

Target equation:

$$\begin{aligned}
& -ia_1u^{(1,0)}(x,t)+a_{10}u^{(10,0)}(x,t)-ia_{11}u^{(11,0)}(x,t)+a_{12}u^{(12,0)}(x,t)-ia_{13}u^{(13,0)}(x,t)+a_{14}u^{(14,0)}(x,t)- \\
& ia_{15}u^{(15,0)}(x,t)+a_{16}u^{(16,0)}(x,t)-ia_{17}u^{(17,0)}(x,t)+a_{18}u^{(18,0)}(x,t)-ia_{19}u^{(19,0)}(x,t)+a_2u^{(2,0)}(x,t)+ \\
& a_{20}u^{(20,0)}(x,t)-ia_{21}u^{(21,0)}(x,t)+a_{22}u^{(22,0)}(x,t)-ia_{23}u^{(23,0)}(x,t)+a_{24}u^{(24,0)}(x,t)-ia_3u^{(3,0)}(x,t)+ \\
& a_4u^{(4,0)}(x,t)-ia_5u^{(5,0)}(x,t)+a_6u^{(6,0)}(x,t)-ia_7u^{(7,0)}(x,t)+a_8u^{(8,0)}(x,t)-ia_9u^{(9,0)}(x,t)-bu(x,t)|u(x,t)|^2+ \\
& iu^{(0,1)}(x,t) = 0
\end{aligned}$$

Substitutions:

$$N = 12$$

$$u(x,t) \rightarrow y(z)e^{i(kx-\omega t)}$$

$$z \rightarrow x - C0t$$

$$y(z) \rightarrow AR(z)^{12}$$

$$R'(z)^2 = R(z)^2 (1 - \chi R(z)^2)$$

Imaginary part of equation after substitutions:

$$\begin{aligned}
& 42504a_{24}y^{(5)}(z)k^{19}-33649a_{23}y^{(5)}(z)k^{18}-26334a_{22}y^{(5)}(z)k^{17}-346104a_{24}y^{(7)}(z)k^{17}+20349a_{21}y^{(5)}(z)k^{16}+ \\
& 245157a_{23}y^{(7)}(z)k^{16}+15504a_{20}y^{(5)}(z)k^{15}+170544a_{22}y^{(7)}(z)k^{15}+1307504a_{24}y^{(9)}(z)k^{15}-11628a_{19}y^{(5)}(z)k^{14}- \\
& 116280a_{21}y^{(7)}(z)k^{14}-817190a_{23}y^{(9)}(z)k^{14}-8568a_{18}y^{(5)}(z)k^{13}-77520a_{20}y^{(7)}(z)k^{13}-497420a_{22}y^{(9)}(z)k^{13}- \\
& 2496144a_{24}y^{(11)}(z)k^{13}+6188a_{17}y^{(5)}(z)k^{12}+50388a_{19}y^{(7)}(z)k^{12}+293930a_{21}y^{(9)}(z)k^{12}+1352078a_{23}y^{(11)}(z)k^{12}+ \\
& 4368a_{16}y^{(5)}(z)k^{11}+31824a_{18}y^{(7)}(z)k^{11}+167960a_{20}y^{(9)}(z)k^{11}+705432a_{22}y^{(11)}(z)k^{11}+2496144a_{24}y^{(13)}(z)k^{11}- \\
& 3003a_{15}y^{(5)}(z)k^{10}-19448a_{17}y^{(7)}(z)k^{10}-92378a_{19}y^{(9)}(z)k^{10}-352716a_{21}y^{(11)}(z)k^{10}-1144066a_{23}y^{(13)}(z)k^{10}- \\
& 2002a_{14}y^{(5)}(z)k^9-11440a_{16}y^{(7)}(z)k^9-48620a_{18}y^{(9)}(z)k^9-167960a_{20}y^{(11)}(z)k^9-497420a_{22}y^{(13)}(z)k^9- \\
& 1307504a_{24}y^{(15)}(z)k^9+1287a_{13}y^{(5)}(z)k^8+6435a_{15}y^{(7)}(z)k^8+24310a_{17}y^{(9)}(z)k^8+75582a_{19}y^{(11)}(z)k^8+ \\
& 203490a_{21}y^{(13)}(z)k^8+490314a_{23}y^{(15)}(z)k^8+792a_{12}y^{(5)}(z)k^7+3432a_{14}y^{(7)}(z)k^7+11440a_{16}y^{(9)}(z)k^7+ \\
& 31824a_{18}y^{(11)}(z)k^7+77520a_{20}y^{(13)}(z)k^7+170544a_{22}y^{(15)}(z)k^7+346104a_{24}y^{(17)}(z)k^7-462a_{11}y^{(5)}(z)k^6- \\
& 1716a_{13}y^{(7)}(z)k^6-5005a_{15}y^{(9)}(z)k^6-12376a_{17}y^{(11)}(z)k^6-27132a_{19}y^{(13)}(z)k^6-54264a_{21}y^{(15)}(z)k^6- \\
& 100947a_{23}y^{(17)}(z)k^6-252a_{10}y^{(5)}(z)k^5-792a_{12}y^{(7)}(z)k^5-2002a_{14}y^{(9)}(z)k^5-4368a_{16}y^{(11)}(z)k^5- \\
& 8568a_{18}y^{(13)}(z)k^5-15504a_{20}y^{(15)}(z)k^5-26334a_{22}y^{(17)}(z)k^5-42504a_{24}y^{(19)}(z)k^5+126a_9y^{(5)}(z)k^4+ \\
& 330a_{11}y^{(7)}(z)k^4+715a_{13}y^{(9)}(z)k^4+1365a_{15}y^{(11)}(z)k^4+2380a_{17}y^{(13)}(z)k^4+3876a_{19}y^{(15)}(z)k^4+ \\
& 5985a_{21}y^{(17)}(z)k^4+8855a_{23}y^{(19)}(z)k^4+56a_8y^{(5)}(z)k^3+120a_{10}y^{(7)}(z)k^3+220a_{12}y^{(9)}(z)k^3+364a_{14}y^{(11)}(z)k^3+ \\
& 560a_{16}y^{(13)}(z)k^3+816a_{18}y^{(15)}(z)k^3+1140a_{20}y^{(17)}(z)k^3+1540a_{22}y^{(19)}(z)k^3+2024a_{24}y^{(21)}(z)k^3- \\
& 21a_7y^{(5)}(z)k^2-36a_9y^{(7)}(z)k^2-55a_{11}y^{(9)}(z)k^2-78a_{13}y^{(11)}(z)k^2-105a_{15}y^{(13)}(z)k^2-136a_{17}y^{(15)}(z)k^2- \\
& 171a_{19}y^{(17)}(z)k^2-210a_{21}y^{(19)}(z)k^2-253a_{23}y^{(21)}(z)k^2-6a_6y^{(5)}(z)k-8a_8y^{(7)}(z)k-10a_{10}y^{(9)}(z)k- \\
& 12a_{12}y^{(11)}(z)k-14a_{14}y^{(13)}(z)k-16a_{16}y^{(15)}(z)k-18a_{18}y^{(17)}(z)k-20a_{20}y^{(19)}(z)k-22a_{22}y^{(21)}(z)k- \\
& 24a_{24}y^{(23)}(z)k+(a_1-C0+k(k(4a_4+k(5a_5+k(k(8a_8+k(9a_9+k(k(12a_{12}+k(13a_{13}+k(k(24a_{14}+ \\
& (a_3+k(k(20a_6+k(35a_7+k(k(120a_{10}+k(165a_{11}+k(k(364a_{14}+k(-2024a_{24}k^9+1771a_{23}k^8+
\end{aligned}$$

$$a_5y^{(5)}(z) + a_7y^{(7)}(z) + a_9y^{(9)}(z) + a_{11}y^{(11)}(z) + a_{13}y^{(13)}(z) + a_{15}y^{(15)}(z) + a_{17}y^{(17)}(z) + a_{19}y^{(19)}(z) + a_{21}y^{(21)}(z) + a_{23}y^{(23)}(z) = 0$$

