

Target equation:

$$-ia_1 u^{(1,0)}(x, t) + a_2 u^{(2,0)}(x, t) - ia_3 u^{(3,0)}(x, t) + a_4 u^{(4,0)}(x, t) - bu(x, t) |u(x, t)|^2 + iu^{(0,1)}(x, t) = 0$$

Substitutions:

$$N = 2$$

$$u(x, t) \rightarrow y(z) e^{i(kx - \omega t)}$$

$$z \rightarrow x - C_0 t$$

$$y(z) \rightarrow AR(z)^2$$

$$R'(z)^2 = R(z)^2 (1 - \chi R(z)^2)$$

Imaginary part of equation after substitutions:

$$y'(z) (a_1 - 2a_2 k - 3a_3 k^2 + 4a_4 k^3 - C_0) + y^{(3)}(z) (a_3 - 4a_4 k) = 0$$

Real part of equation after substitutions:

$$y(z) (a_1 k - a_2 k^2 - a_3 k^3 + a_4 k^4 + \omega) + y''(z) (a_2 + 3k(a_3 - 2a_4 k)) + a_4 y^{(4)}(z) - by(z)^3 = 0$$

Constraints on coefficients from imaginary part of equation:

$$a_3 \rightarrow 4a_4 k$$

$$C_0 \rightarrow a_1 - 2a_2 k - 8a_4 k^3$$

Constraints on coefficients from real part of equation:

$$b \rightarrow \frac{120a_4 \chi^2}{A^2}$$

$$a_2 \rightarrow -2(3a_4 k^2 + 10a_4)$$

$$\omega \rightarrow -a_1 k - 3a_4 k^4 - 20a_4 k^2 + 64a_4$$

y(z) - function:

$$\frac{16a^2 A}{(4a^2 e^z + \chi e^{-z})^2}$$

u(x, t) - function:

$$\frac{16a^2 A e^{i(kx - \omega t)}}{(4a^2 e^{C_0 t + x} + \chi e^{-C_0 t - x})^2}$$