
1 NMR Shielding

Shielding Tensor:

$$\sigma_{\beta\alpha}^K = \frac{d^2 E}{dB_\alpha dm_{K_\beta}} \Big|_{\mathbf{B}, \mathbf{m}_K=0} \quad (1)$$

How do I parameterize energy E with \mathbf{B} and \mathbf{m}_K ?

The one-electronic Hamiltonian in magnetic field:

$$h(\mathbf{r}, \mathbf{B}, \mathbf{m}) = \frac{1}{2}\boldsymbol{\pi}^2 - \phi(\mathbf{r}) \quad (2)$$

in which:

$$\boldsymbol{\pi} = -i\nabla + \mathbf{A} \quad (3)$$

is the kinetic momentum operator.

Vector potential:

$$\mathbf{A}_i = \mathbf{A}_0(\mathbf{r}_i) + \sum_K \mathbf{A}_K(\mathbf{r}_i) \quad (4)$$

with:

$$\mathbf{A}_0(\mathbf{r}_i) = \frac{1}{2}\mathbf{B} \times \mathbf{r}_0 \quad \mathbf{B} = \nabla \times \mathbf{A}(\mathbf{r}) \quad (5)$$

$$\mathbf{A}_K(\mathbf{r}_i) = \alpha^2 \frac{\mathbf{M}_K \times \mathbf{r}_K}{r_K^3} \quad \mathbf{B}_K(\mathbf{r}) = \nabla \times \mathbf{A}_K(\mathbf{r}) \quad (6)$$

The first part is contribution from the external magnetic field, the second part from the nuclear magnetic moments.

Now parameterize with MO coefficients / densities?