Machine-Level Programming IV: Data

15-213: Introduction to Computer Systems 8th Lecture, June 1, 2022

Instructor:

Zack Weinberg

Today

Partial recap: Integers

- Word size
- Addresses
- Endianness

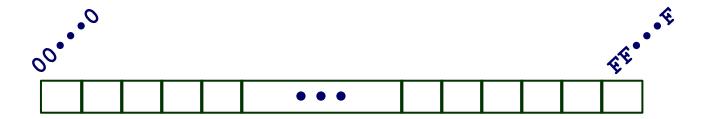
Arrays

- One-dimensional
- Multi-dimensional (nested)
- Multi-level

Structures

- Allocation
- Access
- Alignment
- If we have time: Floating point and SIMD

Byte-Oriented Memory Organization



Programs refer to data by address

- Imagine all of RAM as an enormous array of bytes
- An address is an index into that array
 - A pointer variable stores an address

System provides a private address space to each "process"

- A process is an instance of a program, being executed
- An address space is one of those enormous arrays of bytes
- Each program can see only its own code and data within its enormous array
- We'll come back to this later ("virtual memory" classes)

Machine Words

Any given computer has a "Word Size"

- Nominal size of integer-valued data
 - and of addresses
- Until recently, most machines used 32 bits (4 bytes) as word size
 - Limits addresses to 4GB (2³² bytes)
- Increasingly, machines have 64-bit word size
 - Potentially, could have 16 EB (exabytes) of addressable memory
 - That's $\frac{18.4 \times 10^{18}}{19.4 \times 10^{18}}$ bytes
 - Machines still support multiple data formats
 - Fractions or multiples of word size
 - Always integral number of bytes

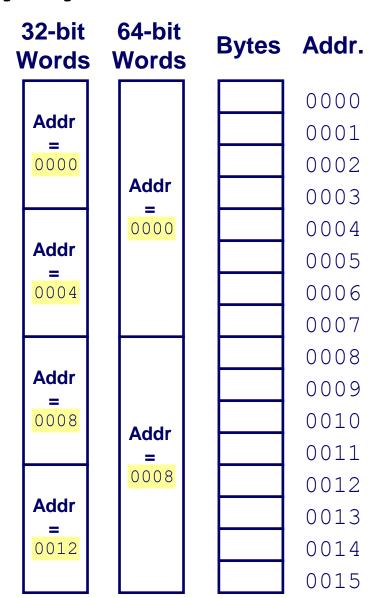
Yes, both of these numbers are correct.

This discrepancy is known as the Great Storage Industry Marketing Lie.

Ask me about it after class if you really want to know.

Addresses Always Specify Byte Locations

- Address of a word is address of the first byte in the word
- Addresses of successive words differ by 4 (32-bit) or 8 (64-bit)



Byte Ordering

- So, how are the bytes within a multi-byte word ordered in memory?
- Conventions
 - Big Endian: Sun, PPC Mac, network packet headers
 - Least significant byte has highest address
 - Little Endian: x86, ARM processors running Android, iOS, and Windows
 - Least significant byte has lowest address

Byte Ordering Example

Example

- Variable x has 4-byte value of 0x01234567
- Address given by &x is 0x100

Big Endian		0x100	0x101	0x102	0x103	
		01	23	45	67	
Little Endia	0x100	0x101	0x102	0x103		
		67	45	23	01	

Examining Data Representations

Code to Print Byte Representation of Data

Casting pointer to unsigned char * allows treatment as a byte array

Printf directives:

%p: Print pointer (must be void *)

%.2x: Print integer in hexadecimal,

with at least two digits

show_bytes Execution Example

```
int a = 15213;
printf("int a = %d;\n", a);
show_bytes((unsigned char *) &a, sizeof(int));
```

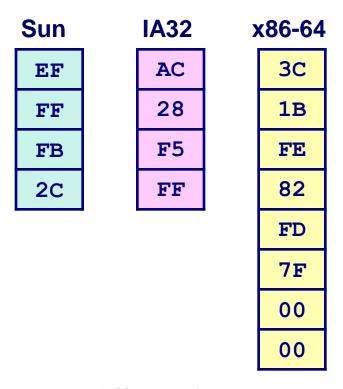
Result (Linux x86-64):

```
int a = 15213;
0x7fffb7f71dbc 6d
0x7fffb7f71dbd 3b
0x7fffb7f71dbe 00
0x7fffb7f71dbf 00
```

Representing Pointers

int
$$B = -15213;$$

int *P = &B



Different compilers & machines assign different locations to objects

May even get different results each time program is run (ASLR)

Representing Strings

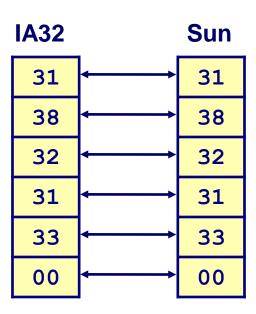
char S[6] = "18213";

Strings in C

- Represented by array of characters
- Each character encoded in ASCII format
 - Standard 7-bit encoding of character set
 - Character "0" has code 0x30
 - Digit i has code 0x30+i
- String should be null-terminated
 - Final character = 0

Compatibility

Byte ordering not an issue



A note about x86 machine code

x86 machine code is a sequence of bytes

- Grouped into variable-length instructions, which look like strings...
- But they contain embedded little-endian numbers...

