Homework 11

The primary purpose of this assignment is to explore objects in object-oriented languages. Concretely, we will extend Jakarascript with object literals, field dereference expressions, and field assignments. We extend our type checker to support the new features, but we do not yet add support for subtyping. At this point, we have many of the key features of Javascript/TypeScript.

Problem 1 Objects and Subtyping (16 Points)

This is a warm-up exercise to get yourself familiar with objects (which you will implement in the second part of this homework) and subtyping (which you will implement in the upcoming final homework assignment).

(a) Indicate whether the following JAKARTASCRIPT subtype relationships are true or false.

```
(i) Num <: Num
(ii) Bool <: Num
(iii) {let f: Num} <: {let f: Any}
(iv) {let f: Num} <: {const f: Any}
(v) {const f: Num} <: {let f: Num}
(vi) {let f: Num} <: {let g: Num}
(vii) {const f: {}} <: {const f: Any, let g: Bool}
(viii) Any => Bool <: Bool => Any
(ix) Bool => Bool <: Any => Any
```

(b) For each of the following programs: (1) say whether the program can be safely evaluated or not, i.e., whether the evaluation will get stuck or produce a value. If it can be safely evaluated, provide the computed value; (2) determine whether the program is well-typed with subtyping (i.e., with the rule TypeSub). If it is not, provide a brief explanation.

```
(i)
1    const x = {let f: 3};
2    const fun = function(y: {let f: Num, const g: Bool}) {
3         y.f = 4; return y;
4     };
5    fun(x).f

(ii)
1    const x = {let f: 3, const g: true};
2    const fun = function(y: {let f: Num}) {
3         return y;
4     };
5    fun(x).f
```

```
(iii)
    const x = {let f: 3, const g: true};
    const fun = function(y: {let f: Num}) {
        return y;
        };
        fun(x).g

(iv)
        const x = {let f: 1, const g: true};
        const y = {const f: false, let g: 2};
        const z = true ? x : y;
        z.f
```

Problem 2 JAKARTASCRIPT Interpreter with Objects (24 Points)

We start from our language in Homework 10 and extend it with object literals and field dereference operations. The syntax of the new language is shown in Figure 1.

An object literal $\{\overline{mut\ f}:e\}$ is a sequence of field names associated with initialization expressions and mutabilites. The mutability of a field indicates whether the field can be reassigned a new value after the object literal has been evaluated. When an object literal is evaluated, we first evaluate the initialization expressions of the fields to obtain an object value $\{\overline{f}:v\}$. Note that object values are not actually values. In JavaScript, objects are dynamically allocated on the heap and then referenced with an extra level of indirection through a heap address. To model object allocation, object literals in JAKARTASCRIPT evaluate to an address a, which is a value that references a memory location. This memory location that stores the object value obtained from the object literal.

Aliasing. The indirection introduced by dynamic allocation of objects means two program variables can reference the same object, which is called aliasing. With mutation, aliasing is now observable as demonstrated by the following example:

```
const x = { f : 1 };
const y = x;
x.f = 2;
console.log(y.f)
```

The code above should print 2 because x and y are aliases (i.e., reference to the same object). Aliasing makes programs more difficult to reason about and is often the source of subtle bugs.

