

Target equation:

$$\begin{aligned}
& -ia_1u^{(1,0)}(x,t)+a_{10}u^{(10,0)}(x,t)-ia_{11}u^{(11,0)}(x,t)+a_{12}u^{(12,0)}(x,t)-ia_{13}u^{(13,0)}(x,t)+a_{14}u^{(14,0)}(x,t)- \\
& ia_{15}u^{(15,0)}(x,t)+a_{16}u^{(16,0)}(x,t)-ia_{17}u^{(17,0)}(x,t)+a_{18}u^{(18,0)}(x,t)+a_2u^{(2,0)}(x,t)-ia_3u^{(3,0)}(x,t)+ \\
& a_4u^{(4,0)}(x,t)-ia_5u^{(5,0)}(x,t)+a_6u^{(6,0)}(x,t)-ia_7u^{(7,0)}(x,t)+a_8u^{(8,0)}(x,t)-ia_9u^{(9,0)}(x,t)-bu(x,t)|u(x,t)|^2+ \\
& iu^{(0,1)}(x,t)=0
\end{aligned}$$

Substitutions:

$$\begin{aligned} N &= 9 \\ u(x, t) &\rightarrow y(z)e^{i(kx - \omega t)} \\ z &\rightarrow x - C_0 t \\ y(z) &\rightarrow AR(z)^9 \\ R'(z)^2 &= R(z)^2(1 - \chi R(z)^2) \end{aligned}$$

Imaginary part of equation after substitutions:

$$\begin{aligned}
& y'(z) (a_1 + k (k (k (k (k (k (-10a_{10}k - 11a_{11}k^2 + 12a_{12}k^3 + 13a_{13}k^4 - 14a_{14}k^5 - 15a_{15}k^6 + 16a_{16}k^7 + 17a_{17}k^8 \\
& y^{(3)}(z) (k (k (k (k (k (k (120a_{10}k + 165a_{11}k^2 - 220a_{12}k^3 - 286a_{13}k^4 + 364a_{14}k^5 + 455a_{15}k^6 - 560a_{16}k^7 - 680a_{17}k^8 \\
& 252a_{10}k^5y^{(5)}(z)+120a_{10}k^3y^{(7)}(z)-10a_{10}ky^{(9)}(z)-462a_{11}k^6y^{(5)}(z)+330a_{11}k^4y^{(7)}(z)-55a_{11}k^2y^{(9)}(z)+\blacksquare \\
& a_{11}y^{(11)}(z)+792a_{12}k^7y^{(5)}(z)-792a_{12}k^5y^{(7)}(z)+220a_{12}k^3y^{(9)}(z)-12a_{12}ky^{(11)}(z)+1287a_{13}k^8y^{(5)}(z)-\blacksquare \\
& 1716a_{13}k^6y^{(7)}(z)+715a_{13}k^4y^{(9)}(z)-78a_{13}k^2y^{(11)}(z)+a_{13}y^{(13)}(z)-2002a_{14}k^9y^{(5)}(z)+3432a_{14}k^7y^{(7)}(z)-\blacksquare \\
& 2002a_{14}k^5y^{(9)}(z) + 364a_{14}k^3y^{(11)}(z) - 14a_{14}ky^{(13)}(z) - 3003a_{15}k^{10}y^{(5)}(z) + 6435a_{15}k^8y^{(7)}(z) - \\
& 5005a_{15}k^6y^{(9)}(z)+1365a_{15}k^4y^{(11)}(z)-105a_{15}k^2y^{(13)}(z)+a_{15}y^{(15)}(z)+4368a_{16}k^{11}y^{(5)}(z)-11440a_{16}k^9y^{(7)}(z)+\blacksquare \\
& 11440a_{16}k^7y^{(9)}(z) - 4368a_{16}k^5y^{(11)}(z) + 560a_{16}k^3y^{(13)}(z) - 16a_{16}ky^{(15)}(z) + 6188a_{17}k^{12}y^{(5)}(z) - \\
& 19448a_{17}k^{10}y^{(7)}(z)+24310a_{17}k^8y^{(9)}(z)-12376a_{17}k^6y^{(11)}(z)+2380a_{17}k^4y^{(13)}(z)-136a_{17}k^2y^{(15)}(z)+\blacksquare \\
& a_{17}y^{(17)}(z) - 8568a_{18}k^{13}y^{(5)}(z) + 31824a_{18}k^{11}y^{(7)}(z) - 48620a_{18}k^9y^{(9)}(z) + 31824a_{18}k^7y^{(11)}(z) - \\
& 8568a_{18}k^5y^{(13)}(z) + 816a_{18}k^3y^{(15)}(z) - 18a_{18}ky^{(17)}(z) + a_5y^{(5)}(z) - 6a_6ky^{(5)}(z) - 21a_7k^2y^{(5)}(z) + \\
& a_7y^{(7)}(z) + 56a_8k^3y^{(5)}(z) - 8a_8ky^{(7)}(z) + 126a_9k^4y^{(5)}(z) - 36a_9k^2y^{(7)}(z) + a_9y^{(9)}(z) = 0
\end{aligned}$$

