

Target equation:

$$\begin{aligned}
& -ia_1u^{(1,0)}(x,t)+a_{10}u^{(10,0)}(x,t)-ia_{11}u^{(11,0)}(x,t)+a_{12}u^{(12,0)}(x,t)-ia_{13}u^{(13,0)}(x,t)+a_{14}u^{(14,0)}(x,t)- \\
& ia_{15}u^{(15,0)}(x,t)+a_{16}u^{(16,0)}(x,t)-ia_{17}u^{(17,0)}(x,t)+a_{18}u^{(18,0)}(x,t)+a_2u^{(2,0)}(x,t)-ia_3u^{(3,0)}(x,t)+ \\
& a_4u^{(4,0)}(x,t)-ia_5u^{(5,0)}(x,t)+a_6u^{(6,0)}(x,t)-ia_7u^{(7,0)}(x,t)+a_8u^{(8,0)}(x,t)-ia_9u^{(9,0)}(x,t)-bu(x,t)|u(x,t)|^2+ \\
& iu^{(0,1)}(x,t)=0
\end{aligned}$$

Substitutions:

$$\begin{aligned} N &= 9 \\ u(x, t) &\rightarrow y(z)e^{i(kx - \omega t)} \\ z &\rightarrow x - C_0 t \\ y(z) &\rightarrow AR(z)^9 \\ R'(z)^2 &= R(z)^2(1 - \chi R(z)^2) \end{aligned}$$

Imaginary part of equation after substitutions:

$$\begin{aligned}
& y'(z) (a_1 + k (k (k (k (k (k (-10a_{10}k - 11a_{11}k^2 + 12a_{12}k^3 + 13a_{13}k^4 - 14a_{14}k^5 - 15a_{15}k^6 + 16a_{16}k^7 + 17a_{17}k^8 \\
& y^{(3)}(z) (k (k (k (k (k (k (120a_{10}k + 165a_{11}k^2 - 220a_{12}k^3 - 286a_{13}k^4 + 364a_{14}k^5 + 455a_{15}k^6 - 560a_{16}k^7 - 680a_{17}k^8 \\
& 252a_{10}k^5y^{(5)}(z)+120a_{10}k^3y^{(7)}(z)-10a_{10}ky^{(9)}(z)-462a_{11}k^6y^{(5)}(z)+330a_{11}k^4y^{(7)}(z)-55a_{11}k^2y^{(9)}(z)+\blacksquare \\
& a_{11}y^{(11)}(z)+792a_{12}k^7y^{(5)}(z)-792a_{12}k^5y^{(7)}(z)+220a_{12}k^3y^{(9)}(z)-12a_{12}ky^{(11)}(z)+1287a_{13}k^8y^{(5)}(z)-\blacksquare \\
& 1716a_{13}k^6y^{(7)}(z)+715a_{13}k^4y^{(9)}(z)-78a_{13}k^2y^{(11)}(z)+a_{13}y^{(13)}(z)-2002a_{14}k^9y^{(5)}(z)+3432a_{14}k^7y^{(7)}(z)-\blacksquare \\
& 2002a_{14}k^5y^{(9)}(z) + 364a_{14}k^3y^{(11)}(z) - 14a_{14}ky^{(13)}(z) - 3003a_{15}k^{10}y^{(5)}(z) + 6435a_{15}k^8y^{(7)}(z) - \\
& 5005a_{15}k^6y^{(9)}(z)+1365a_{15}k^4y^{(11)}(z)-105a_{15}k^2y^{(13)}(z)+a_{15}y^{(15)}(z)+4368a_{16}k^{11}y^{(5)}(z)-11440a_{16}k^9y^{(7)}(z)+\blacksquare \\
& 11440a_{16}k^7y^{(9)}(z) - 4368a_{16}k^5y^{(11)}(z) + 560a_{16}k^3y^{(13)}(z) - 16a_{16}ky^{(15)}(z) + 6188a_{17}k^{12}y^{(5)}(z) - \\
& 19448a_{17}k^{10}y^{(7)}(z)+24310a_{17}k^8y^{(9)}(z)-12376a_{17}k^6y^{(11)}(z)+2380a_{17}k^4y^{(13)}(z)-136a_{17}k^2y^{(15)}(z)+\blacksquare \\
& a_{17}y^{(17)}(z) - 8568a_{18}k^{13}y^{(5)}(z) + 31824a_{18}k^{11}y^{(7)}(z) - 48620a_{18}k^9y^{(9)}(z) + 31824a_{18}k^7y^{(11)}(z) - \\
& 8568a_{18}k^5y^{(13)}(z) + 816a_{18}k^3y^{(15)}(z) - 18a_{18}ky^{(17)}(z) + a_5y^{(5)}(z) - 6a_6ky^{(5)}(z) - 21a_7k^2y^{(5)}(z) + \\
& a_7y^{(7)}(z) + 56a_8k^3y^{(5)}(z) - 8a_8ky^{(7)}(z) + 126a_9k^4y^{(5)}(z) - 36a_9k^2y^{(7)}(z) + a_9y^{(9)}(z) = 0
\end{aligned}$$

