

Target equation:

$$-ia_1u^{(1,0)}(x,t)+a_{10}u^{(10,0)}(x,t)-ia_{11}u^{(11,0)}(x,t)+a_{12}u^{(12,0)}(x,t)-ia_{13}u^{(13,0)}(x,t)+a_{14}u^{(14,0)}(x,t)-ia_{15}u^{(15,0)}(x,t)+a_{16}u^{(16,0)}(x,t)-ia_{17}u^{(17,0)}(x,t)+a_{18}u^{(18,0)}(x,t)-ia_{19}u^{(19,0)}(x,t)+a_2u^{(2,0)}(x,t)+a_{20}u^{(20,0)}(x,t)-ia_{21}u^{(21,0)}(x,t)+a_{22}u^{(22,0)}(x,t)-ia_3u^{(3,0)}(x,t)+a_4u^{(4,0)}(x,t)-ia_5u^{(5,0)}(x,t)+a_6u^{(6,0)}(x,t)-ia_7u^{(7,0)}(x,t)+a_8u^{(8,0)}(x,t)-ia_9u^{(9,0)}(x,t)-bu(x,t)|u(x,t)|^2+iu^{(0,1)}(x,t)=0$$

Substitutions:

$$N = 11$$

$$u(x,t) \rightarrow y(z)e^{i(kx-\omega t)}$$

$$z \rightarrow x - C_0t$$

$$y(z) \rightarrow AR(z)^{11}$$

$$R'(z)^2 = R(z)^2 (1 - \chi R(z)^2)$$

Imaginary part of equation after substitutions:

$$\begin{aligned} & -26334a_{22}y^{(5)}(z)k^{17}+20349a_{21}y^{(5)}(z)k^{16}+15504a_{20}y^{(5)}(z)k^{15}+170544a_{22}y^{(7)}(z)k^{15}-11628a_{19}y^{(5)}(z)k^{14}- \\ & 116280a_{21}y^{(7)}(z)k^{14}-8568a_{18}y^{(5)}(z)k^{13}-77520a_{20}y^{(7)}(z)k^{13}-497420a_{22}y^{(9)}(z)k^{13}+6188a_{17}y^{(5)}(z)k^{12}+ \\ & 50388a_{19}y^{(7)}(z)k^{12}+293930a_{21}y^{(9)}(z)k^{12}+4368a_{16}y^{(5)}(z)k^{11}+31824a_{18}y^{(7)}(z)k^{11}+167960a_{20}y^{(9)}(z)k^{11}+ \\ & 705432a_{22}y^{(11)}(z)k^{11}-3003a_{15}y^{(5)}(z)k^{10}-19448a_{17}y^{(7)}(z)k^{10}-92378a_{19}y^{(9)}(z)k^{10}-352716a_{21}y^{(11)}(z)k^{10}- \\ & 2002a_{14}y^{(5)}(z)k^9-11440a_{16}y^{(7)}(z)k^9-48620a_{18}y^{(9)}(z)k^9-167960a_{20}y^{(11)}(z)k^9-497420a_{22}y^{(13)}(z)k^9+ \\ & 1287a_{13}y^{(5)}(z)k^8+6435a_{15}y^{(7)}(z)k^8+24310a_{17}y^{(9)}(z)k^8+75582a_{19}y^{(11)}(z)k^8+203490a_{21}y^{(13)}(z)k^8+ \\ & 792a_{12}y^{(5)}(z)k^7+3432a_{14}y^{(7)}(z)k^7+11440a_{16}y^{(9)}(z)k^7+31824a_{18}y^{(11)}(z)k^7+77520a_{20}y^{(13)}(z)k^7+ \\ & 170544a_{22}y^{(15)}(z)k^7-462a_{11}y^{(5)}(z)k^6-1716a_{13}y^{(7)}(z)k^6-5005a_{15}y^{(9)}(z)k^6-12376a_{17}y^{(11)}(z)k^6- \\ & 27132a_{19}y^{(13)}(z)k^6-54264a_{21}y^{(15)}(z)k^6-252a_{10}y^{(5)}(z)k^5-792a_{12}y^{(7)}(z)k^5-2002a_{14}y^{(9)}(z)k^5- \\ & 4368a_{16}y^{(11)}(z)k^5-8568a_{18}y^{(13)}(z)k^5-15504a_{20}y^{(15)}(z)k^5-26334a_{22}y^{(17)}(z)k^5+126a_9y^{(5)}(z)k^4+ \\ & 330a_{11}y^{(7)}(z)k^4+715a_{13}y^{(9)}(z)k^4+1365a_{15}y^{(11)}(z)k^4+2380a_{17}y^{(13)}(z)k^4+3876a_{19}y^{(15)}(z)k^4+ \\ & 5985a_{21}y^{(17)}(z)k^4+56a_8y^{(5)}(z)k^3+120a_{10}y^{(7)}(z)k^3+220a_{12}y^{(9)}(z)k^3+364a_{14}y^{(11)}(z)k^3+560a_{16}y^{(13)}(z)k^3+ \\ & 816a_{18}y^{(15)}(z)k^3+1140a_{20}y^{(17)}(z)k^3+1540a_{22}y^{(19)}(z)k^3-21a_7y^{(5)}(z)k^2-36a_9y^{(7)}(z)k^2-55a_{11}y^{(9)}(z)k^2- \\ & 78a_{13}y^{(11)}(z)k^2-105a_{15}y^{(13)}(z)k^2-136a_{17}y^{(15)}(z)k^2-171a_{19}y^{(17)}(z)k^2-210a_{21}y^{(19)}(z)k^2- \\ & 6a_6y^{(5)}(z)k-8a_8y^{(7)}(z)k-10a_{10}y^{(9)}(z)k-12a_{12}y^{(11)}(z)k-14a_{14}y^{(13)}(z)k-16a_{16}y^{(15)}(z)k- \\ & 18a_{18}y^{(17)}(z)k-20a_{20}y^{(19)}(z)k-22a_{22}y^{(21)}(z)k+(a_1-C_0+k(k(4a_4+k(5a_5+k(k(8a_8+k(9a_9+k(\\ & (a_3+k(k(20a_6+k(35a_7+k(k(120a_{10}+k(165a_{11}+k(k(1540a_{22}k^9-1330a_{21}k^8-1140a_{20}k^7+969 \\ & a_5y^{(5)}(z)+a_7y^{(7)}(z)+a_9y^{(9)}(z)+a_{11}y^{(11)}(z)+a_{13}y^{(13)}(z)+a_{15}y^{(15)}(z)+a_{17}y^{(17)}(z)+a_{19}y^{(19)}(z)+ \\ & a_{21}y^{(21)}(z)=0 \end{aligned}$$

Real part of equation after substitutions:

$$\begin{aligned} & -7315a_{22}y^{(4)}(z)k^{18}+5985a_{21}y^{(4)}(z)k^{17}+4845a_{20}y^{(4)}(z)k^{16}+74613a_{22}y^{(6)}(z)k^{16}-3876a_{19}y^{(4)}(z)k^{15}- \\ & 54264a_{21}y^{(6)}(z)k^{15}-3060a_{18}y^{(4)}(z)k^{14}-38760a_{20}y^{(6)}(z)k^{14}-319770a_{22}y^{(8)}(z)k^{14}+2380a_{17}y^{(4)}(z)k^{13}+ \end{aligned}$$

