Artificial Intelligence PBL-1

Classifier for MNIST with LR, and SVM

Team 4

Given Problem

- Problem : making an automated zipcode recognition system
- Main objective:

Find the best model out of the following settings:

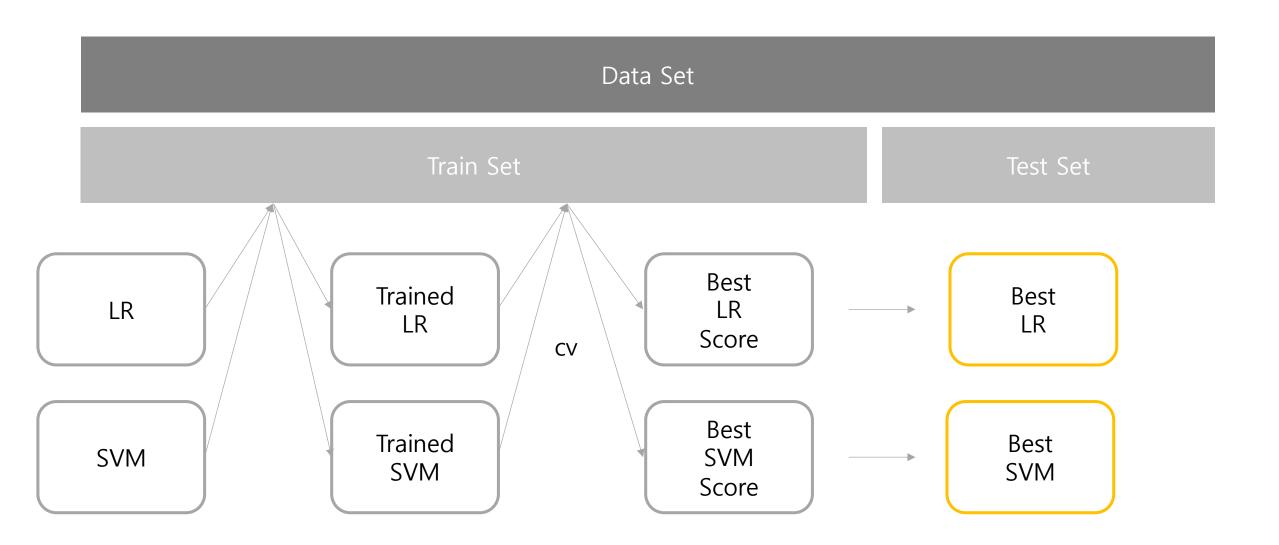
Classifiers: Logistic Regression and SVM

Data: 70k number(0~9) images of MNIST

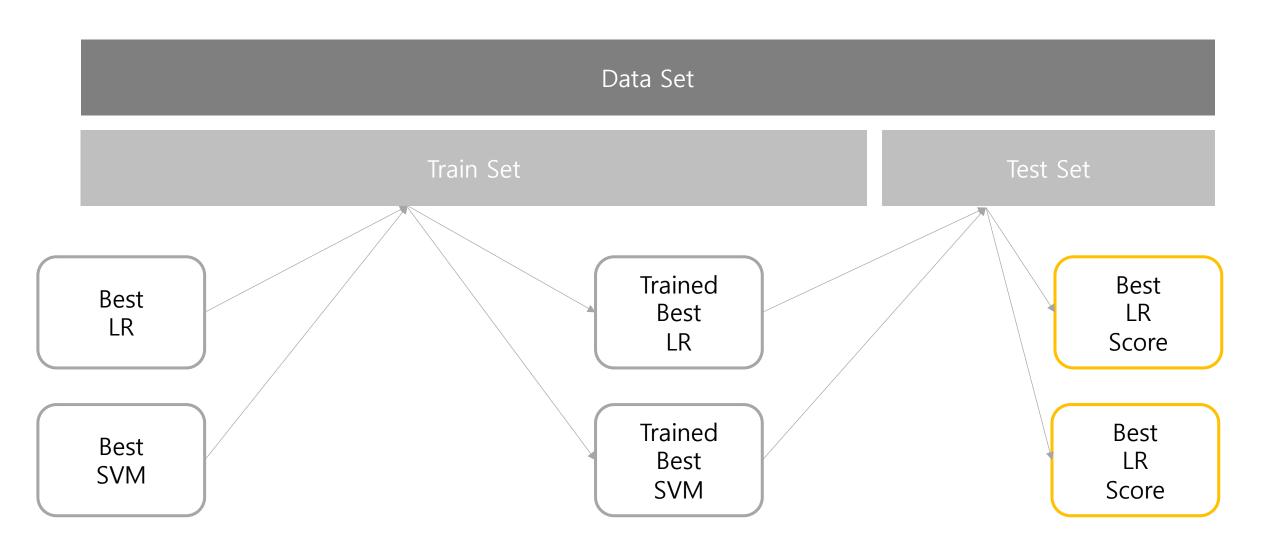
Criterion:

