

Target equation:

$$-ia_1u^{(1,0)}(x,t)+a_{10}u^{(10,0)}(x,t)-ia_{11}u^{(11,0)}(x,t)+a_{12}u^{(12,0)}(x,t)-ia_{13}u^{(13,0)}(x,t)+a_{14}u^{(14,0)}(x,t)-ia_{15}u^{(15,0)}(x,t)+a_{16}u^{(16,0)}(x,t)-ia_{17}u^{(17,0)}(x,t)+a_{18}u^{(18,0)}(x,t)-ia_{19}u^{(19,0)}(x,t)+a_2u^{(2,0)}(x,t)+a_{20}u^{(20,0)}(x,t)-ia_3u^{(3,0)}(x,t)+a_4u^{(4,0)}(x,t)-ia_5u^{(5,0)}(x,t)+a_6u^{(6,0)}(x,t)-ia_7u^{(7,0)}(x,t)+a_8u^{(8,0)}(x,t)-ia_9u^{(9,0)}(x,t)-bu(x,t)|u(x,t)|^2+iu^{(0,1)}(x,t)=0$$

Substitutions:

$$N = 10$$

$$u(x,t) \rightarrow y(z)e^{i(kx-\omega t)}$$

$$z \rightarrow x - C_0t$$

$$y(z) \rightarrow AR(z)^{10}$$

$$R'(z)^2 = R(z)^2 (1 - \chi R(z)^2)$$

Imaginary part of equation after substitutions:

$$\begin{aligned} &15504a_{20}y^{(5)}(z)k^{15}-11628a_{19}y^{(5)}(z)k^{14}-8568a_{18}y^{(5)}(z)k^{13}-77520a_{20}y^{(7)}(z)k^{13}+6188a_{17}y^{(5)}(z)k^{12}+ \\ &50388a_{19}y^{(7)}(z)k^{12}+4368a_{16}y^{(5)}(z)k^{11}+31824a_{18}y^{(7)}(z)k^{11}+167960a_{20}y^{(9)}(z)k^{11}-3003a_{15}y^{(5)}(z)k^{10}- \\ &19448a_{17}y^{(7)}(z)k^{10}-92378a_{19}y^{(9)}(z)k^{10}-2002a_{14}y^{(5)}(z)k^9-11440a_{16}y^{(7)}(z)k^9-48620a_{18}y^{(9)}(z)k^9- \\ &167960a_{20}y^{(11)}(z)k^9+1287a_{13}y^{(5)}(z)k^8+6435a_{15}y^{(7)}(z)k^8+24310a_{17}y^{(9)}(z)k^8+75582a_{19}y^{(11)}(z)k^8+ \\ &792a_{12}y^{(5)}(z)k^7+3432a_{14}y^{(7)}(z)k^7+11440a_{16}y^{(9)}(z)k^7+31824a_{18}y^{(11)}(z)k^7+77520a_{20}y^{(13)}(z)k^7- \\ &462a_{11}y^{(5)}(z)k^6-1716a_{13}y^{(7)}(z)k^6-5005a_{15}y^{(9)}(z)k^6-12376a_{17}y^{(11)}(z)k^6-27132a_{19}y^{(13)}(z)k^6- \\ &252a_{10}y^{(5)}(z)k^5-792a_{12}y^{(7)}(z)k^5-2002a_{14}y^{(9)}(z)k^5-4368a_{16}y^{(11)}(z)k^5-8568a_{18}y^{(13)}(z)k^5- \\ &15504a_{20}y^{(15)}(z)k^5+126a_9y^{(5)}(z)k^4+330a_{11}y^{(7)}(z)k^4+715a_{13}y^{(9)}(z)k^4+1365a_{15}y^{(11)}(z)k^4+ \\ &2380a_{17}y^{(13)}(z)k^4+3876a_{19}y^{(15)}(z)k^4+56a_8y^{(5)}(z)k^3+120a_{10}y^{(7)}(z)k^3+220a_{12}y^{(9)}(z)k^3+364a_{14}y^{(11)}(z)k^3+ \\ &560a_{16}y^{(13)}(z)k^3+816a_{18}y^{(15)}(z)k^3+1140a_{20}y^{(17)}(z)k^3-21a_7y^{(5)}(z)k^2-36a_9y^{(7)}(z)k^2-55a_{11}y^{(9)}(z)k^2- \\ &78a_{13}y^{(11)}(z)k^2-105a_{15}y^{(13)}(z)k^2-136a_{17}y^{(15)}(z)k^2-171a_{19}y^{(17)}(z)k^2-6a_6y^{(5)}(z)k-8a_8y^{(7)}(z)k- \\ &10a_{10}y^{(9)}(z)k-12a_{12}y^{(11)}(z)k-14a_{14}y^{(13)}(z)k-16a_{16}y^{(15)}(z)k-18a_{18}y^{(17)}(z)k-20a_{20}y^{(19)}(z)k+ \\ &(a_1 - C_0 + k(k(4a_4 + k(5a_5 + k(k(8a_8 + k(9a_9 + k(k(20a_{20}k^9 - 19a_{19}k^8 - 18a_{18}k^7 + 17a_{17}k^6 + 16a_{16}k^5 - \\ &(a_3 + k(k(k(20a_6 + k(35a_7 + k(k(k(120a_{10} + k(-1140a_{20}k^9 + 969a_{19}k^8 + 816a_{18}k^7 - 680a_{17}k^6 - 560a_{16}k^5 - \\ &a_5y^{(5)}(z)+a_7y^{(7)}(z)+a_9y^{(9)}(z)+a_{11}y^{(11)}(z)+a_{13}y^{(13)}(z)+a_{15}y^{(15)}(z)+a_{17}y^{(17)}(z)+a_{19}y^{(19)}(z)=0 \end{aligned}$$

