FISF130020.01: Introduction to Computer Science

Lecture 1: Numbers and Computation

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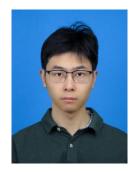
Outline

- 1. Course Introduction
- 2. Binary System
- 3. Computation
- 4. In-class Practice

1. Course Introduction

Instruction Team

- Instructor: Xu, Hui
 - Ph. D. degree from CUHK
 - Research Interests: program analysis, software reliability
 - Email: xuh@fudan.edu.cn
 - Office: Room D6023, X2 Building, Jiangwan Campus
- Tutors:



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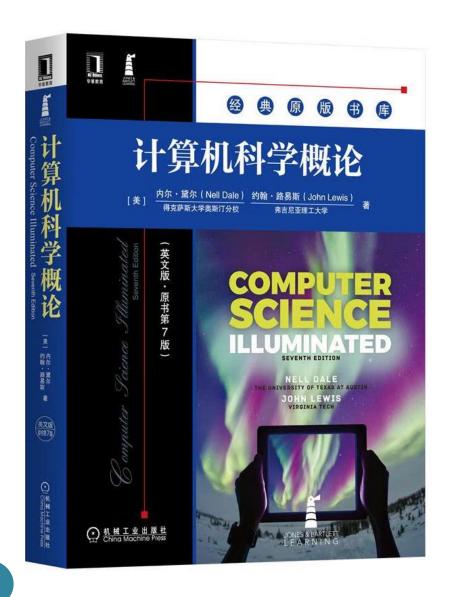
Course Objective

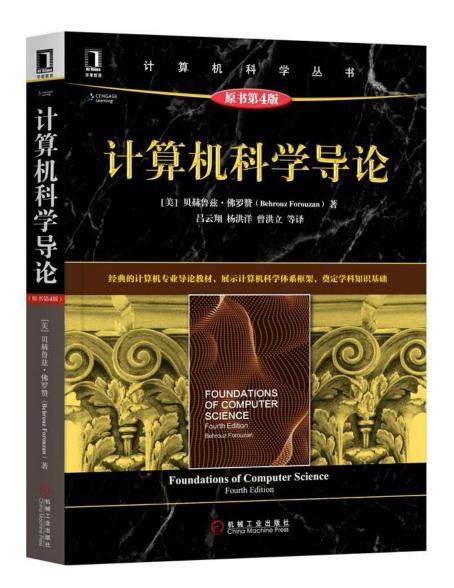
- Understand how computers work
- Learn to write simple algorithms
- Understand how real-world applications work
- Understand how artificial intelligence works
- Know common cybersecurity issues

Tentative Schedule

Week	Date	Course
1	Sep-5	Numbers and Computation
2	Sep-12	Data Structures
3	Sep-19	Algorithm I
4	Sep-26	Algorithm II
5	Oct-3	Holiday
6	Oct-10	Operating System I
7	Oct-17	Operating System II
8	Oct-24	Network I
9	Oct-31	Network II
10	Nov-7	Database
11	Nov-14	B/S Applications
12	Nov-21	C/S Applications
13	Nov-28	Cryptography
14	Dec-5	Cybersecurity
15	Dec-12	Artificial Intelligence I
16	Dec-19	Artificial Intelligence II

Reference Book: No Textbook Available





Course Information

- Time: Thursday 6:30pm 9:10pm
- Classroom: H6304
- Platform:
 - Couse Webpage: eLearning
 - Lecture notes
 - Assignment submission
 - Webpage: https://github.com/hxuhack/intro2cs
 - Notification & Discussion: WeChat Group

Grading

- In-Class Practice: 50%
 - Issued during the third class each week
 - Due one week later (before the class)
 - Any two practices can be waived (count n-2 best graded assignments)
- Final Exam: 50%
 - Closed book
 - Time: 2024-12-24 15:30~17:30

2. Binary System

All Data are Stored in Computers as Bits

- Natural Number
- Negative Integers
- Floating-point Numbers
- Text/Documents
- Multimedia
- Code
- Neural Networks
- ...

Representing Natural Numbers as Bits

Decimal	Binary	Hex
0	0	0
1	01	1
2	10	2
3	11	3
4	100	4
5	101	5
6	110	6
7	111	7
8	1000	8
9	1001	9
10	1010	Α
11	1011	В
12	1100	С
13	1101	D
14	1110	Е
15	1111	F
16	10000	10
•••	•••	•••

DES SCIENCES.

85

E X P L I C A T I O N DE L'ARITHMETIQUE B I N A I R E.

