UM-SJTU Joint Institute

Physics Laboratory

(Vp141)

Laboratory Report

Exercise 2

Measurement of Fluid Viscosity

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**1. Introduction**

The objective of this experiment is to quantitatively express the fluid viscosity using the Stoke’s method. A moving object in a fluid receives a drag force which is related to both the physical property of the object and the property of the fluid. It also undergoes gravity and buoyancy force. By measuring some of the physical quantities and comparing these three forces we can express the viscosity coefficient η.

**2. Theoretical Background**

* A spherical object with radius R and speed v in an infinitely long cylindrical container with radius Rc receives a linear drag force, of which the direction is opposite to its velocity and the magnitude of it is:
* The magnitude of the upward buoyancy force it is acted upon is:

where is the density of the fluid.

* The downward weight of the object can be expressed by

where m is the mass of the object.

* By substituting for v and solving the relational expression, we get the final expression of

**3. Experimental Setup**

The experimental setup is shown in figure 1.

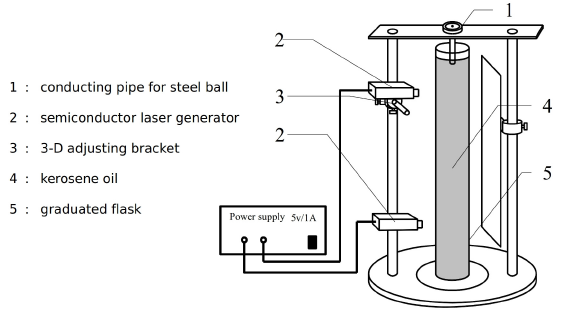


Figure 1 Stoke’s viscosity measurement apparatus.

The experimental equipment is fixed on an iron support. A graduated flask is placed on the center with castor oil in it. The two semiconductor laser generators on the left are on the same vertical line. The laser they send out can travel through the fluid. The steel ball is dropped through the conducting pipe on the top.

For physical quantities measurement, a micrometer is used to measure the diameter of the steel ball. A caliper is used to measure the inner diameter of the graduated flask. A densimeter is used to measure the density of the castor oil. The mass of the steel ball is measured by an electronic scale. A ruler is used to measure the distance between the two laser beams. A stopwatch is used to measure the time cost by the ball travelling through the interval of the two laser beams. A thermometerplaced in castor oil is used to measure the environment temperature.

The information of each measurement device is shown in Table 1.

|  |  |  |  |
| --- | --- | --- | --- |
| apparatus | range | Minimum scale of value | Maximum uncertainty |
| Micrometer | 25.00mm | 0.01mm | 0.005mm |
| Caliper | 125.00mm | 0.02mm | 0.02mm |
| Densimeter | 0.900 ~1.000 g/ | 0.001g/ | 0.0005 g/ |
| Electronic scale | / | 0.001g | 0.001g |
| Ruler | 300mm | 1mm | 0.5mm |
| stopwatch | / | 0.01s | 0.01s |
| Thermometer | 0~100.0 | 0.1 | 0.1 |

Table 1 Information of Each Measurement Device

**4. Measurements**

The physical quantities we need for calculation are:

Environmental factors: temperature **T**, fluid density, acceleration due to gravity **g**,

inner diameter of the graduated flask **D**

Ball properties: diameter of the ball **d**, the mass of one ball **m**

Ball velocity **v**: the distance traveled **s**, time **t**

**4.1 Environmental factors measurement**

1. Read and record the reading of the thermometer placed in castor oil.

2. Read and record the reading of the densimeter.

3. Use a caliper to measure the inner diameter of the graduated flask for 6 times. Record all the readings.

**4.2 Ball properties measurement**

1. Use the electronic scale to measure the mass of 40 steel balls. Record the reading m.

2. Use a micrometer to measure the diameter of one steel ball for 10 times. Record each reading

To measure the mass of one ball, we choose to measure the total mass of 40 balls and then divide it by 40. In this step we have assumed that every ball is of the same size and mass. If the specifications of the balls are different, there will exist errors.

**4.3 Ball velocity measurement**

1. Hang a plumb line from the top and check whether its tip points to the center of the plate to make sure that the platform is on a horizontal plane. Then the graduated flask is placed on the center of the iron support.

2. The power supply is turned on, and the generator sets off two laser beams. Erect a ruler with its side facing the laser beams. Record the two readings where the two laser beams points at. Repeat this step for 6 times. In this step, we record the two readings and then subtract them to get the distance the ball travels.

3. One ball is dropped from the conducting pipe each time. The timer is started as soon as the ball passes the first laser beam and is stopped when the ball passes the second beam.

