

Basic

36.

$$(1) \text{ 与式} = \frac{18x^2y^5z}{8x^3y^6z^3}$$

$$= \frac{9}{4xyz^2}$$

$$(2) \text{ 与式} = \frac{xy^2(x+y)}{y(x^2-y^2)}$$

$$= \frac{xy^2(x+y)}{y(x+y)(x-y)}$$

$$= \frac{xy}{x-y}$$

$$(3) \text{ 与式} = \frac{\{x+(y-1)\}\{x-(y-1)\}}{\{(x+y)+1\}\{(x+y)-1\}}$$

$$= \frac{(x+y-1)(x-y+1)}{(x+y+1)(x+y-1)}$$

$$= \frac{x-y+1}{x+y+1}$$

$$(4) \text{ 与式} = \frac{(x-2)(x-4)}{(x-2)(x^2+2x+4)}$$

$$= \frac{x-4}{x^2+2x+4}$$

37.

$$(1) \text{ 与式} = \frac{2(x+3)}{(x+2)(x+3)} + \frac{x+2}{(x+2)(x+3)}$$

$$= \frac{2x+6+x+2}{(x+2)(x+3)}$$

$$= \frac{3x+8}{(x+2)(x+3)}$$

$$(2) \text{ 与式} = \frac{x-y}{x+y} + \frac{2xy}{(x+y)(x-y)}$$

$$= \frac{(x-y)^2}{(x+y)(x-y)} + \frac{2xy}{(x+y)(x-y)}$$

$$= \frac{x^2-2xy+y^2+2xy}{(x+y)(x-y)}$$

$$= \frac{x^2+y^2}{(x+y)(x-y)}$$

$$(3) \text{ 与式} = \frac{(a+b)^2}{(a+b)(a-b)} + \frac{(a-b)^2}{(a+b)(a-b)}$$

$$= \frac{a^2+2ab+b^2-(a^2-2ab+b^2)}{(a+b)(a-b)}$$

$$= \frac{4ab}{(a+b)(a-b)}$$

$$(4) \text{ 与式} = \frac{1}{2a-1} + \frac{1}{2a+1} - \frac{2}{(2a+1)(2a-1)}$$

$$= \frac{2a+1}{(2a+1)(2a-1)} + \frac{2a-1}{(2a+1)(2a-1)}$$

$$- \frac{2}{(2a+1)(2a-1)}$$

$$= \frac{2a+1+2a-1-2}{(2a+1)(2a-1)}$$

$$= \frac{4a-2}{(2a+1)(2a-1)}$$

$$= \frac{2(2a-1)}{(2a+1)(2a-1)}$$

$$= \frac{2}{(2a+1)}$$

38.

$$(1) \text{ 与式} = \frac{-8x^3y^3 \cdot 6z^3}{9z^2 \cdot x^4y^2}$$

$$= -\frac{16yz}{3x}$$

$$(2) \text{ 与式} = \frac{(a+b)(a+3b)}{(a+2b)(a^2-2ab+4b^2)} \cdot \frac{a+2b}{a(a+b)}$$

$$= \frac{(a+b)(a+3b) \cdot (a+2b)}{(a+2b)(a^2-2ab+4b^2) \cdot a(a+b)}$$

$$= \frac{a+3b}{a(a^2-2ab+4b^2)}$$

39.

$$\begin{aligned}
 (1) \text{ 与式} &= \frac{\left(1 - \frac{1}{a}\right) \cdot a^2}{\left(a - \frac{1}{a^2}\right) \cdot a^2} \\
 &= \frac{a^2 - a}{a^3 - 1} \\
 &= \frac{a(a - 1)}{(a - 1)(a^2 + a + 1)} \\
 &= \frac{a}{a^2 + a + 1}
 \end{aligned}$$

$$\begin{aligned}
 (2) \text{ 与式} &= \frac{\left(x + 1 - \frac{4}{x + 1}\right) \cdot (x + 1)}{\left(1 - \frac{2}{x + 1}\right) \cdot (x + 1)} \\
 &= \frac{(x + 1)^2 - 4}{x + 1 - 2} \\
 &= \frac{\{(x + 1) + 2\}\{(x + 1) - 2\}}{x - 1} \\
 &= \frac{(x + 3)(x - 1)}{x - 1} \\
 &= x + 3
 \end{aligned}$$

40.