Qui se sert des seuls caracteres 0 & I; avec des Remarques sur son utilité, & sur ce qu'elle donne le sens des anciennes figures Chinoises de Fohy.

PAR M. LEIBNITZ.

E calcul ordinaire d'Arithmétique se fait suivant la progression de dix en dix. On se sert de dix caracteres, qui sont 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, qui signifient zero, un, & les nombres suivans jusqu'à neuf inclusivement. Et puis allant à dix, on recommence, & on écrit dix; par 10; & dix sois dix, ou cent, par 100; & dix sois cent, ou mille, par 1000; & dix sois mille, par 1000. Et ainsi de suite.

Mais au lieu de la progression de dix en dix, j'ai employé depuis plusieurs années la progression la plus simple de toutes, qui va de deux en deux; ayant trouvé qu'elle sert à la persection de la science des Nombres. Ainsi je n'y employe point d'autres caracteres que o & 1, & puis allant à deux, je recommence. C'est pourquoi deux s'écrit ici par 10, & deux fois deux ou quarre par 100; & deux sois quatre ou huit par 1000; & deux fois huit ou seize par 100000, & ainsi de suite. Voici la Table des Nombres de cette saçon, qu'on peut continuer tant que l'on voudra.

On voit ici d'un coup d'œil la raison d'une propriété sélébre de la progression Géométrique double en Nombres entiers, qui porte que si on n'a qu'un de ces nombres de chaque degré, on en peut composer tous les autres nom-L iij

1 703.

Question

- What is the binary representation for:
 - 100
 - 1024 (also known as 1 kilo)
- What is the decimal value of:
 - 1111 1111
 - 1 0000 0000 0000 0000 0000 (1 mega)
- More quantifiers:
 - 1 giga: 2³⁰
 - 1 tera: 2⁴⁰
 - 1 peta: 2⁵⁰
 - ...

Representing Negative Integers with Two's Complement

 Employ the leftmost bit as the sign k 	oit
---	-----

- 0 for positive numbers
- 1 for negative numbers
- Padding 0 or 1 to a fixed size, e.g., 4 bits
- Two's complement for negative numbers
 - Invert all the bits of the positive number
 - Add one

$$-(0001)_2 \xrightarrow{\text{invert}} 1110 \xrightarrow{\text{add 1}} \boxed{1111}$$

ecimal	Binary
-8	1000
-7	1001
-6	1010
-5	1011
-4	1100
-3	1101
-2	1110
-1	1111
0	0000
1	0001
2	0010
3	0011
4	0100
5	0101
6	0110
7	0111

Question

- What is the largest integer that 32 bits can represent?
- What is the smallest integer that 32 bits can represent?
- How to represent larger numbers in 32 bits?

Representing Floating-point Numbers with IEEE 754

- Meaning of bits for 32-bit single-precision floating-point numbers:
 - 32 (leftmost): sign bit
 - 24-31: exponent bits, to represent a wide range of values.
 - 1-23: mantissa bits
- Evaluation: $2^{exp} * mantissa$

0100001101001000000000000000000000

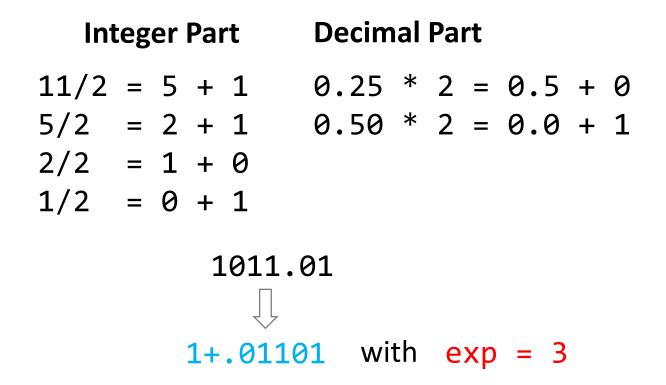
exponent (8 bits) mantissa (23 bits)
$$2^{7} + 2^{2} + 2^{1} - 127 \qquad 1 + 2^{-1} + 2^{-4}$$

$$= 7 \qquad = 1.5625$$

Why do we substract a bias 127?