Real part of equation after substitutions:

$$\begin{aligned} &4845a_{20}y^{(4)}(z)k^{16}-3876a_{19}y^{(4)}(z)k^{15}-3060a_{18}y^{(4)}(z)k^{14}-38760a_{20}y^{(6)}(z)k^{14}+2380a_{17}y^{(4)}(z)k^{13}+ \\ &27132a_{19}y^{(6)}(z)k^{13}+1820a_{16}y^{(4)}(z)k^{12}+18564a_{18}y^{(6)}(z)k^{12}+125970a_{20}y^{(8)}(z)k^{12}-1365a_{15}y^{(4)}(z)k^{11}- \\ &12376a_{17}y^{(6)}(z)k^{11}-75582a_{19}y^{(8)}(z)k^{11}-1001a_{14}y^{(4)}(z)k^{10}-8008a_{16}y^{(6)}(z)k^{10}-43758a_{18}y^{(8)}(z)k^{10}- \\ &184756a_{20}y^{(10)}(z)k^{10}+715a_{13}y^{(4)}(z)k^9+5005a_{15}y^{(6)}(z)k^9+24310a_{17}y^{(8)}(z)k^9+92378a_{19}y^{(10)}(z)k^9+ \\ &495a_{12}y^{(4)}(z)k^8+3003a_{14}y^{(6)}(z)k^8+12870a_{16}y^{(8)}(z)k^8+43758a_{18}y^{(10)}(z)k^8+125970a_{20}y^{(12)}(z)k^8- \\ &330a_{11}y^{(4)}(z)k^7-1716a_{13}y^{(6)}(z)k^7-6435a_{15}y^{(8)}(z)k^7-19448a_{17}y^{(10)}(z)k^7-50388a_{19}y^{(12)}(z)k^7- \end{aligned}$$