Real part of equation after substitutions:

$$\begin{aligned} & -3060a_{18}y^{(4)}(z)k^{14}+2380a_{17}y^{(4)}(z)k^{13}+1820a_{16}y^{(4)}(z)k^{12}+18564a_{18}y^{(6)}(z)k^{12}-1365a_{15}y^{(4)}(z)k^{11}- \\ & 12376a_{17}y^{(6)}(z)k^{11}-1001a_{14}y^{(4)}(z)k^{10}-8008a_{16}y^{(6)}(z)k^{10}-43758a_{18}y^{(8)}(z)k^{10}+715a_{13}y^{(4)}(z)k^9+ \\ & 5005a_{15}y^{(6)}(z)k^9+24310a_{17}y^{(8)}(z)k^9+495a_{12}y^{(4)}(z)k^8+3003a_{14}y^{(6)}(z)k^8+12870a_{16}y^{(8)}(z)k^8+ \\ & 43758a_{18}y^{(10)}(z)k^8-330a_{11}y^{(4)}(z)k^7-1716a_{13}y^{(6)}(z)k^7-6435a_{15}y^{(8)}(z)k^7-19448a_{17}y^{(10)}(z)k^7- \\ & 210a_{10}y^{(4)}(z)k^6-924a_{12}y^{(6)}(z)k^6-3003a_{14}y^{(8)}(z)k^6-8008a_{16}y^{(10)}(z)k^6-18564a_{18}y^{(12)}(z)k^6+ \\ & 126a_9y^{(4)}(z)k^5+462a_{11}y^{(6)}(z)k^5+1287a_{13}y^{(8)}(z)k^5+3003a_{15}y^{(10)}(z)k^5+6188a_{17}y^{(12)}(z)k^5+ \\ & 70a_8y^{(4)}(z)k^4+210a_{10}y^{(6)}(z)k^4+495a_{12}y^{(8)}(z)k^4+1001a_{14}y^{(10)}(z)k^4+1820a_{16}y^{(12)}(z)k^4+3060a_{18}y^{(14)}(z)k^4- \\ & 35a_7y^{(4)}(z)k^3-84a_9y^{(6)}(z)k^3-165a_{11}y^{(8)}(z)k^3-286a_{13}y^{(10)}(z)k^3-455a_{15}y^{(12)}(z)k^3-680a_{17}y^{(14)}(z)k^3- \\ & 15a_6y^{(4)}(z)k^2-28a_8y^{(6)}(z)k^2-45a_{10}y^{(8)}(z)k^2-66a_{12}y^{(10)}(z)k^2-91a_{14}y^{(12)}(z)k^2-120a_{16}y^{(14)}(z)k^2- \end{aligned}$$

$$153a_{18}y^{(16)}(z)k^2 + 5a_5y^{(4)}(z)k + 7a_7y^{(6)}(z)k + 9a_9y^{(8)}(z)k + 11a_{11}y^{(10)}(z)k + 13a_{13}y^{(12)}(z)k + 15a_{15}y^{(14)}(z)k + 17a_{17}y^{(16)}(z)k - by(z)^3 + (-a_{18}k^{18} + a_{17}k^{17} + a_{16}k^{16} - a_{15}k^{15} - a_{14}k^{14} + a_{13}k^{13} + a_{12}k^{12} - a_{11}k^{11} - a_{10}k^{10} - a_9k^9 - a_8k^8 - a_7k^7 - a_6k^6 - a_5k^5 - a_4k^4 - a_3k^3 - a_2k^2 - a_1k) = 0$$