Example Fragment

Address	Instruction Code	Assembly Rendition		
8048365:	5b	pop %ebx		
8048366:	81 c3 ab 12 00 00	add \$0x12ab, %ebx		
804836c:	83 bb 28 00 00 00 00	cmpl \$0x0,0x28(%ebx)		

Deciphering Numbers

- Value:
- Pad to 32 bits:
- Split into bytes:
- Reverse:

0x12ab

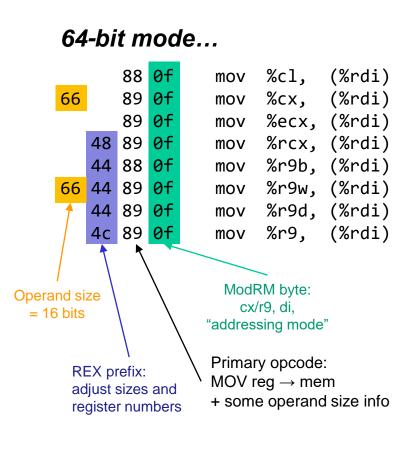
0x000012ab

00 00 12 ab

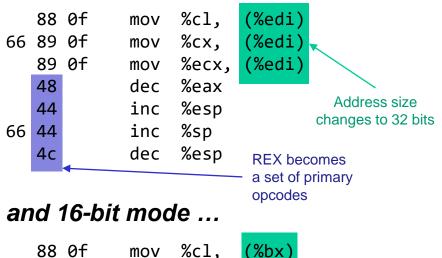
ab 12 00 00

A peek at x86 instruction encoding

and its long, complex history



Same bytes interpreted in 32-bit mode...



66	89	0f 0f 0f	mov mov inc	%cl, %ecx, %cx, %sp	(%bx) (%bx) (%bx)	Address size
66	44		inc	%esp		Address size changes to 16 bits,
		\	Now means Operand siz			register numbering is different

= **32** bits

Today

- Partial recap: Integers
 - Word size
 - Addresses
 - Endianness
- Arrays
 - One-dimensional
 - Multi-dimensional (nested)
 - Multi-level
- Structures
 - Allocation
 - Access
 - Alignment
- If we have time: Floating point and SIMD

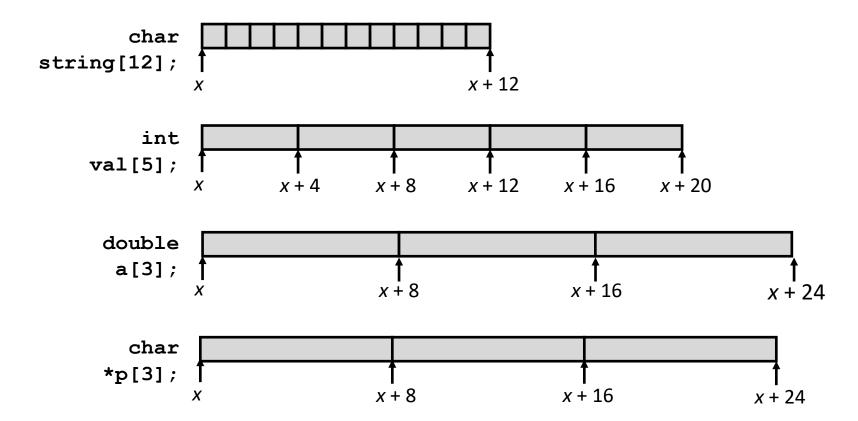
Activity break:
pick a partner (just one other student this time),
get handout
(https://www.cs.cmu.edu/afs/cs/academic/class/
15213-m22/www/activities/213_lecture8.pdf),
do part 1 and 2.1

Array Allocation

Basic Principle

 $T \mathbf{A}[L];$

- Array of data type T and length L
- Contiguously allocated region of L * sizeof (T) bytes in memory



Array Access

■Basic Principle

```
T A[L];
```

- Array of data type T and length L
- Identifier A can be used as a pointer to array element 0: Type T*

```
int val[5]; 1 5 2 1 3

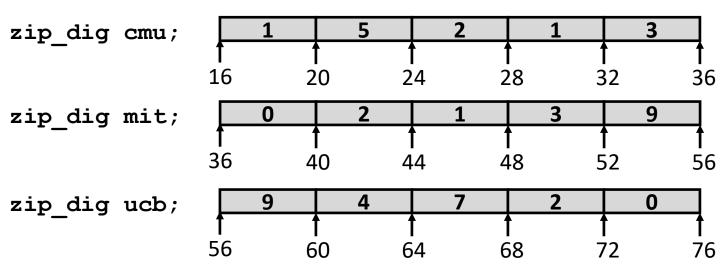
x x + 4 x + 8 x + 12 x + 16 x + 20
```

■Reference Type Value

Array Example

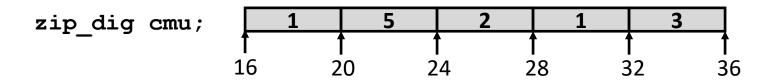
```
#define ZLEN 5
typedef int zip_dig[ZLEN];

zip_dig cmu = { 1, 5, 2, 1, 3 };
zip_dig mit = { 0, 2, 1, 3, 9 };
zip_dig ucb = { 9, 4, 7, 2, 0 };
```



- Declaration "zip_dig cmu" equivalent to "int cmu[5]"
- Example arrays were allocated in successive 20 byte blocks
 - Not guaranteed to happen in general

Array Accessing Example



```
int get_digit
  (zip_dig z, int digit)
{
  return z[digit];
}
```

x86-64

```
# %rdi = z
# %rsi = digit
movl (%rdi,%rsi,4), %eax # z[digit]
```

- Register %rdi contains starting address of array
- Register %rsi contains array index
- Desired digit at
 %rdi + 4*%rsi
- Use memory reference (%rdi,%rsi,4)