Real part of equation after substitutions:

$$\begin{aligned} &10626a_{24}y^{(4)}(z)k^{20} - 8855a_{23}y^{(4)}(z)k^{19} - 7315a_{22}y^{(4)}(z)k^{18} - 134596a_{24}y^{(6)}(z)k^{18} + 5985a_{21}y^{(4)}(z)k^{17} + \\ &100947a_{23}y^{(6)}(z)k^{17} + 4845a_{20}y^{(4)}(z)k^{16} + 74613a_{22}y^{(6)}(z)k^{16} + 735471a_{24}y^{(8)}(z)k^{16} - 3876a_{19}y^{(4)}(z)k^{15} - \\ &54264a_{21}y^{(6)}(z)k^{15} - 490314a_{23}y^{(8)}(z)k^{15} - 3060a_{18}y^{(4)}(z)k^{14} - 38760a_{20}y^{(6)}(z)k^{14} - 319770a_{22}y^{(8)}(z)k^{14} - \\ &1961256a_{24}y^{(10)}(z)k^{14} + 2380a_{17}y^{(4)}(z)k^{13} + 27132a_{19}y^{(6)}(z)k^{13} + 203490a_{21}y^{(8)}(z)k^{13} + 1144066a_{23}y^{(10)}(z)k^{13} + \\ &1820a_{16}y^{(4)}(z)k^{12} + 18564a_{18}y^{(6)}(z)k^{12} + 125970a_{20}y^{(8)}(z)k^{12} + 646646a_{22}y^{(10)}(z)k^{12} + 2704156a_{24}y^{(12)}(z)k^{12} - \\ &1365a_{15}y^{(4)}(z)k^{11} - 12376a_{17}y^{(6)}(z)k^{11} - 75582a_{19}y^{(8)}(z)k^{11} - 352716a_{21}y^{(10)}(z)k^{11} - 1352078a_{23}y^{(12)}(z)k^{11} - \\ &1001a_{14}y^{(4)}(z)k^{10} - 8008a_{16}y^{(6)}(z)k^{10} - 43758a_{18}y^{(8)}(z)k^{10} - 184756a_{20}y^{(10)}(z)k^{10} - 646646a_{22}y^{(12)}(z)k^{10} - \\ &1961256a_{24}y^{(14)}(z)k^{10} + 715a_{13}y^{(4)}(z)k^9 + 5005a_{15}y^{(6)}(z)k^9 + 24310a_{17}y^{(8)}(z)k^9 + 92378a_{19}y^{(10)}(z)k^9 + \\ &293930a_{21}y^{(12)}(z)k^9 + 817190a_{23}y^{(14)}(z)k^9 + 495a_{12}y^{(4)}(z)k^8 + 3003a_{14}y^{(6)}(z)k^8 + 12870a_{16}y^{(8)}(z)k^8 + \\ &43758a_{18}y^{(10)}(z)k^8 + 125970a_{20}y^{(12)}(z)k^8 + 319770a_{22}y^{(14)}(z)k^8 + 735471a_{24}y^{(16)}(z)k^8 - 330a_{11}y^{(4)}(z)k^7 - \\ &1716a_{13}y^{(6)}(z)k^7 - 6435a_{15}y^{(8)}(z)k^7 - 19448a_{17}y^{(10)}(z)k^7 - 50388a_{19}y^{(12)}(z)k^7 - 116280a_{21}y^{(14)}(z)k^7 - \\ &245157a_{23}y^{(16)}(z)k^7 - 210a_{10}y^{(4)}(z)k^6 - 924a_{12}y^{(6)}(z)k^6 - 3003a_{14}y^{(8)}(z)k^6 - 8008a_{16}y^{(10)}(z)k^6 - \\ &18564a_{18}y^{(12)}(z)k^6 - 38760a_{20}y^{(14)}(z)k^6 - 74613a_{22}y^{(16)}(z)k^6 - 134596a_{24}y^{(18)}(z)k^6 + 126a_9y^{(4)}(z)k^5 + \\ &462a_{11}y^{(6)}(z)k^5 + 1287a_{13}y^{(8)}(z)k^5 + 3003a_{15}y^{(10)}(z)k^5 + 6188a_{17}y^{(12)}(z)k^5 + 11628a_{19}y^{(14)}(z)k^5 + \\ &20349a_{21}y^{(16)}(z)k^5 + 33649a_{23}y^{(18)}(z)k^5 + 70a_8y^{(4)}(z)k^4 + 210a_{10}y^{(6)}(z)k^4 + 495a_{12}y^{(8)}(z)k^4 + \\ &1001a_{14}y^{(10)}(z)k^4 + 1820a_{16}y^{(12)}(z)k^4 + 3060a_{18}y^{(14)}(z)k^4 + 4845a_{20}y^{(16)}(z)k^4 + 7315a_{22}y^{(18)}(z)k^4 + \\ &10626a_{24}y^{(20)}(z)k^4 - 35a_7y^{(4)}(z)k^3 - 84a_9y^{(6)}(z)k^3 - 165a_{11}y^{(8)}(z)k^3 - 286a_{13}y^{(10)}(z)k^3 - 455a_{15}y^{(12)}(z)k^3 - \\ &680a_{17}y^{(14)}(z)k^3 - 969a_{19}y^{(16)}(z)k^3 - 1330a_{21}y^{(18)}(z)k^3 - 1771a_{23}y^{(20)}(z)k^3 - 15a_6y^{(4)}(z)k^2 - \\ &28a_8y^{(6)}(z)k^2 - 45a_{10}y^{(8)}(z)k^2 - 66a_{12}y^{(10)}(z)k^2 - 91a_{14}y^{(12)}(z)k^2 - 120a_{16}y^{(14)}(z)k^2 - 153a_{18}y^{(16)}(z)k^2 - \\ &190a_{20}y^{(18)}(z)k^2 - 231a_{22}y^{(20)}(z)k^2 - 276a_{24}y^{(22)}(z)k^2 + 5a_5y^{(4)}(z)k + 7a_7y^{(6)}(z)k + 9a_9y^{(8)}(z)k + \\ &11a_{11}y^{(10)}(z)k + 13a_{13}y^{(12)}(z)k + 15a_{15}y^{(14)}(z)k + 17a_{17}y^{(16)}(z)k + 19a_{19}y^{(18)}(z)k + 21a_{21}y^{(20)}(z)k + \\ &23a_{23}y^{(22)}(z)k - by(z)^3 + (a_{24}k^{24} - a_{23}k^{23} - a_{22}k^{22} + a_{21}k^{21} + a_{20}k^{20} - a_{19}k^{19} - a_{18}k^{18} + a_{17}k^{17} + a_{16}k^{16} - a_{15}k^{15} \\ &(a_2 + k(3a_3 + k(k(15a_6 + k(21a_7 + k(k(45a_{10} + k(55a_{11} + k(k(91a_{14} + k(-276a_{24}k^9 + 253a_{23}k^8 \\ &a_4y^{(4)}(z) + a_6y^{(6)}(z) + a_8y^{(8)}(z) + a_{10}y^{(10)}(z) + a_{12}y^{(12)}(z) + a_{14}y^{(14)}(z) + a_{16}y^{(16)}(z) + a_{18}y^{(18)}(z) + \\ &a_{20}y^{(20)}(z) + a_{22}y^{(22)}(z) + a_{24}y^{(24)}(z)) = 0 \end{aligned}$$