(1)

$$\begin{array}{r}
 \begin{array}{r}
 x - 1 \\
 \hline
 x - 2) \quad x^2 - 3x + 3 \\
 \hline
 x^2 - 2x \\
 \hline
 -x + 3 \\
 \hline
 -x + 2 \\
 \hline
 1
 \end{array}
 \end{array}$$

$$\text{与式} = x - 1 + \frac{1}{x - 2}$$

(2)

$$\begin{array}{r}
 \begin{array}{r}
 x + 5 \\
 \hline
 x^2 - 2x + 3) \quad x^3 + 3x^2 - 4x + 7 \\
 \hline
 x^3 - 2x^2 + 3x \\
 \hline
 5x^2 - 7x + 7 \\
 \hline
 5x^2 - 10x + 15 \\
 \hline
 3x - 8
 \end{array}
 \end{array}$$

$$\text{与式} = x + 5 + \frac{3x - 8}{x^2 - 2x + 3}$$

41.

$$\begin{aligned}
 (1) |1 - 4| + |2 - 1| &= (4 - 1) + (2 - 1) \\
 &= 4
 \end{aligned}$$

$$\begin{aligned}
 (2) |7 - 4| + |2 - 7| &= (7 - 4) + (7 - 2) \\
 &= 8
 \end{aligned}$$

$$\begin{aligned}
 (3) |\pi - 4| + |2 - \pi| &= (4 - \pi) + (\pi - 2) \\
 &= 2
 \end{aligned}$$

42.

$$\begin{aligned}
 (1) \text{ 与式} &= 2\sqrt{2} - 4\sqrt{2} + 6\sqrt{2} \\
 &= 4\sqrt{2}
 \end{aligned}$$

$$\begin{aligned}
 (2) \text{ 与式} &= 2\sqrt{2} \cdot \sqrt{2} + 2\sqrt{2} \cdot 4\sqrt{3} \\
 &\quad - \sqrt{3} \cdot \sqrt{2} - \sqrt{3} \cdot 4\sqrt{3} \\
 &= 4 + 8\sqrt{6} - \sqrt{6} - 12 \\
 &= -8 + 7\sqrt{6}
 \end{aligned}$$

$$\begin{aligned}
 (3) \text{ 与式} &= \frac{3\sqrt{3}}{12\sqrt{3}} \\
 &= \frac{1}{4}
 \end{aligned}$$

$$\begin{aligned}
 (4) \text{ 与式} &= (\sqrt{2})^2 + 2 \cdot \sqrt{2} \cdot \frac{1}{\sqrt{2}} + \left(\frac{1}{\sqrt{2}}\right)^2 \\
 &= 2 + 2 + \frac{1}{2} \\
 &= \frac{9}{2}
 \end{aligned}$$

43.

$$\begin{aligned}
 (1) \text{ 与式} &= |3 - \sqrt{3}| \\
 &= 3 - \sqrt{3}
 \end{aligned}$$

$$\begin{aligned}
 (2) \text{ 与式} &= |2 - 3\sqrt{2}| \\
 &= 3\sqrt{2} - 2
 \end{aligned}$$

44.

$$\begin{aligned}
 (1) \text{ 与式} &= \frac{4\sqrt{3} \cdot \sqrt{2}}{\sqrt{2} \cdot \sqrt{2}} \\
 &= \frac{4\sqrt{6}}{2} \\
 &= 2\sqrt{6}
 \end{aligned}$$

$$\begin{aligned}
 (2) \text{ 与式} &= \frac{\sqrt{5} - \sqrt{3}}{(\sqrt{5} + \sqrt{3})(\sqrt{5} - \sqrt{3})} \\
 &= \frac{\sqrt{5} - \sqrt{3}}{5 - 3} \\
 &= \frac{\sqrt{5} - \sqrt{3}}{2}
 \end{aligned}$$

$$\begin{aligned}
 (3) \text{ 与式} &= \frac{\sqrt{6}(\sqrt{3} + \sqrt{2})}{(\sqrt{3} - \sqrt{2})(\sqrt{3} + \sqrt{2})} \\
 &= \frac{3\sqrt{2} + 2\sqrt{3}}{3 - 2} \\
 &= 3\sqrt{2} + 2\sqrt{3}
 \end{aligned}$$

$$\begin{aligned}
 (4) \text{ 与式} &= \frac{(3 - 2\sqrt{2})(3 - 2\sqrt{2})}{(3 + 2\sqrt{2})(3 - 2\sqrt{2})} \\
 &= \frac{9 - 12\sqrt{2} + 8}{9 - 8} \\
 &= 17 - 12\sqrt{2}
 \end{aligned}$$