$$\begin{aligned}
& 27132a_{19}y^{(6)}(z)k^{13}+203490a_{21}y^{(8)}(z)k^{13}+1820a_{16}y^{(4)}(z)k^{12}+18564a_{18}y^{(6)}(z)k^{12}+125970a_{20}y^{(8)}(z)k^{12}+ \\
& 646646a_{22}y^{(10)}(z)k^{12}-1365a_{15}y^{(4)}(z)k^{11}-12376a_{17}y^{(6)}(z)k^{11}-75582a_{19}y^{(8)}(z)k^{11}-352716a_{21}y^{(10)}(z)k^{11}- \\
& 1001a_{14}y^{(4)}(z)k^{10}-8008a_{16}y^{(6)}(z)k^{10}-43758a_{18}y^{(8)}(z)k^{10}-184756a_{20}y^{(10)}(z)k^{10}-646646a_{22}y^{(12)}(z)k^{10}+ \\
& 715a_{13}y^{(4)}(z)k^9+5005a_{15}y^{(6)}(z)k^9+24310a_{17}y^{(8)}(z)k^9+92378a_{19}y^{(10)}(z)k^9+293930a_{21}y^{(12)}(z)k^9+ \\
& 495a_{12}y^{(4)}(z)k^8+3003a_{14}y^{(6)}(z)k^8+12870a_{16}y^{(8)}(z)k^8+43758a_{18}y^{(10)}(z)k^8+125970a_{20}y^{(12)}(z)k^8+ \\
& 319770a_{22}y^{(14)}(z)k^8-330a_{11}y^{(4)}(z)k^7-1716a_{13}y^{(6)}(z)k^7-6435a_{15}y^{(8)}(z)k^7-19448a_{17}y^{(10)}(z)k^7- \\
& 50388a_{19}y^{(12)}(z)k^7-116280a_{21}y^{(14)}(z)k^7-210a_{10}y^{(4)}(z)k^6-924a_{12}y^{(6)}(z)k^6-3003a_{14}y^{(8)}(z)k^6- \\
& 8008a_{16}y^{(10)}(z)k^6-18564a_{18}y^{(12)}(z)k^6-38760a_{20}y^{(14)}(z)k^6-74613a_{22}y^{(16)}(z)k^6+126a_9y^{(4)}(z)k^5+ \\
& 462a_{11}y^{(6)}(z)k^5+1287a_{13}y^{(8)}(z)k^5+3003a_{15}y^{(10)}(z)k^5+6188a_{17}y^{(12)}(z)k^5+11628a_{19}y^{(14)}(z)k^5+ \\
& 20349a_{21}y^{(16)}(z)k^5+70a_8y^{(4)}(z)k^4+210a_{10}y^{(6)}(z)k^4+495a_{12}y^{(8)}(z)k^4+1001a_{14}y^{(10)}(z)k^4+ \\
& 1820a_{16}y^{(12)}(z)k^4+3060a_{18}y^{(14)}(z)k^4+4845a_{20}y^{(16)}(z)k^4+7315a_{22}y^{(18)}(z)k^4-35a_7y^{(4)}(z)k^3- \\
& 84a_9y^{(6)}(z)k^3-165a_{11}y^{(8)}(z)k^3-286a_{13}y^{(10)}(z)k^3-455a_{15}y^{(12)}(z)k^3-680a_{17}y^{(14)}(z)k^3-969a_{19}y^{(16)}(z)k^3- \\
& 1330a_{21}y^{(18)}(z)k^3-15a_6y^{(4)}(z)k^2-28a_8y^{(6)}(z)k^2-45a_{10}y^{(8)}(z)k^2-66a_{12}y^{(10)}(z)k^2-91a_{14}y^{(12)}(z)k^2- \\
& 120a_{16}y^{(14)}(z)k^2-153a_{18}y^{(16)}(z)k^2-190a_{20}y^{(18)}(z)k^2-231a_{22}y^{(20)}(z)k^2+5a_5y^{(4)}(z)k+7a_7y^{(6)}(z)k+ \\
& 9a_9y^{(8)}(z)k+11a_{11}y^{(10)}(z)k+13a_{13}y^{(12)}(z)k+15a_{15}y^{(14)}(z)k+17a_{17}y^{(16)}(z)k+19a_{19}y^{(18)}(z)k+ \\
& 21a_{21}y^{(20)}(z)k-by(z)^3+(-a_{22}k^{22}+a_{21}k^{21}+a_{20}k^{20}-a_{19}k^{19}-a_{18}k^{18}+a_{17}k^{17}+a_{16}k^{16}-a_{15}k^{15}-a_{14}k^{14}+ \\
& (a_2+k(3a_3+k(k(15a_6+k(21a_7+k(k(45a_{10}+k(55a_{11}+k(k(231a_{22}k^9-210a_{21}k^8-190a_{20}k^7+ \\
& a_4y^{(4)}(z)+a_6y^{(6)}(z)+a_8y^{(8)}(z)+a_{10}y^{(10)}(z)+a_{12}y^{(12)}(z)+a_{14}y^{(14)}(z)+a_{16}y^{(16)}(z)+a_{18}y^{(18)}(z)+ \\
& a_{20}y^{(20)}(z)+a_{22}y^{(22)}(z)=0
\end{aligned}$$

