereas the tail
 552 propeller exhibits a slight and secondary tendency toward lateral instability.

553 From the perspective of the surface pressure as shown in Fig. 20, when the eVTOL aircraft
 554 operates at a non-zero angle of sideslip, the upwind (right, in this case) wing exhibits a lower
 555 surface pressure and a larger low-pressure region on its upper surface compared with the opposite
 556 wing, while the pressure difference on the lower surface is relatively small. Consequently, the
 557 pressure difference between the upper and lower surfaces of the right wing is greater than that of
 558 the left wing, generating a rolling moment about the aircraft's longitudinal axis. When the aircraft
 559 begins to roll to the right from level flight, the lift vector tilts to the right, causing the aircraft to
 560 yaw to the right and produce a positive angle of sideslip. The increased lift on the right wing then
 561 produces a negative rolling moment that induces leftward roll, thereby creating a tendency to return

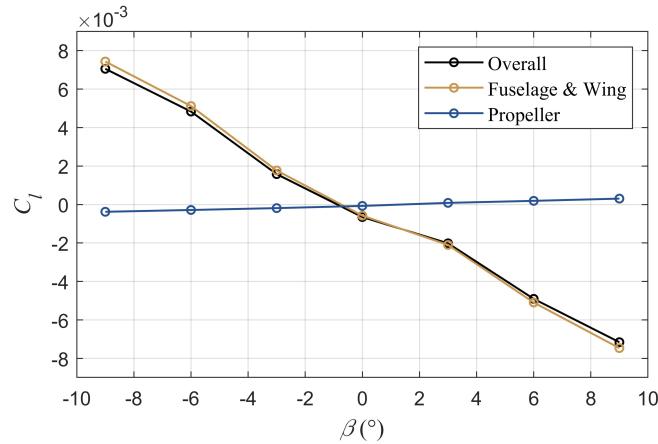


FIG. 19. Variation of rolling moment coefficient with angle of sideslip.

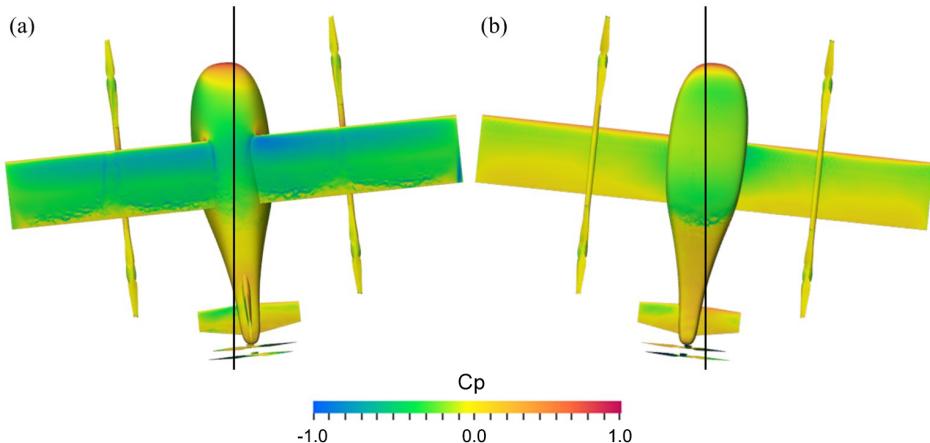


FIG. 20. Surface pressure contour of eVTOL aircraft ($\alpha = 3^\circ$, $\beta = 6^\circ$). (a) Top view, (b) bottom view.