Constraints on coefficients from imaginary part of equation:

$$a_{23} \rightarrow 24a_{24}k$$

$$a_{21} \rightarrow 22a_{22}k + 4048a_{24}k^3$$

$$a_{19} \rightarrow 20a_{20}k + 3080a_{22}k^3 + 680064a_{24}k^5$$

$$a_{17} \rightarrow 18a_{18}k + 2280a_{20}k^3 + 421344a_{22}k^5 + 94140288a_{24}k^7$$

$$a_{15} \rightarrow 16a_{16}k + 1632a_{18}k^3 + 248064a_{20}k^5 + 46387968a_{22}k^7 + 10376351744a_{24}k^9$$

$$\begin{aligned}
a_{13} &\rightarrow 14a_{14}k + 1120a_{16}k^3 + 137088a_{18}k^5 + 21085440a_{20}k^7 + 3947525120a_{22}k^9 + 883115778048a_{24}k^{11} \\
a_{11} &\rightarrow 12a_{12}k + 728a_{14}k^3 + 69888a_{16}k^5 + 8656128a_{18}k^7 + 1332930560a_{20}k^9 + 249576198144a_{22}k^{11} + \\
&55834388004864a_{24}k^{13} \\
a_9 &\rightarrow 10a_{10}k + 440a_{12}k^3 + 32032a_{14}k^5 + 3111680a_{16}k^7 + 385848320a_{18}k^9 + 59422904320a_{20}k^{11} + \\
&11126417899520a_{22}k^{13} + 2489170300469248a_{24}k^{15} \\
a_7 &\rightarrow 240a_{10}k^3 + 12672a_{12}k^5 + 933504a_{14}k^7 + 90787840a_{16}k^9 + 11259076608a_{18}k^{11} + 1733987205120a_{20}k^{13} + \\
&324674387017728a_{22}k^{15} + 72635234665365504a_{24}k^{17} + 8a_8k \\
a_5 &\rightarrow 4032a_{10}k^5 + 215424a_{12}k^7 + 15887872a_{14}k^9 + 1545363456a_{16}k^{11} + 191651217408a_{18}k^{13} + \\
&29515853365248a_{20}k^{15} + 5526593941929984a_{22}k^{17} + 1236393972835811328a_{24}k^{19} + 6a_6k + 112a_8k^3 \\
a_3 &\rightarrow 32640a_{10}k^7 + 1745920a_{12}k^9 + 128780288a_{14}k^{11} + 12526223360a_{16}k^{13} + 1553465966592a_{18}k^{15} + \\
&239246490992640a_{20}k^{17} + 44796883073761280a_{22}k^{19} + 10021832059523170304a_{24}k^{21} + 4a_4k + \\
&40a_6k^3 + 896a_8k^5 \\
C0 &\rightarrow a_1 - 79360a_{10}k^9 - 4245504a_{12}k^{11} - 313155584a_{14}k^{13} - 30460116992a_{16}k^{15} - 3777576173568a_{18}k^{17} - \\
&2a_2k - 581777702256640a_{20}k^{19} - 108932957168730112a_{22}k^{21} - 24370173276164456448a_{24}k^{23} - \\
&8a_4k^3 - 96a_6k^5 - 2176a_8k^7 \\
\text{Constraints on coefficients from real part of equation:} \\
b &\rightarrow \frac{258867142816712385002471424000000a_{24}\chi^{12}}{A^2} \\
a_{22} &\rightarrow -276a_{24}k^2 - 6920a_{24} \\
a_{20} &\rightarrow 10626a_{24}k^4 + 1598520a_{24}k^2 + 21332080a_{24} \\
a_{18} &\rightarrow -134596a_{24}k^6 - 50619800a_{24}k^4 - 4053095200a_{24}k^2 - 38682744320a_{24} \\
a_{16} &\rightarrow 735471a_{24}k^8 + 516321960a_{24}k^6 + 103353927600a_{24}k^4 + 5918459880960a_{24}k^2 + 45889768165120a_{24} \\
a_{14} &\rightarrow -1961256a_{24}k^{10} - 2212808400a_{24}k^8 - 826831420800a_{24}k^6 - 118369197619200a_{24}k^4 - \\
&5506772179814400a_{24}k^2 - 37462825494456320a_{24} \\
a_{12} &\rightarrow 2704156a_{24}k^{12} + 4474790320a_{24}k^{10} + 2687202117600a_{24}k^8 + 718106465556480a_{24}k^6 + \\
&83519378060518400a_{24}k^4 + 3409117119995525120a_{24}k^2 + 21546002383306854400a_{24} \\
a_{10} &\rightarrow -1961256a_{24}k^{14} - 4474790320a_{24}k^{12} - 3941229772480a_{24}k^{10} - 1692679525954560a_{24}k^8 - \\
&367485263466280960a_{24}k^6 - 37500288319950776320a_{24}k^4 - 1422036157298252390400a_{24}k^2 - 87815133500866 \\
a_8 &\rightarrow 735471a_{24}k^{16} + 2212808400a_{24}k^{14} + 2687202117600a_{24}k^{12} + 1692679525954560a_{24}k^{10} + \\
&590601316285094400a_{24}k^8 + 112500864959852328960a_{24}k^6 + 10665271179736892928000a_{24}k^4 + \\
&395168100753899800166400a_{24}k^2 + 2512903900229278907760640a_{24} \\
a_6 &\rightarrow -134596a_{24}k^{18} - 516321960a_{24}k^{16} - 826831420800a_{24}k^{14} - 718106465556480a_{24}k^{12} - \\
&367485263466280960a_{24}k^{10} - 112500864959852328960a_{24}k^8 - 19908506202175533465600a_{24}k^6 - \\
&1844117803518199067443200a_{24}k^4 - 70361309206419809417297920a_{24}k^2 - 491495535786667276574392320a_{24} \\
a_4 &\rightarrow 10626a_{24}k^{20} + 50619800a_{24}k^{18} + 103353927600a_{24}k^{16} + 118369197619200a_{24}k^{14} + 83519378060518400a_{24}k^{12}
\end{aligned}$$