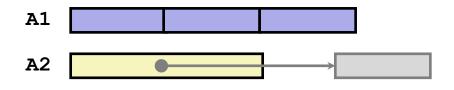
Decl		An		*An			
	Cmp	Bad	Size	Cmp	Bad	Size	
int A1[3]							
int *A2							

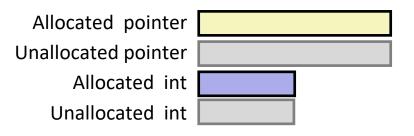
Cmp: Compiles (Y/N)

Bad: Possible bad pointer reference (Y/N)

■ Size: Value returned by sizeof

Decl		An		*A <i>n</i>			
	Cmp	Bad	Size	Cmp	Bad	Size	
int A1[3]	Y	N	12	Y	N	4	
int *A2	Y	N	8	Y	Y	4	





- Cmp: Compiles (Y/N)
- Bad: Possible bad pointer reference (Y/N)
- Size: Value returned by sizeof

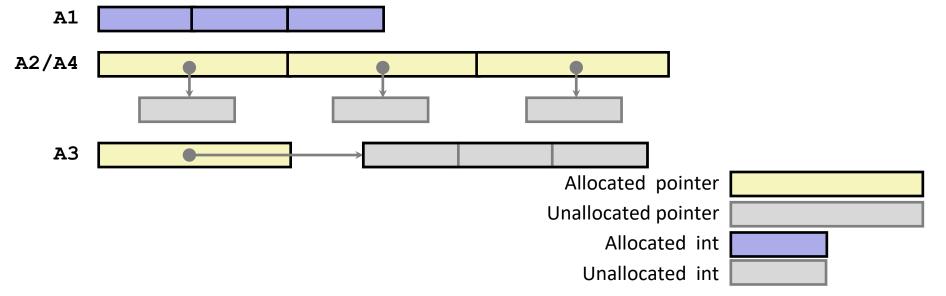
Decl	An			*An			**An		
	Cmp	Bad	Size	Cmp	Bad	Size	Cmp	Bad	Size
int A1[3]									
int *A2[3]									
int (*A3)[3]									
int (*A4[3])									

Cmp: Compiles (Y/N)

Bad: Possible bad pointer reference (Y/N)

■ Size: Value returned by sizeof

Decl	An			*An			**An		
	Cmp	Bad	Size	Cmp	Bad	Size	Cmp	Bad	Size
int A1[3]	Y	N	12	Y	N	4	N	-	-
int *A2[3]	Y	N	24	Y	N	8	Y	Y	4
int (*A3)[3]	Y	N	8	Y	Y	12	Y	Y	4
int (*A4[3])	Y	N	24	Y	N	8	Y	Y	4



Multidimensional (Nested) Arrays

Declaration

$T \mathbf{A}[R][C];$

- 2D array of data type T
- R rows, C columns
- Type T element requires K bytes

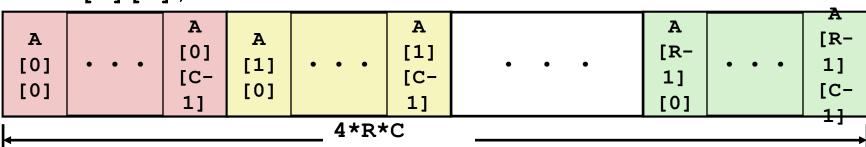
Array Size

• *R* * *C* * *K* bytes

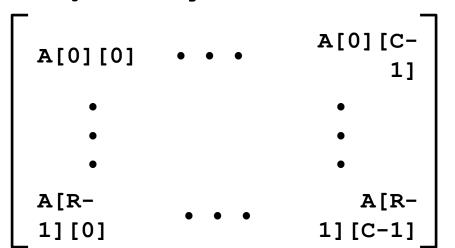
Arrangement

Row-Major Ordering

int A[R][C];

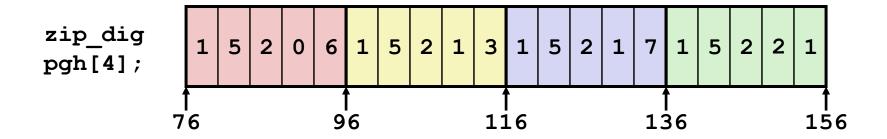


Bytes



Nested Array Example

```
#define PCOUNT 4
zip_dig pgh[PCOUNT] =
  {{1, 5, 2, 0, 6},
   {1, 5, 2, 1, 3},
   {1, 5, 2, 1, 7},
   {1, 5, 2, 2, 1 }};
```



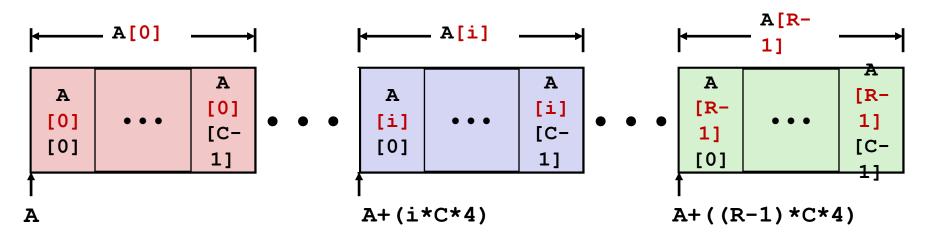
- "zip_dig pgh[4]" equivalent to "int pgh[4][5]"
 - Variable pgh: array of 4 elements, allocated contiguously
 - Each element is an array of 5 int's, allocated contiguously
- "Row-Major" ordering of all elements in memory