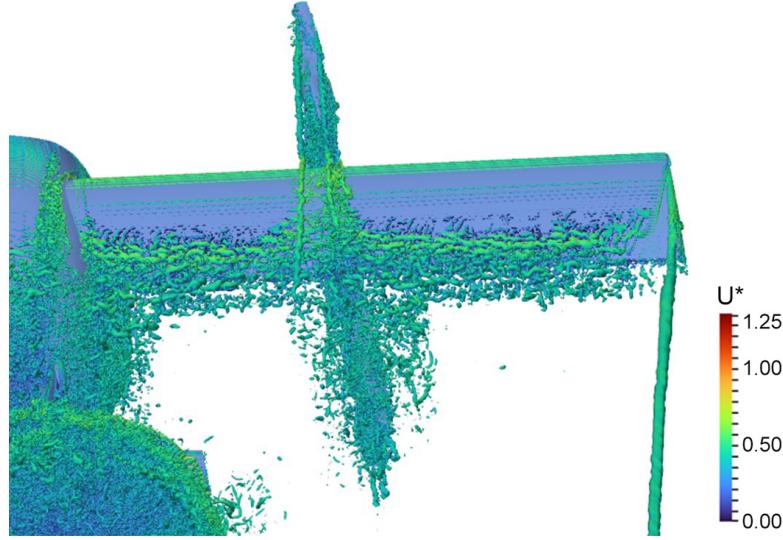


FIG. 21. Q-criterion isosurface ($Q^* = 10^4$ and $Q^* = 10^5$) above the right wing under $\alpha = 3^\circ$, $\beta = 6^\circ$.

562 to the level state.

563 Additionally, Fig. 21 shows that the wingtip vortex of the upwind wing rolls upward and moves
 564 toward the upper surface behind the wingtip. The low-pressure vortex core remains attached to
 565 the upper surface of the wing and generates vortex-induced lift, thereby contributing to the lateral
 566 stability of the aircraft to some extent. However, the vortex shed from the upper front lift rotor
 567 deflects laterally along the incident flow direction. The vortex is attached to the upper surface of
 568 the fixed-wing again, and the position of the low-pressure region induced by this vortex structure
 569 shifts consequently (Fig. 20a), leading to a change in the distribution of vortex-induced lift. This
 570 variation reduces the magnitude of the negative rolling moment at positive angles of sideslip, thereby
 571 exhibiting a slightly adverse influence on the lateral stability of the aircraft, although the effect is
 572 not pronounced and the global lateral stability still maintained.

573 Notably, while the eVTOL aircraft lacks inherent longitudinal and directional stability, such static
 574 instability is acceptable in modern aircraft design, given that control can be maintained via closed-
 575 loop feedback mechanisms, including active control surfaces, thrust vectoring and AI-driven flight
 576 control laws.

577 IV. CONCLUSION

578 While previous studies primarily focused on flight stability analysis of fixed-wing aircraft and
 579 rotocraft based on FVM, few studies employed LBM method as a high-fidelity numerical method
 580 to analyse the flight stability of eVTOL aircraft, which have novel configurations, or the wake
 581 interactions that dominate the phenomenon. Based on LBM numerical method, this study reveals
 582 the typical vortical structures of an eVTOL aircraft, investigates the static stability, and analyses the
 583 dictating flow mechanisms, including the flow characteristics surrounding the tail propellers.

584 In this study, the numerical performance of FVM-LES and LBM-LES is first validated and com-
 585 pared by simulating an eVTOL lift rotor and comparing with test-stand experimental results. Based
 586 on the LBM-LES, further numerical simulations are conducted for a specific eVTOL configuration
 587 to analyse its flow-field structures and static stability. The main conclusions are summarised below:

- 588 (1) For weakly compressible flows surrounding an eVTOL aircraft, LBM-LES is capable of ac-
 589 curately capturing the influence of compressibility on aerodynamic forces with an numerical
 590 error below 11% for thrust and below 7% for torque regarding rotor simulations. The sim-

591 ulations based on LBM-LES are 8~9 times faster than those based on FVM-LES for the
 592 same physical time, which exhibits significant advantages in computational efficiency and
 593 cost compared with FVM-LES.