Model selection: f1-score(micro)

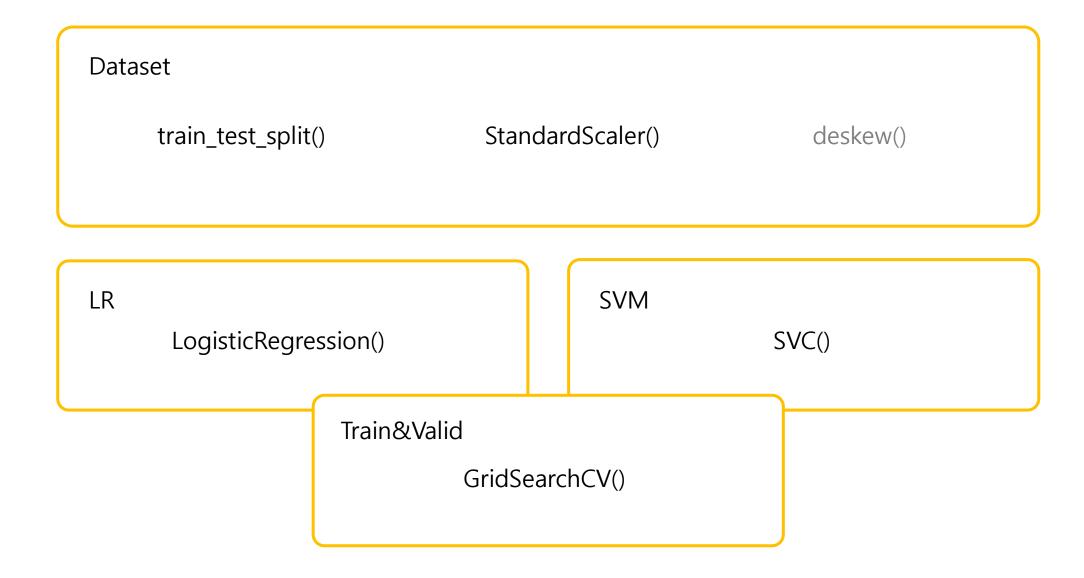
Test performance: f1-score(micro) of the final model on the test images