Nested Array Row Access

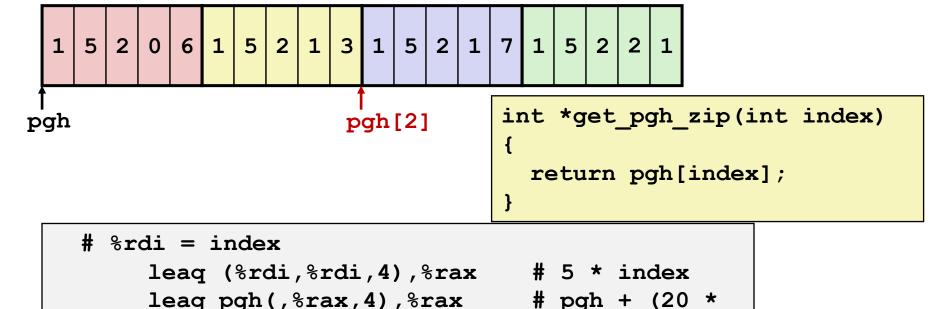
Row Vectors

- A[i] is array of C elements
- Each element of type T requires K bytes
- Starting address A + i * (C * K)

int A[R][C];



Nested Array Row Access Code



index)

Row Vector

- pgh[index] is array of 5 int's
- Starting address pgh+20*index

■ Machine Code

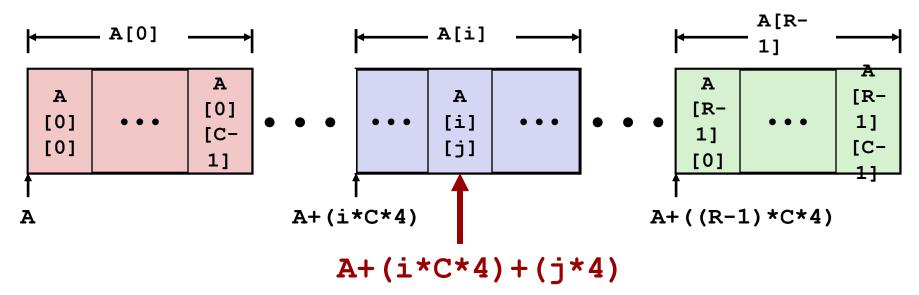
- Computes and returns address
- Compute as pgh + 4* (index+4*index)

Nested Array Element Access

Array Elements

- A[i][j] is element of type T, which requires K bytes
- Address A + i * (C * K) + j * K= A + (i * C + j) * K

int A[R][C];



Nested Array Element Access Code

```
1 5 2 0 6 1 5 2 1 3 1 5 2 1 7 1 5 2 2 1

pgh [1][1] int get_pgh_digit(int index, int dig)
{
    return pgh[index][dig];
}
```

```
leaq (%rdi,%rdi,4), %rax # 5*index
addl %rax, %rsi # 5*index+dig
movl pgh(,%rsi,4), %eax # M[pgh +
```

4* (5*index+dig)] Array Elements

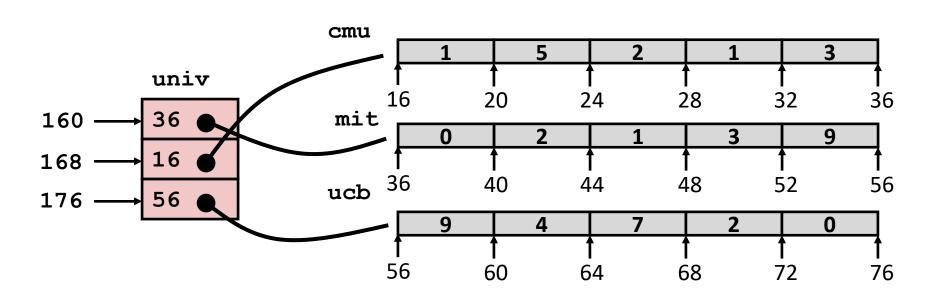
- pgh[index][dig] is int
- Address: pgh + 20*index + 4*dig
 = pgh + 4*(5*index + dig)

Multi-Level Array Example

```
zip_dig cmu = { 1, 5, 2, 1, 3 };
zip_dig mit = { 0, 2, 1, 3, 9 };
zip_dig ucb = { 9, 4, 7, 2, 0 };
```

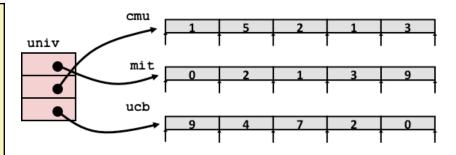
```
#define UCOUNT 3
int *univ[UCOUNT] = {mit, cmu, ucb};
```

- Variable univ denotes array of 3 elements
- Each element is a pointer
 - 8 bytes
- Each pointer points to array of int's



Element Access in Multi-Level Array

```
int get_univ_digit
  (size_t index, size_t digit)
{
  return univ[index][digit];
}
```



```
salq $2, %rsi  # 4*digit
addq univ(,%rdi,8), %rsi # p = univ[index] + 4*digit
movl (%rsi), %eax  # return *p
ret
```

Computation

- Element access Mem [Mem [univ+8*index]+4*digit]
- Must do two memory reads
 - First get pointer to row array
 - Then access element within array