 $2^7 * 1.5625 = 200$

Convert Numbers to Floating-point Representation



Question

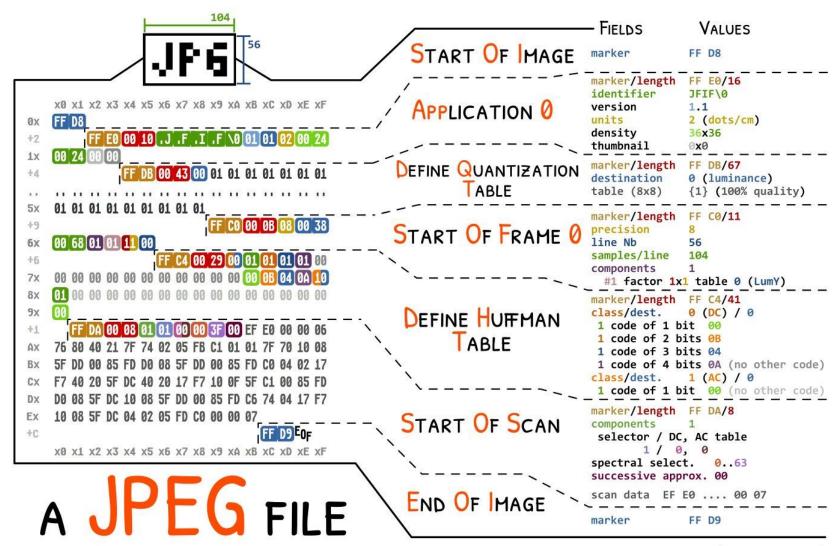
- Which of the following numbers can be represented by floatingpoint numbers without precision loss?
 - 0.1
 - 0.2
 - 0.3
 - 0.4
 - 0.5

Encoding Characters in Bits (as Bytes)

- ASCII (American Standard Code for Information Interchange)
- 1 byte = 8 bits, or 1 B = 8 b

	0	1	2	3	4	5	6	7	8	9	Α	В	С	D	Ε	F
0x	NUL	SOH	STX	ETX	EOT	ENQ	ACK	BEL	BS	НТ	LF	VT	FF	CR	SO	SI
1x	DLE	DC1	DC2	DC3	DC4	NAK	SYN	ETB	CAN	EM	SUB	ESC	FS	GS	RS	US
2x	SP	!	11	#	\$	%	&	! -	()	*	+	,	-		/
3x	0	1	2	3	4	5	6	7	8	9	:	;	<	=	>	?
4x	@	Α	В	С	D	Е	F	<u>G</u>	Н	1	J	K	L	M	N	0
5x	Р	Q	R	S	Т	U	V	W	Χ	Υ	Z	[\]	٨	_
6x	`	a	b	С	d	е	f	g	h	i	j	k	T	m	n	0
7x	p	q	r	S	t	u	V	W	X	У	Z	{		}	~	DEL

Images

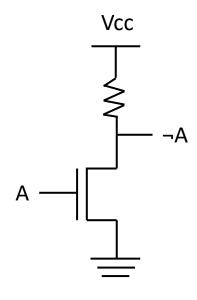


3. Computation

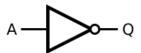
High-level Idea

- Compose logic gates based on transistors
- Compose artithmatic computation units based on logic gates
- Manufacture CPUs with ALU, control unit, etc.
- Build computers with CPU, memory, input, and output

Transistor => Logical Gates: NOT



Simplified Representation:



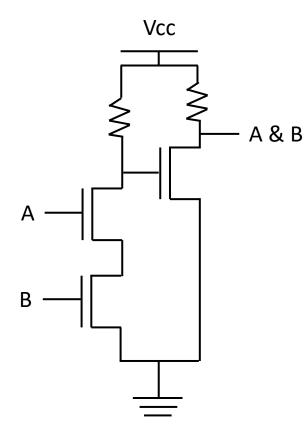
Operator Symbol: -

Truth Table:

A	¬ A
0	1
1	0

NMOS NOT

Transistor => Logical Gates: AND



Simplified Representation:

 $A \longrightarrow Q$

Operator Symbol: 8

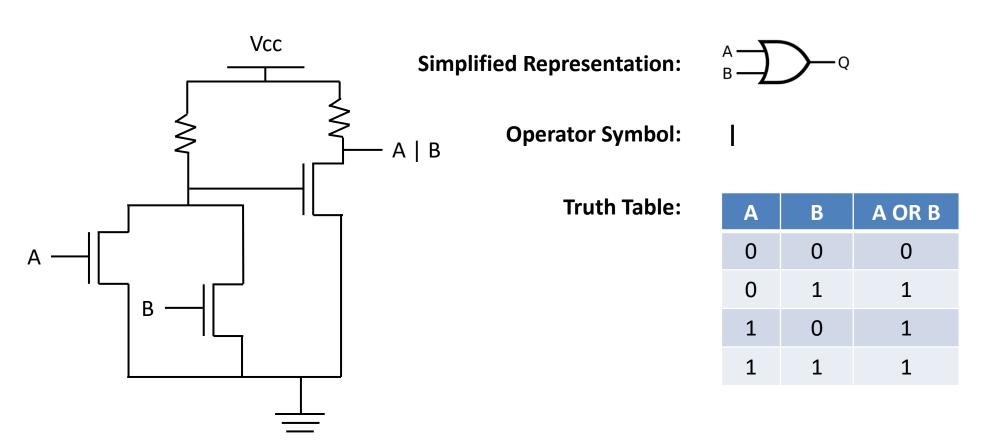
&

Truth Table:

A	В	A & B
0	0	0
0	1	0
1	0	0
1	1	1

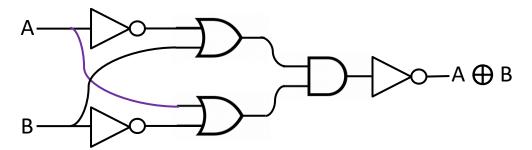
NMOS AND

Transistor => Logical Gates: OR



NMOS OR

Logical Gates: XOR



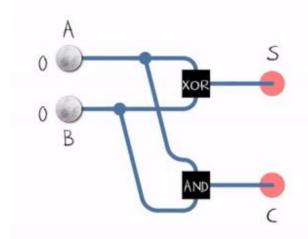
Simplified Representation: A D O

Operator Symbol:

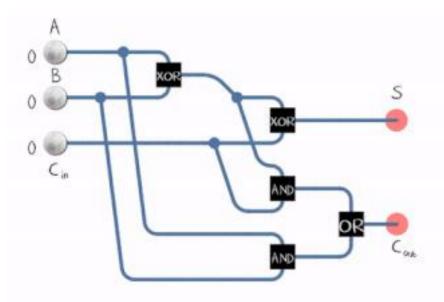
Truth Table:

Α	В	A ⊕ B
0	0	0
0	1	1
1	0	1
1	1	0

Combinational Circuits: Adder



Half Adder

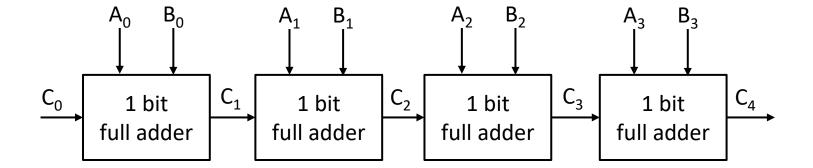


Full Adder (with carrier input)

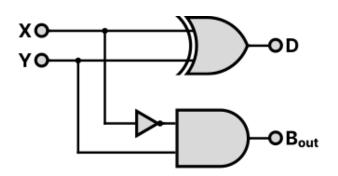
Inputs	5	Outputs		
Α	В	$\mathbf{C}_{\mathrm{out}}$	S	
0	0	0	0	
0	1	0	1	
1	0	0	1	
1	1	1	0	

Inpu	ts		Outp	uts
Α	В	\mathbf{C}_{in}	$\mathbf{C}_{\mathrm{out}}$	S
0	0	0	0	0
0	0	1	0	1
0	1	0	0	1
0	1	1	1	0
1	0	0	0	1
1	0	1	1	0
1	1	0	1	0
1	1	1	1	1

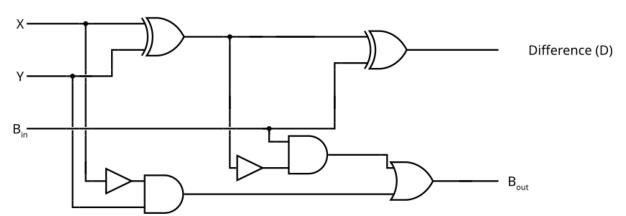
Add 4-bits with Full Adder



Combinational Circuits: Subtractor



Half Subtractor



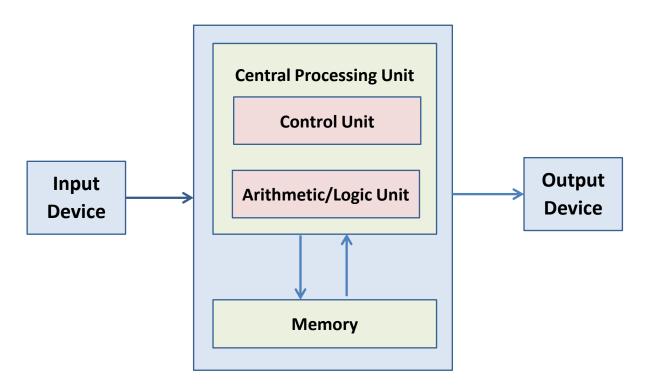
Full Subtractor

Inputs		Outputs		
Χ	Υ	D	B _{out}	
0	0	0	0	
0	1	1	1	
1	0	1	0	
1	1	0	0	

Inputs			Outputs		
X	Υ	B_{in}	D	B_out	
0	0	0	0	0	
0	0	1	1	1	
0	1	0	1	1	
0	1	1	0	1	
1	0	0	1	0	
1	0	1	0	0	
1	1	0	0	0	
1	1	1	1	1	