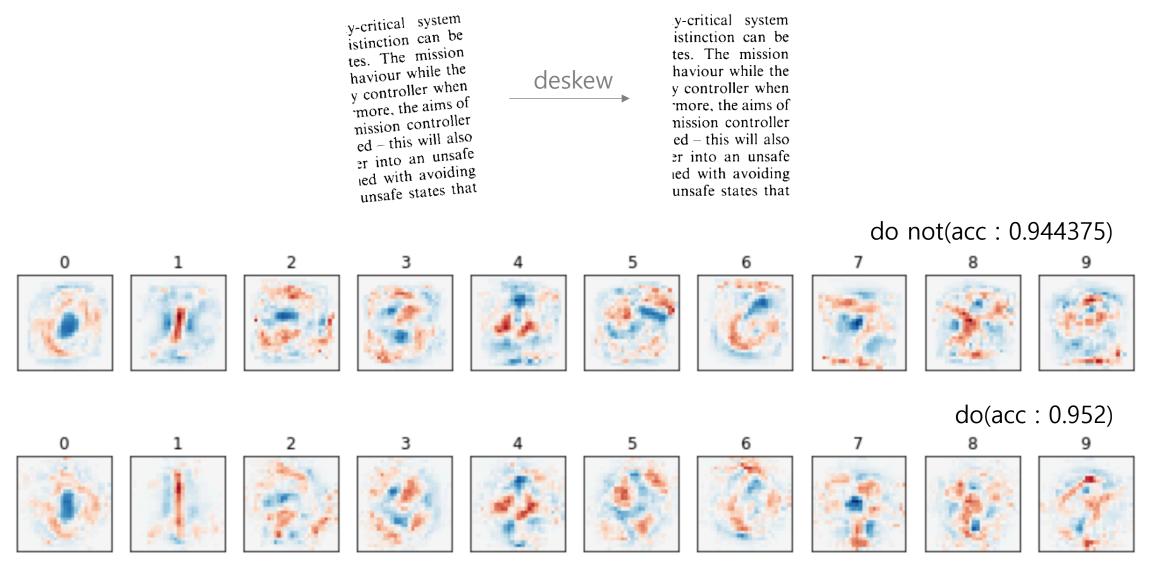
Solution



Solution



deskew()



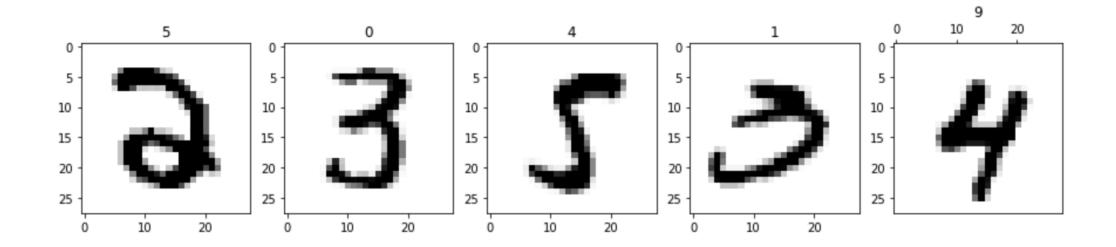
Logistic Regression C: 0.01, penalty: I2, solver: lbfgs

Dataset

MNIST DATA

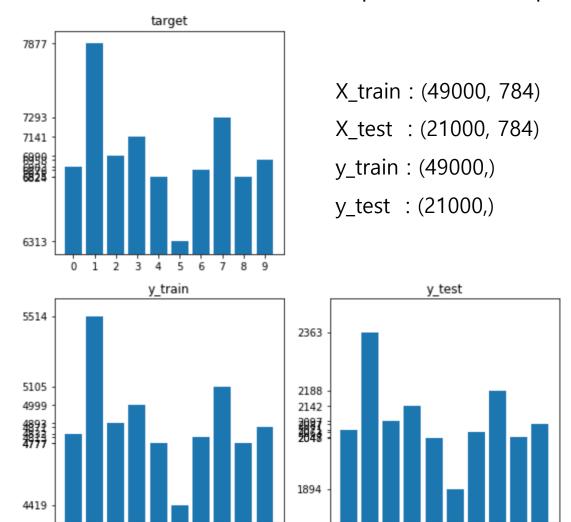
- 28x28 pixel
- pixel value range [0, 255]
- 70000 samples
- 786 features

- many pixel values are zero
- large '1's, small '5's
- no outlier, missing value



Dataset

from sklearn.model_selection import train_test_split



Dataset

from sklearn.preprocessing import StandardScaler

```
scaler = StandardScaler()
scaler.fit(X_train)
X_train = scaler.transform(X_train)
X_test = scaler.transfrom(X_test)
```