In Figure 2, we show the updated and new AST nodes. Note that in our Scala representation of ASTs, we treat field dereference as a unary operator FldDeref that is parameterized by the dereferenced field name. That is, a field dereference expression e.f in JakartaScript is represented in Scala by the expression UnOp(FldDeref(f), e). This design choice simplifies some aspects of our implementation. In particular, we will not have to extend the substitution function subst of our interpreter with an extra case for field dereference expressions.

```
n \in Num
                                                                                                        numbers (double)
                 s \in Str
                                                                                                                         strings
                 a \in Addr
                                                                                                                     addresses
   b \in Bool ::= true \mid false
                                                                                                                      Booleans
                 x \in Var
                                                                                                                      variables
                f \in Fld
                                                                                                                  field names
    	au \in \mathit{Typ} ::= \mathsf{Bool} \mid \mathsf{Num} \mid \mathsf{String} \mid \mathsf{Undefined} \mid
                                                                                                                           types
                       (\overline{\tau}) \Rightarrow \tau_0 \mid \{\overline{mutf}: \underline{\tau}\}
     v \in Val ::= undefined | n | b | s | a | function p(\overline{x : \tau}) t e
                                                                                                                          values
   e \in Expr ::= x \mid v \mid uop \mid e \mid e_1 \mid bop \mid e_2 \mid e_1 \mid e_2 \mid e_3 \mid e \mid f \mid \{\overline{mutf : e}\}\}
                                                                                                                  expressions
                       console.log(e) \mid e_1(\overline{e}) \mid mut \ x = e_1; e_2
uop \in Uop ::= - \mid ! \mid *
                                                                                                           unary operators
 bop \in Bop ::= + | - | * | / | === | !== | < | > |
                                                                                                          binary operators
                      <= | >= | && | | | | , |=
              p ::= x \mid \epsilon
                                                                                                            function names
               t ::= :\tau \mid \epsilon
                                                                                                                 return types
mut \in Mut ::= \mathbf{const} \mid \mathbf{let}
                                                                                                                   mutability
       o \in Obj = Fld \rightharpoonup Val
                                                                                                                        objects
    k \in Con ::= v \mid o
                                                                                                         memory contents
   M \in Mem = Addr \rightharpoonup Con
                                                                                                                     memories
```

Figure 1: Abstract syntax of JakartaScript

Type Checking. The inference rules defining the typing relation are given in figures 3 and 4. The only change compared to Homework 10 are the new rules for typing objects, which are summarized in Figure 4. A template for the new type inference function

```
def typeInfer(env: Map[String,(Mut,Typ)], e: Expr): Typ
```

has been provided for you. The only missing cases are for the new rules in Figure 4. Your first task is to implement those missing cases.

Evaluation. The new big-step operational semantics is given in figures 5, 6, and 7. The rules are identical to those given in Homework 10, except that we add new rules for evaluating object literals, field dereference operations, and field assignments. These new rules are summarized in Figure 7.

Your second task is to update the subst and eval functions of the interpreter to account for the new language primitives.

• The subst function has the same signature as last time

```
sealed abstract class Expr extends Positional
/** Memory contents */
sealed trait Con
/** Values */
sealed abstract class Val extends Expr with Con
/** Object literals */
type Fld = String
case class ObjLit(fes: Map[Fld, (Mut, Expr)]) extends Expr
\mathsf{ObjLit}(\mathsf{Map}(\overline{(f,(mut,e))})) \ \{\overline{mut\ f\!:\!e}\}
case class FldDeref(f: String) extends Uop
{\sf UnOp}({\sf FldDeref}(f),\ e)\ e.f
/** Objects (to be stored in memory) */
case class Obj(fvs: Map[Fld, Val]) extends Con
\operatorname{Obj}(\operatorname{Map}(\overline{f,v})) \ \{\overline{f\!:\!v}\}
/** Types */
sealed abstract class Typ
/** Object types */
case class TObj(fts: Map[Fld, (Mut, Typ)]) extends Typ
TObj(Map(\overline{(f,(mut,\tau))})) \{\overline{mut\ f:\tau}\}
```

Figure 2: Representing in Scala the abstract syntax of JakartaScript. After each case class or case object, we show the correspondence between the representation and the concrete syntax.

Figure 3: Type checking rules for non-object primitives of JakartaScript (no changes compared to Homework 10)