45.

$$\begin{aligned}
 (1) \text{ 与式} &= 2 + 3 - 3i + 4i \\
 &= 5 + i
 \end{aligned}$$

$$\begin{aligned}
 (2) \text{ 与式} &= 4 - 2 + i + 7i \\
 &= 2 + 8i
 \end{aligned}$$

$$\begin{aligned}
 (3) \text{ 与式} &= 3 - 5i + 9i - 15i^2 \\
 &= 3 + 4i + 15 \\
 &= 18 + 4i
 \end{aligned}$$

$$\begin{aligned}
 (4) \text{ 与式} &= 4 + 12i + 9i^2 \\
 &= 4 + 12i - 9 \\
 &= -5 + 12i
 \end{aligned}$$

$$\begin{aligned}
 (5) \text{ 与式} &= \frac{(1 - i)(1 - i)}{(1 + i)(1 - i)} \\
 &= \frac{1 - 2i + i^2}{1 - i^2} \\
 &= \frac{-2i}{2} \\
 &= -i
 \end{aligned}$$

$$\begin{aligned}
 (6) \text{ 与式} &= \frac{(1 - 3i) + (1 + 3i)}{(1 + 3i)(1 - 3i)} \\
 &= \frac{2}{1 - 9i^2} \\
 &= \frac{2}{10} \\
 &= \frac{1}{5}
 \end{aligned}$$

46.

$$\begin{aligned}
 (1) \text{ 与式} &= (\sqrt{3}i)^2 \\
 &= 3i^2 \\
 &= -3
 \end{aligned}$$

$$\begin{aligned}
 (2) \text{ 与式} &= \sqrt{8}i \cdot \sqrt{2}i \\
 &= 4i^2 \\
 &= -4
 \end{aligned}$$

$$\begin{aligned}
 (3) \text{ 与式} &= 2\sqrt{2}i + \sqrt{2}i \\
 &= 3\sqrt{2}i
 \end{aligned}$$

$$\begin{aligned}
 (4) \text{ 与式} &= \sqrt{5}i \cdot \sqrt{5} \\
 &= 5i
 \end{aligned}$$

$$\begin{aligned}
 (5) \text{ 与式} &= \sqrt{2} \cdot \sqrt{3}i \\
 &= \sqrt{6}i
 \end{aligned}$$

$$\begin{aligned}
 (6) \text{ 与式} &= \frac{\sqrt{12}i}{\sqrt{3}i} \\
 &= \sqrt{4} \\
 &= 2
 \end{aligned}$$

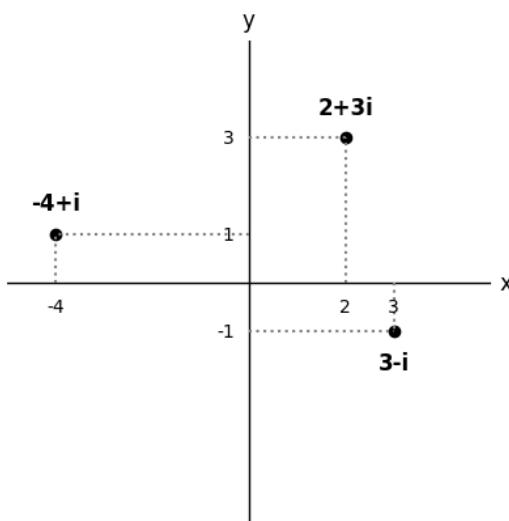
$$\begin{aligned}
 (7) \text{ 与式} &= \frac{\sqrt{8}}{\sqrt{2}i} \\
 &= -\sqrt{4}i \\
 &= -2i
 \end{aligned}$$

$$\begin{aligned}
 (8) \text{ 与式} &= \frac{\sqrt{27}i}{\sqrt{3}} \\
 &= \sqrt{9}i \\
 &= 3i
 \end{aligned}$$

47.