Constraints on coefficients from imaginary part of equation:

$$\begin{aligned}
a_{21} &\rightarrow 22a_{22}k \\
a_{19} &\rightarrow 20a_{20}k + 3080a_{22}k^3 \\
a_{17} &\rightarrow 18a_{18}k + 2280a_{20}k^3 + 421344a_{22}k^5 \\
a_{15} &\rightarrow 16a_{16}k + 1632a_{18}k^3 + 248064a_{20}k^5 + 46387968a_{22}k^7 \\
a_{13} &\rightarrow 14a_{14}k + 1120a_{16}k^3 + 137088a_{18}k^5 + 21085440a_{20}k^7 + 3947525120a_{22}k^9 \\
a_{11} &\rightarrow 12a_{12}k + 728a_{14}k^3 + 69888a_{16}k^5 + 8656128a_{18}k^7 + 1332930560a_{20}k^9 + 249576198144a_{22}k^{11} \\
a_9 &\rightarrow 10a_{10}k + 440a_{12}k^3 + 32032a_{14}k^5 + 3111680a_{16}k^7 + 385848320a_{18}k^9 + 59422904320a_{20}k^{11} + \\
& 11126417899520a_{22}k^{13} \\
a_7 &\rightarrow 240a_{10}k^3+12672a_{12}k^5+933504a_{14}k^7+90787840a_{16}k^9+11259076608a_{18}k^{11}+1733987205120a_{20}k^{13}+ \\
& 324674387017728a_{22}k^{15}+8a_8k \\
a_5 &\rightarrow 4032a_{10}k^5+215424a_{12}k^7+15887872a_{14}k^9+1545363456a_{16}k^{11}+191651217408a_{18}k^{13}+ \\
& 29515853365248a_{20}k^{15}+5526593941929984a_{22}k^{17}+6a_6k+112a_8k^3 \\
a_3 &\rightarrow 32640a_{10}k^7+1745920a_{12}k^9+128780288a_{14}k^{11}+12526223360a_{16}k^{13}+1553465966592a_{18}k^{15}+ \\
& 239246490992640a_{20}k^{17}+44796883073761280a_{22}k^{19}+4a_4k+40a_6k^3+896a_8k^5
\end{aligned}$$

$$C0 \rightarrow a_1 - 79360a_{10}k^9 - 4245504a_{12}k^{11} - 313155584a_{14}k^{13} - 30460116992a_{16}k^{15} - 3777576173568a_{18}k^{17} - \blacksquare$$

$$2a_2k - 581777702256640a_{20}k^{19} - 108932957168730112a_{22}k^{21} - 8a_4k^3 - 96a_6k^5 - 2176a_8k^7$$