$$\begin{array}{c} \Gamma \vdash e_1 : \tau_1 & \ldots & \Gamma \vdash e_n : \tau_n \\ \hline \Gamma \vdash \{ \mathit{mut}_1 \ f_1 \colon e_1, \ldots, \mathit{mut}_n \ f_n \colon e_n \} \colon \{ \mathit{mut}_1 \ f_1 \colon \tau_1, \ldots, \mathit{mut}_n \ f_n \colon \tau_n \} \\ \hline \\ \Gamma \vdash e : \{ \mathit{mut}_1 \ f_1 \colon \tau_1, \ldots, \mathit{mut}_n \ f_n \colon \tau_n \} \\ \hline \\ \frac{f = f_i \quad \tau = \tau_i \quad i \in [1, n]}{\Gamma \vdash e \cdot f \colon \tau} & \text{TypeDerefflo} \\ \hline \\ \Gamma \vdash e_1 \colon \{ \mathit{mut}_1 \ f_1 \colon \tau_1, \ldots, \mathit{mut}_n \ f_n \colon \tau_n \} \\ f = f_i \quad \tau = \tau_i \quad \mathit{mut}_i = \mathbf{let} \quad i \in [1, n] \\ \hline \\ \Gamma \vdash e_2 \colon \tau \\ \hline \\ \Gamma \vdash e_1 \colon f = e_2 \colon \tau \\ \hline \end{array} \quad \text{TypeAssignFld}$$

Figure 4: Type checking rules for objects of JakartaScript

The only missing case is the case for object literals. For object literals of the form $\{mut_1 \ f: e_1, \ldots, mut_n \ f_n: e_n\}$ the substitution function should simply recurse into the field initialization expressions. That is, we have

$$\{mut_1 \ f: e_1, \dots, mut_n \ f_n: e_n\}[e_r/x] = \{mut_1 \ f: e_1[e_r/x], \dots, mut_n \ f_n: e_n[e_r/x]\}$$

Hint: use the mapValues method of the Map data structure in the Scala standard library to implement the recursive substitution inside the field initialization expressions in fes.

• The eval function has the same signature as last time

That is, eval takes an expression and returns a state monad State[Mem, Val] that encapsulates a computation from an input memory state to an output memory state and a result value. We suggest to proceed as follows:

- (a) Copy over your solution from Homework 10 for the missing non-object cases (or see the sample solution for Homework 10 once it is released).
- (b) Then implement the new cases for the rules EVALDEREFFLD and EVALASSIGN-FLD. **Hint:** The helper functions eToAddr and read0bj will be useful here.
- (c) Finally, implement the case for the rule EVALOBJLIT. The template that has been provided for this case splits the evaluation into two parts: (1) the construction of the map o for the object to be stored in memory, (2) the actual allocation and update of the memory. Part (1) should be implemented with a foldLeft over the map fes holding the fields and associated expressions of the object literal. This foldLeft constructs a state monad sm whose result is the map o for the object. Part (2) should then be implemented with a flatMap call on the state monad returned by foldLeft. Hint: in part (1) use a for expression in the body of the function to which foldLeft is applied in order to extract the

current field/value map from the accumulated state monad sm. Then extend this map in the yield part with the current field fi and the value obtained from fi's initialization expression ei.

$$\frac{\langle M, e \rangle \Downarrow \langle M', v \rangle}{\langle M, e \rangle \Downarrow \langle M', e \rangle} \text{ EVALUMINUS } \frac{\langle M, e \rangle \Downarrow \langle M', b \rangle}{\langle M, e \rangle \Downarrow \langle M', e \rangle} \text{ EVALNOT}$$

$$\frac{\langle M, e_1 \rangle \Downarrow \langle M', \text{true} \rangle \qquad \langle M', e_2 \rangle \Downarrow \langle M'', v_2 \rangle}{\langle M, e_1 \rangle \Downarrow \langle M', e_2 \rangle \Downarrow \langle M'', v_2 \rangle} \text{ EVALANDTRUE}$$

$$\frac{\langle M, e_1 \rangle \Downarrow \langle M', \text{false} \rangle \qquad \langle M', e_2 \rangle \Downarrow \langle M'', v_2 \rangle}{\langle M, e_1 \rangle \Downarrow \langle M', e_2 \rangle} \text{ EVALORFALSE}$$

$$\frac{\langle M, e_1 \rangle \Downarrow \langle M', \text{false} \rangle}{\langle M, e_1 \rangle \Downarrow \langle M', \text{false} \rangle} \text{ EVALANDFALSE} \qquad \frac{\langle M, e_1 \rangle \Downarrow \langle M', \text{true} \rangle}{\langle M, e_1 \rangle \Downarrow \langle M', e_2 \rangle} \text{ EVALORTRUE}$$