$$\begin{aligned}
& 210a_{10}y^{(4)}(z)k^6 - 924a_{12}y^{(6)}(z)k^6 - 3003a_{14}y^{(8)}(z)k^6 - 8008a_{16}y^{(10)}(z)k^6 - 18564a_{18}y^{(12)}(z)k^6 - \\
& 38760a_{20}y^{(14)}(z)k^6 + 126a_9y^{(4)}(z)k^5 + 462a_{11}y^{(6)}(z)k^5 + 1287a_{13}y^{(8)}(z)k^5 + 3003a_{15}y^{(10)}(z)k^5 + \\
& 6188a_{17}y^{(12)}(z)k^5 + 11628a_{19}y^{(14)}(z)k^5 + 70a_8y^{(4)}(z)k^4 + 210a_{10}y^{(6)}(z)k^4 + 495a_{12}y^{(8)}(z)k^4 + \\
& 1001a_{14}y^{(10)}(z)k^4 + 1820a_{16}y^{(12)}(z)k^4 + 3060a_{18}y^{(14)}(z)k^4 + 4845a_{20}y^{(16)}(z)k^4 - 35a_7y^{(4)}(z)k^3 - \\
& 84a_9y^{(6)}(z)k^3 - 165a_{11}y^{(8)}(z)k^3 - 286a_{13}y^{(10)}(z)k^3 - 455a_{15}y^{(12)}(z)k^3 - 680a_{17}y^{(14)}(z)k^3 - 969a_{19}y^{(16)}(z)k^3 - \\
& 15a_6y^{(4)}(z)k^2 - 28a_8y^{(6)}(z)k^2 - 45a_{10}y^{(8)}(z)k^2 - 66a_{12}y^{(10)}(z)k^2 - 91a_{14}y^{(12)}(z)k^2 - 120a_{16}y^{(14)}(z)k^2 - \\
& 153a_{18}y^{(16)}(z)k^2 - 190a_{20}y^{(18)}(z)k^2 + 5a_5y^{(4)}(z)k + 7a_7y^{(6)}(z)k + 9a_9y^{(8)}(z)k + 11a_{11}y^{(10)}(z)k + \\
& 13a_{13}y^{(12)}(z)k + 15a_{15}y^{(14)}(z)k + 17a_{17}y^{(16)}(z)k + 19a_{19}y^{(18)}(z)k - by(z)^3 + (a_{20}k^{20} - a_{19}k^{19} - a_{18}k^{18} + a_{17}k^{17} + \\
& (a_2 + k(3a_3 + k(k(15a_6 + k(21a_7 + k(k(45a_{10} + k(-190a_{20}k^9 + 171a_{19}k^8 + 153a_{18}k^7 - 136a_{17}k^6 - \\
& a_4y^{(4)}(z) + a_6y^{(6)}(z) + a_8y^{(8)}(z) + a_{10}y^{(10)}(z) + a_{12}y^{(12)}(z) + a_{14}y^{(14)}(z) + a_{16}y^{(16)}(z) + a_{18}y^{(18)}(z) + \\
& a_{20}y^{(20)}(z) = 0
\end{aligned}$$

Constraints on coefficients from imaginary part of equation:

$$\begin{aligned}
a_{19} &\rightarrow 20a_{20}k \\
a_{17} &\rightarrow 6(3a_{18}k + 380a_{20}k^3) \\
a_{15} &\rightarrow 16(a_{16}k + 102a_{18}k^3 + 15504a_{20}k^5) \\
a_{13} &\rightarrow 2(7a_{14}k + 560a_{16}k^3 + 68544a_{18}k^5 + 10542720a_{20}k^7) \\
a_{11} &\rightarrow 4(3a_{12}k + 182a_{14}k^3 + 17472a_{16}k^5 + 2164032a_{18}k^7 + 333232640a_{20}k^9) \\
a_9 &\rightarrow 2(5a_{10}k + 220a_{12}k^3 + 16016a_{14}k^5 + 1555840a_{16}k^7 + 192924160a_{18}k^9 + 29711452160a_{20}k^{11}) \\
a_7 &\rightarrow 8(30a_{10}k^3 + 1584a_{12}k^5 + 116688a_{14}k^7 + 11348480a_{16}k^9 + 1407384576a_{18}k^{11} + 216748400640a_{20}k^{13} + \\
a_5 &\rightarrow 2(2016a_{10}k^5 + 107712a_{12}k^7 + 7943936a_{14}k^9 + 772681728a_{16}k^{11} + 95825608704a_{18}k^{13} + 147579266820 \\
a_3 &\rightarrow 4k(8160a_{10}k^6 + 436480a_{12}k^8 + 32195072a_{14}k^{10} + 3131555840a_{16}k^{12} + 388366491648a_{18}k^{14} + 5981162 \\
C0 &\rightarrow a_1 - 79360a_{10}k^9 - 4245504a_{12}k^{11} - 313155584a_{14}k^{13} - 30460116992a_{16}k^{15} - 3777576173568a_{18}k^{17} - \\
& 2a_2k - 581777702256640a_{20}k^{19} - 8a_4k^3 - 96a_6k^5 - 2176a_8k^7
\end{aligned}$$