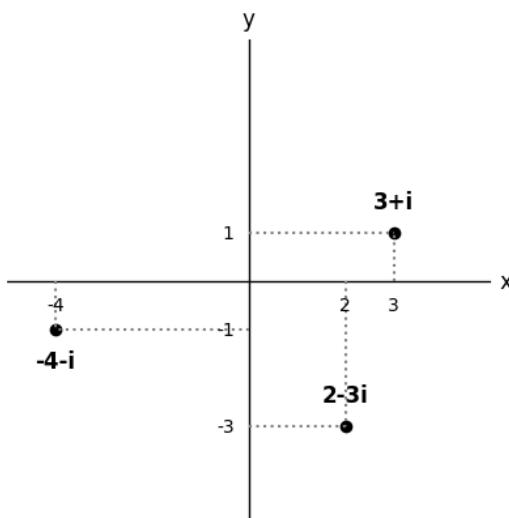
- (1) $1 + 3i$
 (2) $3 - 2i$
 (3) $-3 + i$
 (4) $-3i$

48.



49.

- (1) $\overline{2+3i} = 2 - 3i$
 (2) $\overline{-4+i} = -4 - i$
 (3) $\overline{3-i} = 3 + i$



50.

$$(1) \text{与式} = 4 + 3i + 4 - 3i \\ = 8$$

$$(2) \text{与式} = (4 + 3i)(4 - 3i) \\ = 16 - 9i^2 \\ = 16 + 9 \\ = 25$$

$$(3) \text{与式} = 3 - 2i - (3 + 2i) \\ = 3 - 2i - 3 - 2i \\ = -4i$$

$$(4) \text{与式} = (3 - 2i)(3 + 2i) \\ = 9 - 4i^2 \\ = 9 + 4 \\ = 13$$

51.

$$(1) \text{与式} = |1 + i| \\ = \sqrt{1^2 + 1^2} \\ = \sqrt{2}$$

$$(2) \text{与式} = |1 - i| \\ = \sqrt{1^2 + (-1)^2} \\ = \sqrt{2}$$

$$(3) \text{与式} = |-3i| \\ = \sqrt{0 + (-3)^2} \\ = 3$$

$$(4) \text{与式} = |1 + 2i| \\ = \sqrt{1^2 + 2^2} \\ = \sqrt{5}$$

$$(5) \text{与式} = |-3 - 4i| \\ = \sqrt{(-3)^2 + (-4)^2} \\ = 5$$

$$(6) \text{与式} = |1 + \sqrt{3}i| \\ = \sqrt{1^2 + (\sqrt{3})^2} \\ = 2$$

Check

52.

$$(1) \text{ 与式} = \frac{6x^4y^6}{8x^3y^9} = \frac{3x}{4y^3}$$

$$(2) \text{ 与式} = \frac{a}{a+3b} + \frac{3ab}{(a+3b)(a-3b)} = \frac{a(a-3b)+3ab}{(a+3b)(a-3b)} = \frac{a^2-3ab+3ab}{(a+3b)(a-3b)} = \frac{a^2}{(a+3b)(a-3b)}$$

$$(3) \text{ 与式} = -\frac{y}{x} \cdot \frac{y^3}{x^2} \cdot \left(-\frac{x^3}{y^2}\right) = \frac{x^3y^4}{x^3y^2} = y^2$$

$$(4) \text{ 与式} = \frac{(x-1)^2}{x(x-2)} \cdot \frac{x-2}{(x+1)(x+2)} \cdot \frac{x(x+1)}{x-1} = \frac{x-1}{x+2}$$

$$(5) \text{ 与式} = \frac{x^2-2x}{x^2+3x-10} = \frac{x(x-2)}{(x-2)(x+5)} = \frac{x}{x+5}$$

$$(6) \text{ 与式} = \frac{x(x+2)+2-x^2}{x+2-x} = \frac{2x+2}{2} = x+1$$

53.