Constraints on coefficients from real part of equation:

$$b \rightarrow -\frac{72511804710563693278003200000a_{22}\chi^{11}}{A^2}$$

$$a_{20} \rightarrow -231a_{22}k^2 - 5291a_{22}$$

$$a_{18} \rightarrow 7315a_{22}k^4 + 1005290a_{22}k^2 + 12329911a_{22}$$

$$a_{16} \rightarrow -74613a_{22}k^6 - 25634895a_{22}k^4 - 1886476383a_{22}k^2 - 16676560901a_{22}$$

$$a_{14} \rightarrow 319770a_{22}k^8 + 205079160a_{22}k^6 + 37729527660a_{22}k^4 + 2001187308120a_{22}k^2 + 14519691974986a_{22} \blacksquare$$

$$a_{12} \rightarrow -646646a_{22}k^{10} - 666507270a_{22}k^8 - 228892467804a_{22}k^6 - 30351340839820a_{22}k^4 - 1321291969723726a_{22}k^2 - 8528645356058126a_{22}$$

$$a_{10} \rightarrow 646646a_{22}k^{12} + 977543996a_{22}k^{10} + 539532245538a_{22}k^8 + 133545899695208a_{22}k^6 + 14534211666960986a_{22}k^4 + 562890593499836316a_{22}k^2 + 3441772651808322766a_{22}$$

$$a_8 \rightarrow -319770a_{22}k^{14} - 666507270a_{22}k^{12} - 539532245538a_{22}k^{10} - 214627338795870a_{22}k^8 - 43602635000882958a_{22}k^6 - 4221679451248772370a_{22}k^4 - 154879769331374524470a_{22}k^2 - 952258695948480426506a_{22}$$

$$a_6 \rightarrow 74613a_{22}k^{16} + 205079160a_{22}k^{14} + 228892467804a_{22}k^{12} + 133545899695208a_{22}k^{10} + 43602635000882958a_{22}k^8 + 7880468308997708424a_{22}k^6 + 722772256879747780860a_{22}k^4 + 26663243486557451942168a_{22}k^2 + 176635043848108568605861a_{22}$$

$$a_4 \rightarrow -7315a_{22}k^{18} - 25634895a_{22}k^{16} - 37729527660a_{22}k^{14} - 30351340839820a_{22}k^{12} - 14534211666960986a_{22}k^{10} - 4221679451248772370a_{22}k^8 - 722772256879747780860a_{22}k^6 - 66658108716393629855420a_{22}k^4 - 2649525657721628529087915a_{22}k^2 - 20872739425587616666078551a_{22}$$

$$a_2 \rightarrow 231a_{22}k^{20} + 1005290a_{22}k^{18} + 1886476383a_{22}k^{16} + 2001187308120a_{22}k^{14} + 1321291969723726a_{22}k^{12} + \blacksquare$$

$$562890593499836316a_{22}k^{10} + 154879769331374524470a_{22}k^8 + 26663243486557451942168a_{22}k^6 + 2649525657721628529087915a_{22}k^4 + 125236436553525699996471306a_{22}k^2 + 1410931579974248996727086475$$

$$\omega \rightarrow -a_1k + 21a_{22}k^{22} + 100529a_{22}k^{20} + 209608487a_{22}k^{18} + 250148413515a_{22}k^{16} + 188755995674818a_{22}k^{14} + \blacksquare$$

$$93815098916639386a_{22}k^{12} + 30975953866274904894a_{22}k^{10} + 6665810871639362985542a_{22}k^8 + 8831752192405462618218276762849998235653a_{22}k^4 + 1410931579974248996727086475a_{22}k^2 - 41236408035934408387856390$$

y(z) - function:

$$\frac{4194304a^{11}A}{(4a^2e^z + \chi e^{-z})^{11}}$$

u(x, t) - function:

$$\frac{4194304a^{11}Ae^{i(kx-\omega t)}}{(4a^2e^{C0t+x} + \chi e^{-C0t-x})^{11}}$$