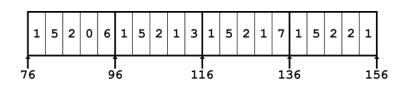
Array Element Accesses

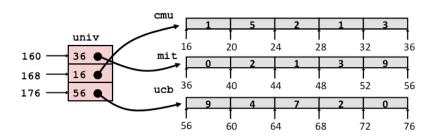
Nested array

```
int get_pgh_digit
   (size_t index, size_t digit)
{
   return pgh[index][digit];
}
```

Multi-level array

```
int get_univ_digit
  (size_t index, size_t digit)
{
  return univ[index][digit];
}
```





Accesses looks similar in C, but address computations very different:

Mem[pgh+20*index+4*digit] Mem[Mem[univ+8*index]+4*digit]

N X N Matrix Code

- Fixed dimensions
 - Know value of N at compile time
- Variable dimensions, explicit indexing
 - Traditional way to implement dynamic arrays
- Variable dimensions, implicit indexing
 - "New" feature in C99

Example: Array Access

```
#include <stdio.h>
#define ZLEN 5
#define PCOUNT 4
typedef int zip dig[ZLEN];
int main(int argc, char** argv) {
zip dig pgh[PCOUNT] =
    {{1, 5, 2, 0, 6},
    {1, 5, 2, 1, 3},
    {1, 5, 2, 1, 7},
    {1, 5, 2, 2, 1 }};
    int *linear zip = (int *) pgh;
    int *zip2 = (int *) pgh[2];
    int result =
       pgh[0][0] +
       linear zip[7] +
        *(linear zip + 8) +
        zip2[1];
   printf("result: %d\n", result);
    return 0;
```

```
linux> ./array
result: 9
```

Example: Array Access

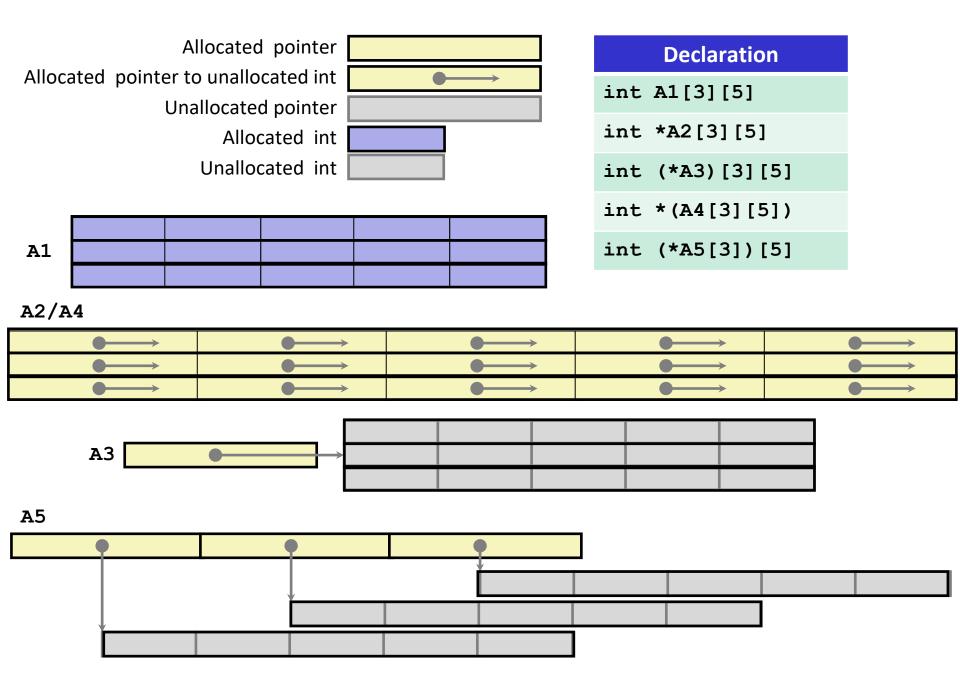
```
#include <stdio.h>
#define ZLEN 5
#define PCOUNT 4
typedef int zip dig[ZLEN];
int main(int argc, char** argv) {
zip dig pgh[PCOUNT] =
    \{\{1, 5, 2, 0, 6\},
    {1, 5, 2, 1, 3},
    {1, 5, 2, 1, 7},
    {1, 5, 2, 2, 1 }};
    int *linear zip = (int *) pgh;
    int *zip2 = (int *) pgh[2];
    int result =
       pgh[0][0] +
        linear zip[7] +
        *(linear zip + 8) +
        zip2[1];
   printf("result: %d\n", result);
    return 0;
```

```
linux> ./array
result: 9
```

Decl	An			*A <i>n</i>			**An		
	Cmp	Bad	Size	Cmp	Bad	Size	Cmp	Bad	Size
int A1[3][5]									
int *A2[3][5]									
int (*A3)[3][5]									
int *(A4[3][5])									
int (*A5[3])[5]									

- Cmp: Compiles (Y/N)
- Bad: Possible bad pointer reference (Y/N)
- Size: Value returned by sizeof

Decl	***An					
	Cmp	Bad	Size			
int A1[3][5]						
int *A2[3][5]						
int (*A3)[3][5]						
int *(A4[3][5])						
int (*A5[3])[5]						



Understanding Pointers & Arrays #3

Decl	An			*An			**An		
	Cmp	Bad	Size	Cmp	Bad	Size	Cmp	Bad	Size
int A1[3][5]	Y	N	60	Y	N	20	Y	N	4
int *A2[3][5]	Y	N	120	Y	N	40	Y	N	8
int (*A3)[3][5]	Y	N	8	Y	Y	60	Y	Y	20
int *(A4[3][5])	Y	N	120	Y	N	40	Y	N	8
int (*A5[3])[5]	Y	N	24	Y	N	8	Y	Y	20