$$\frac{\langle M, e_1 \rangle \Downarrow \langle M', e_1 \rangle}{\langle M, e_1 \rangle \Downarrow \langle M', e_2 \rangle} \text{ EVALORTRUE} \qquad \frac{\langle M, e_1 \rangle \Downarrow \langle M', e_1 \rangle}{\langle M, e_1 \rangle \Downarrow \langle M', e_2 \rangle} \text{ EVALORTRUE}$$

$$\frac{\langle M, e_1 \rangle \Downarrow \langle M', e_1 \rangle}{\langle M, e_1 \rangle \Downarrow \langle M', e_2 \rangle} \text{ EVALORTRUE} \qquad \frac{\langle M, e_1 \rangle \Downarrow \langle M', e_1 \rangle}{\langle M, e_1 \rangle \Downarrow \langle M', e_2 \rangle} \text{ EVALPRINT}$$

$$\frac{\langle M, e_1 \rangle \Downarrow \langle M', e_1 \rangle}{\langle M, e_1 \rangle \Downarrow \langle M', e_2 \rangle} \text{ EVALPRINT} \qquad \text{EVALPLUSNUM}$$

$$\frac{\langle M, e_1 \rangle \Downarrow \langle M', e_1 \rangle}{\langle M, e_1 \rangle \Downarrow \langle M'', e_2 \rangle} \text{ EVALPLUSSTR} \qquad \frac{\langle M, e_1 \rangle \Downarrow \langle M', e_1 \rangle}{\langle M, e_1 \rangle \Downarrow \langle M'', e_2 \rangle} \text{ EVALPLUSSTR}$$

$$\frac{\langle M, e_1 \rangle \Downarrow \langle M', e_1 \rangle}{\langle M, e_1 \rangle \Downarrow \langle M'', e_2 \rangle} \text{ EVALCONSTDECL} \qquad \frac{\langle M, e_1 \rangle \Downarrow \langle M', e_2 \rangle}{\langle M, e_1 \rangle \Downarrow \langle M'', e_2 \rangle} \text{ EVALCONSTDECL}$$

$$\frac{\langle M, e_1 \rangle \Downarrow \langle M', e_1 \rangle}{\langle M, e_1 \rangle \bowtie \langle M'', e_2 \rangle} \text{ EVALCONSTDECL} \qquad \frac{\langle M, e_1 \rangle \Downarrow \langle M'', e_2 \rangle}{\langle M, e_1 \rangle \bowtie \langle M'', e_2 \rangle} \text{ EVALINEQUALNUM}$$

$$\frac{\langle M, e_1 \rangle \Downarrow \langle M', e_1 \rangle}{\langle M, e_1 \rangle \bowtie \langle M'', e_2 \rangle} \text{ EVALINEQUALNUM}$$

$$\frac{\langle M, e_1 \rangle \Downarrow \langle M', e_1 \rangle}{\langle M, e_1 \rangle \bowtie \langle M'', e_2 \rangle} \text{ EVALINEQUALSTR}$$

$$\frac{\langle M, e_1 \rangle \Downarrow \langle M', e_1 \rangle}{\langle M, e_1 \rangle \bowtie \langle M'', e_2 \rangle} \text{ EVALIFTHEN}$$

$$\frac{\langle M, e_1 \rangle \Downarrow \langle M', e_1 \rangle}{\langle M, e_1 \rangle \Downarrow \langle M'', e_2 \rangle} \text{ EVALIFTHEN}$$

$$\frac{\langle M, e_1 \rangle \Downarrow \langle M', false \rangle}{\langle M, e_1 \rangle \Downarrow \langle M'', e_2 \rangle} \text{ EVALIFELSE}$$

$$\frac{\langle M, e_1 \rangle \Downarrow \langle M', false \rangle}{\langle M, e_1 \rangle \Downarrow \langle M'', e_2 \rangle} \text{ EVALIFELSE}$$

Figure 5: Big-step operational semantics of non-imperative non-object primitives of JAKAR-TASCRIPT (no changes compared to Homework 10).