(1)

$$\begin{array}{r} x+1 \\ \hline x^2-4x+3 \Big) \end{array} \begin{array}{r} x^3-3x^2-x+6 \\ \underline{-x^3+4x^2+3x} \\ x^2-4x+6 \\ \underline{x^2-4x+3} \\ 3 \end{array}$$

$$\text{与式} = x+1 + \frac{3}{x^2-4x+3}$$

(2)

$$\begin{array}{r} x-2 \\ x^2-3x+2 \Big) \end{array} \begin{array}{r} x^3-5x^2+9x+2 \\ \underline{x^3-3x^2+2x} \\ -2x^2+7x+2 \\ \underline{-2x^2+6x-4} \\ x+6 \end{array}$$

$$\text{与式} = x-2 + \frac{x+6}{x^2-3x+2}$$

54.

$$(1) \text{ 与式} = 3\sqrt{2}-2\sqrt{2}+4\sqrt{2} = 5\sqrt{2}$$

$$(2) \text{ 与式} = \sqrt{20}-\sqrt{10}+\sqrt{10}-\sqrt{5} = 2\sqrt{5}-\sqrt{5} = \sqrt{5}$$

$$(3) \text{ 与式} = \frac{2\sqrt{3}}{(\sqrt{3}+1)(3-\sqrt{3})} = \frac{2\sqrt{3}}{3\sqrt{3}-3+3-\sqrt{3}} = \frac{2\sqrt{3}}{2\sqrt{3}} = 1$$

$$(4) X = 2 + \sqrt{3} \text{ として}$$

$$\begin{aligned} \text{与式} &= (X+\sqrt{7})(X-\sqrt{7}) \\ &= X^2 - 7 \\ &= (2+\sqrt{3})^2 - 7 \\ &= 4+4\sqrt{3}+3-7 \\ &= 4\sqrt{3} \end{aligned}$$

55.

$$\begin{aligned}(1) \text{ 与式} &= |1 - \sqrt{2}| \\&= \sqrt{2} - 1\end{aligned}$$

$$\begin{aligned}(2) \text{ 与式} &= \frac{\sqrt{3} + 1}{(\sqrt{3} - 1)(\sqrt{3} + 1)} \\&\quad + \frac{\sqrt{5} - \sqrt{3}}{(\sqrt{5} + \sqrt{3})(\sqrt{5} - \sqrt{3})} \\&= \frac{\sqrt{3} + 1}{3 - 1} + \frac{\sqrt{5} - \sqrt{3}}{5 - 3} \\&= \frac{\sqrt{3} + 1 + \sqrt{5} - \sqrt{3}}{2} \\&= \frac{1 + \sqrt{5}}{2}\end{aligned}$$

56.

$$\begin{aligned}(1) \text{ 与式} &= |5 - 7| \\&= |7 - 5| \\&= 2\end{aligned}$$

$$\begin{aligned}(2) \text{ 与式} &= (3 + 2\sqrt{3} + 1) - (3 - 2\sqrt{3} + 1) \\&= 3 + 2\sqrt{3} + 1 - 3 + 2\sqrt{3} - 1 \\&= 4\sqrt{3}\end{aligned}$$

$$\begin{aligned}(3) \text{ 与式} &= |6 - 2\sqrt{5}| |6 + 2\sqrt{5}| \\&= 36 - 20 \\&= 16\end{aligned}$$

$$\begin{aligned}(4) \text{ 与式} &= |\sqrt{5} - 1| + |3 - \sqrt{5}| \\&= \sqrt{5} - 1 + 3 - \sqrt{5} \\&= 2\end{aligned}$$

57.

$$\begin{aligned}(1) \text{ 与式} &= 6 - 9i + 4i - 6i^2 \\&= 6 - 5i + 6 \\&= 12 - 5i\end{aligned}$$

$$\begin{aligned}(2) \text{ 与式} &= -\frac{1}{2i}(1 + 2i + i^2) \\&= \frac{1}{2i} + 1 + \frac{1}{2}i \\&= -\frac{1}{2}i + 1 + \frac{1}{2}i \\&= 1\end{aligned}$$

$$\begin{aligned}(3) \text{ 与式} &= \sqrt{3}i \cdot 3\sqrt{3}i \\&= 9i^2 \\&= -9\end{aligned}$$

$$\begin{aligned}(4) \text{ 与式} &= \frac{4\sqrt{2}}{\sqrt{2}i} \\&= -4i\end{aligned}$$

58.