Constraints on coefficients from real part of equation:

$$\begin{aligned}
b &\rightarrow \frac{24365525776399090483200000a_{20}\chi^{10}}{A^2} \\
a_{18} &\rightarrow -10a_{20}(19k^2 + 394) \\
a_{16} &\rightarrow 3(1615a_{20}k^4 + 200940a_{20}k^2 + 2247712a_{20}) \\
a_{14} &\rightarrow -40(969a_{20}k^6 + 301410a_{20}k^4 + 20229408a_{20}k^2 + 164687312a_{20}) \\
a_{12} &\rightarrow 26(4845a_{20}k^8 + 2813160a_{20}k^6 + 472019520a_{20}k^4 + 23056223680a_{20}k^2 + 156108843136a_{20}) \\
a_{10} &\rightarrow -52(3553a_{20}k^{10} + 3315510a_{20}k^8 + 1038442944a_{20}k^6 + 126809230240a_{20}k^4 + 5151591823488a_{20}k^2 + \\
a_8 &\rightarrow 2(62985a_{20}k^{12} + 86203260a_{20}k^{10} + 43392080160a_{20}k^8 + 9891119958720a_{20}k^6 + 1004560405580160a_{20}k^4 + \\
a_6 &\rightarrow -8(4845a_{20}k^{14} + 9142770a_{20}k^{12} + 6749879136a_{20}k^{10} + 2472779989680a_{20}k^8 + 468794855937408a_{20}k^6 + \\
a_4 &\rightarrow 4845a_{20}k^{16} + 12056400a_{20}k^{14} + 12272507520a_{20}k^{12} + 6594079972480a_{20}k^{10} + 2009120811160320a_{20}k^8 + \\
& 345262912169011200a_{20}k^6 + 30959235054582661120a_{20}k^4 + 1167103227884922470400a_{20}k^2 + 85429229933656
\end{aligned}$$

$$a_2 \rightarrow -2 \left(95a_{20}k^{18} + 301410a_{20}k^{16} + 404588160a_{20}k^{14} + 299730907840a_{20}k^{12} + 133941387410688a_{20}k^{10} + 301410a_{20}k^8 + 95a_{20}k^6 \right) \\
\omega \rightarrow -a_1k - 19a_{20}k^{20} - 66980a_{20}k^{18} - 101147040a_{20}k^{16} - 85637402240a_{20}k^{14} - 44647129136896a_{20}k^{12} - 14796981950100480a_{20}k^{10} - 3095923505458266112a_{20}k^8 - 389034409294974156800a_{20}k^6 - 2562876898009699527078846148397498368000a_{20}k^2 + 13835476912905325117440000a_{20}$$

y(z) - function:

$$\frac{1048576a^{10}A}{(4a^2e^z + \chi e^{-z})^{10}}$$

u(x, t) - function:

$$\frac{1048576a^{10}Ae^{i(kx-\omega t)}}{(4a^2e^{C0t+x} + \chi e^{-C0t-x})^{10}}$$