4. Repeat step 3 until 6 sets of valid time are recorded.

In step 2, there existing two spot on the ruler means that the two laser generators are at the same vertical line. Since the ball has a small possibility to follow a route that exactly intersects with the range of the laser beam, step 3 must be repeated several times to achieve 6 valid time lengths. What’s more, error exists in this step because the time is recorded by human who has reaction time. There might be inaccuracy in measuring the time.

**5. Results**

**5.1 Environmental Factors Measurement**

Fluid density:0.956±0.0005g/=956

Temperature: **T**= 26.8±0.1

Acceleration due to gravity (given by instructor): **g** =9.81m/

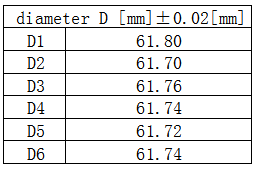


Table 2 Measurement data for the inner diameter of the flask

From table 2 we get the average inner diameter of the flask is:

Consider the uncertainty, we get **D**= 61.740.04mm=(6.174

**5.2 Ball Density Measurement**

**5.2.1 The diameter of the ball**

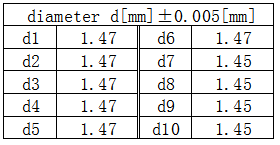
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Table 3 Measurement data for the diameter of the balls

From table 3 we get the average diameter of the ball is:

Consider the uncertainty, we get **d**= 1.460.008mm=(1.46

**5.2.2 The mass of one ball**

Mass of 40 metal balls M =1.31±0.001g=(1.31

Consider the uncertainty, the mass of one ball **m**=

**5.3 Ball Velocity Measurement**

**5.3.1 The distance traveled**

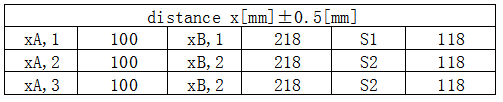


Table 4 Distance measurement data

The data in the last column are the results of the data in the second column subtracting from the data in the fourth column.

From the table we can get the average distance the ball travels is:

Consider the uncertainty, we get **S**= 1180.5mm=0.118

**5.3.2 The time cost**

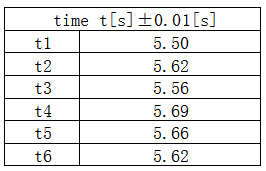


Table 5 Time measurement data

From table 5 we can get the average time the ball travels is:

Consider the uncertainty, we get **t** =5.610.05s.

**5.3.2 The velocity of the ball**

User equation v=, we get 21.03m/s,

Consider the uncertainty, we get the velocity of the ball

**v**=21.03=(2.103

**5.4 Calculation of the fluid viscosity**

According to equation (1)

=1.0006kg/m

Consider the uncertainty, we get the viscosity of the fluid is

0.0318 kg/m

**6. Conclusions and discussion**

In this experiment, we apply the knowledge of stoke’s method and measured the viscosity of castor oil at t=26.8, which is 0.0318 kg/m.

According to authoritative data, the viscosity of castor oil at T=300K is 0.650 kg/m, which indicates that our experimental data is larger than standard. Below is the error analysis.

* As our experimental data is relative larger, considering equation (1) we assume the radius of the ball might be measured smaller than reality. This error might result from the misuse of the micrometer. For example, the ball might not be put onto the anvil entirely so that the reading was smaller than its diameter. The density of the ball calculated using the experimental data is 20g/, which is too big and proves the possibility of this error.
* Error might also exist if the ball had not reached the constant velocity. Since the flask is not long enough, the actual constant velocity might be larger than the measured velocity. This will result in a larger.
* Since the stopwatch is started and stopped by human, there might exist error in time measuring. Also, the refraction effect of the light in the oil might cause errors, too.

To make the result more accurate, some improvements can be made:

* Let machines detect the ball velocity. For example, a photoelectric gate sensor can be used. It will also eliminate the error caused by the velocity not reaching a constant value if the velocity is detected at different positions.
* Release the balls in the fluid to eliminate the possibility that bubbles stick to the surface of the balls.

**7.Reference**

[1] Standard viscosity of the castor oil: <https://www.engineeringtoolbox.com/absolute-viscosity-liquids-d_1259.html>

**A. Measurement uncertainty analysis**

**A.1 Uncertainty of the Fluid Density**

The maximum error of the densimeter is g/; therefore, g/.