$$\begin{aligned}(1) \text{ 与式} &= |3 - 2i| \\&= \sqrt{3^2 + (-2)^2} \\&= \sqrt{13}\end{aligned}$$

$$\begin{aligned}(2) \text{ 与式} &= |(2 - i)(1 - 2i)| \\&= |2 - 4i - i + 2i^2| \\&= |2 - 5i - 2| \\&= |-5i| \\&= \sqrt{0^2 + (-5)^2} \\&= 5\end{aligned}$$

$$\begin{aligned}(3) \text{ 与式} &= \left| \frac{2-i}{2+i} \right| \\&= \frac{\sqrt{2^2 + (-1)^2}}{\sqrt{2^2 + 1^2}} \\&= \frac{\sqrt{5}}{\sqrt{5}} \\&= 1\end{aligned}$$

$$\begin{aligned}(4) \text{ 与式} &= \left| \frac{3-4i}{1+2i} \right| \\&= \frac{\sqrt{3^2 + (-4)^2}}{\sqrt{1^2 + 2^2}} \\&= \frac{5}{\sqrt{5}} \\&= \sqrt{5}\end{aligned}$$

59.

$$\begin{aligned}(1) \text{ 与式} &= 2 + 3i + \overline{2 + 3i} \\&= 2 + 3i + 2 - 3i \\&= 4\end{aligned}$$

$$\begin{aligned}
(2) \text{ 与式} &= (2+3i)^2 \\
&= 4 + 12i + 9i^2 \\
&= 4 + 12i - 9 \\
&= \mathbf{-5 + 12i}
\end{aligned}$$

$$\begin{aligned}
(3) \text{ 与式} &= |2+3i|^2 \\
&= (\sqrt{2^2+3^2})^2 \\
&= \mathbf{13}
\end{aligned}$$

$$\begin{aligned}
(4) \text{ 与式} &= (2+3i)(\overline{2+3i}) \\
&= (2+3i)(2-3i) \\
&= 4 - 9i^2 \\
&= 4 + 9 \\
&= \mathbf{13}
\end{aligned}$$

Step up

60.

$$\begin{aligned}
(1) \text{ 与式} &= \frac{3}{(x-2)(x-3)} - \frac{2}{(x-3)(x-1)} \\
&\quad - \frac{1}{(x-2)(x-1)} \\
&= \frac{3(x-1) - 2(x-2) - (x-3)}{(x-1)(x-2)(x-3)} \\
&= \frac{3x - 2x - x - 3 + 4 + 3}{(x-1)(x-2)(x-3)} \\
&= \frac{4}{(x-1)(x-2)(x-3)}
\end{aligned}$$

(2) 与式

$$\begin{aligned}
&= \frac{-(b+c)}{(a-b)(c-a)} + \frac{-(c+a)}{(b-c)(a-b)} + \frac{-(a+b)}{(c-a)(b-c)} \\
&= \frac{-(b+c)(b-c) - (c+a)(c-a) - (a+b)(a-b)}{(a-b)(b-c)(c-a)} \\
&= \frac{-(b^2 - c^2) - (c^2 - a^2) - (a^2 - b^2)}{(a-b)(b-c)(c-a)} \\
&= \frac{-b^2 + c^2 - c^2 + a^2 - a^2 + b^2}{(a-b)(b-c)(c-a)} \\
&= \mathbf{0}
\end{aligned}$$

$$\begin{aligned}
(3) \text{ 与式} &= \frac{(x-y)^2}{(x-y)(x^2+xy+y^2)} \cdot \left(-\frac{x-y}{xy(x+y)}\right) \\
&= -\frac{x+y}{xy(x^2+xy+y^2)}
\end{aligned}$$

$$\begin{aligned}
(4) \text{ 与式} &= \frac{(2x+3y)(x+y)}{(x-y)^2} \cdot \frac{(x+y)(x-y)}{(2x-y)(x+y)} \\
&\quad \cdot \frac{(2x-y)(x-y)}{(2x-3y)(x+y)} \\
&= \frac{\mathbf{2x+3y}}{2x-3y}
\end{aligned}$$

61.

