

Target equation:

$$-ia_1u^{(1,0)}(x,t) + a_{10}u^{(10,0)}(x,t) + a_2u^{(2,0)}(x,t) - ia_3u^{(3,0)}(x,t) + a_4u^{(4,0)}(x,t) - ia_5u^{(5,0)}(x,t) + a_6u^{(6,0)}(x,t) - ia_7u^{(7,0)}(x,t) + a_8u^{(8,0)}(x,t) - ia_9u^{(9,0)}(x,t) - bu(x,t)|u(x,t)|^2 + iu^{(0,1)}(x,t) = 0$$

Substitutions:

$$N = 5$$

$$u(x,t) \rightarrow y(z)e^{i(kx-\omega t)}$$

$$z \rightarrow x - C_0t$$

$$y(z) \rightarrow AR(z)^5$$

$$R'(z)^2 = R(z)^2 (1 - \chi R(z)^2)$$

Imaginary part of equation after substitutions:

$$y'(z) (a_1 - 10a_{10}k^9 - 2a_2k - 3a_3k^2 + 4a_4k^3 + 5a_5k^4 - 6a_6k^5 - 7a_7k^6 + 8a_8k^7 + 9a_9k^8 - C_0) + y^{(3)}(z) (120a_{10}k^5y^{(5)}(z) + 120a_{10}k^3y^{(7)}(z) - 10a_{10}ky^{(9)}(z) + a_5y^{(5)}(z) - 6a_6ky^{(5)}(z) - 21a_7k^2y^{(5)}(z) + a_7y^{(7)}(z) + 56a_8k^3y^{(5)}(z) - 8a_8ky^{(7)}(z) + 126a_9k^4y^{(5)}(z) - 36a_9k^2y^{(7)}(z) + a_9y^{(9)}(z) = 0$$

Real part of equation after substitutions:

$$y(z) (a_1k - a_{10}k^{10} - a_2k^2 - a_3k^3 + a_4k^4 + a_5k^5 - a_6k^6 - a_7k^7 + a_8k^8 + a_9k^9 + \omega) + y''(z) (45a_{10}k^8 + a_2 + 3a_3k - 210a_{10}k^6y^{(4)}(z) + 210a_{10}k^4y^{(6)}(z) - 45a_{10}k^2y^{(8)}(z) + a_{10}y^{(10)}(z) + a_4y^{(4)}(z) + 5a_5ky^{(4)}(z) - 15a_6k^2y^{(4)}(z) + a_6y^{(6)}(z) - 35a_7k^3y^{(4)}(z) + 7a_7ky^{(6)}(z) + 70a_8k^4y^{(4)}(z) - 28a_8k^2y^{(6)}(z) + a_8y^{(8)}(z) + 126a_9k^5y^{(4)}(z) - 84a_9k^3y^{(6)}(z) + 9a_9ky^{(8)}(z) - by(z)^3 = 0$$

Constraints on coefficients from imaginary part of equation:

$$a_9 \rightarrow 10a_{10}k$$

$$a_7 \rightarrow 8(30a_{10}k^3 + a_8k)$$

$$a_5 \rightarrow 2(2016a_{10}k^5 + 3a_6k + 56a_8k^3)$$

$$a_3 \rightarrow 4(8160a_{10}k^7 + a_4k + 10a_6k^3 + 224a_8k^5)$$

$$C_0 \rightarrow a_1 - 79360a_{10}k^9 - 2a_2k - 8a_4k^3 - 96a_6k^5 - 2176a_8k^7$$

Constraints on coefficients from real part of equation:

$$b \rightarrow -\frac{3632428800a_{10}\chi^5}{A^2}$$

$$a_8 \rightarrow -5a_{10}(9k^2 + 89)$$

$$a_6 \rightarrow 14(15a_{10}k^4 + 890a_{10}k^2 + 5187a_{10})$$

$$a_4 \rightarrow -10(21a_{10}k^6 + 3115a_{10}k^4 + 108927a_{10}k^2 + 536233a_{10})$$

$$a_2 \rightarrow 45a_{10}k^8 + 12460a_{10}k^6 + 1089270a_{10}k^4 + 32173980a_{10}k^2 + 176396581a_{10}$$

$$\omega \rightarrow -a_1k + 9a_{10}k^{10} + 3115a_{10}k^8 + 363090a_{10}k^6 + 16086990a_{10}k^4 + 176396581a_{10}k^2 - 2029052025a_{10}$$

y(z) - function:

$$\frac{1024a^5A}{(4a^2e^z + \chi e^{-z})^5}$$

u(x, t) - function:

$$\frac{1024a^5 A e^{i(kx - \omega t)}}{(4a^2 e^{C_0 t + x} + \chi e^{-C_0 t - x})^5}$$