Real part of equation after substitutions:

$$\begin{aligned} & -3060a_{18}y^{(4)}(z)k^{14}+2380a_{17}y^{(4)}(z)k^{13}+1820a_{16}y^{(4)}(z)k^{12}+18564a_{18}y^{(6)}(z)k^{12}-1365a_{15}y^{(4)}(z)k^{11}- \\ & 12376a_{17}y^{(6)}(z)k^{11}-1001a_{14}y^{(4)}(z)k^{10}-8008a_{16}y^{(6)}(z)k^{10}-43758a_{18}y^{(8)}(z)k^{10}+715a_{13}y^{(4)}(z)k^9+ \\ & 5005a_{15}y^{(6)}(z)k^9+24310a_{17}y^{(8)}(z)k^9+495a_{12}y^{(4)}(z)k^8+3003a_{14}y^{(6)}(z)k^8+12870a_{16}y^{(8)}(z)k^8+ \\ & 43758a_{18}y^{(10)}(z)k^8-330a_{11}y^{(4)}(z)k^7-1716a_{13}y^{(6)}(z)k^7-6435a_{15}y^{(8)}(z)k^7-19448a_{17}y^{(10)}(z)k^7- \\ & 210a_{10}y^{(4)}(z)k^6-924a_{12}y^{(6)}(z)k^6-3003a_{14}y^{(8)}(z)k^6-8008a_{16}y^{(10)}(z)k^6-18564a_{18}y^{(12)}(z)k^6+ \\ & 126a_9y^{(4)}(z)k^5+462a_{11}y^{(6)}(z)k^5+1287a_{13}y^{(8)}(z)k^5+3003a_{15}y^{(10)}(z)k^5+6188a_{17}y^{(12)}(z)k^5+ \\ & 70a_8y^{(4)}(z)k^4+210a_{10}y^{(6)}(z)k^4+495a_{12}y^{(8)}(z)k^4+1001a_{14}y^{(10)}(z)k^4+1820a_{16}y^{(12)}(z)k^4+3060a_{18}y^{(14)}(z)k^4- \\ & 35a_7y^{(4)}(z)k^3-84a_9y^{(6)}(z)k^3-165a_{11}y^{(8)}(z)k^3-286a_{13}y^{(10)}(z)k^3-455a_{15}y^{(12)}(z)k^3-680a_{17}y^{(14)}(z)k^3- \\ & 15a_6y^{(4)}(z)k^2-28a_8y^{(6)}(z)k^2-45a_{10}y^{(8)}(z)k^2-66a_{12}y^{(10)}(z)k^2-91a_{14}y^{(12)}(z)k^2-120a_{16}y^{(14)}(z)k^2- \end{aligned}$$

$$153a_{18}y^{(16)}(z)k^2 + 5a_5y^{(4)}(z)k + 7a_7y^{(6)}(z)k + 9a_9y^{(8)}(z)k + 11a_{11}y^{(10)}(z)k + 13a_{13}y^{(12)}(z)k + 15a_{15}y^{(14)}(z)k + 17a_{17}y^{(16)}(z)k - by(z)^3 + (-a_{18}k^{18} + a_{17}k^{17} + a_{16}k^{16} - a_{15}k^{15} - a_{14}k^{14} + a_{13}k^{13} + a_{12}k^{12} - a_{11}k^{11} - a_{10}k^{10} - a_9k^9 - a_8k^8 - a_7k^7 - a_6k^6 - a_5k^5 - a_4k^4 - a_3k^3 - a_2k^2 - a_1k) = 0$$

