

Problem Set 7

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I worked on this PS with JungWoo Hong

Question 0:

0A: Yes, I followed the honor code on this problem set.

0B: 6hrs

Question 1:

Question 1A: $B \geq A \geq D \geq C$

Question 1B: $c \geq a \geq d \geq b$

Question 1C: This is prisoner's dilemma.

Question 2:

Question 2A:

$$MR_1 = 300q_1 - 4q_1 - 2q_2$$

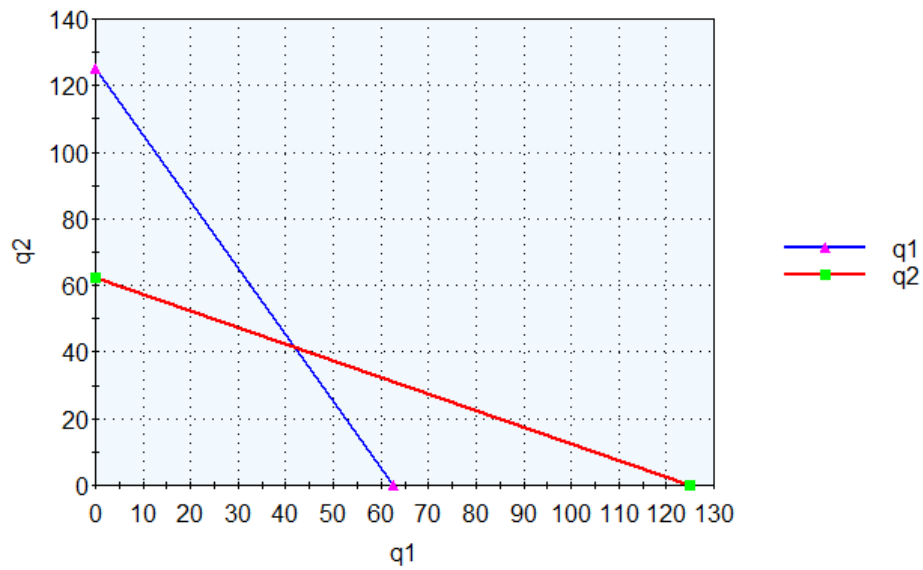
$$MR_1 = MC_1$$

$$300q_1 - 4q_1 - 2q_2 = 50$$

$$BR_1 = q_1 = 62.5 - \left(\frac{1}{2}\right)q_2$$

$$BR_2 = q_2 = 62.5 - \left(\frac{1}{2}\right)q_1$$

Best Response Functions



(I worked on this graph with Asli Mumtaz and Jungwoo Hong)

Question 2B:

$$q_1 = 62.5 - \left(\frac{1}{2}\right)q_2$$

$$q_1 = 62.5 - \left(\frac{1}{2}\right)[62.5 - \left(\frac{1}{2}\right)q_1]$$

$$q_1 = 41.67$$

$$q_2 = 41.67$$

Question 2C:

$$P = 300 - 2(Q)$$

$$P = 300 - 2(2 \cdot 41.67)$$

$$P = 133.32$$

$$\text{Profit}_1 = q_1(P - MC_1)$$

$$\text{Profit}_1^* = 41.67(133.32 - 50)$$

$$\text{Profit}_1^* = 3471.9444$$

$$\text{Profit}_2^* = 3471.9444$$

Question 2D:

$$MC_1 = 40, MC_2 = 50$$

$$MR_1 = MC_1$$

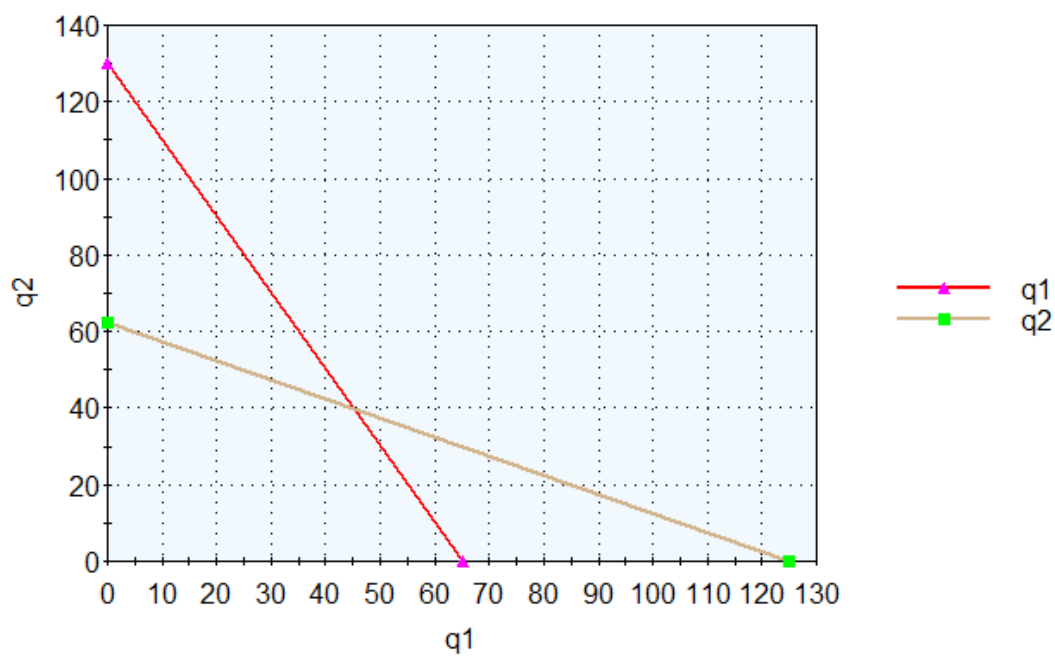
$$300 - 4q_1 - 2q_2 = 40$$

$$BR_1 = q_1 = 65 - (1/2)q_2$$

$$MR_2 = MC_2$$

$$BR_2 = q_2 = 62.5 - (1/2)q_1$$

Best Response Functions



(I worked on this graph with Asli Mumtaz and Jungwoo Hong)

Question 2E:

$$q_1 = 65 - \left(\frac{1}{2}\right)q_2$$

$$q_1 = 65 - \left(\frac{1}{2}\right)[62.5 - \left(\frac{1}{2}\right)q_1]$$

$$\mathbf{q_1 = 45}$$

$$\mathbf{q_2 = 40}$$

Question 2F:

$$P = 300 - 2(45 + 40)$$

$$P = 130$$

$$\text{Profit}_1 = q_1(P - MC_1)$$

$$\text{Profit}_1 = 45(130 - 40)$$

$$\mathbf{\text{Profit}_1 = 4050}$$

$$\text{Profit}_2 = q_2(P - MC_2)$$

$$\text{Profit}_2 = 40(130 - 50)$$

$$\mathbf{\text{Profit}_2 = 3200}$$

Question 2G:

Firm1 makes profit of \$3471.94 at MC=50 and makes profit of \$4050 at MC = 40.

Therefore, it would be willing to pay (\$4050 - \$3471.94) \$578 to upgrade its factory.