Scaler:

StandardScaler() # mean: 0, std: 1

MinMaxScaler() # max: 1, min: 0

RobustScaler() # median: 0, IQR: 1

Standard score :
$$\frac{X - \mu}{\sigma}$$
 Min-Max Feature scaling : $\frac{X - X_{min}}{X_{max} - X_{min}}$

GridSearchCV

from sklearn.model_selection import GridSearchCV

$$F_1 = \left(\frac{2}{recall^{-1} + precision^{-1}}\right) = 2 \cdot \left(\frac{precision \cdot recall}{precision + recall}\right)$$

- f1_score macro : Calculate metrics for each label, and find their unweighted mean.

 This does not take label imbalance into account.
 - micro: Calculate metrics globally by counting the total true positives,
 false negatives and false positives.
- cv : Determines the cross-validation splitting strategy.

1	2	3	4	5	6	7	8	9	10

Logistic Regression

```
parameters = {'solver':['saga'], 'penalty':['ll', 'l2'], 'C':[100.0, 10.0, 1.0, 0.1, 0.01]}

lc = LogisticRegression(multi_class='ovr')

clf = GridSearchCV(estimator=lc, param_grid=parameters, scoring='f1_micro', cv=10, n_jobs=-1)

clf.fit(X_train, y_train)
```

Support Vector Machine

```
parameters = {'kernel':['linear'], 'C':[100.0, 10.0, 1.0, 0.1, 0.01, 0.001]}

svc = SVC()
clf = GridSearchCV(estimator=svc, param_grid=parameters, scoring='f1_micro', cv=10, n_jobs=-1)
clf.fit(X_train, y_train)
```

LogisticRegression

from sklearn.linear_model import LogisticRegression

LogisticRegression(): Logistic Regression classifier.

- multi_class : ovr(one-vs-rest)
- penalty: l1, l2

$$\|x\|_{p} := (\sum_{i=1}^{n} |x_{i}|^{p})^{1/p}$$
 if $p = 1, |1|$ if $p = 2, |2|$

best parameter :

- C: 100.0, 10.0, 1.0, 0.1, 0.01
- solver : saga

$$w^{k+1} = w^k - \alpha(f'_j(w^k) - f'_j(\theta_j^k) + \frac{1}{n} \sum_{i=1}^n f'_i(\theta_i^k))$$

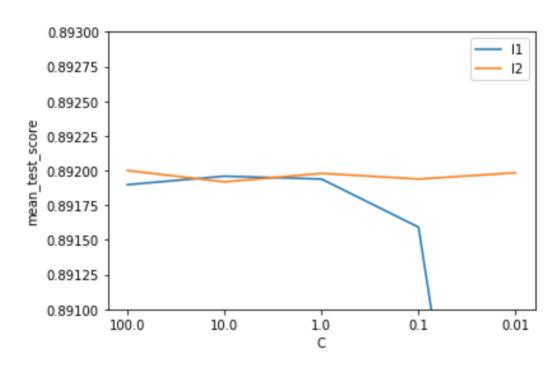
best score :

$$f1_micro = 0.892$$

Validation

- Logistic Regression

C f1		mean_test_score	mean_fit_time(min)	
1000	I 1	0.89189796	14	
100.0	12	0.892	10	
10.0	I 1	0.89195918	15	
10.0	12	0.89191837	10	
1.0	I 1	0.89193878	15	
	12	0.89197959	10	
0.1	I 1	0.89159184	16	
0.1	12	0.89193878	10	
0.01	I 1	0.88708163	14	
	12	0.8919837	11	



Intel Xeon, RAM 13GB

SupportVectorMachine

from sklearn.svm import SVC

SVC(): C-Support Vector Classification

- kernel : linear

- C: 100.0, 10.0, 1.0, 0.1, 0.01, 0.001

best parameter :