- Cmp: Compiles (Y/N)
- Bad: Possible bad pointer reference (Y/N)
- Size: Value returned by sizeof

Decl	***An				
	Cmp	Bad	Size		
int A1[3][5]	N	-	_		
int *A2[3][5]	Y	Y	4		
int (*A3)[3][5]	Y	Y	4		
int *(A4[3][5])	Y	Y	4		
int (*A5[3])[5]	Y	Y	4		

Today

Partial recap: Integers

- Word size
- Addresses
- Endianness

Arrays

- One-dimensional
- Multi-dimensional (nested)
- Multi-level

Structures

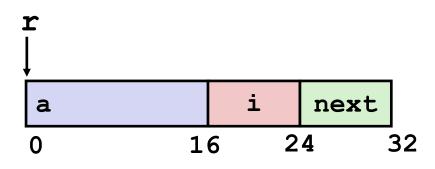
- Allocation
- Access
- Alignment

■ If we have time: Floating point and SIMD

Activity break: do part 2.2 now

Structure Representation

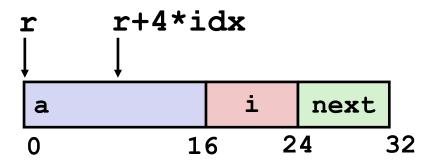
```
struct rec {
   int a[4];
   size_t i;
   struct rec *next;
};
```



- Structure represented as block of memory
 - Big enough to hold all of the fields
- Fields ordered according to declaration
 - Even if another ordering could yield a more compact representation
- Compiler determines overall size + positions of fields
 - Machine-level program has no understanding of the structures in the source code

Generating Pointer to Structure Member

```
struct rec {
   int a[4];
   size_t i;
   struct rec *next;
};
```



Generating Pointer to Array Element

- Offset of each structure member determined at compile time
- Compute as r + 4*idx

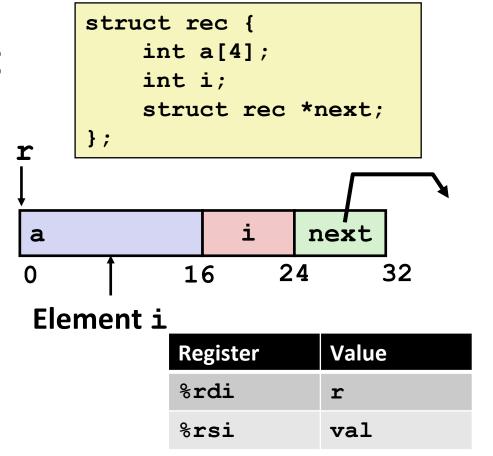
```
int *get_ap
  (struct rec *r, size_t idx)
{
   return &r->a[idx];
}
```

```
# r in %rdi, idx in %rsi
leaq (%rdi,%rsi,4), %rax
ret
```

Following Linked List

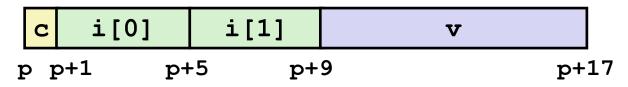
C Code

```
void set_val
  (struct rec *r, int val)
{
  while (r) {
    int i = r->i;
    r->a[i] = val;
    r = r->next;
  }
}
```



Structures & Alignment

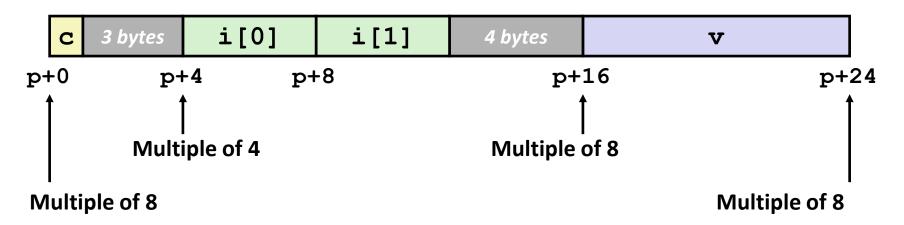
Unaligned Data



```
struct S1 {
  char c;
  int i[2];
  double v;
} *p;
```

Aligned Data

- Primitive data type requires K bytes
- Address must be multiple of K



Alignment Principles

Aligned Data

- Primitive data type requires K bytes
- Address must be multiple of K
- Required on some machines; advised on x86-64

Motivation for Aligning Data

- Memory accessed by (aligned) chunks of 4 or 8 bytes (system dependent)
 - Inefficient to load or store datum that spans quad word boundaries
 - Virtual memory trickier when datum spans 2 pages

Compiler

Inserts gaps in structure to ensure correct alignment of fields

Specific Cases of Alignment (x86-64)

- 1 byte: char, ...
 - no restrictions on address
- 2 bytes: short, ...
 - lowest 1 bit of address must be 0₂
- 4 bytes: int, float, ...
 - lowest 2 bits of address must be 00₂
- 8 bytes: double, long, char *, ...
 - lowest 3 bits of address must be 000₂

Satisfying Alignment with Structures

Within structure:

Must satisfy each element's alignment requirement

Overall structure placement

- Each structure has alignment requirement K
 - K = Largest alignment of any element
- Initial address & structure length must be multiples of K

Example:

K = 8, due to double element

```
        c
        3 bytes
        i [0]
        i [1]
        4 bytes
        v

        p+0
        p+4
        p+8
        p+16
        p+24

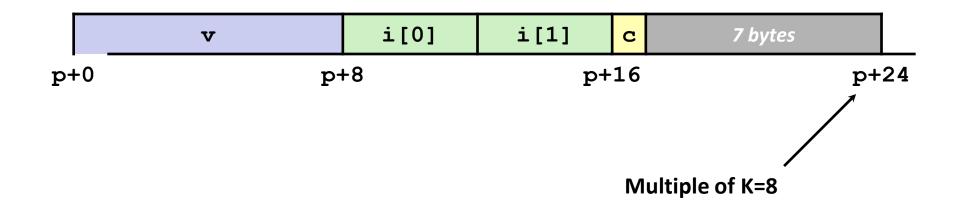
        Multiple of 4
        Multiple of 8
        Multiple of 8

Multiple of 8
```

Meeting Overall Alignment Requirement

- For largest alignment requirement K
- Overall structure must be multiple of K

```
struct S2 {
  double v;
  int i[2];
  char c;
} *p;
```

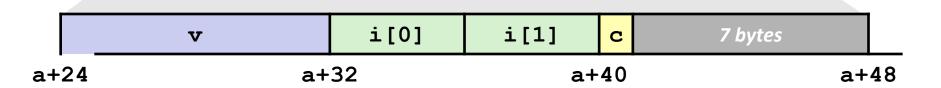


Arrays of Structures

- Overall structure length multiple of K
- Satisfy alignment requirement for every element

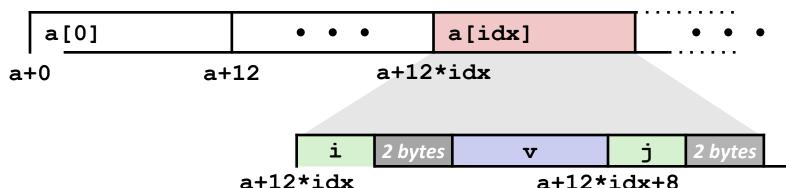
```
struct S2 {
  double v;
  int i[2];
  char c;
} a[10];
```





Accessing Array Elements

- Compute array offset 12*idx
 - sizeof (S3), including alignment spacers
- Element j is at offset 8 within structure
- Assembler gives offset a+8
 - Resolved during linking



```
short get_j(int idx)
{
  return a[idx].j;
}
```

```
# %rdi = idx
leaq (%rdi,%rdi,2),%rax #
3*idx
movzwl a+8(,%rax,4),%eax
```

Saving Space

Put large data types first

```
struct S4 {
  char c;
  int i;
  char d;
} *p;
struct S5 {
  int i;
  char c;
  char d;
} *p;
Effect (K=4)
```

```
c 3 bytes i d 3 bytes

i c d 2 bytes
```

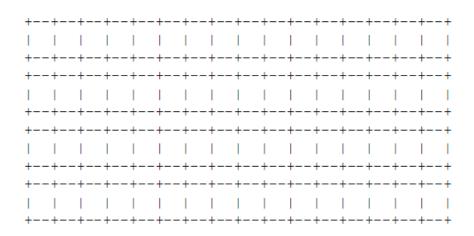
Example Struct Exam Question

Problem 5. (8 points):

Struct alignment. Consider the following C struct declaration:

```
typedef struct {
  char a;
  long b;
  float c;
  char d[3];
  int *e;
  short *f;
} foo;
```

 Show how foo would be allocated in memory on an x86-64 Linux system. Label the bytes with the names of the various fields and clearly mark the end of the struct. Use an X to denote space that is allocated in the struct as padding.



Example Struct Exam Question

Problem 5. (8 points):

Struct alignment. Consider the following C struct declaration:

```
typedef struct {
  char a;
  long b;
  float c;
  char d[3];
  int *e;
  short *f;
} foo;
```

 Show how foo would be allocated in memory on an x86-64 Linux system. Label the bytes with the names of the various fields and clearly mark the end of the struct. Use an X to denote space that is allocated in the struct as padding.

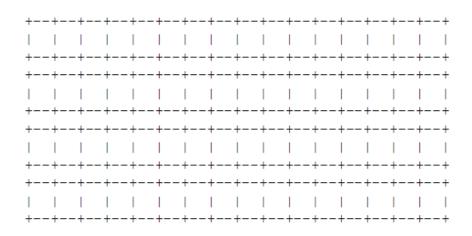
Example Struct Exam Question (Cont'd)

Problem 5. (8 points):

Struct alignment. Consider the following C struct declaration:

```
typedef struct {
  char a;
  long b;
  float c;
  char d[3];
  int *e;
  short *f;
} foo;
```

Rearrange the elements of foo to conserve the most space in memory. Label the bytes with the names of the various fields and clearly mark the end of the struct. Use an X to denote space that is allocated in the struct as padding.



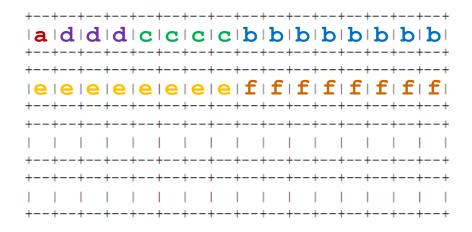
Example Struct Exam Question (Cont'd)

Problem 5. (8 points):

Struct alignment. Consider the following C struct declaration:

```
typedef struct {
  char a;
  long b;
  float c;
  char d[3];
  int *e;
  short *f;
} foo;
```

Rearrange the elements of foo to conserve the most space in memory. Label the bytes with the names of the various fields and clearly mark the end of the struct. Use an X to denote space that is allocated in the struct as padding.