$$\frac{\langle M,e\rangle \Downarrow \langle M',v\rangle \quad a \in \operatorname{dom}(M')}{\langle M,*a=e\rangle \Downarrow \langle M'[a\mapsto v],v\rangle} \text{ EVALASSIGNVAR}$$

$$\frac{a\in \operatorname{dom}(M)}{\langle M,*a\rangle \Downarrow \langle M,M(a)\rangle} \text{ EVALDEREFVAR}$$

$$\langle M,e_d\rangle \Downarrow \langle M_d,v_d\rangle \quad a \notin \operatorname{dom}(M_d)$$

$$\frac{M'=M_d[a\mapsto v_d] \quad \langle M',e_b[*a/x]\rangle \Downarrow \langle M'',v_b\rangle}{\langle M,\operatorname{let} x=v_d;e_b\rangle \Downarrow \langle M'',v_b\rangle} \text{ EVALLETDECL}$$

$$\langle M,e_0\rangle \Downarrow \langle M_0,v_0\rangle \quad v_0 = \operatorname{function} x_0(\overline{x_i}:\overline{\tau_i}):\tau \ e$$

$$v_0'=(\operatorname{function}(\overline{x_i}:\overline{\tau_i}):\tau \ (e[v_0/x_0])) \quad \langle M_0,v_0'(\overline{e_i})\rangle \Downarrow \langle M',v\rangle} \text{ EVALCALLREC}$$

$$\langle M,e_0\rangle \Downarrow \langle M_0,v_0\rangle \quad v_0 = \operatorname{function}(x_1:\tau_1,\overline{x_i}:\overline{\tau_i}):\tau \ e$$

$$\langle M,e_0\rangle \Downarrow \langle M_0,v_0\rangle \quad v_0 = \operatorname{function}(x_1:\tau_1,\overline{x_i}:\overline{\tau_i}):\tau \ e$$

$$\langle M,e_0\rangle \Downarrow \langle M_1,v_1\rangle \quad v_0' = (\operatorname{function}(\overline{x_i}:\overline{\tau_i}):\tau \ (e[v_1/x_1]))$$

$$\frac{\langle M_1,v_0'(\overline{e_i})\rangle \Downarrow \langle M',v\rangle}{\langle M,e_0(e_1,\overline{e_i})\rangle \Downarrow \langle M',v\rangle} \text{ EVALCALLCONST}$$

$$\frac{\langle M,e_0\rangle \Downarrow \langle M_0,\operatorname{function}()t\ e\rangle \quad \langle M_0,e\rangle \Downarrow \langle M',v\rangle}{\langle M,e_0()\rangle \Downarrow \langle M',v\rangle} \text{ EVALCALL}$$

Figure 6: Big-step operational semantics of imperative non-object primitives of Jakar-tascript (no changes compared to Homework 10).

$$M_{0} = M \quad \text{for all } i \in [1, n] : \langle M_{i-1}, e_{i} \rangle \Downarrow \langle M_{i}, v_{i} \rangle$$

$$a \notin \text{dom}(M_{n}) \quad o = \{f_{1} \mapsto v_{1}, \dots, f_{n} \mapsto v_{n}\} \quad M' = M_{n}[a \mapsto o]$$

$$\langle M, \{mut_{1} \ f_{1} : e_{1}, \dots, mut_{n} \ f_{n} : e_{n}\} \rangle \Downarrow \langle M', a \rangle$$

$$\frac{\langle M, e \rangle \Downarrow \langle M', a \rangle \quad M'(a) = o}{\langle M, e . f \rangle \Downarrow \langle M', o(f) \rangle} \quad \text{EVALDEREFFLD}$$

$$\langle M, e_{1} \rangle \Downarrow \langle M_{1}, a \rangle \quad \langle M_{2}, e_{2} \rangle \Downarrow \langle M_{2}, v_{2} \rangle$$

$$\frac{M_{2}(a) = o \quad M' = M_{2}[a \mapsto o[f \mapsto v_{2}]]}{\langle M, e_{1} . f = e_{2} \rangle \Downarrow \langle M', v_{2} \rangle} \quad \text{EVALASSIGNFLD}$$

Figure 7: Big-step operational semantics of objects in JakartaScript.