$$\begin{aligned}
(1) \text{ 与式} &= \frac{(x+1)(x+1) - (x-1)(x-1)}{(x+1)(x+1) + (x-1)(x-1)} \\
&= \frac{(x+1)^2 - (x-1)^2}{(x+1)^2 + (x-1)^2} \\
&= \frac{(x^2 + 2x + 1) - (x^2 - 2x + 1)}{(x^2 + 2x + 1) + (x^2 - 2x + 1)} \\
&= \frac{4x}{2x^2 + 2} \\
&= \frac{\mathbf{2x}}{x^2 + 1}
\end{aligned}$$

$$\begin{aligned}
(2) \text{ 与式} &= \frac{2(t+2) + (t+2)(t-2)}{2(t+2) - (t+2)(t-2)} \\
&= \frac{2t + 4 + t^2 - 4}{2t + 4 - (t^2 - 4)} \\
&= \frac{2t + t^2}{2t - t^2} \\
&= \frac{t(2+t)}{t(2-t)} \\
&= -\frac{\mathbf{t+2}}{t-2}
\end{aligned}$$

$$\begin{aligned}
(3) \text{ 与式} &= \frac{a - \frac{a}{a+1}}{a + \frac{a}{a-1}} \\
&= \frac{a(a+1)(a-1) - a(a-1)}{a(a+1)(a-1) + a(a+1)} \\
&= \frac{(a-1)\{a(a+1) - a\}}{(a+1)\{a(a-1) + a\}} \\
&= \frac{a^2(a-1)}{a^2(a+1)} \\
&= \frac{\mathbf{a-1}}{a+1}
\end{aligned}$$

$$\begin{aligned}
(4) \text{ 与式} &= \frac{1}{1 - \frac{1}{1 - \frac{x}{x-1}}} \\
&= \frac{1}{1 - \frac{x-1}{x-1-x}} \\
&= \frac{1}{1 - \frac{x-1}{-1}} \\
&= \frac{1}{1+x-1} \\
&= \frac{1}{x}
\end{aligned}$$

62.

$$\begin{aligned}
(1) \text{ 与式} &= \frac{2 + \sqrt{3} - \sqrt{7}}{(2 + \sqrt{3} + \sqrt{7})(2 + \sqrt{3} - \sqrt{7})} \\
&= \frac{2 + \sqrt{3} - \sqrt{7}}{(2 + \sqrt{3})^2 - (\sqrt{7})^2} \\
&= \frac{2 + \sqrt{3} - \sqrt{7}}{4 + 4\sqrt{3} + 3 - 7} \\
&= \frac{2 + \sqrt{3} - \sqrt{7}}{4\sqrt{3}} \\
&= \frac{2\sqrt{3} + 3 - \sqrt{21}}{12}
\end{aligned}$$

$$\begin{aligned}
(2) \text{ 与式} &= \frac{1 + \sqrt{2} + \sqrt{3} + 1 + \sqrt{2} - \sqrt{3}}{(1 + \sqrt{2} - \sqrt{3})(1 + \sqrt{2} + \sqrt{3})} \\
&= \frac{2 + 2\sqrt{2}}{(1 + \sqrt{2})^2 - (\sqrt{3})^2} \\
&= \frac{2 + 2\sqrt{2}}{1 + 2\sqrt{2} + 2 - 3} \\
&= \frac{2(1 + \sqrt{2})}{2\sqrt{2}} \\
&= \frac{1 + \sqrt{2}}{\sqrt{2}} \\
&= \frac{2 + \sqrt{2}}{2}
\end{aligned}$$

63.

(1) $\alpha = a + bi, \beta = c + di$ と置く

$$\begin{aligned}
|\alpha| &= |a + bi| \\
&= \sqrt{a^2 + b^2} \\
|\bar{\alpha}| &= |\overline{a - bi}| \\
&= \sqrt{a^2 + (-b)^2} \\
&= \sqrt{a^2 + b^2}
\end{aligned}$$

(2)

$$\begin{aligned}
|\alpha + \beta|^2 &= (\alpha + \beta)(\overline{\alpha + \beta}) \\
&= (\alpha + \beta)(\bar{\alpha} + \bar{\beta}) \\
&= \alpha\bar{\alpha} + \alpha\bar{\beta} + \bar{\alpha}\beta + \beta\bar{\beta} \\
&= |\alpha|^2 + \alpha\bar{\beta} + \bar{\alpha}\beta + |\beta|^2
\end{aligned}$$

(3)

$$\begin{aligned}
|\alpha| &= |\beta \cdot \frac{\alpha}{\beta}| \\
&= |\beta| \left| \frac{\alpha}{\beta} \right| \\
\frac{|\alpha|}{|\beta|} &= \frac{1}{|\beta|} \cdot |\beta| \left| \frac{\alpha}{\beta} \right| \\
&= \left| \frac{\alpha}{\beta} \right|
\end{aligned}$$