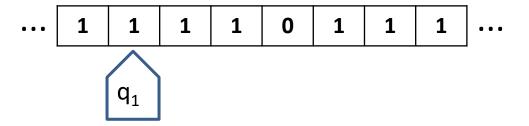
Von Neumann Model (an implementation of Turing Maching)

- Control unit: fetch instructions from memory at the address specified by the program counter.
- ALU: performs the operation specified by the instruction, write the results to memory or registers.



Turing machine

- Infinite tape: composed on 0/1s
- Head: read/write symbos
- State register: finite number of values
- Table of instructions



	0	1
q_1	1 R q ₂	1 R q ₁
q_2	0 L q ₃	1 R q ₂
q_3	0 H q ₃	$0 H q_3$

230 A. M. Turing [Nov. 12,

ON COMPUTABLE NUMBERS, WITH AN APPLICATION TO THE ENTSCHEIDUNGSPROBLEM

By A. M. TURING.

[Received 28 May, 1936.—Read 12 November, 1936.]

The "computable" numbers may be described briefly as the real numbers whose expressions as a decimal are calculable by finite means. Although the subject of this paper is ostensibly the computable numbers it is almost equally easy to define and investigate computable functions of an integral variable or a real or computable variable, computable predicates, and so forth. The fundamental problems involved are, however, the same in each case, and I have chosen the computable numbers for explicit treatment as involving the least cumbrous technique. I hope shortly to give an account of the relations of the computable numbers, functions, and so forth to one another. This will include a development of the theory of functions of a real variable expressed in terms of computable numbers. According to my definition, a number is computable if its decimal can be written down by a machine.

In §§ 9. 10 I give some arguments with the intention of showing that the computable numbers include all numbers which could naturally be regarded as computable. In particular, I show that certain large classes of numbers are computable. They include, for instance, the real parts of all algebraic numbers, the real parts of the zeros of the Bessel functions. the numbers π , e, etc. The computable numbers do not, however, include all definable numbers, and an example is given of a definable number which is not computable.

Although the class of computable numbers is so great, and in many ways similar to the class of real numbers, it is nevertheless enumerable. In §8 I examine certain arguments which would seem to prove the contrary. By the correct application of one of these arguments, conclusions are reached which are superficially similar to those of Gödel†. These results

[†] Gödel, "Über formal unentscheidhare Sätze der Principia Mathematica und verwandter Systeme, I", Monatshefte Math. Phys., 38 (1931), 173-193.

Summary

- All data are stored in computers as bits
 - Integers => negative integers => floating-point numbers => files
- Computers are made of transistors that accept bit inputs
 - Transistors => logic gates => arithmatic units => CPU => computer

4. In-class Practice

Setup Rust Programming Environment

- 1) Install Rust
 - https://www.rust-lang.org/tools/install
- 2) Or use the web version
 - https://play.rust-lang.org/

Option 1: Analyze Floating-point Number

- 1) Write a program that output the bits of a floating-point number;
- Interpret the bit representation;

```
fn main() {
    let number: f32 = 200.1;
    let bits = number.to_bits();
    println!("Bit representation of {}: {:032b}", number, bits);
}
```

Option 1: Analyze Floating-point Number

3) Write a program that evaluate the bits of a floating-point number.

```
use std::num::ParseIntError;
fn bits_to_f32(bits: &str) -> Result<f32, ParseIntError> {
   let int value = u32::from str radix(bits, 2)?;
   let float value = f32::from bits(int value);
   Ok(float value)
fn main() {
   match bits to f32(bit sequence) {
       Ok(float) => println!("The f32 value is: {}", float),
       Err(e) => println!("Failed to parse bit sequence: {}", e),
```

Option 2: Analyze Files

- 1) Change the file path of the following program and execute it;
- Try to interpret the output;
- 3) Modify the output and create a new jpg file.
 - e.g., via hex editor tools like https://hexed.it/

```
use std::fs::File;
use std::io::{self, Read};
fn main() -> io::Result<()> {
    let mut file = File::open("/home/aisr/john.jpg")?;
    let mut buffer = Vec::new();
    file.read_to_end(&mut buffer)?;
    for byte in buffer {
        print!("{:02x} ", byte); // Prints in hexadecimal format
   0k(())
```