**A.2 Uncertainty of the Temperature**

The maximum error of the thermometer is 0.1℃; therefore,

**A.3 Uncertainty of the Inner Diameter of the Flask**

As the maximum uncertainty of the caliper is 0.02mm,

n=6, so

The total uncertainty

The corresponding relative uncertainty

Therefore, the experimental found inner diameter of the flask **D**= 61.740.04mm

**A.4 Uncertainty of the Diameter of the Ball**

As the maximum uncertainty of the micrometer is 0.005mm,

n=10, so

The total uncertainty

The corresponding relative uncertainty

Therefore, the experimental found diameter of the ball **d**= 1.460.008mm

**A.5 Uncertainty of the Mass of one Ball**

As the minimum scale of value of the electronic scale is 0.001g,

**A.6 Uncertainty of the Distance the Ball Travels**

As the maximum uncertainty of the ruler is 0.5mm,

We use the last column data of Table 4.

n=3 and , so

The total uncertainty

The corresponding relative uncertainty

Therefore, the experimental found distance the ball travels **S**= 1180.5mm

**A.4 Uncertainty of the Time the Ball Travels**

As the maximum uncertainty of the stopwatch is 0.01s,

We use the last column data of Table 4.

n=6, so

The total uncertainty

The corresponding relative uncertainty

Therefore, the experimental found time the ball travels **t** =5.610.05s

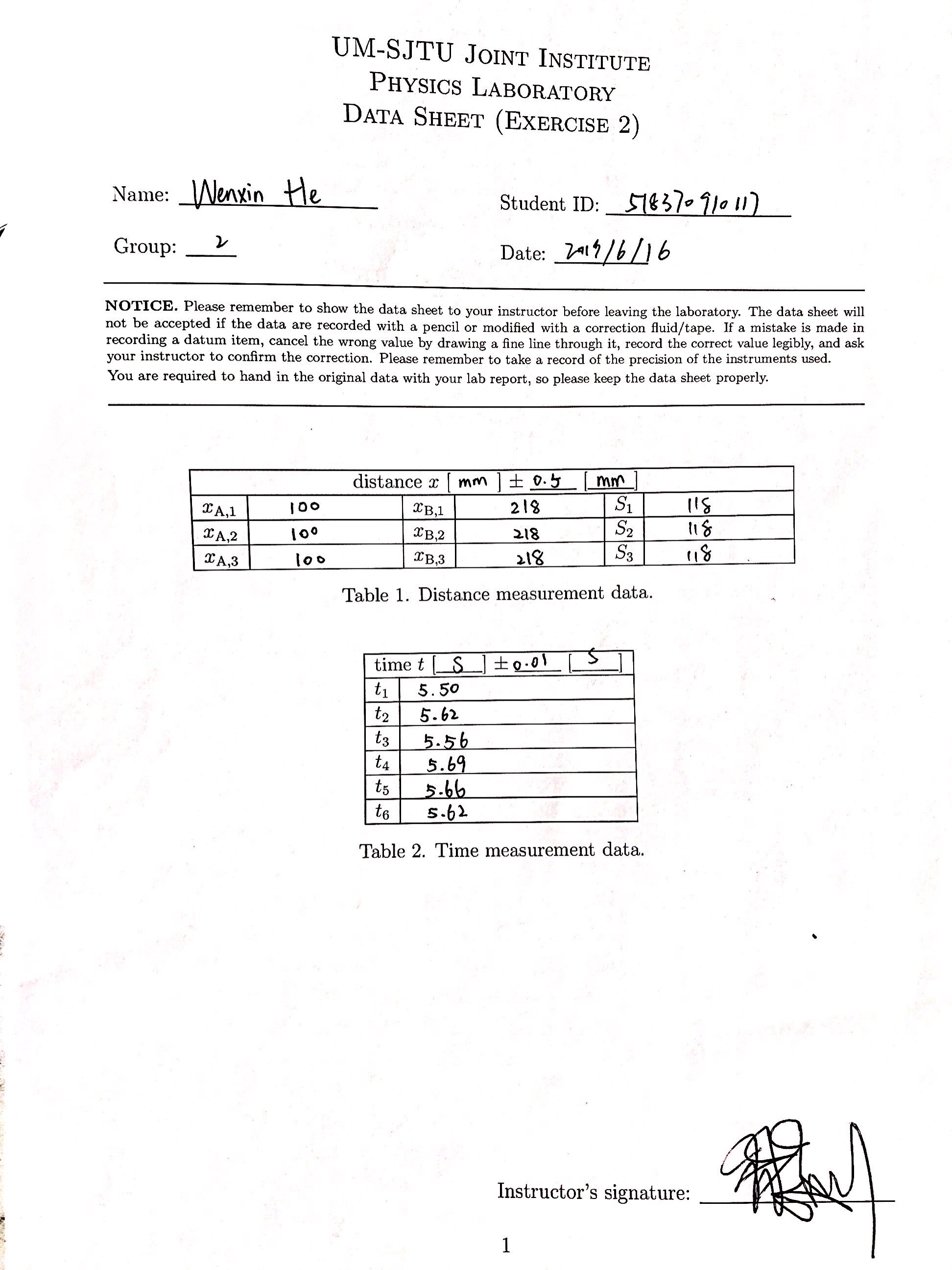
**A.5 Uncertainty of the Velocity of the Ball**