Today

- Partial recap: Integers
 - Word size
 - Addresses
 - Endianness
- Arrays
 - One-dimensional
 - Multi-dimensional (nested)
 - Multi-level
- Structures
 - Allocation
 - Access
 - Alignment
- If we have time: Floating point and SIMD

Activity break: do part 2.3, 2.4, 2.5 now

Background

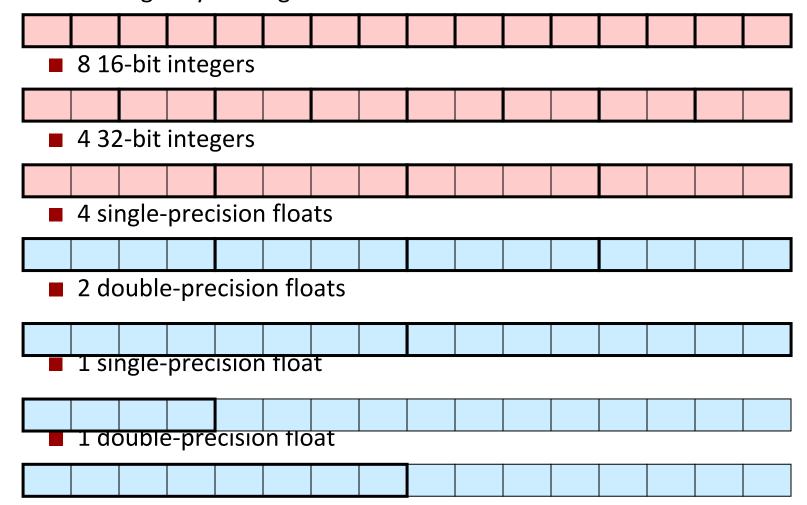
History

- x87 FP
 - Legacy, very ugly
- SSE FP
 - Supported by Shark machines
 - Special case use of vector instructions
- AVX FP
 - Newest version
 - Similar to SSE
 - Documented in book

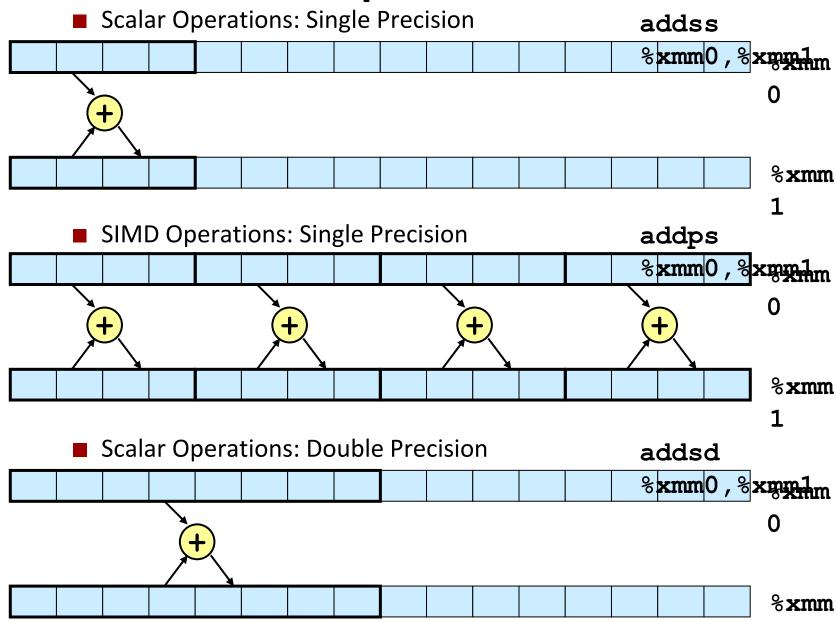
Programming with SSE3

XMM Registers

- 16 total, each 16 bytes
- 16 single-byte integers



Scalar & SIMD Operations



FP Basics

- Arguments passed in %xmm0, %xmm1, ...
- Result returned in %xmm0
- All XMM registers caller-saved

```
float fadd(float x, float y)
{
   return x + y;
}
```

```
double dadd(double x, double y)
{
    return x + y;
}
```

```
# x in %xmm0, y in %xmm1
addss %xmm1, %xmm0
ret
```

```
# x in %xmm0, y in %xmm1
addsd %xmm1, %xmm0
ret
```

FP Memory Referencing

- Integer (and pointer) arguments passed in regular registers
- FP values passed in XMM registers
- Different mov instructions to move between XMM registers, and between memory and XMM registers

```
double dincr(double *p, double v)
{
    double x = *p;
    *p = x + v;
    return x;
}
```

```
# p in %rdi, v in %xmm0
movapd %xmm0, %xmm1  # Copy v
movsd (%rdi), %xmm0  # x = *p
addsd %xmm0, %xmm1  # t = x + v
movsd %xmm1, (%rdi) # *p = t
ret
```

Other Aspects of FP Code

Lots of instructions

Different operations, different formats, ...

Floating-point comparisons

- Instructions ucomiss and ucomisd
- Set condition codes CF, ZF, and PF

Using constant values

- Set XMM0 register to 0 with instruction xorpd %xmm0, %xmm0
- Others loaded from memory

Summary

Arrays

- Elements packed into contiguous region of memory
- Use index arithmetic to locate individual elements

Structures

- Elements packed into single region of memory
- Access using offsets determined by compiler
- Possible require internal and external padding to ensure alignment

Combinations

Can nest structure and array code arbitrarily

Floating Point

Data held and operated on in XMM registers