$$\begin{aligned}
& 37500288319950776320a_{24}k^{10}+10665271179736892928000a_{24}k^8+1844117803518199067443200a_{24}k^6+175903273016049523543244800a_{24}k^4+7372433036800009148615884800a_{24}k^2+6225462009658990373957428 \\
& a_2 \rightarrow -276a_{24}k^{22}-1598520a_{24}k^{20}-4053095200a_{24}k^{18}-5918459880960a_{24}k^{16}-5506772179814400a_{24}k^{14}-3409117119995525120a_{24}k^{12}-1422036157298252390400a_{24}k^{10}-395168100753899800166400a_{24}k^8-70361309206419809417297920a_{24}k^6-7372433036800009148615884800a_{24}k^4-37352772057953942243744573 \\
& 4576576829303784219511829299200a_{24} \\
& \omega \rightarrow -a_1k-23a_{24}k^{24}-145320a_{24}k^{22}-405309520a_{24}k^{20}-657606653440a_{24}k^{18}-688346522476800a_{24}k^{16}-487016731427932160a_{24}k^{14}-237006026216375398400a_{24}k^{12}-79033620150779960033280a_{24}k^{10}-17590327301604952354324480a_{24}k^8-2457477678933336382871961600a_{24}k^6-18676386028976971121872286 \\
& 4576576829303784219511829299200a_{24}k^2 + 147398965045111810582370058240000a_{24}
\end{aligned}$$

y(z) - function:

$$\frac{16777216a^{12}A}{(4a^2e^z + \chi e^{-z})^{12}}$$

u(x, t) - function:

$$\frac{16777216a^{12}Ae^{i(kx-\omega t)}}{(4a^2e^{C0t+x} + \chi e^{-C0t-x})^{12}}$$