C = 0.01

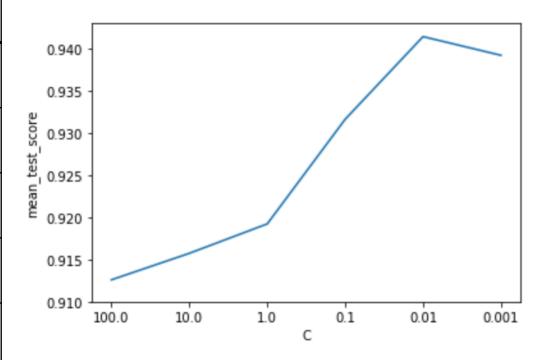
best score :

 $f1_{micro} = 0.94155102$

Validation

- SVM

C £1	mean_test_score	mean_fit_time(min)
100.0	0.91259184	215
10.0	0.91573469	23
1.0	0.91922449	10
0.1	0.93163265	9
0.01	0.94144102	9
0.001	0.93922449	11



AMD 2700x, RAM 32GB

Test

LR

multi_class = ovr

penalty = 12

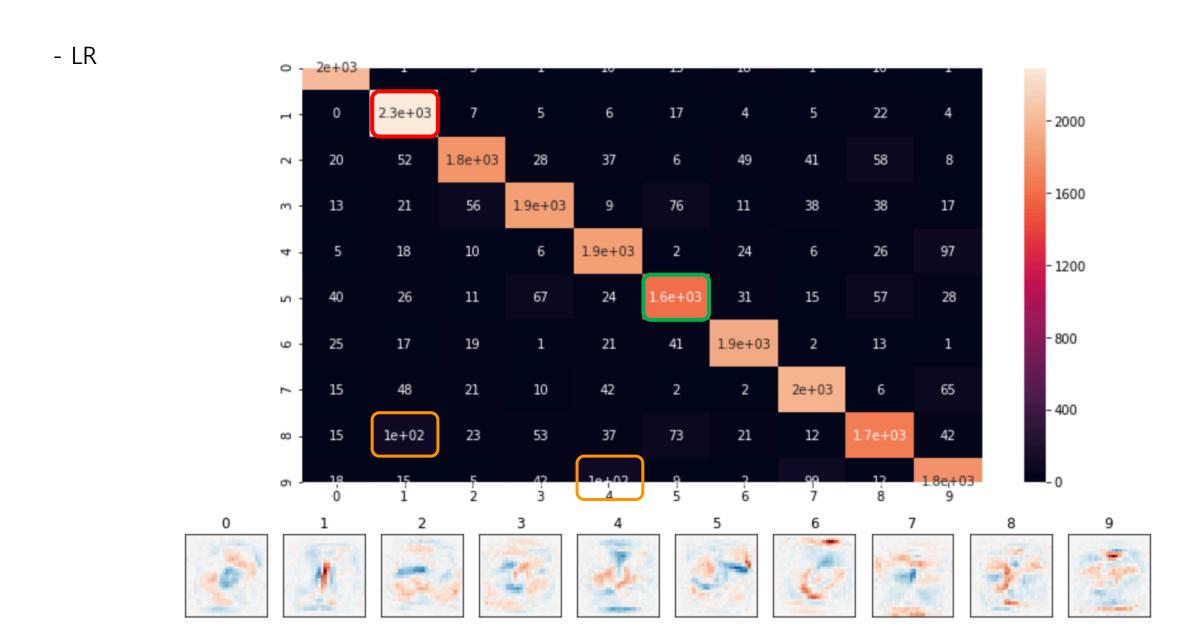
C = 100.0

solver = saga

SV M

kernel = linear

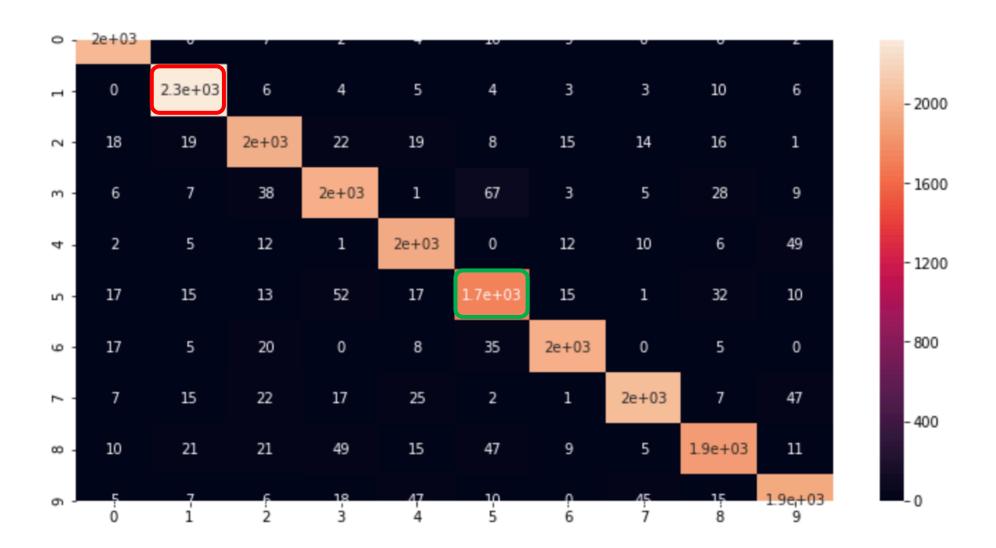
C = 0.01



- LR

	precision	recall	f1-score	support
0	0.93	0.97	0.95	2071
1	0.88	0.97	0.93	2363
2	0.92	0.86	0.89	2097
3	0.90	0.87	0.88	2142
4	0.87	0.90	0.89	2047
5	0.87	0.84	0.86	1894
6	0.92	0.93	0.93	2063
7	0.90	0.90	0.90	2188
8	0.87	0.82	0.84	2048
9	0.87	0.86	0.86	2087
micro avg	0.89	0.89	0.89	21000
macro avg	0.89	0.89	0.89	21000
weighted avg	0.89	0.89	0.89	21000

- SVM



- SVM

	precision	recall	f1-score	support
0	0.96	0.98	0.97	2071
1	0.96	0.98	0.97	2363
2	0.93	0.94	0.93	2097