64.

$$\begin{aligned}
\text{左辺} &= \sqrt{(\sqrt{a} + \sqrt{b})^2} \\
&= \sqrt{a} + \sqrt{b} = \text{右辺}
\end{aligned}$$

65.

$$\begin{aligned}
(1) \text{ 与式} &= \sqrt{1 + 2\sqrt{2} + 2} \\
&= \sqrt{(1 + \sqrt{2})^2} \\
&= \sqrt{2} + 1
\end{aligned}$$

$$\begin{aligned}
(2) \text{ 与式} &= \sqrt{3 + 2 - 2\sqrt{6}} \\
&= \sqrt{(\sqrt{3} - \sqrt{2})^2} \\
&= \sqrt{3} - \sqrt{2}
\end{aligned}$$

$$\begin{aligned}
(3) \text{ 与式} &= \sqrt{4 + 2 - 2\sqrt{8}} \\
&= \sqrt{(\sqrt{4} - \sqrt{2})^2} \\
&= 2 - \sqrt{2}
\end{aligned}$$

$$\begin{aligned}
 (4) \text{ 与式} &= \sqrt{4 + 3 - 2\sqrt{12}} \\
 &= \sqrt{(\sqrt{4} - \sqrt{3})^2} \\
 &= 2 - \sqrt{3}
 \end{aligned}$$

$$\begin{aligned}
 (5) \text{ 与式} &= \sqrt{\frac{1}{2} + \frac{3}{2} + 2\sqrt{\frac{3}{2}}} \\
 &= \sqrt{(\sqrt{\frac{1}{2}} + \sqrt{\frac{3}{2}})^2} \\
 &= \frac{1}{\sqrt{2}} + \frac{\sqrt{3}}{\sqrt{2}} \\
 &= \frac{\sqrt{6} + \sqrt{2}}{2}
 \end{aligned}$$

$$\begin{aligned}
 (6) \text{ 与式} &= \sqrt{\frac{7}{2} + \frac{1}{2} - 2\sqrt{\frac{7}{2}}} \\
 &= \sqrt{(\sqrt{\frac{7}{2}} - \sqrt{\frac{1}{2}})^2} \\
 &= \frac{\sqrt{7}}{\sqrt{2}} - \frac{1}{\sqrt{2}} \\
 &= \frac{\sqrt{14} - \sqrt{2}}{2}
 \end{aligned}$$

66.

$$\begin{aligned}
 (1) \text{ 与式} &= \sqrt{(\sqrt{x} - 1)^2} \\
 &= \sqrt{x} - 1
 \end{aligned}$$

$$\begin{aligned}
 (2) \text{ 与式} &= \sqrt{(\sqrt{a} + \sqrt{1-a})^2} \\
 &= \sqrt{a} + \sqrt{1-a}
 \end{aligned}$$

67.

$$\begin{aligned}
 \text{与式} &= \frac{5}{\sqrt{(\sqrt{6}-1)^2}} \\
 &= \frac{5}{\sqrt{6}-1} \\
 &= \frac{5(\sqrt{6}+1)}{(\sqrt{6}-1)(\sqrt{6}+1)} \\
 &= \frac{5\sqrt{6}+1}{6-1} \\
 &= \sqrt{6}+1
 \end{aligned}$$

$$\begin{aligned}
 2 < \sqrt{6} < 3 \text{ より}, 3 < \sqrt{6} + 1 < 4 \\
 \text{よって } a = 3, b = \sqrt{6} + 1 - 3 = \sqrt{6} - 2
 \end{aligned}$$

$$\begin{aligned}
 \frac{1}{a} + \frac{1}{b} &= \frac{1}{3} + \frac{1}{\sqrt{6}-2} \\
 &= \frac{\sqrt{6}-2+3}{3\sqrt{6}-6} \\
 &= \frac{\sqrt{6}+1}{3\sqrt{6}-6} \\
 &= \frac{(\sqrt{6}+1)(3\sqrt{6}+6)}{(3\sqrt{6}-6)(3\sqrt{6}+6)} \\
 &= \frac{18+9\sqrt{6}+6}{54-36} \\
 &= \frac{24+9\sqrt{6}}{18} \\
 &= \frac{8+3\sqrt{6}}{6}
 \end{aligned}$$