

Target equation:

$$-ia_1u^{(1,0)}(x,t)+a_{10}u^{(10,0)}(x,t)-ia_{11}u^{(11,0)}(x,t)+a_{12}u^{(12,0)}(x,t)-ia_{13}u^{(13,0)}(x,t)+a_{14}u^{(14,0)}(x,t)+a_2u^{(2,0)}(x,t)-ia_3u^{(3,0)}(x,t)+a_4u^{(4,0)}(x,t)-ia_5u^{(5,0)}(x,t)+a_6u^{(6,0)}(x,t)-ia_7u^{(7,0)}(x,t)+a_8u^{(8,0)}(x,t)-ia_9u^{(9,0)}(x,t)-bu(x,t)|u(x,t)|^2+iu^{(0,1)}(x,t)=0$$

Substitutions:

$$N = 7$$

$$u(x,t) \rightarrow y(z)e^{i(kx-\omega t)}$$

$$z \rightarrow x - C_0t$$

$$y(z) \rightarrow AR(z)^7$$

$$R'(z)^2 = R(z)^2 (1 - \chi R(z)^2)$$

Imaginary part of equation after substitutions:

$$y'(z)(a_1+k(k(k(-10a_{10}k^5-11a_{11}k^6+12a_{12}k^7+13a_{13}k^8-14a_{14}k^9+5a_5-6a_6k-7a_7k^2+8a_8k^3+9a_9k^4)-10a_{10}k^5+165a_{11}k^6-220a_{12}k^7-286a_{13}k^8+364a_{14}k^9-10a_5+20a_6k+35a_7k^2-56a_8k^3-8a_9k^4)+252a_{10}k^5y^{(5)}(z)+120a_{10}k^3y^{(7)}(z)-10a_{10}ky^{(9)}(z)-462a_{11}k^6y^{(5)}(z)+330a_{11}k^4y^{(7)}(z)-55a_{11}k^2y^{(9)}(z)+a_{11}y^{(11)}(z)+792a_{12}k^7y^{(5)}(z)-792a_{12}k^5y^{(7)}(z)+220a_{12}k^3y^{(9)}(z)-12a_{12}ky^{(11)}(z)+1287a_{13}k^8y^{(5)}(z)-1716a_{13}k^6y^{(7)}(z)+715a_{13}k^4y^{(9)}(z)-78a_{13}k^2y^{(11)}(z)+a_{13}y^{(13)}(z)-2002a_{14}k^9y^{(5)}(z)+3432a_{14}k^7y^{(7)}(z)-2002a_{14}k^5y^{(9)}(z)+364a_{14}k^3y^{(11)}(z)-14a_{14}ky^{(13)}(z)+a_5y^{(5)}(z)-6a_6ky^{(5)}(z)-21a_7k^2y^{(5)}(z)+a_7y^{(7)}(z)+56a_8k^3y^{(5)}(z)-8a_8ky^{(7)}(z)+126a_9k^4y^{(5)}(z)-36a_9k^2y^{(7)}(z)+a_9y^{(9)}(z)=0$$

Real part of equation after substitutions:

$$y(z)(a_1k-a_{10}k^{10}-a_{11}k^{11}+a_{12}k^{12}+a_{13}k^{13}-a_{14}k^{14}-a_2k^2-a_3k^3+a_4k^4+a_5k^5-a_6k^6-a_7k^7+a_8k^8+y''(z)(k(k(k(45a_{10}k^5+55a_{11}k^6-66a_{12}k^7-78a_{13}k^8+91a_{14}k^9-10a_5+15a_6k+21a_7k^2-28a_8k^3-36a_9k^4)+210a_{10}k^6y^{(4)}(z)+210a_{10}k^4y^{(6)}(z)-45a_{10}k^2y^{(8)}(z)+a_{10}y^{(10)}(z)-330a_{11}k^7y^{(4)}(z)+462a_{11}k^5y^{(6)}(z)-165a_{11}k^3y^{(8)}(z)+11a_{11}ky^{(10)}(z)+495a_{12}k^8y^{(4)}(z)-924a_{12}k^6y^{(6)}(z)+495a_{12}k^4y^{(8)}(z)-66a_{12}k^2y^{(10)}(z)+a_{12}y^{(12)}(z)+715a_{13}k^9y^{(4)}(z)-1716a_{13}k^7y^{(6)}(z)+1287a_{13}k^5y^{(8)}(z)-286a_{13}k^3y^{(10)}(z)+13a_{13}ky^{(12)}(z)-1001a_{14}k^{10}y^{(4)}(z)+3003a_{14}k^8y^{(6)}(z)-3003a_{14}k^6y^{(8)}(z)+1001a_{14}k^4y^{(10)}(z)-91a_{14}k^2y^{(12)}(z)+a_{14}y^{(14)}(z)+a_4y^{(4)}(z)+5a_5ky^{(4)}(z)-15a_6k^2y^{(4)}(z)+a_6y^{(6)}(z)-35a_7k^3y^{(4)}(z)+7a_7ky^{(6)}(z)+70a_8k^4y^{(4)}(z)-28a_8k^2y^{(6)}(z)+a_8y^{(8)}(z)+126a_9k^5y^{(4)}(z)-84a_9k^3y^{(6)}(z)+9a_9ky^{(8)}(z)-by(z)^3=0$$

Constraints on coefficients from imaginary part of equation:

$$a_{13} \rightarrow 14a_{14}k$$

$$a_{11} \rightarrow 4(3a_{12}k+182a_{14}k^3)$$

$$a_9 \rightarrow 2(5a_{10}k+220a_{12}k^3+16016a_{14}k^5)$$

$$a_7 \rightarrow 8(30a_{10}k^3+1584a_{12}k^5+116688a_{14}k^7+a_8k)$$

$$a_5 \rightarrow 2(2016a_{10}k^5+107712a_{12}k^7+7943936a_{14}k^9+3a_6k+56a_8k^3)$$

$$a_3 \rightarrow 4k(8160a_{10}k^6+436480a_{12}k^8+32195072a_{14}k^{10}+a_4+10a_6k^2+224a_8k^4)$$

$$C0 \rightarrow a_1 - 79360a_{10}k^9 - 4245504a_{12}k^{11} - 313155584a_{14}k^{13} - 2a_2k - 8a_4k^3 - 96a_6k^5 - 2176a_8k^7$$

Constraints on coefficients from real part of equation:

$$b \rightarrow -\frac{3379030566912000a_{14}\chi^7}{A^2}$$

$$a_{12} \rightarrow -7a_{14}(13k^2 + 185)$$

$$a_{10} \rightarrow 7(143a_{14}k^4 + 12210a_{14}k^2 + 97171a_{14})$$

$$a_8 \rightarrow -3003a_{14}k^6 - 641025a_{14}k^4 - 30608865a_{14}k^2 - 186879835a_{14}$$

$$a_6 \rightarrow 7(429a_{14}k^8 + 170940a_{14}k^6 + 20405910a_{14}k^4 + 747519340a_{14}k^2 + 4119846629a_{14})$$

$$a_4 \rightarrow -7(143a_{14}k^{10} + 91575a_{14}k^8 + 20405910a_{14}k^6 + 1868798350a_{14}k^4 + 61797699435a_{14}k^2 + 35481813383a_{14})$$

$$a_2 \rightarrow 91a_{14}k^{12} + 85470a_{14}k^{10} + 30608865a_{14}k^8 + 5232635380a_{14}k^6 + 432583896045a_{14}k^4 + 14902361621070a_{14}k^2 + 109758994449399a_{14}$$

$$\omega \rightarrow -a_1k + 13a_{14}k^{14} + 14245a_{14}k^{12} + 6121773a_{14}k^{10} + 1308158845a_{14}k^8 + 144194632015a_{14}k^6 + 7451180810535a_{14}k^4 + 109758994449399a_{14}k^2 - 1905200718446025a_{14}$$

y(z) - function:

$$\frac{16384a^7A}{(4a^2e^z + \chi e^{-z})^7}$$

u(x, t) - function:

$$\frac{16384a^7Ae^{i(kx-\omega t)}}{(4a^2e^{C0t+x} + \chi e^{-C0t-x})^7}$$