3	0.92	0.92	0.92	2142
4	0.93	0.95	0.94	2047
5	0.90	0.91	0.91	1894
6	0.97	0.96	0.96	2063
7	0.96	0.93	0.95	2188
8	0.94	0.91	0.92	2048
9	0.93	0.93	0.93	2087
micro avg	0.94	0.94	0.94	21000
macro avg	0.94	0.94	0.94	21000
weighted avg	0.94	0.94	0.94	21000

- micro

	Accuracy	Precision	Recall	F1-score
LR	0.893619	0.893619	0.893619	0.893619
SVM	0.941905	0.941905	0.941905	0.941905

- macro

	Accuracy	Precision	Recall	F1-score
LR	0.893524	0.89332	0.892042	0.892141
SVM	0.941905	0.941301	0.941153	0.941147

$$ACC = \frac{TP + TN}{ALL} \qquad PRE_{micro} = \frac{TP_1 + \dots + TP_k}{TP_1 + \dots + TP_k + FP_1 + \dots + FP_k} \qquad REC_{micro} = \frac{TP_1 + \dots + TP_k}{TP_1 + \dots + TP_k + FN_1 + \dots + FN_k} \qquad F1 = 2 \cdot \frac{PRE \times REC}{PRE + REC}$$

$$REC_{micro} = \frac{TP_1 + \dots + TP_k}{TP_1 + \dots + TP_k + FN_1 + \dots + FN_k}$$

$$F1 = 2 \cdot \frac{PRE \times REC}{PRE + REC}$$

Question and Answer

Thank you