Constraints on coefficients from imaginary part of equation:

$$\begin{aligned} a_{17} &\rightarrow 18a_{18}k \\ a_{15} &\rightarrow 16(a_{16}k + 102a_{18}k^3) \\ a_{13} &\rightarrow 14(a_{14}k + 80a_{16}k^3 + 9792a_{18}k^5) \\ a_{11} &\rightarrow 4(3a_{12}k + 182a_{14}k^3 + 17472a_{16}k^5 + 2164032a_{18}k^7) \\ a_9 &\rightarrow 2(5a_{10}k + 220a_{12}k^3 + 16016a_{14}k^5 + 1555840a_{16}k^7 + 192924160a_{18}k^9) \\ a_7 &\rightarrow 8(30a_{10}k^3 + 1584a_{12}k^5 + 116688a_{14}k^7 + 11348480a_{16}k^9 + 1407384576a_{18}k^{11} + a_8k) \\ a_5 &\rightarrow 2(2016a_{10}k^5 + 107712a_{12}k^7 + 7943936a_{14}k^9 + 772681728a_{16}k^{11} + 95825608704a_{18}k^{13} + 3a_6k + 56a_8k) \\ a_3 &\rightarrow 4k(8160a_{10}k^6 + 436480a_{12}k^8 + 32195072a_{14}k^{10} + 3131555840a_{16}k^{12} + 388366491648a_{18}k^{14} + a_4 + 10a_6) \\ C0 &\rightarrow a_1 - 79360a_{10}k^9 - 4245504a_{12}k^{11} - 313155584a_{14}k^{13} - 30460116992a_{16}k^{15} - 3777576173568a_{18}k^{17} - 2a_2k - 8a_4k^3 - 96a_6k^5 - 2176a_8k^7 \end{aligned}$$

Constraints on coefficients from real part of equation:

$$\begin{aligned} b &\rightarrow -\frac{10002268381116211200000a_{18}\chi^9}{A^2} \\ a_{16} &\rightarrow -3a_{18}(51k^2 + 947) \\ a_{14} &\rightarrow 12(255a_{18}k^4 + 28410a_{18}k^2 + 287171a_{18}) \\ a_{12} &\rightarrow -52(357a_{18}k^6 + 99435a_{18}k^4 + 6030591a_{18}k^2 + 44922041a_{18}) \\ a_{10} &\rightarrow 858(51a_{18}k^8 + 26516a_{18}k^6 + 4020394a_{18}k^4 + 179688164a_{18}k^2 + 1133241371a_{18}) \\ a_8 &\rightarrow -78(561a_{18}k^{10} + 468765a_{18}k^8 + 132673002a_{18}k^6 + 14824273530a_{18}k^4 + 560954478645a_{18}k^2 + 329368a_{18}) \\ a_6 &\rightarrow 4(4641a_{18}k^{12} + 5687682a_{18}k^{10} + 2587123539a_{18}k^8 + 539603556492a_{18}k^6 + 51046857556695a_{18}k^4 + 1798352775339666a_{18}k^2 + 214711843034298020a_{18}k^6 + 13088574157438344492a_{18}k^4 + 24354706537150319002a_{18}k^2 + 5669162887825953140625a_{18}) \\ a_4 &\rightarrow -12(255a_{18}k^{14} + 430885a_{18}k^{12} + 287458171a_{18}k^{10} + 96357777945a_{18}k^8 + 17015619185565a_{18}k^6 + 1498352775339666a_{18}k^4 + 214711843034298020a_{18}k^2 + 13088574157438344492a_{18}k^0 + 24354706537150319002a_{18}) \\ a_2 &\rightarrow 3(51a_{18}k^{16} + 113640a_{18}k^{14} + 104530244a_{18}k^{12} + 51390814904a_{18}k^{10} + 14584816444770a_{18}k^8 + 23978015619185565a_{18}k^6 + 1798352775339666a_{18}k^4 + 214711843034298020a_{18}k^2 + 13088574157438344492a_{18}k^0 + 24354706537150319002a_{18}) \\ \omega &\rightarrow -a_1k + 17a_{18}k^{18} + 42615a_{18}k^{16} + 44798676a_{18}k^{14} + 25695407452a_{18}k^{12} + 8750889866862a_{18}k^{10} + 1798352775339666a_{18}k^8 + 214711843034298020a_{18}k^6 + 13088574157438344492a_{18}k^4 + 24354706537150319002a_{18}k^2 + 5669162887825953140625a_{18} \end{aligned}$$

y(z) - function:

$$\frac{262144a^9A}{(4a^2e^z + \chi e^{-z})^9}$$

u(x, t) - function:

$$\frac{262144a^9Ae^{i(kx-\omega t)}}{(4a^2e^{C0t+x} + \chi e^{-C0t-x})^9}$$