Constraints on coefficients from imaginary part of equation:

$$a_{17} \rightarrow 18a_{18}k$$

$$a_{15} \rightarrow 16a_{16}k + 1632a_{18}k^3$$

$$a_{13} \rightarrow 14a_{14}k + 1120a_{16}k^3 + 137088a_{18}k^5$$

$$a_{11} \rightarrow 12a_{12}k + 728a_{14}k^3 + 69888a_{16}k^5 + 8656128a_{18}k^7$$

$$a_9 \rightarrow 10a_{10}k + 440a_{12}k^3 + 32032a_{14}k^5 + 3111680a_{16}k^7 + 385848320a_{18}k^9$$

$$a_7 \rightarrow 240a_{10}k^3 + 12672a_{12}k^5 + 933504a_{14}k^7 + 90787840a_{16}k^9 + 11259076608a_{18}k^{11} + 8a_8k$$

$$a_5 \rightarrow 4032a_{10}k^5 + 215424a_{12}k^7 + 15887872a_{14}k^9 + 1545363456a_{16}k^{11} + 191651217408a_{18}k^{13} + 6a_6k + 112a_8k^3$$

$$a_3 \rightarrow 32640a_{10}k^7 + 1745920a_{12}k^9 + 128780288a_{14}k^{11} + 12526223360a_{16}k^{13} + 1553465966592a_{18}k^{15} + 4a_4k + 40a_6k^3 + 896a_8k^5$$

$$C_0 \rightarrow a_1 - 79360a_{10}k^9 - 4245504a_{12}k^{11} - 313155584a_{14}k^{13} - 30460116992a_{16}k^{15} - 3777576173568a_{18}k^{17} - 2a_2k - 8a_4k^3 - 96a_6k^5 - 2176a_8k^7$$

Constraints on coefficients from real part of equation:

$$b \rightarrow -\frac{10002268381116211200000a_{18}\chi^9}{A^2}$$

$$a_{16} \rightarrow -153a_{18}k^2 - 2841a_{18}$$

$$a_{14} \rightarrow 3060a_{18}k^4 + 340920a_{18}k^2 + 3446052a_{18}$$

$$a_{12} \rightarrow -18564a_{18}k^6 - 5170620a_{18}k^4 - 313590732a_{18}k^2 - 2335946132a_{18}$$

$$a_{10} \rightarrow 43758a_{18}k^8 + 22750728a_{18}k^6 + 3449498052a_{18}k^4 + 154172444712a_{18}k^2 + 972321096318a_{18}$$

$$a_8 \rightarrow -43758a_{18}k^{10} - 36563670a_{18}k^8 - 10348494156a_{18}k^6 - 1156293335340a_{18}k^4 - 43754449334310a_{18}k^2 - 256907539334238a_{18}$$

$$a_6 \rightarrow 18564a_{18}k^{12} + 22750728a_{18}k^{10} + 10348494156a_{18}k^8 + 2158414225968a_{18}k^6 + 204187430226780a_{18}k^4 + 7193411101358664a_{18}k^2 + 42942368606859604a_{18}$$

$$a_4 \rightarrow -3060a_{18}k^{14} - 5170620a_{18}k^{12} - 3449498052a_{18}k^{10} - 1156293335340a_{18}k^8 - 204187430226780a_{18}k^6 - 17983527753396660a_{18}k^4 - 644135529102894060a_{18}k^2 - 4362858052479448164a_{18}$$

$$a_2 \rightarrow 153a_{18}k^{16} + 340920a_{18}k^{14} + 313590732a_{18}k^{12} + 154172444712a_{18}k^{10} + 43754449334310a_{18}k^8 +$$

$$7193411101358664a_{18}k^6 + 644135529102894060a_{18}k^4 + 26177148314876688984a_{18}k^2 + 24354706537150319002$$

$$\omega \rightarrow -a_1k + 17a_{18}k^{18} + 42615a_{18}k^{16} + 44798676a_{18}k^{14} + 25695407452a_{18}k^{12} + 8750889866862a_{18}k^{10} +$$

$$1798352775339666a_{18}k^8 + 214711843034298020a_{18}k^6 + 13088574157438344492a_{18}k^4 + 24354706537150319002$$

y(z) - function:

$$\frac{262144a^9A}{(4a^2e^z + \chi e^{-z})^9}$$

u(x, t) - function:

$$\frac{262144a^9Ae^{i(kx-\omega t)}}{(4a^2e^{C_0t+x} + \chi e^{-C_0t-x})^9}$$