- 594 (2) Four main categories of vortex structures dominate the flow field of eVTOL aircraft, includ-
 595 ing wingtip vortices, wing root vortices, tip vortices from lift rotors, and tail propeller tip
 596 vortices. The wingtip vortices form through convergence of three flow components at the
 597 trailing edge and positively influence lateral stability. The wing root vortices gradually merge
 598 with vortices from the rear fuselage. The tip vortices from the upper front lift rotors adhere
 599 to the upper wing surface, delaying flow separation and wing stall, yet adversely affecting
 600 both longitudinal and lateral stability. The tail propeller tip vortices form a pair of typical
 601 intersecting double-helical structures.
- 602 (3) When the tail-propeller rotational speed is insufficient, the propellers produce significantly
 603 reduced thrust, indicating that the compound-wing configuration eVTOL with tail-mounted
 604 propulsion imposes stringent performance requirements on the thrust power system.
- 605 (4) The eVTOL demonstrates lateral stability. This is because the wing encountering the incom-
 606 ing flow earlier has a lower surface pressure and a larger low-pressure region on its upper
 607 surface compared with the opposite wing. Furthermore, the tip vortex on this side rolls up-
 608 ward toward the upper surface, generating additional vortex-induced lift. Consequently, the
 609 lift on the earlier flow-encountering wing becomes greater, inducing a restoring rolling mo-
 610 ment that promotes a tendency to reduce sideslip and roll.
- 611 (5) The eVTOL aircraft examined in this study exhibits longitudinal instability during cruise. In
 612 directional, the aircraft is mildly unstable. That is mainly because the vertical tail, enveloped
 613 by low-energy, highly-turbulent flow induced by the fixed-wing and tail-propeller vortices,
 614 produces much lower lateral force and restoring moment under sideslip. Nevertheless, the
 615 drag acting on the propellers tends to align them with the oncoming flow, imparting a weath-
 616 ervane effect that partially augments directional stability. This indicates that compared with
 617 conventional low-speed aircraft, the typical aerodynamic configurations of eVTOL aircraft
 618 pose greater challenges to the control system, which must be compensated through appropri-
 619 ate control law design with advanced fly-by-wire systems. In addition, since static stability
 620 is closely related to the safety margin of the eVTOL aircraft, we encourage relevant industry
 621 personnel to refine the standards before full commercialisation of eVTOL aircraft so as to
 622 take this factor into account.
- 623 (6) For eVTOL aircraft development, LBM-LES is highly recommended for high-fidelity un-
 624 steady simulations where complex moving boundaries, such as rotors, and rapid turnaround
 625 time are prioritised. Nevertheless, it should be noted that LBM-LES encounters inherent lim-
 626 itations when simulating supersonic flow regimes, where FVM-LES may still offer superior
 627 robustness and advantages.
- 628 (7) In light of the identified longitudinal and directional static instabilities, we recommend incor-
 629 porating advanced strategies such as active control, thrust vectoring, and AI-driven control
 630 laws into the eVTOL design. Enhancing controllability in this manner is crucial for eVTOL
 631 aircraft, given their role as small-scale civil aircraft operating in low-altitude airspace.

632 Based on our existing findings, our subsequent research will further focus on the scaled wind tun-
 633 nel testing of the eVTOL aircraft to validate the simulation results further, as well as on the dynamic
 634 stability derivatives calculated via simulations of oscillatory motions such as phugoid and plunging
 635 modes. Meanwhile, we are aim at developing a workflow for the rapid iterative development of
 636 eVTOL aircraft using LBM-based CFD simulations.

637 DISCLOSURE STATEMENT

638 No potential conflict of interest was reported by the authors.

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646 **AUTHORSHIP CONTRIBUTION STATEMENT**

647 R.Mo: Formal analysis, Investigation, Methodology, Software, Validation, Writing - original
 648 draft, Data curation, Writing - review & editing, Visualization. Q.Zhou: Software, Data curation,
 649 Visualization. Q.Jia: Conceptualization, Methodology, Supervision, Funding acquisition, Project
 650 administration. C.Xia: Supervision, Writing - review. H.Wei: Conceptualization, Supervision,
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 652 and approved the final version of the manuscript to be published and agree to be accountable for all
 653 aspects of the work.

654 **DATA AVAILABILITY STATEMENT**

655 Data supporting the findings of this study are available from the corresponding author upon rea-
 656 sonable request.

657 **REFERENCES**

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