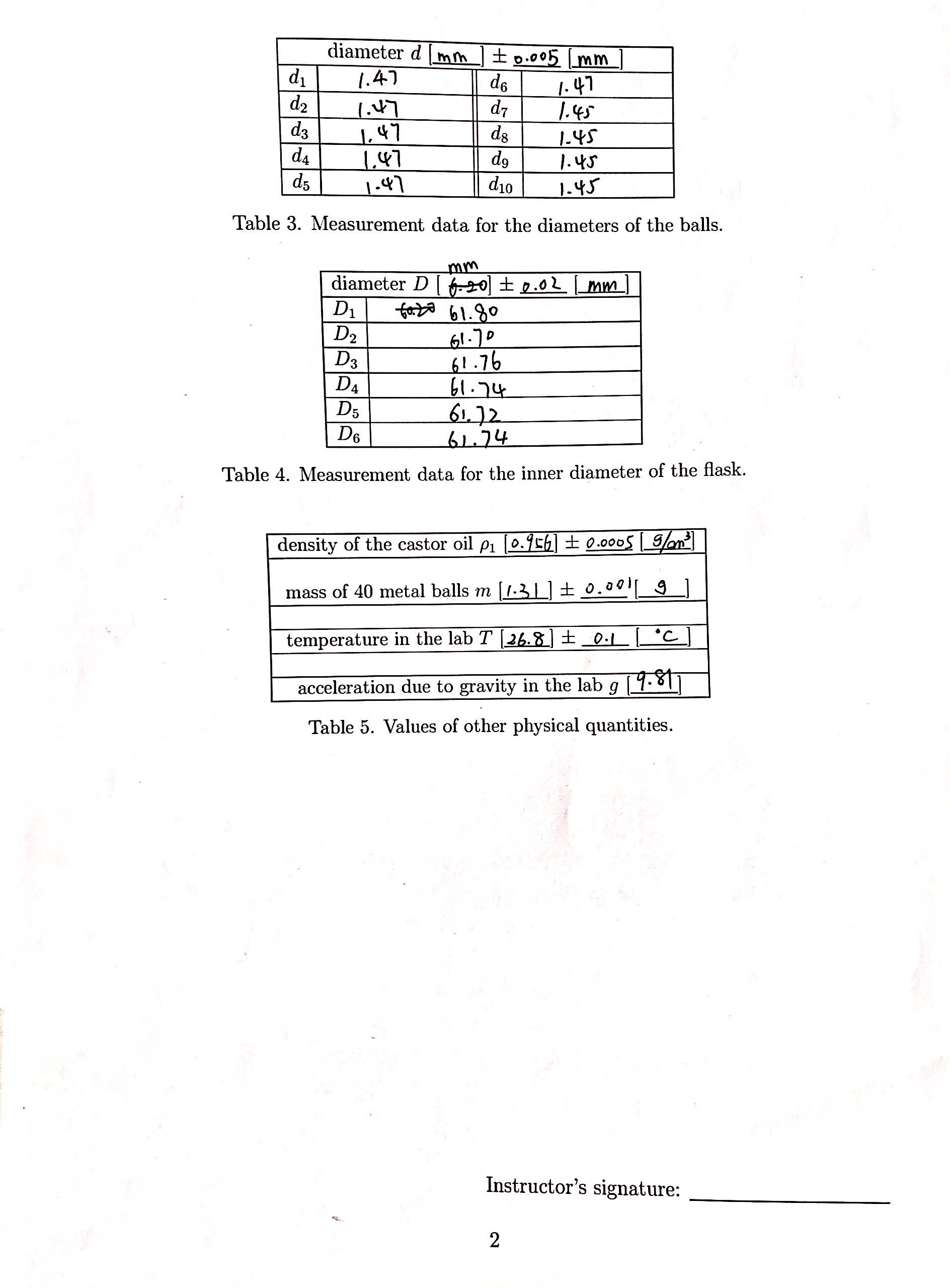
Therefore, the experimental found velocity of the ball is **v**=21.03

**A.6 Uncertainty of the Fluid Viscosity**

=0.0318 kg/m

**B. Data sheet**

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